

Acm Code Library

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头文件

```
#include <cstdio>
```

```
#include <cstring>
```

```
#include <iostream>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <vector>
```

```
#include <queue>
```

```
#include <stack>
```

```
#include <set>
```

```
#include <map>
```

```
//#include <tr1/unordered_set>
```

```
//#include <tr1/unordered_map>
```

```
#include <bitset>
```

```
//#pragma comment(linker, "/STACK:1024000000,1024000000")
```

```
#define lson l, m, rt<<1
```

```
#define rson m+1, r, rt<<1|1
```

```
#define inf 1e9
```

```
#define debug(a) cout << #a " = " << (a) << endl;
```

```
#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << " ] = " << (a)[i]
```

```
<< endl; }

#define clr(x, y) memset(x, y, sizeof x)

#define LL long long

#define uLL unsigned LL

using namespace std;
```

输入输出挂

```
template<class T>

inline bool read(T &n)

{

    T x = 0, tmp = 1;

    char c = getchar();

    while ((c < '0' || c > '9') && c != '-' && c != EOF) c = getchar();

    if (c == EOF) return false;

    if (c == '-') c = getchar(), tmp = -1;

    while (c >= '0' && c <= '9') x *= 10, x += (c - '0'), c = getchar();

    n = x*tmp;

    return true;

}

template <class T>

inline void write(T n)
```

```

{

    if (n < 0)

    {

        putchar('-');

        n = -n;

    }

    int len = 0, data[20];

    while (n)

    {

        data[len++] = n % 10;

        n /= 10;

    }

    if (!len) data[len++] = 0;

    while (len--) putchar(data[len] + 48);

}

```

bitset

#include <bitset> // 正常情况 加速 32 倍 可能还要加速更多

```

bitset<n>p;

```

`b.any()` b 中是否存在置为 1 的二进制位？

`b.none()` b 中不存在置为 1 的二进制位吗？

`b.count()` b 中置为 1 的二进制位的个数

`b.size()` b 中二进制位的个数

`b[pos]` 访问 b 中在 pos 处的二进制位

`b.test(pos)` b 中在 pos 处的二进制位是否为 1？

`b.set()` 把 b 中所有二进制位都置为 1

`b.set(pos)` 把 b 中在 pos 处的二进制位置为 1

`b.reset()` 把 b 中所有二进制位都置为 0

`b.reset(pos)` 把 b 中在 pos 处的二进制位置为 0

`b.flip()` 把 b 中所有二进制位逐位取反

`b.flip(pos)` 把 b 中在 pos 处的二进制位取反

`b.to_ulong()` 用 b 中同样的二进制位返回一个 unsigned long 值

`os << b` 把 b 中的位集输出到 os 流

以及所有位操作。

```
#include <bitset>
```

```
using std::bitset;
```

```
bitset<32> bitvec; //32 位，全为 0。
```

`bitset<n> b;` `b` 有 `n` 位, 每位都为 0

`bitset<n> b(u);` `b` 是 unsigned long 型 `u` 的一个副本

`bitset<n> b(s);` `b` 是 string 对象 `s` 中含有的位串的副本

`bitset<n> b(s, pos, n);` `b` 是 `s` 中从位置 `pos` 开始的 `n` 个位的副本

hdu 5413 $n \leq 2e4$

普通 n^2 111.363s

bitset 2.385s

离散化

```
int sub[maxn], len, n, A[maxn];

int main()

{

    while (~scanf("%d", &n))

    {

        len = 0;

        for (int i = 0; i < n; i++)

        {

            scanf("%d", &A[i]);

            sub[len++] = A[i];

        }

        sort(sub, sub + len);

        len = unique(sub, sub + len) - sub;

        for (int i = 0; i < n; i++)

            A[i] = lower_bound(sub, sub + len, A[i]) - sub + 1;

    }

    return 0;

}
```

多重背包

```
int dp[maxn];

int w[maxn], v[maxn], c[maxn];

int n, C;

void f()
{
    clr(dp, 0);

    for (int i = 0; i < n; i++)
    {
        int cnt = c[i];

        int k = 1;

        while (cnt >= k)
        {
            for (int j = C; j >= w[i] * k; j--)
            {
                dp[j] = max(dp[j], dp[j - w[i] * k] + v[i] * k);
            }
        }
    }
}
```

```

    }

    cnt -= k;

    k <= 1;

}

if (cnt)

{

    k = cnt;

    for (int j = C; j >= w[i] * k; j--)

    {

        dp[j] = max(dp[j], dp[j - w[i] * k] + v[i] * k);

    }

}

}

}

```

数位 DP

```
#include<cstdio>
```

```
#include<cstdlib>
```

```
#include<algorithm>
```

```
#include<cmath>
```

```
#include<cstring>
```

```

#include<iostream>

using namespace std;

typedef long long LL;

const int MAX_N = 1010;

const int MAX_K = 10;


int num[9];

int dp[9][2];


/*len : 表示长度

s : 当前的状态 ( 对于此题就是上一位是否是6 )

fp : 表示之前的状态是否充满的 ( 如果说充满的此处的放置就是有限制的 否则就可以随便放 )

*/

int dfs(int len, int s, bool fp)

{

    if (len == 0) return 1;

    if (!fp&&dp[len][s] != -1) return dp[len][s];

    int res = 0;

    int fmax = fp ? num[len] : 9;          //根据充满状态选择限制条件

    for (int i = 0; i <= fmax; i++)

    {

        if (i == 4 || s&&i == 2) continue; //跳过62和4的情况
    }

```

```

        res += dfs(len - 1, i == 6, fp&& i == fmax);

    }

    return fp ? res : dp[len][s] = res;

}

int solve(int n)

{

    int len = 0;

    while (n != 0)

    {

        num[++len] = n % 10;

        n /= 10;

    }

    return dfs(len, 0, 1);

}

int main()

{

    int n, m;

    memset(dp, -1, sizeof(dp));

    while (scanf("%d%d", &n, &m), n | m){

        printf("%d\n", solve(m) - solve(n - 1));

    }

    return 0;

```

```
}
```

快速幂运算

```
struct mat
```

```
{
```

```
    int m[100][100];
```

```
};
```

```
int n;
```

```
mat mul(mat a, mat b)
```

```
{
```

```
    mat c;
```

```
    clr(c.m, 0);
```

```
    for (int k = 1; k <= n; k++)
```

```
        for (int i = 1; i <= n; i++) if (a.m[i][k])
```

```
            for (int j = 1; j <= n; j++)
```

```
                c.m[i][j] += a.m[i][k] * b.m[k][j];
```

```
}
```

```
mat add(mat a, mat b)
```

```

{

    mat c;

    for (int i = 1; i <= n; i++)

        for (int j = 1; j <= n; j++)

            c.m[i][j] = a.m[i][j] + b.m[i][j];

}

```

```

mat re;

```

```

mat sum_pow_mat(mat a, int n)

