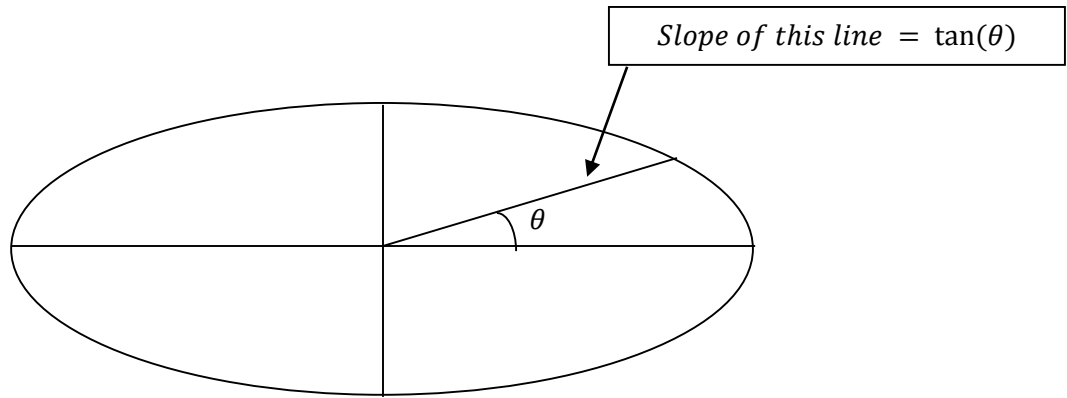


## Partial Solution to ellipsoid Problem

Given:

- user HAS to specify a  $\varphi$  value of  $\frac{\pi}{2}$  **or**  $\pi$
- User specifies a value for  $\theta$  with the idea of spherical coordinates in mind



Equation of the line from the origin

- $y = \tan(\theta) x$
- $\frac{1}{x} = \frac{\tan(\theta)}{y}$
- $x = \frac{y}{\tan(\theta)}$

Lower bound for  $x$

Equation of ellipse in  $xy$  plane:

- $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$

Solving the equation for  $x$  in the  $xy$  plane:

- $\frac{x^2}{a^2} = 1 - \frac{y^2}{b^2}$
- $x = \pm a \sqrt{1 - \frac{y^2}{b^2}}$

Upper bound for  $x$

Solving for  $x$  bounds:

- $x = m(y^2) + a$
- $0 = m(b^2) + a$
- $-\frac{a}{b^2} = m$
- $x = -\frac{a}{b^2}(y^2) + a$

When  $x$  is 0,  $y$  is  $b^2$

Solve for  $m$

Setting the equations equal to each other to find the  $y$  value where the two equations intersect

- $\frac{y}{\tan(\theta)} = a\sqrt{1 - \frac{y^2}{b^2}}$
- $\frac{y^2}{\tan^2(\theta)} = a^2\left(1 - \frac{y^2}{b^2}\right)$
- $\frac{y^2}{a^2\tan^2(\theta)} = \left(1 - \frac{y^2}{b^2}\right)$
- $\frac{y^2}{a^2\tan^2(\theta)} + \frac{y^2}{b^2} = 1$
- $y^2\left(\frac{1}{a^2\tan^2(\theta)} + \frac{1}{b^2}\right) = 1$
- $y^2\left(\frac{b^2}{a^2b^2\tan^2(\theta)} + \frac{a^2\tan^2(\theta)}{a^2b^2\tan^2(\theta)}\right) = 1$
- $y^2 = \frac{a^2b^2\tan^2(\theta)}{b^2 + a^2\tan^2(\theta)}$
- $y = \frac{ab(\tan(\theta))}{\sqrt{b^2 + a^2\tan^2(\theta)}}$

Upper bound for  $y$

Triple integral:

$$\int_0^{\frac{ab(\tan(\theta))}{\sqrt{b^2 + a^2\tan^2(\theta)}}} \int_{\frac{y}{\tan(\theta)}}^{a\sqrt{1 - \frac{y^2}{b^2}}} \int_0^{c\sqrt{1 - \frac{x^2}{a^2} - \frac{y^2}{b^2}}} dz dx dy$$

**\*This definite integral will be the algorithm\***