

Date

NAME- Anshul Aery
Class: KKG-1B
Subject: CC

1) Given three integers x, a, b return x th magical no. Since the ans may be very large return $10^9 + 1$ if.

Approach

1) We count no. of multiples of a
 $L = X$ (X is a trial value)
ie X/a

2) Same way we count multiples of b
ie X/b

3) No. of multiples of both a and b
ie $X/\text{lcm}(a, b)$

So

total numbers that are $L = X$

$$\text{count}(X) = \frac{X}{a} + \frac{X}{b} - \frac{X}{\text{lcm}(a, b)}$$

Now

we need smallest x such that $\text{count}(x) \geq x$

Set $\text{low} = 1$

$\text{high} = x \cdot \min(a, b)$

$\text{mid} = (\text{low} + \text{high}) / 2$

Special

$$L=10^8 \quad R=10^9 \quad lcm = \frac{a \times b}{gcd}$$

Date

for mid
compute

$$count = \frac{mid}{a} + \frac{mid}{b} - \frac{mid}{lcm}$$

if $count \geq x$

mid could be ans.

~~no~~ search left side

else

search right side

return the final ans.

Time complexity:

$$\text{Binary search runs in } = O(\log(\text{common}(a, b)))$$