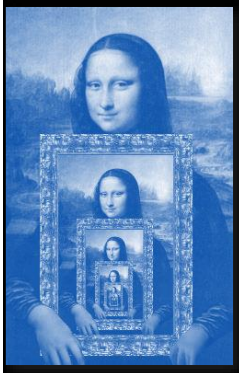

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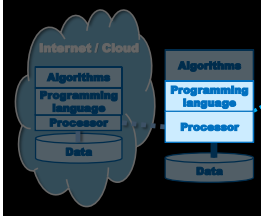
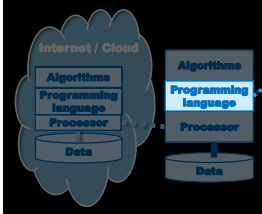
Subprograms

Conceptual map of the lectures



Topic
Imperative Programming
Digital Circuits
Computers
Subprograms
Numerical Methods
Computational Complexity
Object-oriented Programming
Text Processing
Databases and Machine Learning
Parallel Processing
Computer Networks & Cybersec.
Software Engineering
Embedded Systems
Professionalism in Computing

Conceptual map of the lectures



Topic
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Professionalism in Computing

Agenda

- Very simple programs
- Conditionals
- Iteration
- Simple functions
- Simple arrays

- Declarative programming

```python
def GCD(a, b):
    while a != b:
        if a > b:
            a-= b
        else:
            b-= a
    return a

x = int(input())
y = int(input())
print(GCD(x, y))
```

```c
#include <stdio.h>
int GCD(int a, int b) {
    while ( a != b ) {
        if(a > b){
            a-= b;}
        else{
            b-= a;}
        }
    return a;
    }
int main(void) {
    int x, y;
    scanf("%d", &x);
    scanf("%d", &y);
    printf("%d", GCD(x,y));
    }
```

Aim of this lecture

Help the students to
better understand subprograms.

Subprogram as a generalization of function

Subprograms

- Function
- Procedure ?

```
def GCD(a, b):
    while a != b:
        if a > b:
            a-= b
        else:
            b-= a
    return a

x = int(input())
y = int(input())
print(GCD(x, y))
```

```
x = int(input())
y = int(input())
while x != y:
    if x > y:
        x-= y
    else:
        y-= x
print(x)
```

Why to bother with subprograms?

Code understandability

„Software understandability [...] closely relate to software maintainability"[1]

Maintenance ≈ 4 · 1st_release

1) Celia Chen et al., Assessing Software Understandability in Systems by Leveraging Fuzzy Method and Linguistic Analysis, Procedia Computer Science, 153 (2019)

Code understandability

How to take care of code understandability?

Comment: Text neglected by computer

```
# any text until end of line
```

```
// any text until end of line
/* any text different from --> */
```


Are those programs correct?

```
H = int(input())
L = int(input()
r = 2*H - L//2
print(r)
```

```
#include <stdio.h>
int main(){
    int H, L, r;
    scanf("%d", &H);
    scanf("%d", &L);
    r = 2*H - L/2;
    printf("%d\n", r);
    }
```

Are those programs correct?

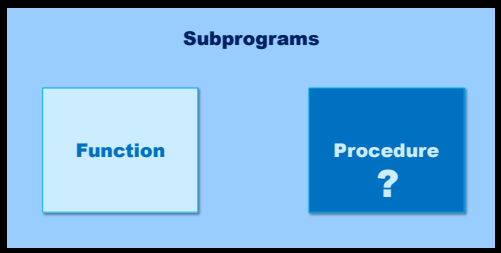
```
# H = heads of cows & hens
# L = legs  of cows & hens
# Given: H and L.
# Find: the number of hens.



H = int(input())
L = int(input()
r = 2*H - L//2
print(r)
```

```
/* H = heads of cows & hens
   L = legs  of cows & hens
   Given: H and L.
   Find: the number of hens.
*/
#include <stdio.h>
int main(){
    int H, L, r;
    scanf("%d", &H);
    scanf("%d", &L);
    r = 2*H - L/2;
    printf("%d\n", r);
    }
```

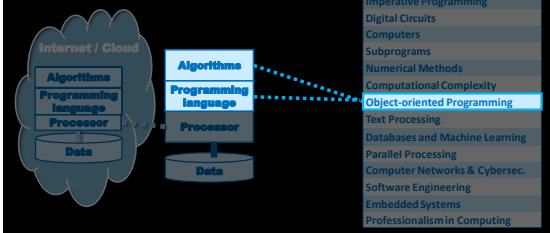

Code understandability

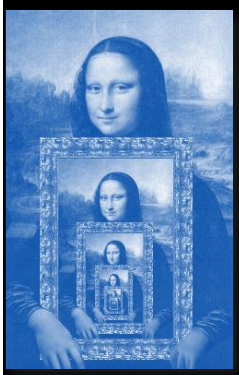
How to take care of code understandability?

Subprogram as a generalization of function



Conceptual map of the lectures

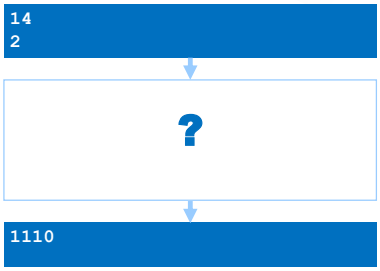




Subprograms

- Functions and procedures
- Stack
- Subprogram implementation
- Recursion
- Subprogram parameters

Converting a decimal number x to base b.



Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
```

Converting a decimal number x to base b.

	digits
0	0
1	1
2	1
3	1

```
digits = [0]*99
def int2digits(14, 2):
    # digits[] = digits of n in base b
    # digits[0] is least significant
```

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
def length(n, b):
    # number of digits of n in base b
```

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits
    # digits[0] is leas
def length(14, 2):
    # number of digits of n in base b
```

length(14, 2) = 4
$14_{10} = 1110_2$

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
def length(n, b):
    # number of digits of n in base b

x = int(input())
base = int(input())

int2digits(x, base)
j = length(x, base) - 1
while j >= 0:
   print(digits[j], end="")
   j -= 1
```

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
def length(n, b):
    # number of digits of n in base b

x = int(input())
base = int(input())

int2digits(x, base)
j = length(x, base) - 1
while j >= 0:
   print(digits[j], end="")
   j -= 1
```

Function vs procedure

length(n, b)

Pure function

Returns a value

No side-effect

Converting a decimal number x to base b.

Global variable

Returns no value

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
def length(n, b):
    # number of digits of n in base b

x = int(input())
base = int(input())

int2digits(x, base)
j = length(x, base) - 1
while j >= 0:
   print(digits[j], end="")
   j -= 1
```

Function vs procedure

length(n, b)

Pure function

Returns a value

No side-effect

int2digits(n, b)

Procedure

Does not return a value

Has a side-effect

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
    # 2 <= b <= 10
    digits[0] = n % b
    i = 1
    while n > b-1:
       n //= b
       digits[i] = n % b
       i += 1
    return
```

```
def length(n, b):
    # number of digits of n in base b
    L= 1
    while n > b-1:
       n //= b
       L+= 1
    return L
```

Let's take another look ...

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
    # 2 <= b <= 10
    digits[0] = n % b
    i = 1
    while n > b-1:
       n //= b
       digits[i] = n % b
       i += 1
    return
```

```
def length(n, b):
    # number of digits of n in base b
    L= 1
    while n > b-1:
       n //= b
       L+= 1
    return L
```

Let's remove the comments

```
digits = [0]*99
def int2digits(n, b):
    # digits[] = digits of n in base b
    # digits[0] is least significant
    # 2 <= b <= 10
    digits[0] = n % b
    i = 1
    while n > b-1:
       n //= b
       digits[i] = n % b
       i += 1
    return
```

```
def length(n, b):
    # number of digits of n in base b
    L= 1
    while n > b-1:
       n //= b
       L+= 1
    return L
```

What is the difference?

```
digits = [0]*99
def int2digits(n, b):
    digits[0] = n % b
    i = 1
    while n > b-1:
        n //= b
        digits[i] = n % b
        i += 1
    return
```

```
def length(n, b):

    L= 1
    while n > b-1:
        n //= b

        L += 1
    return L
```

After code slicing

```
digits = [0]*99
def int2digits(n, b):
    digits[0] = n % b
    i = 1
    while n > b-1:
        n //= b
        digits[i] = n % b
        i += 1
    return
```

```
def length(n, b):

    L= 1
    while n > b-1:
        n //= b

        L += 1
    return L
```

After code slicing

```
def int2digits(n, b):

    i = 1
    while n > b-1:
        n //= b

        i += 1
    return
```

```
def length(n, b):

    L= 1
    while n > b-1:
        n //= b

        L += 1
    return L
```

After code slicing

```
def int2digits(n, b):

    i = 1
    while n > b-1:
        n //= b

        i += 1
    return
```

```
def length(n, b):

    ▮ = 1
    while n > b-1:
        n //= b

        ▮ += 1
    return ▮
```

Converting a decimal number x to base b.

```
digits = [0]*99
def int2digits(n, b):
    digits[0] = n % b
    i = 1
    while n > b-1:
        n //= b
        digits[i] = n % b
        i += 1
    return i
```

```
x = int(input())
base = int(input())

j = int2digits(x, base) - 1
while j >= 0:
    print(digits[j], end="")
    j -= 1
```

Function vs procedure

`int2digits(n, b)`

Pure function	Function with side effect	Procedure
Returns a value	Returns a value	Does not return a value
No side-effect	Has a side-effect	Has a side-effect

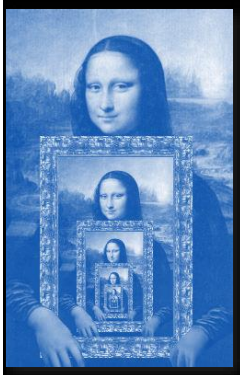
Which variant is better?

```
digits = [0]*99
def int2digits(n, b):
    digits[0] = n % b
    i = 1
    while n > b-1:
        n //= b
        digits[i] = n % b
        i += 1
    return

def length(n, b):
    L= 1
    while n > b-1:
        n //= b
        L += 1
    return L
```