```

```

{

    if (n % 2)

    {

        if (n == 1) return re = a;

        mat p = sum_pow_mat(a, n - 1);

        re = mul(re, a);

        return add(a, mul(a, p));

    }

    else

    {

        mat p = sum_pow_mat(a, n / 2);

        mat ans = add(p, mul(p, re));

    }

}

```

```

        re = mul(re, re);

        return ans;
    }
}

```

KMP

```

vector<int> ans;

void getFail(char *P, int *f)
{
    int m = strlen(P);

    f[0] = 0;

    f[1] = 0;

    for (int i = 1; i < m; i++)
    {
        int j = f[i];
    }
}

```



```

        while (j&&P[i] != P[j]) j = f[j];

        f[i + 1] = P[i] == P[j] ? j + 1 : 0 ;

    }

}

void find(char *T, char *P, int *f)

{

    int n = strlen(T), m = strlen(P);

    getFail(P, f);

    int j = 0;

    for (int i = 0; i < n; i++)

    {

        while (j&&P[j] != T[i]) j = f[j];

        if (P[j] == T[i]) j++;

        if (j == m) ans.push_back(i - m + 1);

    }

}

```

后缀数组

```
#include <string.h>
```

```
const int maxn = 1e5;
```

```
#define FOR(i,a,b) for(i=a; (a<b)?(i<=b):(i>=b) ; (a<b)?(i++):(i--) )
```

```
struct suffix_array
```

```
{
```

```
    char s[maxn];
```

```
    int sa[maxn], t[maxn], t2[maxn], c[maxn];
```

```
    int m, n;
```

```
    ///构造sa数组
```

```
    void build_sa()
```

```
    {
```

```
        int i, *x = t, *y = t2;
```

```
        FOR(i, 0, m - 1) c[i] = 0;
```

```
        FOR(i, 0, n - 1) c[x[i]] = s[i]++;
```

```
        FOR(i, 1, m - 1) c[i] += c[i - 1];
```

```
        FOR(i, n - 1, 0) sa[--c[x[i]]] = i;
```

```
        for (int k = 1; k <= n; k <<= 1)
```

```
        {
```

```
            int p = 0;
```

```
            FOR(i, n - k, n - 1) y[p++] = i;
```

```

FOR(i, 0, n - 1) if (sa[i] >= k) y[p++] = sa[i] - k;

FOR(i, 0, m - 1) c[i] = 0;

FOR(i, 0, n - 1) c[x[y[i]]]++;

FOR(i, 0, m - 1) c[i] += c[i - 1];

FOR(i, n - 1, 0) sa[--c[x[y[i]]]] = y[i];

swap(x, y);

p = 1;

x[sa[0]] = 0;

FOR(i, 1, n - 1)

    x[sa[i]] = y[sa[i - 1]] == y[sa[i]] &&

        y[sa[i - 1] + k] == y[sa[i] + k] ? p - 1 : p++;

    if (p >= n) break;

    m = p;

}

}

///匹配模式串

int len;

int cmp(char *pa, int p)

{

    return strncmp(pa, s + sa[p], len);

}

int find_first(char *P)

```

```

{

    len = strlen(P);

    if (cmp(P, 0)<0) return -1;

    if (cmp(P, n - 1)>0) return -1;

    int L = 0, R = n - 1, ans = n;

    while (R >= L)

    {

        int M = L + (R - L) / 2;

        int res = cmp(P, M);

        if (res <= 0)

        {

            R = M - 1;

            if (res == 0) ans = min(ans, M);

        }

        else L = M + 1;

    }

    if (ans == n) return -1;

    else return ans;

}

int find_last(char *P)

{

    len = strlen(P);

```

```

    if (cmp(P, 0)<0) return -1;

    if (cmp(P, n - 1)>0) return -1;

    int L = 0, R = n - 1, ans = -1;

    while (R >= L)

    {

        int M = L + (R - L) / 2;

        int res = cmp(P, M);

        if (res >= 0)

        {

            L = M + 1;

            if (res == 0) ans = max(ans, M);

        }

    }

    return ans;

}

///构造rank , height数组

int rank[maxn], height[maxn];

void getHeight()

{

    int i, j, k = 0;

    for (int i = 0; i < n; i++) rank[sa[i]] = i;

    for (int i = 0; i < n; i++)

```

```

    {

        if (k) k--;

        int j = sa[rank[i] - 1];

        while (s[i + k] == s[j + k]) k++;

        height[rank[i]] = k;

    }

}

int d[maxn][30], flog[maxn];

void RMQ_init()

{

    for (int i = 0; i < n; i++) d[i][0] = height[i];

    flog[0] = -1;

    for (int i = 1; i < n; i++) flog[i] = flog[i >> 1] + 1;

    for (int j = 1; (1 << j) <= n; j++)

        for (int i = 0; i + (1 << j) <= n; i++)

            d[i][j] = min(d[i][j - 1], d[i + (1 << (j - 1))][j - 1]);

}

int RMQ(int L, int R)

{

    int k = flog[R - L + 1];

    return min(d[L][k], d[R - (1 << k) + 1][k]);

}

```

```

int query(int j, int k)

{

    if (j == k) return n - k;

    if (rank[j]>rank[k]) swap(j, k);

    return RMQ(rank[j] + 1, rank[k]);

}

void init(char *ss, int mm = 200)

{

    strcpy(s, ss);

    n = strlen(s);

    m = mm;

}

int all()

{

    build_sa();

    getHeight();

    RMQ_init();

}

}sp;

```

字符串 Hash

/*题意：

给出两个串A，B，让你找出B串在A串中匹配的第一个位置，匹配要求可以有最多两个位置不一样。

解法：

首先将A，B串的hash值求出来，然后就可以O(1)来求出每个子串的hash值了，判位置最裸的方法

就是枚举每一个位置然后O(n)的判是否匹配，复杂度是O(n^2)，然后我们可以通过二分来加速判匹

配的过程将其将成O(logn)的复杂度，具体操作如下：

二分一个求一个最长的匹配长度，然后跳过一个不匹配的位置然后再用一次二分求一个最长匹配长

度，如此循环两次，如果求出来的最长匹配的长度+不匹配位置数（0 or 1 or 2）等于B串长的话就

表明找到了一个符合条件的位置。*/

```
#include <iostream>
```

```
#include <cstdio>
```

```
#include <cstdlib>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <cstring>
```

```
#include <vector>
```



```

#include <queue>

#include <stack>

#include <set>

#include <vector>

//#pragma comment(linker, "/STACK:1024000000,1024000000")

#define lson l, m, rt<<1

#define rson m+1, r, rt<<1|1

#define inf 1e9

#define debug(a) cout << #a" = " << (a) << endl;

#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << "]" = " << (a)[i]

<< endl; }

#define clr(x, y) memset(x, y, sizeof x)

using namespace std;

typedef unsigned long long uLL;

const int maxn = 100005;

const uLL magic = 7;

uLL base[maxn];

uLL hash_a[maxn], hash_b[maxn];

