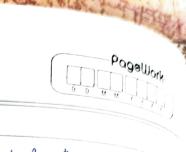


3. Denote de is the language fulowellR) There exist a DEA M that accepts L(R). -stortof M We concommet DAN N= (QES.S,F) where S'= S(S,O) Observe if N accepts W. T. e S(s', w) EF ( ) S(S, OW) EF ( Macceptow. Hince de is regular . (NisDFA acceptingit) b) dr = dr + dr c)  $\frac{d(R^*)}{d\sigma} = \frac{dR}{d\sigma}R^*$ 4. a) R-(R-+R3)) = L (R1R2+R1R3) b) L((R,+R2)R3) = L(R,R3+R2R3)  $C)L((R_1+R_2)^*)=L((R_1^*R_2^*)^*)$ A regex R is said to be (+) free if R does not contain + operator. A regex R is said to be (+) reparable if one of the following two Conditions: -> Ris (+) free, or  $\rightarrow R = R_1 + R_2$  and  $R_1, R_2$  are (+) separable 1) Show that if R is (+) separable then R=Ri+Ri-Ri where Ris are (+)-free. Induction on length of R Base case: All regex with that is 4) free I.H. All Rupho length K (that are (+) separable) (an be represented as & R (when (+) free ) or R1+R2+R3-RA Induction Step: Suppose R is length K+1 (+1 separable regex. (1) Af Ris +) free we are done (2) 9f R is (+) separable & R=R,+R2 where (+) separable As R, and Rz must have length less than oregual to k they can be represented as (R,+R, +Rn) form Hence R can also be represented as such. (e) Show that if R, and Rz are (+) separable than There is a (+) separable regex Equivalent to RiRz. RiRz = (XI+XI . - XK) (YI 1 YI - - Yz) in representation (Xi, y) are (+) free) Observe L((xin - )(Vi+Yi - yi))= L( E Exit; ) Observe XiY; is (+) free flance ZZ xiy; royex 95 4) separable . Non. (7) Show that if R is (+) separable, then there exists (+) There regex R, such that L(R) = L(R)



	Base (ose: When Ris (+) free we use dore
	Indiction Hypothesis: For all (+) separable regex R les upto length k
	L(R*) = L(R,*) where R, is +) free.
	Induction stansition: Take R that is (+) separable and K+1 length
	(I) If Ris (+) free done
	(2) If Rist separated Else R= x1+x2
	By Inductive inductive $L(x_i^*) = L(y_i^*)$ , $L(x_i^*) = L(y_i^*)$
	Where y, and y'z are (+) free.
-	Observe L(x) = L((x+x,x) = L((x*x*)) = L((y,*y,*)*)
	As y, and ye are (+) free => yi*yi* is (+) free.
	Hince we are done.
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