Faster

God subroutine

```
digits = [0]*99
def int2digits(n, b):
    digits[0] = n % b
    i = 1
    while n > b-1:
        n //= b
        digits[i] = n % b
        i += 1
    return i
```

Subprograms

- Functions and procedures
- Stack
- Subprogram implementation
- Recursion
- Subprogram parameters

116 10	116 10

```
#include <stdio.h>
int digit = 0;
void int2LSdigit(int n, int b){
     digit= n % b;
     return;
     }
 int main(){
     int x, base;
     scanf("%d", &x);
     scanf("%d", &base);
     int2LSdigit(x, base);
     printf("%d\n", digit);}
```

```
digit = 0
def int2LSdigit(n, b):
    digit = n % b
    return


x = int(input())
base = int(input())
int2LSdigit(x, base)
print(digit)
```

6	0

116 10	116 10

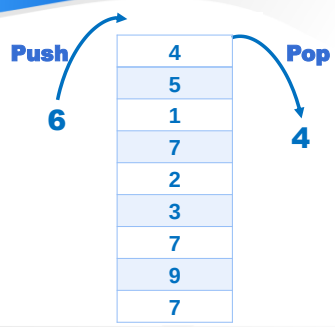
```
#include <stdio.h>
int digit = 0;
void int2LSdigit(int n, int b){
     digit= n % b;
     return;
     }
 int main(){
     int x, base;
     scanf("%d", &x);
     scanf("%d", &base);
     int2LSdigit(x, base);
     printf("%d\n", digit);}
```

```
digit = 0
def int2LSdigit(n, b):
    global digit
    digit = n % b
    return


x = int(input())
base = int(input())
int2LSdigit(x, base)
print(digit)
```

6	6

Stack of books

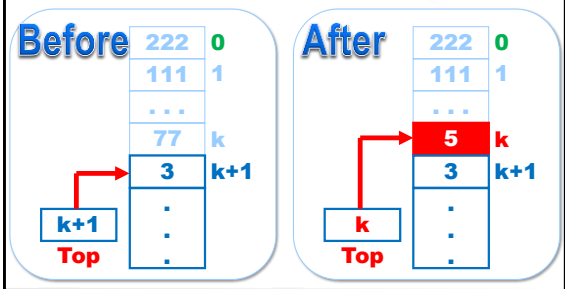
Stack of integers



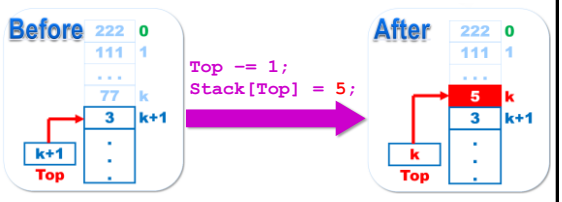
Stack implemented as an array

```
int Top=99, Stack[100];
```

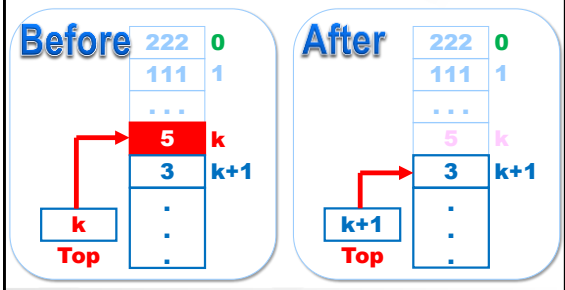

push(5);



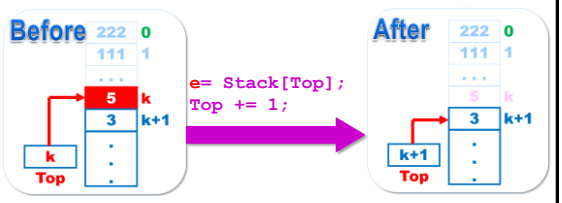
push(5);



e = pop()



e = pop()

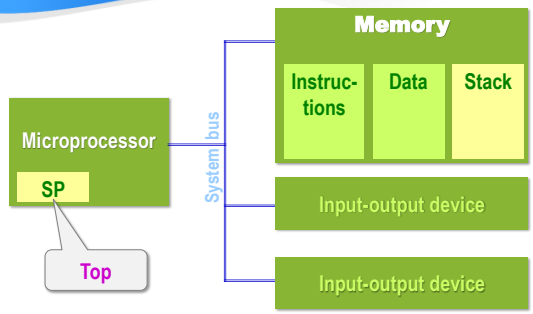



```
Top= 99
Stack= [0]*100
def push(e):
    global Top
    Top -= 1
    Stack[Top] = e
    return
def pop():
    global Top
    e= Stack[Top]
    Top += 1
    return e

x= int(input())
y= int(input())
push(x)
push(y)
print(pop())
print(pop())
```

```
#include <stdio.h>
 int Top=99, Stack[100];
void push (int e){
     Top -= 1;
     Stack[Top] = e;
     return;}
 int pop (){
     int e;
     e= Stack[Top];
     Top= Top + 1;
     return e;}
 int main(){
     int x, y;
     scanf("%d", &x);
     scanf("%d", &y);
     push(x);
     push(y);
     printf("%d\n", pop());
     printf("%d\n", pop());}
```

Hardware implemented stack

Architecture of IBM PC



Hardware stack

push ***source***
pop ***destination***

Quiz

```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX

Stack

What is the value of AX?

Quiz

```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	

Stack

What is the value of AX?

