

# Applied Statistic with R

Fall 2019, ASDS, YSU

## Midterm 1 Material Coverage

Exam Time and Place: October 29, 18:30 - 23:00, #241 YSU MMF

### 1 Descriptive Statistics

#### 1. Introduction

- Populations and Samples; Observation, Variable and Parameter; Statistics (numerical characteristic of a Sample)
- Sampling: Representative Sample; Sampling Methods (Systematic, Stratified, Cluster)
- Types of Variables (Features)
- Measurement Levels

#### 2. Exploratory Data Analysis for Univariate Data: Graphical Summaries

- Frequency and Relative Frequency Tables
- BarPlot, Frequency Polygon
- Empirical Distribution Function
- Frequency, Relative Frequency and Density Histograms
- Stem-and-Leaf Plots

#### 3. Exploratory Data Analysis for Univariate Data: Numerical Summaries

- Order Statistics (Ranks)
- Statistics for the central tendency
  - The Sample Mean, Trimmed Mean, Weighted Mean, Winsorized Mean
  - The Sample Median
  - The Sample Mode
- Statistics for the Spread/Variability
  - Deviations (from the Mean, from the Median), Absolute Deviations
  - The Range
  - The Sample Variance and Standard Deviation (with  $n$  or  $n - 1$  in the denominators)
  - Properties of the Sample Variance
  - The Mean Absolute Deviation (MAD) from the Mean or Median

#### 4. Exploratory Data Analysis for Univariate Data: Quantiles and BoxPlots

- Sample Quartiles
- The InterQuartile Range, IQR
- BoxPlot
- Outliers (BoxPlot Method)
- Sample Quantiles
- Theoretical Quantiles

#### 5. Exploratory Data Analysis for Bivariate Data

- ScatterPlot
- Q-Q Plot (Data vs Data, Data vs Distribution, Distribution vs Distribution)
- Sample Covariance and the (Pearson's) Correlation Coefficient
- Properties of Sample Covariance and Correlation Coefficient
- Spearman's  $\rho$  and Kentall's  $\tau$

#### 6. Probability Refresher

- R.V.s and their main characteristics
- Important Discrete and Continuous Distributions

#### 7. Convergence of Random Variables

- Convergence almost sure
- Convergence in Probability
- Convergence in Quadratic Mean
- Convergence in Distributions
- Relationship between the convergence types
- Properties of Convergent Sequences of RVs
- Standardization; the Weak and Strong LLN
- The CLT

#### 8. Parametric Inference and Point Estimation

- Parametric Modeling, The Problem of the Point Estimation
- Statistics and Estimators, Estimates
- MSE and Comparison of Estimators
- Properties of Estimators:
  - Bias, Unbiasedness, Asymptotic Unbiasedness,
  - Consistency, Strong Consistency, Weak Consistency