



Potential energy $U = -w$ or $U = qV$

Electric Potential $V = \frac{-w}{q}$ or $\frac{U}{q}$

Scalar quantity

Electric Potential Si Unit: $V = J/C$

Vol + Joule
Coulomb

Change in V

$$\Delta V_{\text{in electric field}} = V_f - V_i$$

Change in U

$$\Delta U = q, \Delta V = q(V_f - V_i)$$

Work by the E

$$W = -\Delta U$$

$$W = -q \Delta V$$

Conservation Of Energy

$$\Delta K \rightarrow \text{Kinetic energy}$$

$$\Delta K = -\Delta U$$

$$\Delta K = -q \Delta U$$

Electron Volts

$$1.602 \times 10^{-19} C \leftarrow \text{Volt} \rightarrow 1eV = e(1V)$$

$$J \rightarrow eV$$

$$1.602 \times 10^{-19} C \rightarrow$$

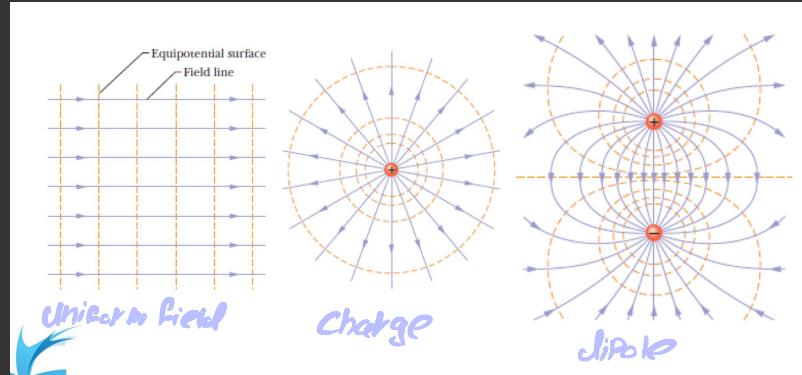
$$eV \rightarrow J$$

$$1.602 \times 10^{-19} J \rightarrow$$

Equipotential surfaces and El. Fi.

$+ve q \rightarrow$ Out Arrow

$-ve q \rightarrow$ In Arrow



Calculating U from E

- $\Delta V = - \int E \cdot d$ general formula

Special Cases:

- Uniform field $\rightarrow \Delta V = - E \Delta X$ ↑
 Vector: From Higher $V \rightarrow$ lower V

Potential due to a Char. Particle

$$V = \frac{kq}{r}$$

Potential Due to a Group of Charged Particles

$$= \sum V \quad \text{or} \quad K \sum \frac{q}{r}$$

Potential due to a Char. Particle

Example 1:

The electric potential at a distance 5 cm from a point charge 2.5 nC is:

$$V = \frac{kq}{r} = \frac{K(2.5 \times 10^{-9})}{5 \times 10^{-2}} \approx 449.5 \text{ V}$$

Solution:

- (A) 450 V
- (B) 320 V
- (C) 280 V
- (D) 150 V

$$V = \frac{kq}{r} = \frac{K(2.5 \times 10^{-9})}{5 \times 10^{-2}} \approx 450 \text{ V}$$



Potential due to a Char. Particle

Example 3:

As shown in the arrangement below, the electric potential at point A is: $V = V_1 + V_2$

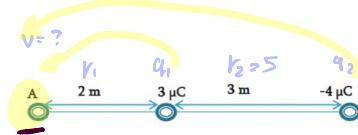
$$V_1 = \frac{kq_1}{r_1} = \frac{(9 \times 10^9)(3 \mu\text{C})}{2 \text{ m}} = 13485 \text{ V}$$

$$V_2 = \frac{kq_2}{r_2} = -7192 \text{ V}$$

$$= -7192 + 13485 = 6293 \approx 6300 \text{ V}$$

Solution:

- (A) 1200 V
- (B) 2400 V
- (C) 5600 V
- (D) 6300 V ✓



Potential due to a Char. Particle

Example 4:

Referring to Example 3, the work needed to bring a charge 6 nC from infinity to point A is:

Solution:

- (A) $-1.52 \times 10^{14} \text{ eV}$
- (B) $-2.36 \times 10^{14} \text{ eV}$ ✓
- (C) $-4.57 \times 10^{14} \text{ eV}$
- (D) $-6.39 \times 10^{14} \text{ eV}$

$$(B) W = -1U = -(V_A - V_B)$$

$$V_A = qV_A = 3.78 \times 10^{-5} \text{ J}$$

$$V_B = qV_B = \text{zero}$$

$$= \frac{-3.78 \times 10^{-5} \text{ J}}{1.602 \times 10^{-19}} = -2.36 \times 10^{14} \text{ eV}$$

Potential due to a Char. Particle

Example 2:

$$\frac{E = 180}{2 \text{ cm}} \quad 180 = \frac{kq}{(2 \times 10^{-2})^2} \quad q = 8 \times 10^{-12} \text{ C}$$