Quiz

```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	7

Stack

What is the value of AX?

```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	7

Stack: 3

What is the value of AX?


```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	7

Stack: 7, 3

What is the value of AX?


```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	7
7	

Stack: 3

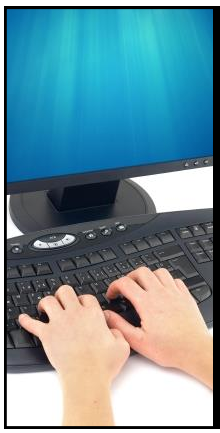
What is the value of AX?


```
mov  ax, 3
mov  bx, 7
push ax
push bx
pop  ax
pop  bx
```

AX	BX
3	7
7	3

Stack: (empty)

What is the value of AX?



Introduction to Computing

Computers and Assembly Language

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Faculty of Computing & Telecom.
Poznan University of Technology


```
mov bx, ax
add ax, ax
add ax, ax
sub ax, bx
```

ax = 3 * ax;

ax	bx
3	5
3	3
6	3
12	3
9	3

New question

How to fix it?

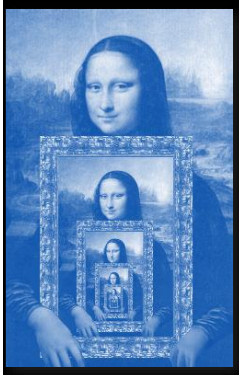
```
mov bx, ax
add ax, ax
add ax, ax
sub ax, bx ; ax= 3*ax
```

```
push bx
mov  bx, ax
add  ax, ax
add  ax, ax
sub  ax, bx
pop  bx      ; ax= 3*ax
```


Quiz

What result is expected?

```
mov  ax, sp
mov  bx, 1
push bx
sub  ax, sp
printReg ax
```

Subprograms

- Functions and procedures
- Stack
- Subprogram implementation
- Recursion
- Subprogram parameters

How many digits?

Given: A natural number x.
Question: How many decimal and octal digits are necessary to represent x?
Assume x is hard-coded.

How many digits?

65

?

$65_{10} = 101_8$

2
3

How many digits?

C

```c
#include <stdio.h>
int length(int n, int b){
    // number of digits of n in base b
    // n, b are natural numbers; b > 1
    int L;
    L= 1;
    while (n > b-1){
       n /= b;
       L+= 1; }
    return L; }
int main(){
    int digits;
    digits= length(65, 10);
    printf("%d\n", digits);
    digits= length(65,  8);
    printf("%d\n", digits);}
```

How many digits?

```
def length(n, b):
    # number of digits of n in base b
    # n, b are natural numbers; b > 1
    L= 1
    while n > b-1:
        n //= b
        L+= 1
    return L
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

How many digits?

```
def length(n, b):
    # number of digits of n in base b
    # n, b are natural numbers; b > 1
    L= 1
    while n > b-1:
        n //= b
        L+= 1
    return L
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

How many digits?

```
L= 1
while n > b-1:
    n //= b
    L+= 1
```

```
        mov  cx, 1 ; L= 1
loop:   mov  si, bx
        sub  si, 1
        cmp  ax, si
        jng  pool  ; while n > b-1:
        mov  dx, 0
        div  bx    ;    n //= b
        add  cx, 1 ;    L += 1
        jmp  loop
pool:
```

How many digits?

```
L= 1
while n > b-1:
    n //= b
    L+= 1
```

```
        mov  cx, 1 ; L= 1
loop:   mov  si, bx
        sub  si, 1
        cmp  ax, si
        jng  pool  ; while n > b-1:
        mov  dx, 0
        div  bx    ;    n //= b
        add  cx, 1 ;    L += 1
        jmp  loop
pool:
```

ax: n
bx: b
si: b-1

DIV z
ax = (dx:ax) / z;
dx = (dx:ax) % z;

How many digits?

```
L= 1
while n > b-1:
    n //= b
    L+= 1
```

```
        mov  cx, 1 ; L= 1
loop:   mov  si, bx
        sub  si, 1
        cmp  ax, si
        jng  pool  ; wh      1:
        mov  dx, 0
        div  bx    ;    n //= b
        add  cx, 1 ;    L += 1
        jmp  loop
pool:
```

ax: n
bx: b

How many digits?

```
L= 1
while n > b-1:
    n //= b
    L+= 1
```

```
        push dx    ; tmp
        push si    ; tmp
        push ax    ; param n
        push bx    ; param b
        mov  cx, 1 ; L= 1
loop:   mov  si, bx
        sub  si, 1
        cmp  ax, si
        jng  pool  ; while n > b-1:
        mov  dx, 0
        div  bx    ;    n //= b
        add  cx, 1 ;    L += 1
        jmp  loop
pool:   pop  bx    ; param b
        pop  ax    ; param n
        pop  si    ; tmp
        pop  dx    ; tmp
```

How many digits?

```
def length(n, b):
    # number of digits of n in base b
    # n, b are natural numbers; b > 1
    L= 1
    while n > b-1:
        n //= b
        L+= 1
    return L
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

How many digits?

