

INGENIØRHØJSKOLEN ÅRHUS

DISCRETE MATHEMATICS

Hand in 3

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Problems

- 1 Which of the following sets are well-ordered? (Why/why not?)
 - a. $S = x \in \mathbb{Q} : x \leq -10$
 - b. $S = -2, -1, 0, 1, 2$
 - c. $S = x \in \mathbb{Q} : -1 \leq x \leq -10$
 - d. hest
- 2 Let $a, b \in \mathbb{Z}$ Disprove the statement: if ab and $(a + b)^2$ are of opposite parity, then a^2b^2 and $a+ab+b$ are of opposite parity.
- 3 Let $a, b \in \mathbb{R}^+$. Use a proof by contradiction to prove that $x < y$, then $\sqrt{x} < \sqrt{y}$
- 4 Prove that there is no largest negative rational number.
- 5 Prove that there exists no positive integer x such that $2x < x^2 < 3x$.
- 6 Prove that if n is an odd integer, then $7n-5$ is even by