A point charge produces an electric field of 180 N/C at 2 cm. The electric potential at 4 cm from the charge is:

$$V = \frac{kq}{r_2}$$

- (A) 3.7 V
- (B) 2.4 V
- (C) 1.8 V
- (D) 0.4 V

$$180 = \frac{kq}{(2 \times 10^{-2})^2}$$

$$q = 8 \times 10^{-12} \text{ C}$$

$$V = \frac{8 \times 10^{-12}}{4 \text{ cm}}$$

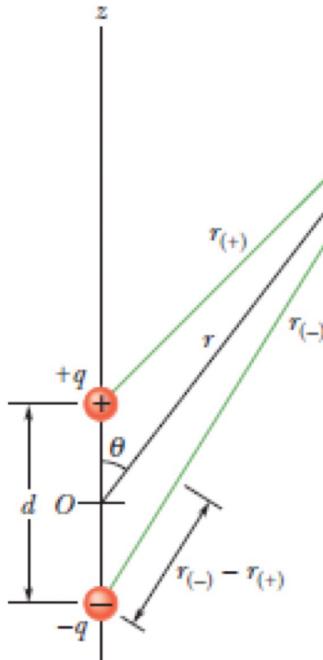
$$k = 8.99 \times 10^9$$



Potential Due to an Electric Dipole

$$V = \frac{K P \cos \theta}{r^2}$$

$P = |q|d$
 → dipole momentum



Example 5:

Two equal and opposite charges $6.0 \mu\text{C}$ and $-6.0 \mu\text{C}$ are separated by a distance of 2 cm. The electric potential at a point 30 cm away from the axis of the dipole is: $P = |q|d = 1.2 \times 10^{-7}$

Solution:

- (A) $9.4 \times 10^4 \text{ V}$
 (B) $7.6 \times 10^4 \text{ V}$
 (C) $5.7 \times 10^4 \text{ V}$
 (D) $1.2 \times 10^4 \text{ V}$ ✓

$$\frac{k \times (6 \times 10^{-6})(2 \times 10^{-2}) \cos(0)}{(30 \times 10^{-2})^2} = 1.2 \times 10^4 \text{ V}$$

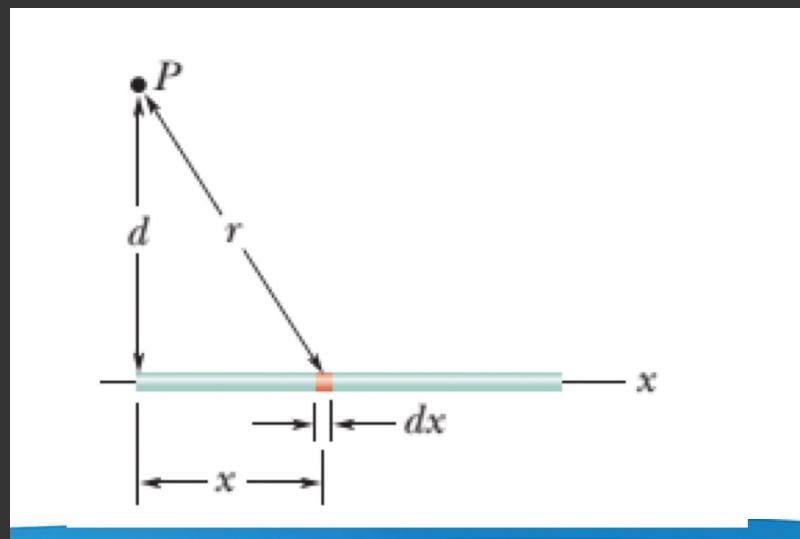
$$P = 6 \times 10^{-6} \times 2 \times 10^{-2}$$