```
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

```
mov  ax, 65
mov  bx, 10
jmp  leng
printReg cx
mov  bx, 8
jmp  leng
printReg cx
```

```
leng: push dx     ; tmp
      push si     ; tmp
      push ax     ; param n
      push bx     ; param b
      mov  cx, 1  ; L= 1
loop: mov  si, bx
      sub  si, 1
      cmp  ax, si
      jng  pool   ; while n > b-1:
      mov  dx, 0
      div  bx     ;    n //= b
      add  cx, 1  ;    L += 1
      jmp  loop
pool: pop  bx     ; param b
      pop  ax     ; param n
      pop  si     ; tmp
      pop  dx     ; tmp
```

What's missing?

How many digits?

```
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

```
mov  ax, 65
mov  bx, 10
jmp  leng
printReg cx
mov  bx, 8
jmp  leng
printReg cx
```

```
leng: push dx     ; tmp
      push si     ; tmp
      push ax     ; param n
      push bx     ; param b
      mov  cx, 1  ; L= 1
loop: mov  si, bx
      sub  si, 1
      cmp  ax, si
      jng  pool   ; while n > b-1:
      mov  dx, 0
      div  bx     ;    n //= b
      add  cx, 1  ;    L += 1
      jmp  loop
pool: pop  bx     ; param b
      pop  ax     ; param n
      pop  si     ; tmp
      pop  dx     ; tmp
      jmp  ???
```


CALL & RET (Intel x86 family)

CALL *label* L1: ...	≡	push* L1 jmp *label*
RET	≡	pop* reg jmp reg

* Regular PUSH/POP manipulates 2-byte data.
Here 4 bytes are pushed and popped.

How many digits?

```
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

```
mov  ax, 65
mov  bx, 10
call leng
printReg cx
mov  bx, 8
call leng
printReg cx
```

```
leng: push dx     ; tmp
      push si     ; tmp
      push ax     ; param n
      push bx     ; param b
      mov  cx, 1  ; L= 1
loop: mov  si, bx
      sub  si, 1
      cmp  ax, si
      jng  pool   ; while n > b-1:
      mov  dx, 0
      div  bx     ;    n //= b
      add  cx, 1  ;    L += 1
      jmp  loop
pool: pop  bx     ; param b
      pop  ax     ; param n
      pop  si     ; tmp
      pop  dx     ; tmp
      ret
```


How many digits?

```
digits= length(65, 10)
print(digits)
digits= length(65,  8)
print(digits)
```

```
mov  ax, 65
mov  bx, 10
call leng
printReg cx
mov  bx, 8
call leng
printReg cx
```

```
leng: push dx     ; tmp
      push si     ; tmp
      push ax     ; param n
      push bx     ; param b
      mov  cx, 1  ; L= 1
loop: mov  si, bx
      sub  si, 1
      cmp  ax, si
      jng  pool   ; while n > b-1:
      mov  dx, 0
      div  bx     ;    n //= b
      add  cx, 1  ;    L += 1
      jmp  loop
pool: pop  bx     ; param b
      pop  ax     ; param n
      pop  si     ; tmp
      pop  dx     ; tmp
      ret
```

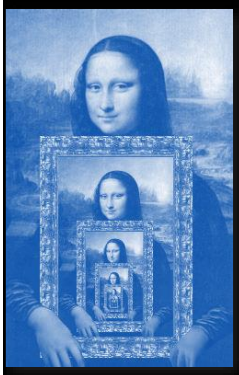
CALL & RET (Intel x86 family)

CALL *label* L1: ...	≡	push* L1 jmp *label*
RET	≡	pop* reg jmp reg

* Regular PUSH/POP manipulates 2-byte data.
Here 4 bytes are pushed and popped.

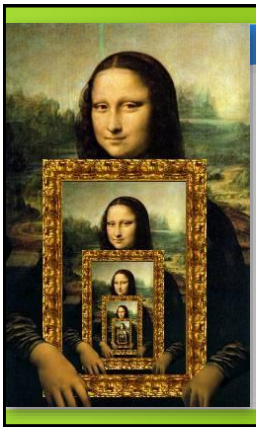
Quiz


```
        mov  ax, sp
        mov  bx, 1
        push bx
        call lab
lab:    sub  ax, sp
        printReg ax
```

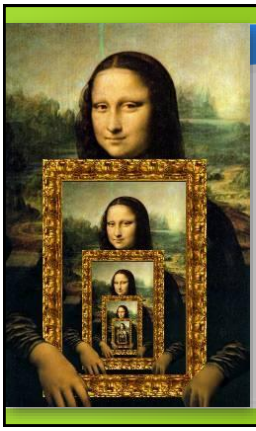
Subprograms

- Functions and procedures
- Stack
- Subprogram implementation
- **Recursion**
- Subprogram parameters