```

```
char s1[maxn], s2[maxn];
```

```
void init_hash(int len, char cc[], uLL ha[])
```

```
{  
  
    ha[0] = 0;  
  
    for (int i = 1; i <= len; i++)  
  
        ha[i] = ha[i - 1] * magic + cc[i - 1];  
  
    base[0] = 1;  
  
    for (int i = 1; i <= len; i++)  
  
        base[i] = base[i - 1] * magic;  
  
}
```

```
uLL sub_hash(uLL ha[], int L, int R)
```

```
{  
  
    return ha[R] - ha[L] * base[R - L];  
  
}
```

```
bool cmp(int La, int Ra, int Lb, int Rb)
```

```
{  
  
    uLL ua = sub_hash(hash_a, La, Ra);  
  
    uLL ub = sub_hash(hash_b, Lb, Rb);
```

```

        if (ua == ub) return true;

        else return false;

    }

```

```

int get_max(int La, int Lb, int len)

{

    int st = -1, ed = len + 1;

    while (ed - st > 1)

    {

        int m = (st + ed) >> 1;

        if (cmp(La, La + m, Lb, Lb + m) == true) st = m;

        else ed = m;

    }

    return st;

}

```

```

int main()

{

    //freopen("input.txt", "r", stdin);

    int T;

    scanf("%d", &T);

```

```

for (int kk = 1; kk <= T; kk++)

{

    scanf("%s%s", s1, s2);

    int len_a = strlen(s1);

    int len_b = strlen(s2);

    init_hash(len_a, s1, hash_a);

    init_hash(len_b, s2, hash_b);

    //debugarry(hash_a, len_a+1); debugarry(hash_b, len_b+1);

    int ans = -1;

    for (int i = 0; i + len_b - 1 < len_a; i++)

    {

        int ptr_a = i, ptr_b = 0;

        int sum = 0, cnt = 0;

        while (cnt <= 2)

        {

            int maxlen = get_max(ptr_a, ptr_b, len_b - ptr_b);

            sum += maxlen;

            if (sum + cnt == len_b)

            {

                ans = i;

                break;

            }

        }

    }

```

```

        else

        {

            cnt++;

            ptr_a += maxlen + 1;

            ptr_b += maxlen + 1;

        }

    }

    //debug(sum);

    if (ans != -1) break;

}

printf("Case #%%d: %%d\\n", kk, ans);

}

return 0;

}

```

Hash another :

```
#define ULL long long
```

```
cons ULL x = 233;
```

```
ULL pow_x[maxn];
```

```

void Hash_init(char *T, ULL *H)
{
    int len = strlen(T);

    pow_x[0] = 1ull;

    for (int i = 1; i <= len; i++)

        pow_x[i] = pow_x[i - 1] * x;

    H[len] = 0;

    for (int i = len - 1; i >= 0; i++)

        H[i] = H[i + 1] * x + (ULL)T[i];
}

```

```

void Hash(char *H, int i, int len)
{
    return H[i] - H[i + len] * pow_x[len];
}

```

AC 自动机 和 Trie 树

```

#define cls(p) clr(p,0)

```

```

const int maxn = 1e5;

```

```
const int maxsize = 30;
```

```
struct Trie
```

```
{
```

```
    int ch[maxn][maxsize];
```

```
    int val[maxn];
```

```
    vector<int> vv[maxn];
```

```
    int sz;
```

```
    init()
```

```
    {
```

```
        sz = 1;
```

```
        cls(ch[0]);
```

```
        vv[0].clear();
```

```
    }
```

```
    int idx(int c)
```

```
    {
```

```
        return c - 'a';
```

```
    }
```

```
    void insert(char *s, int v)
```

```
    {
```

```
        int u = 0, n = strlen(s);
```

```
        for (int i = 0; i < n; i++)
```

```

{

    int c = idx(s[i]);

    if (!ch[u][c])

    {

        cls(ch[sz]);

        val[sz] = 0;

        vv[sz].clear();

        ch[u][c] = sz++;

    }

    u = ch[u][c];

}

val[u] = v;

vv.push_back(v);

}

///AC

vector<pair<int, int> > ans;

int last[maxn];

void print(int i, int j)

{

    if (j)

    {

        ans.push_back(make_pair(i, j));

```



```

        printf(i, last[j]);

    }

}

void find(char *T)

{

    ans.clear();

    int n = strlen(T);

    int j = 0;

    for (int i = 0; i < n; i++)

    {

        int c = u = idx(T[i]);

        while (j && !ch[j][c]) j = f[j];

        j = ch[j][c];

        if (val[j]) print(i, j);

        else if (last[j]) print(i, last[j]);

    }

}

int getFail()

{

    queue<int> q;

    for (int c = 0; c < maxsize; c++)

    {

```

```

    int u = ch[0][c];

    if (u)

    {

        f[u] = 0;

        q.push(u);

        last[u] = 0;

    }

}

while (!q.empty())

{

    int r = q.front(); q.pop();

    for (int c = 0; c<maxszie; c++)

    {

        int u = ch[r][c];

        if (!u) continue;

        q.push(u);

        int v = f[r];

        while (v&&!ch[v][c]) v = f[v];

        f[u] = ch[v][c];

        last[u] = val[f[u]] ? f[u] : last[f[u]];

    }

}

```

```
    }  
}
```

ST 表

```
const int maxn = 100000;  
  
//maxn 即数组大小  
  
int flog[(maxn << 1) + 10];  
  
int A[maxn];  
  
int dmax[maxn][30];  
  
int n;  
  
void RMQ_init(int *A) //RMQ 初始化  
{  
    for (int i = 0; i < n; i++) dmax[i][0] = A[i];  
  
    for (int j = 1; (1 << j) <= n; j++)  
        for (int i = 0; i + (1 << j) - 1 < n; i++)  
            dmax[i][j] = max(dmax[i][j - 1], dmax[i + (1 << (j - 1))][j - 1]);  
  
    flog[0] = -1;  
  
    for (int i = 1; i < 2 * maxn; i++) flog[i] = flog[i >> 1] + 1;  
}
```

```

int RMQ(int L, int R) //RMQ 查询
{
    int k = flog[R - L + 1];

    return max(dmax[L][k], dmax[R - (1 << k) + 1][k]);
}

int dsum[maxn][30];

void st_sum_init(int *A)
{
    for (int i = 0; i < n; i++) dmax[i][0] = A[i];

    for (int j = 1; (1 << j) <= n; j++)

        for (int i = 0; i + (1 << j) - 1 < n; i++)

            dmax[i][j] = dmax[i][j - 1] + dmax[i + (1 << (j - 1))][j - 1];

    flog[0] = -1;

    for (int i = 1; i < 2 * maxn; i++) flog[i] = flog[i >> 1] + 1;
}

int st_sum(int L, int R)
{
    if (L > R) return 0;

```

```
int k = flog[R - L + 1];

return dmax[L][k] + st_sum(L + (1 << k), R);

}
```

