

## Lab 3

### Knowledge-Based Systems in Bioinformatics

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#### Task 1

$A = (U, A \cup \{d\})$

```
info_TA <- c(  
  -(4 / 9) * log2(4 / 9) - (5 / 9) * log2(5 / 9)  
)
```

$\text{Info}([4,5]) = 0.9910761$  bits.

Table 1. Decision system A discretized using equal frequency with three levels.

Cuts	decision
[91, 105)	No
[45, 91)	{Yes, No}
[21, 45)	Yes

Calculate bits.

```
info_T1 <- c(  
  -(0 / 3) * log2(0 / 3) - (3 / 3) * log2(3 / 3),  
  -(1 / 3) * log2(1 / 3) - (2 / 3) * log2(2 / 3),  
  -(3 / 3) * log2(3 / 3) - (0 / 3) * log2(0 / 3)  
)  
info_T1[1] <- 0 # defined as 0 bits  
info_T1[3] <- 0 # defined as 0 bits  
info_T1 <- sum(info_T1 * c(3 / 9, 3 / 9, 3 / 9))
```

$\text{Info}([0,3],[1,2],[3,0]) = 0.3060986$  bits.

$\text{Gain}(\text{feature\_1}) = \text{info}([4,5]) - \text{info}([0,3],[1,2],[3,0]) = 0.6849774$  bits.

$\text{Gain\_ratio}(\text{feature\_1}) = \text{gain}(\text{feature\_1}) / \text{split\_info}(\text{feature\_1})$

Table 2. Decision system A discretized using naive method.

Cuts	decision
[78, 105)	No
[62, 78)	Yes
[45, 62)	No
[21, 45)	Yes

Calculate bits.

```
info_T2 <- c(
  -(0 / 4) * log2(0 / 4) - (4 / 4) * log2(4 / 4),
  -(1 / 1) * log2(1 / 1) - (0 / 1) * log2(0 / 1),
  -(0 / 1) * log2(0 / 1) - (1 / 1) * log2(1 / 1),
  -(3 / 3) * log2(3 / 3) - (0 / 3) * log2(0 / 3)
)
info_T2 <- c(0, 0, 0, 0) # defined as 0 bits
info_T2 <- sum(info_T2 * c(4 / 9, 1 / 9, 1 / 9, 3 / 9))
```

Info([0,3],[1,2],[3,0]) = 0 bits.

Gain = info([4,5]) - info([0,3],[1,2],[3,0]) = 0.9910761 bits.

$B = (U, B \cup \{d\})$

Table 3. Decision system A discretized using equal frequency with three levels.

Cuts	decision
[0.67, 0.97)	{A, B}
[0.29, 0.67)	{A, B}
[0.04, 0.29)	{A, B}

Table 4. Decision system A discretized using naive method.

Cuts	decision
[0.89, 0.97)	A
[0.75, 0.89)	B
[0.39, 0.75)	A
[0.17, 0.39)	B
[0.08, 0.17)	A
[0.03, 0.08)	B

## Task 2