Factorial

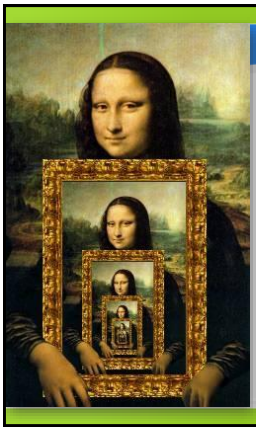
n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
4! = 1 • 2 • 3 • 4 = 24



Factorial

n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
0! = 1

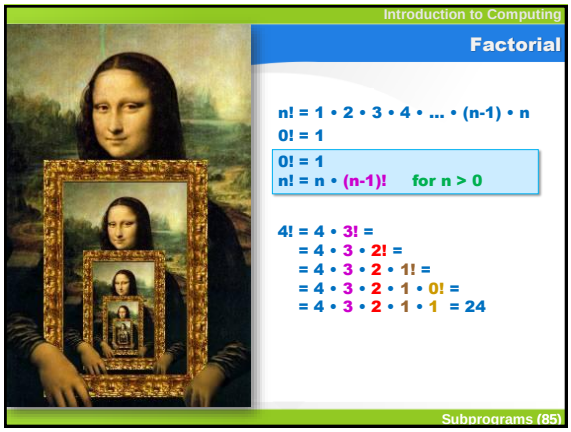
```
def fact(n):
    prod= 1
    j= 2
    while j <= n:
        prod *= j
        j += 1
    return prod
print(fact(4))
```

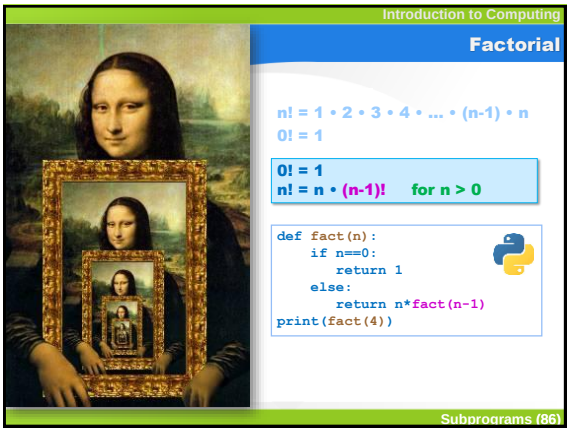



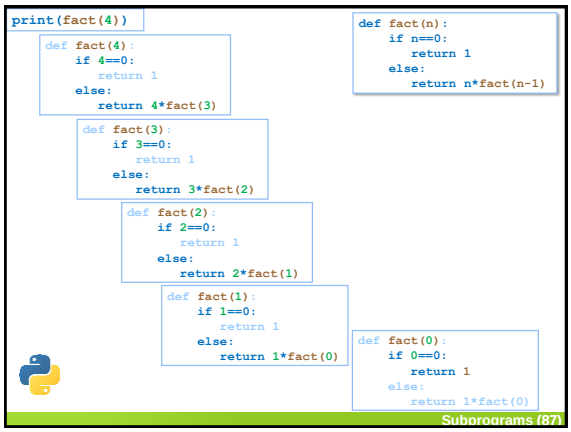
Factorial

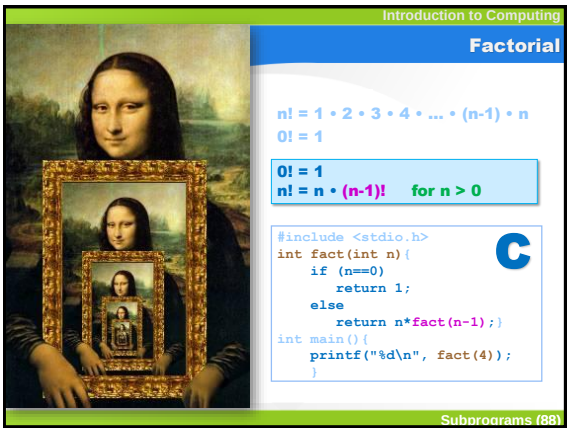
n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
0! = 1

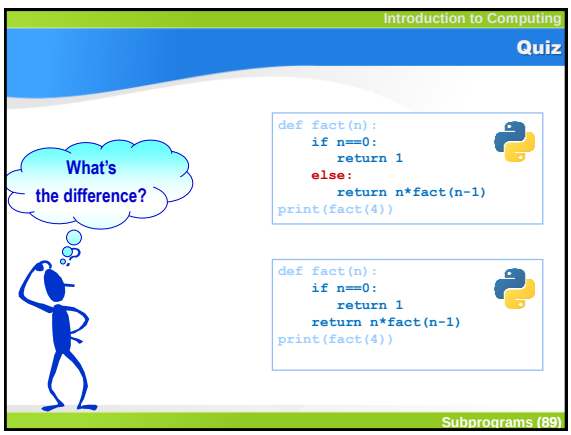
```
#include <stdio.h>
int fact(int n){
    int prod, j;
    prod= 1;
    j= 2;
    while (j <= n){
        prod *= j;
        j += 1; }
    return prod; }
int main(){
    printf("%d\n", fact(4));}
```