静态主席树

```
#include <iostream>

#include <cstdio>

#include <cstdlib>

#include <algorithm>

#include <cmath>

#include <cstring>

#include <vector>

#include <queue>

#include <stack>

#include <set>

#include <vector>

#include <deque>

#include <set>

//#pragma comment(linker, "/STACK:1024000000,1024000000")
```

```

#define lson l, (l+r>>1), ls[rt]

#define rson (l+r>>1)+1, r, rs[rt]

#define inf 1e9

#define debug(a) cout << #a" = " << (a) << endl;

#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << "]" = " << (a)[i]
<< endl; }

#define clr(x, y) memset(x, y, sizeof x)

#define LL long long

using namespace std;

const int maxn = 1e5 + 20, maxs = maxn * 20;

#define head(p) ( p >= 0 ? h[p] : 0 )

struct __sad
{
    int ls[maxs], rs[maxs];

    int sum[maxs];

    int h[maxn];

    int si, len;

    void pushup(int rt)
    {

```

```

        sum[rt] = sum[ls[rt]] + sum[rs[rt]];

    }

    void build(int p, int add, int l, int r, int &rt, int rt2)

    {

        if (!rt)

        {

            if (p<l || p>r)

            {

                rt = rt2;

                return;

            }

            sum[si] = ls[si] = rs[si] = 0;

            rt = si++;

        }

        if (l == r)

        {

            sum[rt] = sum[rt2] + add;

            return;

        }

        build(p, add, lson, ls[rt2]);

        build(p, add, rson, rs[rt2]);

        pushup(rt);

```

```

}

void init(int *A, int n)

{

    clr(h, 0);

    si = 1;

    ls[0] = rs[0] = sum[0] = 0;

    len = n;

    for (int i = 0; i < n; i++)

    {

        build(A[i], 1, 0, n, head(i - 1));

    }

}

int query(int k, int l, int r, int rt, int rt2)

{

    if (l == r) return l;

    int nk = sum[ls[rt]] - sum[ls[rt2]];

    if (nk >= k) return query(k, lson, ls[rt2]);

    return query(k - nk, rson, rs[rt2]);

}

int query(int L, int R, int k)

{

    return query(k, 0, len, head(R), head(L - 1));

```



```
}  
  
};
```

动态主席树

用于解决动态修改某一个数，动态查询区间第k大

空间复杂度为 $n \lg n \lg n$

时间复杂度为 $n \lg n \lg n$

zoi 2112 Dynamic Rankings

裸动态主席树（其实这道题用整体二分更好）

N 50000 M 10000

输入格式

N M

a1 ... an

(M){

Q l r k

C pos t

```
}
```

```
#include <iostream>
```

```
#include <cstdio>
```

```
#include <cstdlib>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <cstring>
```

```
#include <vector>
```

```
#include <queue>
```

```
#include <stack>
```

```
#include <set>
```

```
#include <vector>
```

```
#include <map>
```

```
#include <tr1/unordered_set>
```

```
#include <tr1/unordered_map>
```

```
//#pragma comment(linker, "/STACK:1024000000,1024000000")
```

```
#define inf 1e9
```

```
#define debug(a) cout << #a " = " << (a) << endl;
```

```
#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << " ] = " << (a)[i]
```

```
<< endl; }
```

```

#define clr(x, y) memset(x, y, sizeof x)

#define LL long long

using namespace std;

const int maxn = 100010; /// N×2

const int M = 8000030;    /// (M+N)*800

int n, q, m, tot;

int a[maxn], t[maxn];

int T[maxn], lson[M], rson[M], c[M];

int S[maxn];

struct Query
{
    int kind;

    int l, r, k;
} query[100010];

void Init_hash(int k)
{
    sort(t, t + k);

    m = unique(t, t + k) - t;
}

```

```

int get_hash(int x)

{

    return lower_bound(t, t + m, x) - t;

}

int build(int l, int r)

{

    int root = tot++;

    c[root] = 0;

    if (l != r)

    {

        int mid = (l + r) >> 1;

        lson[root] = build(l, mid);

        rson[root] = build(mid + 1, r);

    }

    return root;

}

int Insert(int root, int pos, int val)

{

    int newroot = tot++, tmp = newroot;

    int l = 0, r = m - 1;

    c[newroot] = c[root] + val;

    while (l < r)

```

```

{

    int mid = (l + r) >> 1;

    if (pos <= mid)

    {

        lson[newroot] = tot++; rson[newroot] = rson[root];

        newroot = lson[newroot]; root = lson[root];

        r = mid;

    }

    else

    {

        rson[newroot] = tot++; lson[newroot] = lson[root];

        newroot = rson[newroot]; root = rson[root];

        l = mid + 1;

    }

    c[newroot] = c[root] + val;

}

return tmp;

}

int lowbit(int x)

{

    return x & (-x);

}

```

```
int use[maxn];
```

```
void add(int x, int pos, int val)
```

```
{  
  
    while (x <= n)  
  
    {  
  
        S[x] = Insert(S[x], pos, val);  
  
        x += lowbit(x);  
  
    }  
}
```

```
int sum(int x)
```

```
{  
  
    int ret = 0;  
  
    while (x > 0)  
  
    {  
  
        ret += c[lsn[use[x]]];  
  
        x -= lowbit(x);  
  
    }  
  
    return ret;  
}
```

```

int Query(int left, int right, int k)
{
    int left_root = T[left - 1];

    int right_root = T[right];

    int l = 0, r = m - 1;

    for (int i = left - 1; i; i -= lowbit(i)) use[i] = S[i];

    for (int i = right; i; i -= lowbit(i)) use[i] = S[i];

    while (l < r)
    {
        int mid = (l + r) / 2;

        int tmp = sum(right) - sum(left - 1) + c[lson[right_root]] - c[lson[left_root]];

        if (tmp >= k)
        {
            r = mid;

            for (int i = left - 1; i; i -= lowbit(i))

                use[i] = lson[use[i]];

            for (int i = right; i; i -= lowbit(i))

                use[i] = lson[use[i]];

            left_root = lson[left_root];

            right_root = lson[right_root];

        }

        else

```

```

    {

        l = mid + 1;

        k -= tmp;

        for (int i = left - 1; i; i -= lowbit(i))

            use[i] = rson[use[i]];

        for (int i = right; i; i -= lowbit(i))

            use[i] = rson[use[i]];

        left_root = rson[left_root];

        right_root = rson[right_root];

    }

}

return l;

}

```

```

void Modify(int x, int p, int d)

```

```

{

    while (x <= n)

    {

        S[x] = Insert(S[x], p, d);

        x += lowbit(x);

    }

}

```



```

int main()

{

    //freopen("input.txt","r",stdin);

    while (~scanf("%d", &n))

    {

        tot = 0;

        m = 0;

        q = maxn;

        for (int i = 1; i <= n; i++)

        {

            scanf("%d", &a[i]);

            t[m++] = a[i];

        }

        scanf("%d", &q);

        int op;

        for (int i = 0; i < q; i++)

        {

            scanf("%d", &op);

            if (op == 2)

            {

                query[i].kind = 0;

