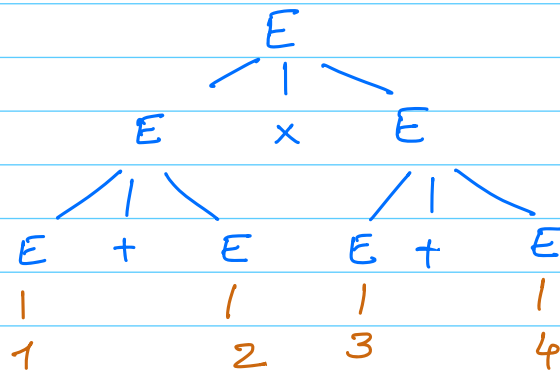
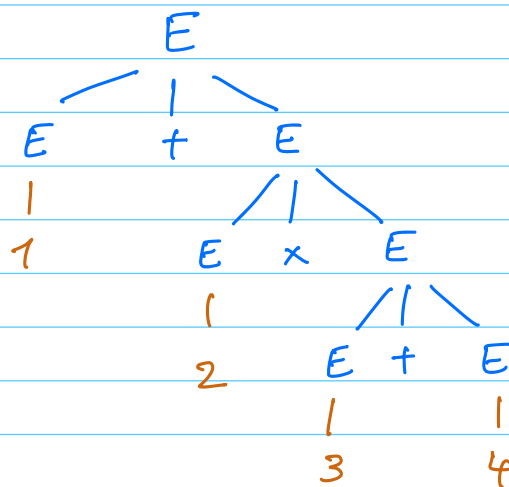


leftmost derivations: Each time expand the left-most non-terminal using a production rule.

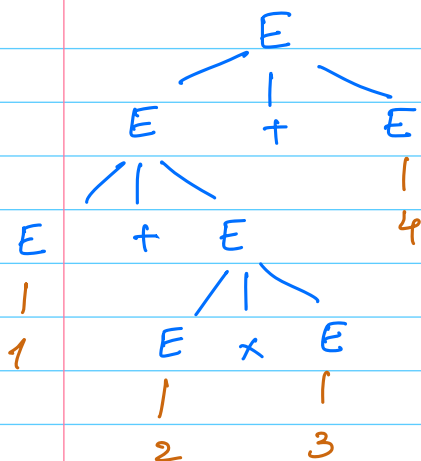
$$E \rightarrow E + E \mid E \times E \mid 0 \mid 1 \mid 2 \mid \dots \mid 9 \quad [1 + 2 \times 3 + 4]$$



parsed as  $(1+2) \times (3+4)$



parsed as  $1 + 2 \times (3+4)$



parsed as  $1 + (2 \times 3) + 4$

A CFG is ambiguous if it has more than one leftmost derivation

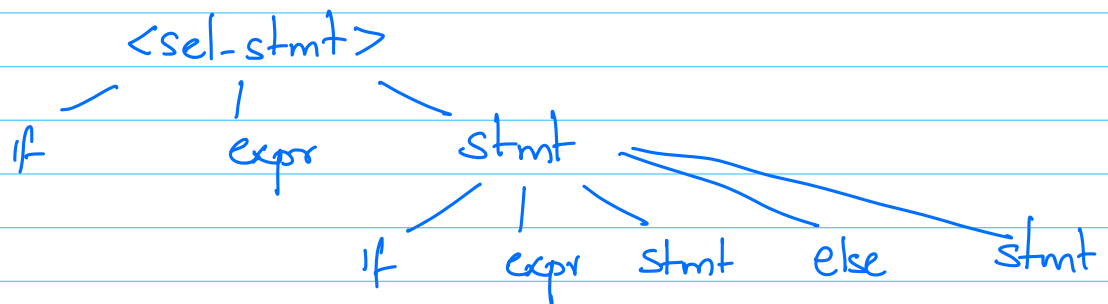
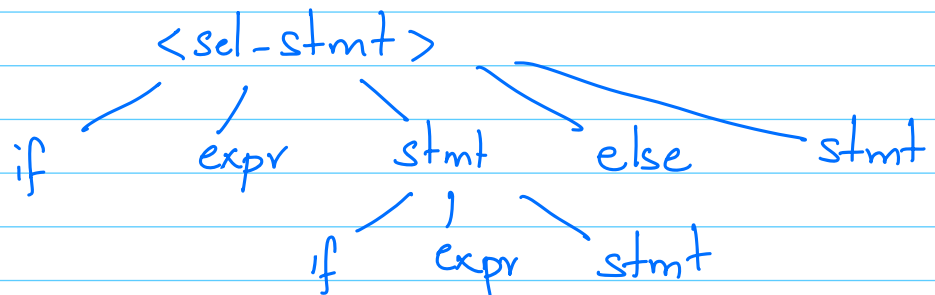
$$E \rightarrow E + T \mid T$$
$$T \rightarrow T \times F \mid F$$
$$F \rightarrow 0 \mid 1 \mid 2 \mid \dots \mid 9$$

} Implements the precedence of the operators

Dangling else

$$\langle \text{sel-stmt} \rangle := \text{if}(\langle \text{expr} \rangle) \langle \text{stmt} \rangle \mid$$
$$\text{if}(\langle \text{expr} \rangle) \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$$

if — if — else —



$\langle \text{stmt} \rangle := \langle \text{matched} \rangle \mid \langle \text{unmatched} \rangle$

$\langle \text{matched} \rangle := \text{if } \langle \text{expr} \rangle \langle \text{matched} \rangle \text{ else } \langle \text{matched} \rangle$

$\langle \text{matched} \rangle := \langle \text{non-sel-stmt} \rangle$

$\langle \text{unmatched} \rangle := \text{if } \langle \text{expr} \rangle \langle \text{stmt} \rangle \mid$

$\text{if } \langle \text{expr} \rangle \langle \text{matched} \rangle \text{ else } \langle \text{unmatched} \rangle$

Inherently ambiguous languages

$L = \{ a^i b^j c^k d^l \mid i=j \text{ and } k=l \text{ or } i=l \text{ and } j=k \}$

Closure properties

- Union

$S \rightarrow S_1 \mid S_2$

$S_1 \rightarrow \dots$

$S_2 \rightarrow \dots$

- Concatenation

$S \rightarrow S_1 \cdot S_2$

$S_1 \rightarrow \dots$

$S_2 \rightarrow \dots$

- Kleene closure

$S \rightarrow SS_1 \mid \epsilon$

$S_1 \rightarrow \dots$

Not closed under intersection and  
complementation