

Connection with MAP:

Exercise 1:

1.1) $C_4^3 C_{28}^2$

1.2) $C_4^4 C_{28}^1$

1.6) $C_4^2 C_{30}^3 = 6 \times \frac{30!}{27!3!} = 6 \times \frac{30 \times 29 \times 27}{6}$

1.3) $\begin{matrix} \text{Ar} & \text{Roi.} \\ \downarrow & \downarrow \\ C_4^2 & C_4^2 \end{matrix} C_{24}^1 = 6 \times 6 \times 24$

1.4) $4^5 = 1024$

1.5) $8 \times 28 = 224$

Exercise 2:

x_i	p_i	g_i
0	0,5487	-1
1	0,3472	1
2	0,0894	2
3	0,0046	3

$E(X) = \frac{-17}{216} \approx -0,0787$

$G' = G^2 - \mu^2$
 $E(G') = E(G^2) - \mu^2$
 $(= \text{Var}(G))$
 $= 1,245$

Exercise 3:

1) $\Omega = \{(G, G), (G, F), (F, G), (F, F)\}$

$P(A) = \frac{2}{4} (= GF, FG)$

$P(B) = \frac{3}{4} (= GG, GF, FF)$

$P(A \cap B) = \frac{2}{4}$

$P(A) \times P(B)$ done A et B ne sont pas indépendants

2) $\Omega' = \{(a, b, c), a, b \in \{F, C\}\}$ and $|\Omega'| = 8$

$P(A) = 1 - \frac{2}{8} = \frac{6}{8}$

$P(B) = \frac{4}{8}$

$P(A \cap B) = P(C \cap C) = \frac{3}{8}$

$P(A) \times P(B) = \frac{6}{8} \times \frac{4}{8} = \frac{3}{8}$