```

```

        scanf("%d%d%d", &query[i].l, &query[i].r, &query[i].k);

    }

    else

    {

        query[i].kind = 1;

        scanf("%d%d", &query[i].l, &query[i].r);

        t[m++] = query[i].r;

    }

}

Init_hash(m);

T[0] = build(0, m - 1);

for (int i = 1; i <= n; i++)

    T[i] = Insert(T[i - 1], get_hash(a[i]), 1);

for (int i = 1; i <= n; i++)

    S[i] = T[0];

for (int i = 0; i < q; i++)

{

    if (query[i].kind == 0)

        printf("%d\n", t[Query(query[i].l, query[i].r, query[i].k)]);

    else

    {

        Modify(query[i].l, get_hash(a[query[i].l]), -1);

```

```

        Modify(query[i].l, get_hash(query[i].r, 1);

        a[query[i].l] = query[i].r;

    }

}

}

return 0;

}

```

CDQ 分治

```

////////////////////////////////////
//////////

////////////////////////////////////
//////////

////////////////////////////////////
//////////

////////////////////////////////////
//////////

```

CDQ分治，即中序遍历

可解决降维问题，和动态转静态问题

顺序一般为(l, m) -> (l, r) -> (m + 1, r)

```

////////////////////////////////////
//////////

```

```
////////////////////////////////////  
  
/////////  
  
////////////////////////////////////  
  
/////////
```

HDU 5432 Boring Class

序列 $L_0 \sim L_n$, $R_0 \sim R_n$

选取一些位置，要求L递增，R递减。

输出字典序最小的答案。

解法，因为需要输出字典序最小，需要从后向前进行CDQ

```
#include <iostream>
```

```
#include <cstdio>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <cstring>
```

```
#include <stdio.h>
```

```
#include <string>
```

```
#define clr(x, y) memset(x, y, sizeof x)
```

```
#define inf 1e9
```

```
using namespace std;
```

```
template<class T>
```

```
inline bool read(T &n)
```

```
{
```

```
    T x = 0, tmp = 1;
```

```
    char c = getchar();
```

```
    while ((c < '0' || c > '9') && c != '-' && c != EOF) c = getchar();
```

```
    if (c == EOF) return false;
```

```
    if (c == '-') c = getchar(), tmp = -1;
```

```
    while (c >= '0' && c <= '9') x *= 10, x += (c - '0'), c = getchar();
```

```
    n = x*tmp;
```

```
    return true;
```

```
}
```

```
template <class T>
```

```
inline void write(T n)
```

```
{
```

```
    if (n < 0)
```

```
    {
```

```
        putchar('-');
```

```
        n = -n;
```

```

    }

    int len = 0, data[20];

    while (n)

    {

        data[len++] = n % 10;

        n /= 10;

    }

    if (!len) data[len++] = 0;

    while (len--) putchar(data[len] + 48);

}

```

```

const int maxn = 55005;

```

```

struct node

```

```

{

    int Li, Ri, id;

    bool operator < (const node & A) const

    {

        return Ri > A.Ri;

    }

}

```

```
} q[maxn], tmp[maxn];
```

```
int Li[maxn], Ri[maxn], su[maxn];
```

```
int dp[maxn], rmax[maxn];
```

```
int n;
```

```
void upp(int x, int a)
```

```
{
```

```
    while (x <= n)
```

```
    {
```

```
        rmax[x] = max(rmax[x], a);
```

```
        x += x & -x;
```

```
    }
```

```
}
```

```
void cl(int x) /// CDQ分治中用到树状数组要这样清空
```

```
{
```

```
    while (x <= n)
```

```
    {
```

```
        rmax[x] = 0;
```

```
        x += x & -x;
```

```
    }
```

```
}
```

```

int get_max(int x)
{
    int ans = 0;

    while (x > 0)
    {
        ans = max(ans, rmax[x]);

        x -= x & -x;
    }

    return ans;
}

```

```

void CDQ(int L, int R)
{
    if (L == R)
    {
        int &ret = dp[q[L].id];

        ret = max(ret, 1);

        return;
    }

```

```

    int mid = (L + R) >> 1;

```



```
CDQ(mid + 1, R);
```

```
int L1 = L, L2 = mid + 1;
```

```
int ptr = mid + 1;
```

```
sort(q + L, q + mid + 1);
```

```
sort(q + mid + 1, q + R + 1);
```

```
for (int i = L; i <= mid; i++)
```

```
{
```

```
    while (ptr <= R && q[i].Ri <= q[ptr].Ri)
```

```
    {
```

```
        upp(q[ptr].Li, dp[q[ptr].id]);
```

```
        ptr++;
```

```
    }
```

```
    int &ret = dp[q[i].id];
```

```
    ret = max(ret, get_max(q[i].Li) + 1);
```

```
}
```

```
for (int i = mid + 1; i <= R; i++) ///**特殊清空
```

```
    cl(q[i].Li);
```

```

    for (int i = L; i <= mid; i++)
    {
        while (q[i].id != i)
            swap(q[i], q[q[i].id]);
    }

    CDQ(L, mid);
}

int main()
{
    //freopen("input.txt", "r", stdin);

    //freopen("output.txt", "w", stdout);

    int len;

    string ans;

    int maxlen, rr;

    while (read(n))
    {
        for (int i = 0; i < n; i++)
        {

```

```

        read(q[i].Li);

        su[i] = q[i].Li;

        q[i].id = i;

        Li[i] = q[i].Li;

    }

    sort(su, su + n);

    len = unique(su, su + n) - su;

    for (int i = 0; i < n; i++)

        q[i].Li = lower_bound(su, su + len, q[i].Li) - su + 1;


    for (int i = 0; i < n; i++)

    {

        read(q[i].Ri);

        su[i] = q[i].Ri;

        Ri[i] = q[i].Ri;

    }


    clr(dp, 0);

    clr(rmax, 0);

    CDQ(0, n - 1);


    //for (int i = 0; i < n; i++) printf("Ri=%d i=%d dp=%d\n", q[i].Ri, q[i].id, dp[q[i].id]);

```

```

maxlen = 0; rr = -1; ans = "";

for (int i = 0; i < n; i++) maxlen = max(maxlen, dp[i]);

write(maxlen); putchar('\n');

for (int i = 0; i < n; i++)
{
    if (dp[i] == maxlen)
    {
        if (rr == -1 || (Li[rr] >= Li[i] && Ri[rr] <= Ri[i]))
        {
            maxlen--;

            if (rr != -1) putchar(' ');

            write(i + 1);

            rr = i;
        }
    }

    putchar('\n');

    //cout<<"maxlen:"<<maxlen<<endl;
}

return 0;

