

1 Machine Dynamics - Assignment 1

Student ID: D08522005

Student Name: 張元

1.1 Part I

1.1.1 Q2 Statics

Calculate the reaction forces at all joints and the required torque on Link 2 to achieve static balance when θ_2 is equal to 90 degree. List all the data in a table.

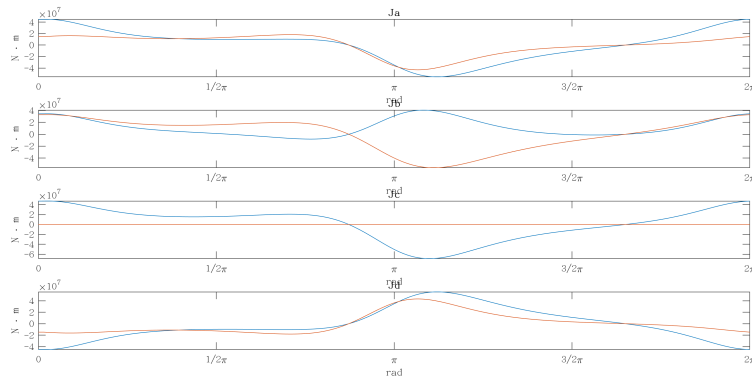
| Joint | Reaction Force (N) | Required Torque ($N \cdot m$) |
|-------|------------------------|---------------------------------|
| A | 1035.4742 | 0 |
| B | 1036.2480 | 0 |
| C | 1036.5765 | 0 |
| D | 1044.4153 | 0 |

1.2 Part II

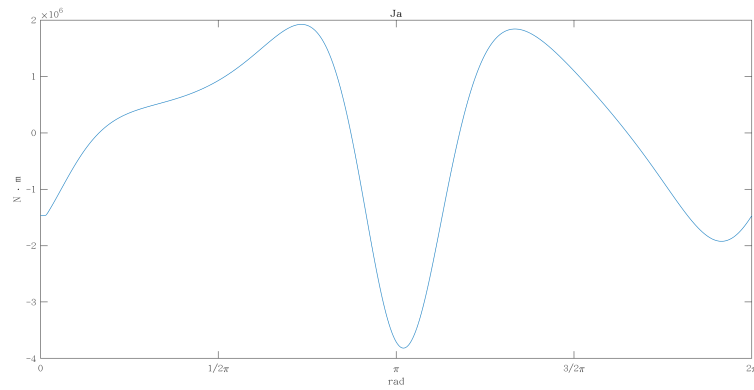
1.2.1 Q3 Kinetostatics

Calculate the reaction force at all joints and the required torque on Link 2 when θ_2 varies from θ to 360 degree (interval ≤ 1 degree). Take the angle of Link 2 (θ_2) as the horizontal axis to draw plots for these variables.

The reaction forces of each joint splitted with x and y axis: (Ja ~ Jd)



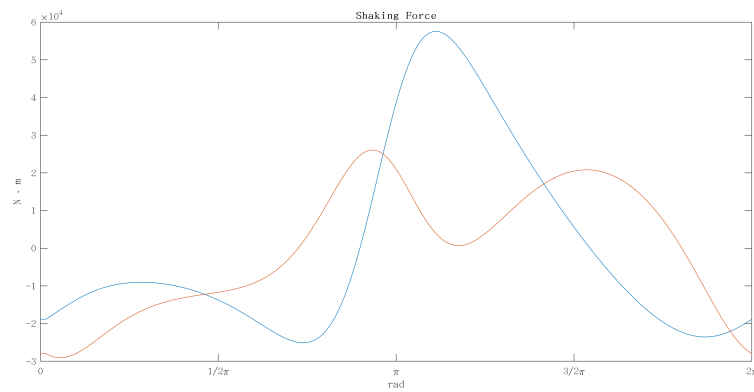
The required torque on Joint A:



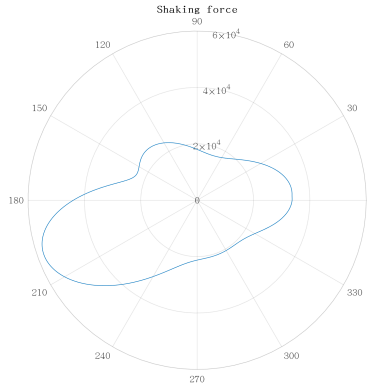
1.2.2 Q4

Continued from 3, draw (a) the plots of the x and y components of the shaking force with θ_2 as the horizontal axis, and (b) the polar plots of the shaking force and shaking moment.

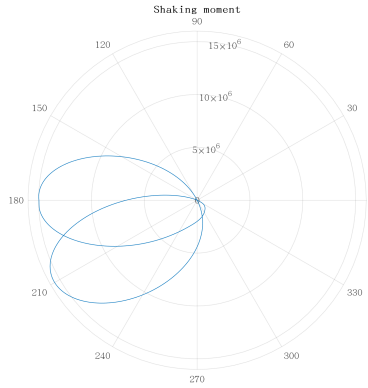
The shaking force is composed by Joint A and Joint D based on the frame.



The polar plot of shaking force. (Composed)



The shaking moment can be obtained by $M_S = \overrightarrow{R_1} \times \overrightarrow{F_{41}} + \overrightarrow{T_{21}}$.



1.2.2.1 a. What is the maximum input torque? When does it happen? Use degree as the unit and be accurate to 2 decimal places.

According to the torque of Joint A, the extremum of input torque is $3.8172 \times 10^6 \text{ N} \cdot \text{m}$ at $\theta_2 = 183.9195 \text{ deg}$.

1.2.2.2 b. What are the maximum shaking force and shaking moment? When do they happen? Use degree as the unit and be accurate to 3 decimal places.

According to the polar plot, the maximum shaking force is 57694.7620 N at $\theta_2 = 199.6040 \text{ deg}$; the maximum shaking moment is $1556.5653 \times 10^4 \text{ N} \cdot \text{m}$ at $\theta_2 = 209.5842 \text{ deg}$.