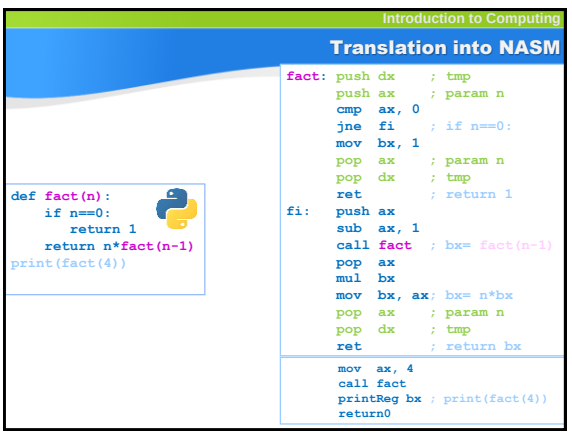

Introduction to Computing
Factorial
n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
0! = 1
0! = 1
n! = n • (n-1)! for n > 0
4! = 4 • 3! =
= 4 • 3 • 2! =
= 4 • 3 • 2 • 1! =
= 4 • 3 • 2 • 1 • 0! =
= 4 • 3 • 2 • 1 • 1 = 24
Subprograms (85)


Introduction to Computing
Factorial
n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
0! = 1
0! = 1
n! = n • (n-1)! for n > 0
def fact(n):
if n==0:
return 1
else:
return n*fact(n-1)
print(fact(4))
Subprograms (86)


print(fact(4))
def fact(4):
if 4==0:
return 1
else:
return 4*fact(3)
def fact(3):
if 3==0:
return 1
else:
return 3*fact(2)
def fact(2):
if 2==0:
return 1
else:
return 2*fact(1)
def fact(1):
if 1==0:
return 1
else:
return 1*fact(0)
def fact(0):
if 0==0:
return 1
else:
return 1*fact(0)
def fact(n):
if n==0:
return 1
else:
return n*fact(n-1)
Subprograms (87)


Introduction to Computing
Factorial
n! = 1 • 2 • 3 • 4 • ... • (n-1) • n
0! = 1
0! = 1
n! = n • (n-1)! for n > 0
#include <stdio.h>
int fact(int n){
if (n==0)
return 1;
else
return n*fact(n-1);}
int main(){
printf("%d\n", fact(4));
}
C
Subprograms (88)


Introduction to Computing
Quiz
What's the difference?
def fact(n):
if n==0:
return 1
else:
return n*fact(n-1)
print(fact(4))
def fact(n):
if n==0:
return 1
return n*fact(n-1)
print(fact(4))
Subprograms (89)

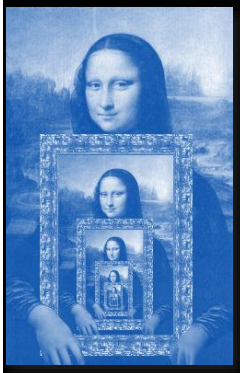

Introduction to Computing
Translation into NASM
def fact(n):
if n==0:
return 1
return n*fact(n-1)
print(fact(4))
fact: push dx ; tmp
push ax ; param n
cmp ax, 0
jne fi ; if n==0:
mov bx, 1
pop ax ; param n
pop dx ; tmp
ret ; return 1
fi: push ax
sub ax, 1
call fact ; bx= fact(n-1)
pop ax
mul bx
mov bx, ax; bx= n*bx
pop ax ; param n
pop dx ; tmp
ret ; return bx
mov ax, 4
call fact
printReg bx ; print(fact(4))
return0

How many digits – Recursion

```
def len(n, b):
    L= 1
    while n > b-1:
        n //= b
        L+= 1
    return L
dig= len(65, 10)
print(dig)
dig= len(65,  8)
print(dig)
```

```
def len(n, b):
    if n < b-1:
        return 1
    return 1 + len(n//b, b)

dig= len(65, 10)
print(dig)
dig= len(65,  8)
print(dig)
```



Subprograms

- Functions and procedures
- Stack
- Subprogram implementation
- Recursion
- Subprogram parameters

Subroutine parameters

```
X= 1
Y= 2
print(X, Y)
```

```
1 2
```

Subroutine parameters

```
def swap1(a, b):

    tmp= a
    a= b
    b= tmp
    return

X= 1
Y= 2
print(X, Y)
swap1(X, Y)
print(X, Y)
```

```
1 2
? ?
```

Subroutine parameters

```
def swap1(a, b):

    tmp= a
    a= b
    b= tmp
    return

X= 1
Y= 2
print(X, Y)
swap1(X, Y)
print(X, Y)
```

```
1 2
1 2
```

```
#include <stdio.h>
void swap1(int a, int b){
    int  tmp;
    tmp= a;
    a= b;
    b= tmp;
    return; }
int main(void){
    int X, Y;
    X= 1;  Y= 2;
    printf("%d %d\n", X, Y);
    swap1(X, Y);
    printf("%d %d\n", X, Y);}
```

```
1 2
1 2
```

C

Subroutine parameters

```
def swap1(a, b):

    tmp= a
    a= b
    b= tmp
    return

X= 1
Y= 2
print(X, Y)
swap1(X, Y)
print(X, Y)
```

```
1 2
1 2
```

```
def swap2(a, b):
    return b, a

X= 1
Y= 2
print(X, Y)
X, Y = swap2(X, Y)
print(X, Y)
```

```
1 2
2 1
```