```

```
}
```

```
////////////////////////////////////
```

```
//////////
```

```
////////////////////////////////////
```

```
//////////
```

```
////////////////////////////////////
```

```
//////////
```

hdu 5354 Bipartite Graph

给一张图，要求找到一个点，删除后成为二分图

解法：CDQ + 可撤销(种族)并查集

保证在进入 (l, r) 前， (l, r) 内的边没有加入，之外的边全部加入

再递归处理

```
#include <iostream>
```

```
#include <cstdio>
```

```
#include <cstdlib>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <cstring>
```

```
#include <vector>
```

```

#include <queue>

#include <stack>

#include <set>


#pragma comment(linker, "/STACK:1024000000,1024000000")

#define lson l, m, rt<<1

#define rson m+1, r, rt<<1|1

#define inf 1e9

#define clr(x, y) memset(x, y, sizeof x)

using namespace std;

const int maxn = 200005;


struct edge

{

    int to, next;

}G[maxn<<1];


struct node

{

    int u, v, hu, hv, fau, fav, colu, colv;

    node(){}

```

```

node(int a, int b, int c, int d, int e, int f, int g, int h)
{
    u = a; v = b; hu = c; hv = d; fau = e; fav = f;

    colu = g;

    colv = h;
}

};

stack<node> stk;

```

```
int head[maxn], si;
```

```
int h[maxn], fa[maxn];
```

```
int ans[maxn], n, m;
```

```
int col[maxn]; //0 代表相同 1 代表不同
```

```
void init(int _n)
```

```

{
    for (int i = 0; i <= _n; i++)

    {
        fa[i] = i;

        h[i] = 1;

        ///

        col[i] = 0;
    }
}

```

```

    }

}

void add(int u, int v)

{

    G[si].to = v;

    G[si].next = head[u];

    head[u] = si++;

}

int find_fa(int x)

{

    int o = x;

    while (fa[o] != o) o = fa[o];

    return o;

}

int find_col(int x)

{

    if (fa[x] == x) return 1;

    ///return 1 ^ find_col(fa[x]);

    return col[x] ^ find_col(fa[x]);

}

bool Merge(int u, int v)

{

```



```

int a = find_fa(u), b = find_fa(v);

int x = find_col(u), y = find_col(v);

if (a == b)

{

    if (x == y)

    {

        //printf("~~~%d %d~fu = %d fv = %d\n", u, v, a, b);

        return false;

    }

    return true;

}

stk.push(node(a, b, h[a], h[b], fa[a], fa[b], col[a], col[b]));

if (h[a] > h[b])

{

    fa[b] = a, h[a] += h[b];

    ///

    col[b] = x ^ y ^ 1;

}

else

{

    fa[a] = b, h[b] += h[a];

    ///

```

```

        col[a] = x ^ y ^ 1;

    }

    return true;

}

bool unite(int L, int R, int a, int b)
{
    for (int u = L; u <= R; u++)

        for (int i = head[u]; i != -1; i = G[i].next)

        {
            int v = G[i].to;

            if (a <= v && v <= b) continue;

            if (!Merge(u, v)) return false;

        }

    return true;

}

void get_del(int x)
{
    node tmp;

    while (stk.size() > x)

    {

```

```

        tmp = stk.top(); stk.pop();

        int u = tmp.u, v = tmp.v;

        h[u] = tmp.hu; h[v] = tmp.hv;

        fa[u] = tmp.fau; fa[v] = tmp.fav;

        /**/col[u] = tmp.colu; col[v] = tmp.colv;

    }

}

```

```

void cdq(int l, int r)

{

    if (l == r)

    {

        ans[l] = 1;

        return;

    }

    int pre = stk.size();

    int m = (l + r) >> 1;

    if (unite(m + 1, r, l, m))    /// 加入右面的边

        cdq(l, m);

    else{

        for (int i = l; i <= m; i++) ans[i] = 0;
    }
}

```

```

    }

    get_del(pre);          /// 删去右面的边

    if (unite(l, m, m + 1, r))    /// 加入左面的边

        cdq(m + 1, r);

    else{

        for (int i = m + 1; i <= r; i++) ans[i] = 0;

    }

    get_del(pre);          /// 删去左面的边

    return;

}

```

```

int main()

{

    //freopen("input.txt", "r", stdin);

    int T;

    scanf("%d", &T);

    while (T--)

    {

        scanf("%d%d", &n, &m);

        init(n);

        clr(head, -1); si = 0;

        while (stk.size()) stk.pop();
    }
}

```

```

    for (int i = 0, st, ed; i < m; i++)
    {
        scanf("%d%d", &st, &ed);

        add(st, ed); add(ed, st);
    }

    cdq(1, n);

    for (int i = 1; i <= n; i++) printf("%d", ans[i]);

    printf("\n");
}

return 0;
}

```

```

////////////////////////////////////
//////////

////////////////////////////////////
//////////

////////////////////////////////////
//////////

////////////////////////////////////
//////////

```

bnu 12753 Arnooks's **Defensive Line**

插入一些区间，并查询有多少区间包含它

解法：裸CDQ动态转静态

(对于某些CDQ问题，可能可以使用先序遍历或后序遍历，但最好用中序遍历)

```
#include <iostream>
```

```
#include <cstdio>
```

```
#include <cstdlib>
```

```
#include <algorithm>
```

```
#include <cmath>
```

```
#include <cstring>
```

```
#include <vector>
```

```
#include <queue>
```

```
#include <stack>
```

```
#include <set>
```

```
#include <vector>
```

```
//#pragma comment(linker, "/STACK:1024000000,1024000000")
```

```
#define lson l, m, rt<<1
```

```
#define rson m+1, r, rt<<1|1
```

```
#define inf 1e9
```

```
#define debug(a) cout << #a " = " << (a) << endl;
```

```
#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << "]" = " << (a)[i]
```

```
<< endl; }
```

```
#define clr(x, y) memset(x, y, sizeof x)
```

```
using namespace std;
```

```
typedef unsigned long long uLL;
```

```
const int maxn = 500000 + 30;
```

```
int ans[maxn];
```

```
struct __sad
```

```
{
```

```
    int l, r;
```

```
    char c;
```

```
    int id;
```

```
    bool operator <(const __sad &a) const{
```

```
        if (l != a.l) return l < a.l;
```

```
        else return r < a.r;
```

```
    }
```

```
}A[maxn], B[maxn], C[maxn];
```

```
int rsum[maxn * 4];
```

```
void upp(int x, int add)
```

```
{
```

```

while (x < maxn * 4)

{

    rsum[x] += add;

    x += x&-x;

}

}

```

```

void clear(int x)

{

    while (x < maxn * 4)

    {

        rsum[x] = 0;

        x += x&-x;

    }

}

```

```

int get(int x)

{

    int ret = 0;

    while (x)

    {

        ret += rsum[x];

        x -= x&-x;
    }
}

```



```

    }

    return ret;
}

void CDQ(int l, int r)
{
    if (l == r) return;

    int mid = l + r >> 1;

    int lb = 0, lc = 0;

    for (int i = l; i <= mid; i++)
    {
        if (A[i].c == '+') B[lb++] = A[i];
    }

    for (int i = mid + 1; i <= r; i++)
    {
        if (A[i].c == '?') C[lc++] = A[i];
    }

    sort(B, B + lb);

    sort(C, C + lc);
}