Potential Due to a Continuous Charge Distribution

Not Important

$$V = k \int \frac{dq}{r}$$

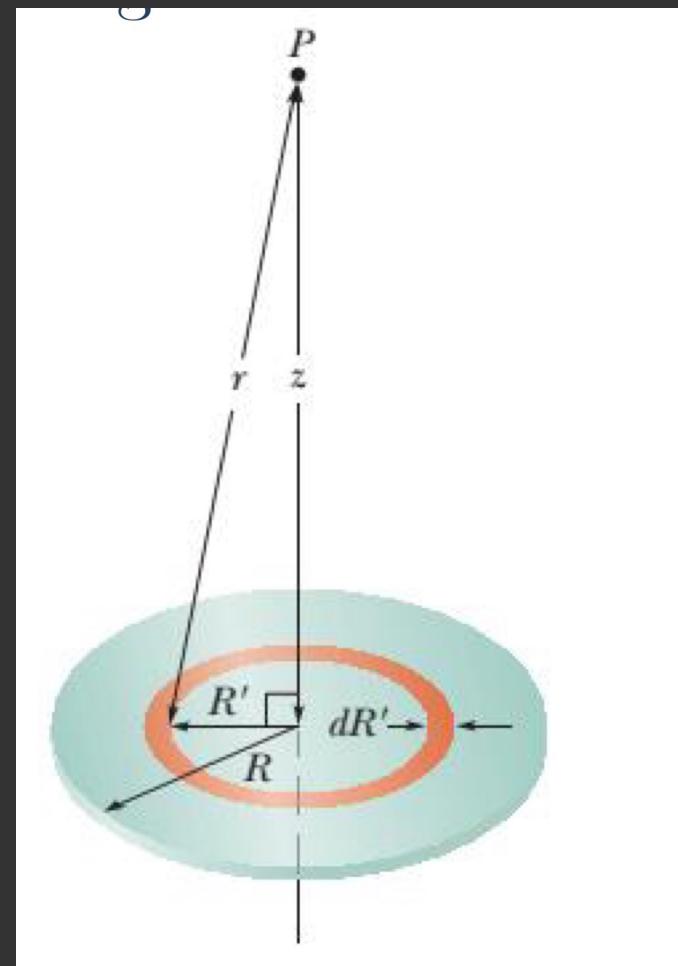
$$dq = \lambda dx$$



Charged Disk

Has magnitude
العرض للعد
 $dq = \sigma(2\pi R')(dR')$,
مساحة المثلثات

$$\checkmark = \frac{\sigma}{2\epsilon_0} (\sqrt{z^2 + R^2} - z).$$



Electric Potential Energy of a System of Charged Particles

For two particles at separation r ,



$$U = W = \frac{kq_1 q_2}{r}$$

Example 6:

Four charges 1, 2, 3 and $-4 \mu\text{C}$ are located at the corners of a square of side 3 m as shown in the figure. The electric potential energy of the system is:

$$U_1 = \frac{k(1)(2)}{3} = 6 \times 10^{-3}$$

Solution:

$$U_2 = \frac{k(1)(3)}{3} = 9 \times 10^{-3}$$

(A) -15 mJ

(B) -24 mJ

(C) -35 mJ

(D) -46 mJ

b energies to Sum

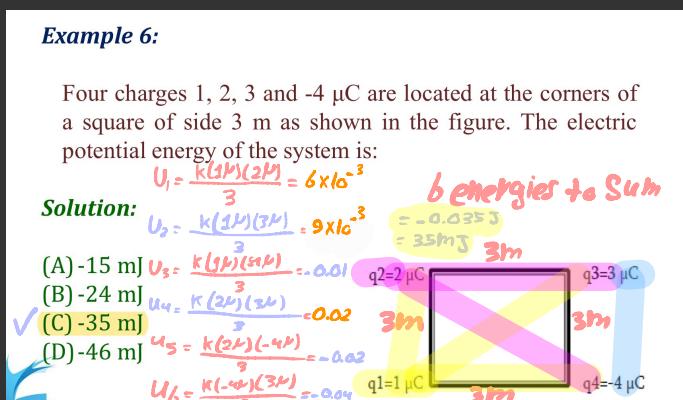
لو في أكثر من نقطتين يسير المسوئ

القانون لكل نقطة في النهاية واجم

عسان يطلعني هجدع طلاقة السفل للنظام

$q_1 \& q_2 \xrightarrow{\text{Same signs}} U = +$ "

$q_1 \& q_2 \xrightarrow{\text{Not same signs}} U = -$ "



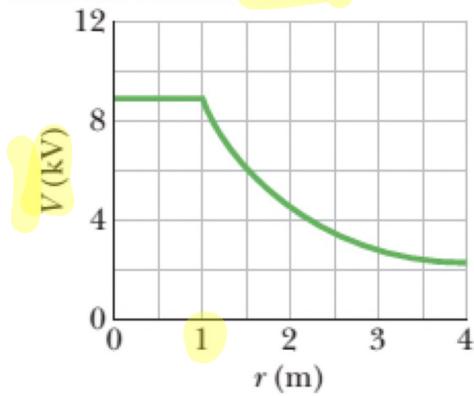
Potential of a Charged Isolated Conductor

Sphere

$$V = \frac{kq}{R} , \text{Electric Potential of a conducting sphere}$$

فَهَا تَعْرِلُ دَاخِلَ الْكُورَةِ التَّائِبِ
وَادِدًا أَنَّهُ السَّنَاتِ عَلَى لِسْطَلِ
الْكُورَةِ فَلَوْ بَدَنَ لِجَهَةِ الْيَمِينِ
هُرَيْتَ يَنْعَصِ التَّائِبِ مِنَ الْجَهَةِ الْيَمَارِ
لَكِنَ الْجَهَةِ الْيَمِينِ رَاحَ تَعْوَضُوا لَا نَزَدُ
فَرِلتَ مِنَ السَّنَاتِ الْجَهَةِ الْيَمِينِ
فِي التَّائِبِ حَسِيرٌ أَكْبَرٌ

A plot of $V(r)$ both inside and outside a charged spherical shell of radius 1.0 m.



A plot of $E(r)$ for the same shell.

لابوبد مبارع الدانل زان الشنات
على المطاع فقط ليس في لعافند