Introduction to Computing

Subroutine parameters

```
def swap1(a, b):

    tmp= a
    a= b
    b= tmp
    return

X= 1
Y= 2
print(X, Y)
swap1(X, Y)
print(X, Y)
```

```
1 2
1 2
```

```
X= 1
Y= 2
print(X, Y)
X, Y = Y, X
print(X, Y)
```

```
1 2
2 1
```

Subprograms (97)

Introduction to Computing

Parameter passing by reference

```
#include <stdio.h>
void swap1(int a, int b){
    int  tmp;
    tmp= a;
    a= b;
    b= tmp;
    return; }
int main(void){
    int X, Y;
    X= 1;  Y= 2;
    printf("%d %d; ", X, Y);
    swap1(X, Y);
    printf("%d %d\n", X, Y);}
```

```
1 2
1 2
```

C

```
#include <stdio.h>
void swap1(int *a, int *b){
    int  tmp;
    tmp= *a;
    *a= *b;
    *b= tmp;
    return; }
main(void){
    int X, Y;
    X= 1;  Y= 2;
    printf("%d %d\n", X, Y);
    swap1(&X, &Y);
    printf("%d %d\n", X, Y);}
```

scanf("%d", &x);

```
1 2
2 1
```

C

Subprograms (98)

Introduction to Computing

Parameter passing by reference

```
#include <stdio.h>
void swap1(int a, int b){
    int  tmp;
    tmp= a;
    a= b;
    b= tmp;
    return; }
int main(void){
    int X, Y;
    X= 1;  Y= 2;
    printf("%d %d; ", X, Y);
    swap1(X, Y);
    printf("%d %d\n", X, Y);}
```

```
1 2
1 2
```

C

Variable pointed by a

```
#include <stdio.h>
void swap1(int *a, int *b){
    int  tmp;
    tmp= *a;
    *a= *b;
    *b= tmp;
    return; }
int main(void){
    int X, Y;
    X= 1;  Y= 2;
    printf("%d %d\n", X, Y);
    swap1(&X, &Y);
    printf("%d %d\n", X, Y);}
```

Pointer to int

```
1 2
2 1
```

C

Subprograms (99)

Introduction to Computing

Pointers

```
#include <stdio.h>
int main(void){
    int A, B, *Adr;
    A=3;
    B=4;
    Adr= &A;     // *Adr == A
    B= B + *Adr;
    printf("%d %d\n", A, B);}
```

```
3 7
```

C

Subprograms (100)

Introduction to Computing

Arrays as parameters

```
def swap(a):

    tmp = a[0]
    a[0]= a[1]
    a[1]= tmp
    return
X= [0]*3
X[0]= 1
X[1]= 2
print(X[0],X[1])
swap (X)
print(X[0],X[1])
```

```
1 2
2 1
```

```
#include <stdio.h>
void swap(int a[]){
    int  tmp;
    tmp = a[0];
    a[0]= a[1];
    a[1]= tmp;
    return; }
int main(void){
    int X[3];
    X[0]= 1;  X[1]= 2;
    printf("%d %d\n", X[0],X[1]);
    swap(X);
    printf("%d %d\n", X[0],X[1]);}
```

```
1 2
2 1
```

C

Subprograms (101)

Introduction to Computing

Functions as parameters

Sigma(From, To, f)

$$\sum_{j=\text{From}}^{\text{To}} f(j)$$

$$\sum_{j=1}^{4} j! = \sum_{j=1}^{4} \text{fact}(j)$$

Subprograms (102)

Functions as parameters

```
def Sigma(From, To, F):



def fact(n):
    if n==0:
       return 1
    return n*fact(n-1)
print(Sigma(1, 4, fact))
```

```
#include <stdio.h>
int Sigma(int From, int To,
          int (*F)(int n)){



int fact(int n){
    if (n==0)
       return 1;
    return n*fact(n-1);}
int main(){
    printf("%d\n",
           Sigma(1, 4, fact)); }
```

Functions as parameters

```
def Sigma(From, To, F):

    Sum= 0
    j= From
    while j <= To:
        Sum+= F(j)
        j+= 1
    return Sum
```

```
int Sigma(int From, int To,
          int (*F)(int n)){
    int j, Sum;
    Sum= 0;
    j= From;
    while (j <= To){
       Sum+= F(j);
       j+= 1; }
    return Sum; }
```

Functions as parameters

```
def Sigma(From, To, F):
    Sum= 0
    j= From
    while j <= To:
        Sum+= F(j)
        j+= 1
    return Sum
def fact(n):
    if n==0:
       return 1
    return n*fact(n-1)
print(Sigma(1, 4, fact))
```

33

```
#include <stdio.h>
int Sigma(int From, int To,
          int (*F)(int n)){
    int j, Sum;
    Sum= 0;
    j= From;
    while (j<=To){
       Sum+= F(j);
       j+= 1; }
    return Sum; }
int fact(int n){
    if (n==0)
       return 1;
    return n*fact(n-1);}
int main(){
    printf("%d\n",
           Sigma(1, 4, fact)); }
```

33