```

```

int sum = 0;

int cn = 0;

for (int i = 0; i < lc; i++)
{
    while (cn < lb && B[cn].l <= C[i].l)
    {
        upp(B[cn].r, 1);

        sum++;

        cn++;
    }

    int ret = sum - get(C[i].r - 1);

    ans[C[i].id] += ret;
}

for (int i = 0; i < lb; i++)

    clear(B[i].r);

CDQ(l, mid);

CDQ(mid + 1, r);
}

```

```

int sub[maxn * 4], len;

int main()
{

    //freopen("input.txt", "r", stdin);

    int n;

    while (~scanf("%d", &n))
    {

        char s[30];

        len = 0;

        for (int i = 1; i <= n; i++)
        {

            scanf("%s%d%d", s, &A[i].l, &A[i].r);

            A[i].c = *s;

            A[i].id = i;

            sub[len++] = A[i].l;

            sub[len++] = A[i].r;

        }

        sort(sub, sub + len);

        len = unique(sub, sub + len) - sub;

        for (int i = 1; i <= n; i++)

```

```

    {

        A[i].l = lower_bound(sub, sub + len, A[i].l) - sub + 1;

        A[i].r = lower_bound(sub, sub + len, A[i].r) - sub + 1;

    }

    clr(ans, 0);

    clr(rsum, 0);

    CDQ(1, n);

    for (int i = 1; i <= n; i++) if (A[i].c == '?')

        printf("%d\n", ans[i]);

    }

    return 0;

}

```

整体二分

```

#include <iostream>

#include <cstdio>

#include <cstdlib>

#include <algorithm>

#include <cmath>

#include <cstring>

```

```

#include <vector>

#include <queue>

#include <stack>

#include <set>

#include <vector>

#include <deque>

#include <set>


//#pragma comment(linker, "/STACK:1024000000,1024000000")

#define lson l, m, ls[rt]

#define rson m+1, r, rs[rt]

#define inf 1e9

#define debug(a) cout << #a" = " << (a) << endl;

#define debugarry(a, n) for (int i = 0; i < (n); i++) { cout << #a "[" << i << "]" = " << (a)[i]

<< endl; }

#define clr(x, y) memset(x, y, sizeof x)

#define LL long long

using namespace std;

const int maxn = 2e6;

struct __sad

{

```

```

    int l, r, id;

    int st, k, v, add;

}p[maxn], p1[maxn], p2[maxn];

int ans[maxn];

int n;

int rsum[maxn];

void upp(int x, int add)
{
    while (x <= n)
    {
        rsum[x] += add;

        x += x&-x;
    }
}

int get(int x)
{
    int ret = 0;

    while (x)
    {

```

```

        ret += rsum[x];

        x -= x&&-x;

    }

    return ret;

}

void Bin(int st, int ed, int l, int r)

{

    if (st>ed) return;

    if (l == r)

    {

        for (int i = st; i <= ed; i++) if (p[i].st == 2)

            ans[p[i].id] = l;

        return;

    }

    int mid = l + (r - l) / 2;

    int ta1 = 0, ta2 = 0;

    for (int i = st; i <= ed; i++)

    {

        if (p[i].st == 1)

        {

            if (p[i].v <= mid)

```

```

        {

            p1[ta1++] = p[i];

            upp(p[i].l, p[i].add);

        }

        else    p2[ta2++] = p[i];

    }

    else

    {

        int t = get(p[i].r) - get(p[i].l - 1);

        if (t >= p[i].k) p1[ta1++] = p[i];

        else p[i].k -= t, p2[ta2++] = p[i];

    }

}

for (int i = st; i <= ed; i++)

{

    if (p[i].st == 1)

        if (p[i].v <= mid)

            upp(p[i].l, p[i].add*(-1));

}

for (int i = 0; i < ta1; i++)

    p[i + st] = p1[i];

for (int i = 0; i < ta2; i++)

```



```

        p[i + st + ta1] = p2[i];

        Bin(st, st + ta1 - 1, l, mid);

        Bin(st + ta1, ed, mid + 1, r);

    }

int A[maxn];

int sub[maxn], len;

int main()

{

    //freopen("1007.in", "r", stdin);

    //freopen("output.txt", "w", stdout);

    int q;

    while (~scanf("%d", &n))

    {

        int cnt = 0, acnt = 0;

        int a, st, l, r, v, k;

        len = 0;

        for (int i = 1; i <= n; i++)

        {

            scanf("%d", &a);

```

```

A[i] = a;

sub[len++] = a;


p[cnt].l = i; p[cnt].st = 1;

p[cnt].v = a; p[cnt].add = 1;


cnt++;

}

scanf("%d", &q);

for (int i = 0; i < q; i++)

{

    scanf("%d", &st);

    if (st == 1)

    {

        scanf("%d%d", &l, &v);


        sub[len++] = v;


        p[cnt].l = l; p[cnt].st = 1;

        p[cnt].v = A[l]; p[cnt].add = -1;

        cnt++;

```

```

        p[cnt].l = l; p[cnt].st = 1;

        p[cnt].v = A[l] = v; p[cnt].add = 1;

        cnt++;

    }

    else{

        scanf("%d%d%d", &l, &r, &k);

        p[cnt].l = l; p[cnt].r = r;

        p[cnt].st = 2; p[cnt].k = k;

        p[cnt].id = acnt++;

        cnt++;

    }

}

sort(sub, sub + len);

len = unique(sub, sub + len) - sub;

for (int i = 0; i < cnt; i++) if (p[i].st == 1)

{

    p[i].v = lower_bound(sub, sub + len, p[i].v) - sub + 1;

}

Bin(0, cnt - 1, 0, len + 7);

```

```

        for (int i = 0; i < acnt; i++)

            printf("%d\n", sub[ans[i] - 1]);

    }

    return 0;
}

```

2-SAT

```

/*
复杂度O(n)
*/

struct two_sat
{
    int n;

    vector<int> G[maxn << 1];

    bool mark[maxn << 1];

    int S[maxn << 1], c;

    bool dfs(int x)
    {

```

```

    if (mark[x ^ 1]) return false;

    if (mark[x]) return true;

    mark[x] = true;

    S[c++] = x;

    for (int i = 0; i < G[x].size(); i++)

    {

        if (!dfs(G[x][i])) return false;

    }

    return true;

}

void init(int n)

{

    this->n = n;

    for (int i = 0; i < (n << 1); i++) G[i].clear();

    clr(mark, 0);

}

// x = xval or y = yval

//2i + 1 means true 2i means false

void add_clause(int x, int xval, int y, int yval)

{

    x = x * 2 + xval;

    y = y * 2 + yval;

```

```

        G[x ^ 1].push_back(y);

        G[y].push_back(x ^ 1);

        G[y ^ 1].push_back(x);

        G[x].push_back(y ^ 1);

    }

    bool solve()
    {

        for (int i = 0; i < (n << 1); i += 2)

            if (!mark[i] && !mark[i + 1])

            {

                c = 0;

                if (!dfs(i))

                {

                    while (c > 0) mark[S[--c]] = false;

                    if (!dfs(i + 1)) return false;

                }

            }

        return true;

    }

} sat;

```

ISAP 网络流

```
const int maxn = 1050;
```

```
const int maxm = 100005;
```

```
struct edge
```

```
{
```

```
    int to, next;
```

```
    int cap;
```

```
} G[maxm];
```

```
int head[maxn], si;
```

```
void add(int st, int ed, int val)
```

```
{
```

```
    G[si].to = ed;
```

```
    G[si].cap = val;
```

```
    G[si].next = head[st];
```

```
    head[st] = si++;
```

```
    G[si].to = st;
```

```
    G[si].cap = 0;
```

```
    G[si].next = head[ed];
```

```

        head[ed] = si++;
    }

    int nn, n, m;

    int h[maxn], gap[maxn];

    int source, sink;

    int dfs(int u, int cost)
    {
        if (u == sink) return cost;

        int minh = nn - 1, lv = cost, d;

        for (int i = head[u]; i != -1; i = G[i].next)
        {
            int v = G[i].to;

            int val = G[i].cap;

            if (val > 0)
            {
                if (h[v] + 1 == h[u])
                {
                    d = min(val, lv);

```



```

        d = dfs(v, d);

        G[i].cap -= d;

        G[i ^ 1].cap += d;

        lv -= d;

        if (h[source] >= nn) return cost - lv;

        if (lv == 0) break;
    }

    if (h[v] < minh) minh = h[v];
}

}

if (lv == cost)
{
    --gap[h[u]];

    if (gap[h[u]] == 0) h[source] = nn;

    h[u] = minh + 1;

    ++gap[h[u]];
}

return cost - lv;
}

int sap(int st, int ed)

```

```

{

    source = st;

    sink = ed;

    int ret = 0;

    clr(gap, 0); clr(h, 0);


    gap[st] = nn;


    while (h[st] < nn)

    {

        ret += dfs(st, inf);

    }


    return ret;

}

```

最小费用最大流

```

const int maxn = 2000;

const int maxm = 2500000;


struct edge

```

```

{

    int to, next;

    int cap, flow, cc;

} G[maxm];


int head[maxn], si;

int pre[maxn], dis[maxn];

bool vis[maxn];

int nn, n, m, k;


void add(int st, int ed, int val, int cost)
{

    G[si].to = ed;

    G[si].cap = val;

    G[si].cc = cost;

    G[si].flow = 0;

    G[si].next = head[st];

    head[st] = si++;

    G[si].to = st;

    G[si].cap = 0;

    G[si].cc = -cost;

    G[si].flow = 0;

```

```

    G[si].next = head[ed];

    head[ed] = si++;
}

```

```

bool spfa(int s, int t)
{
    queue<int> que;

    for (int i = 0; i < nn; i++)
    {
        dis[i] = inf;

        vis[i] = false;

        pre[i] = -1;
    }

    dis[s] = 0;

    vis[s] = true;

    que.push(s);

    while (que.size())
    {
        int u = que.front(); que.pop();

        vis[u] = false;

        for (int i = head[u]; i != -1; i = G[i].next)

```

```

    {

        int v = G[i].to;

        if (G[i].cap > G[i].flow &&

            dis[v] > dis[u] + G[i].cc)

        {

            dis[v] = dis[u] + G[i].cc;

            pre[v] = i;

            if (!vis[v])

            {

                vis[v] = true;

                que.push(v);

            }

        }

    }

}

// if (dis[t] > 0) return false; 加上这句话可以保证只求出最小费用，不要求最大流

if (pre[t] == -1) return false;

return true;

}

int min_cost_maxflow(int s, int t, int &cost)

{

```

```

int flow = 0;

cost = 0;

while (spfa(s, t))
{
    int rmin = inf;

    for (int i = pre[t]; i != -1; i = pre[G[i ^ 1].to])
        rmin = min(rmin, G[i].cap - G[i].flow);

    for (int i = pre[t]; i != -1; i = pre[G[i ^ 1].to])
    {
        G[i].flow += rmin;

        G[i ^ 1].flow -= rmin;

        cost += G[i].cc * rmin;
    }

    flow += rmin;
}

return flow;
}

```

尺取法

```
/*
```

HDU 5289

求一个序列连续区间最大值-最小值不超过K的个数

*/

#include <cstdio>

#include <iostream>

#include <algorithm>

#include <cstring>

#include <string>

#include <cmath>

#include <queue>

#include <bitset>

#define clr(x, y) memset(x, y, sizeof x)

#define inf 1000000000

using namespace std;

typedef long long LL;

const int maxn = 200010;

int A[maxn];

int dmax[maxn][30];

int dmin[maxn][30];

int flog[(maxn << 1) + 10];

```
int n, K;
```

```
int rmax_init(int A[])
```

```
{
```

```
    for (int i = 0; i < n; i++) dmax[i][0] = A[i];
```

```
    for (int j = 1; (1 << j) <= n; j++)
```

```
        for (int i = 0; i + (1 << j) - 1 < n; i++)
```

```
            dmax[i][j] = max(dmax[i][j - 1], dmax[i + (1 << (j - 1))][j - 1]);
```

```
}
```

```
int rmax_find(int L, int R)
```

```
{
```

```
    int k = flog[R - L + 1];
```

```
    return max(dmax[L][k], dmax[R - (1 << k) + 1][k]);
```

```
}
```

```
int rmin_init(int A[])
```

```
{
```

```
    for (int i = 0; i < n; i++) dmin[i][0] = A[i];
```

```
    for (int j = 1; (1 << j) <= n; j++)
```

```
        for (int i = 0; i + (1 << j) - 1 < n; i++)
```

```
            dmin[i][j] = min(dmin[i][j - 1], dmin[i + (1 << (j - 1))][j - 1]);
```

```
}
```

```
int rmin_find(int L, int R)
```



```

{

    int k = flog[R - L + 1];

    return min(dmin[L][k], dmin[R - (1 << k) + 1][k]);

}


int main()

{

    //freopen("input.txt", "r", stdin);


    flog[0] = -1;

    for (int i = 1; i < 2 * maxn; i++) flog[i] = flog[i > 1] + 1;


    int T, he, ta;

    LL ans;

    scanf("%d", &T);

    while (T--)

    {

        scanf("%d%d", &n, &K);

        for (int i = 0; i < n; i++) scanf("%d", &A[i]);


        rmax_init(A); rmin_init(A);

```

```

    he = ta = 0;

    ans = 0;

    while (he < n)

    {

        while (ta < n && rmax_find(he, ta) - rmin_find(he, ta) < K) { ta++; }

        ans += ta - he;

        he++;

    }

    printf("%l64d\n", ans);

}

return 0;

}

```

倍增法求 LCA

```
/*
```

```
倍增法求LCA，复杂度O(nlogn)
```

```
*/
```

```
const int maxn = 100000;
```

```

const int maxk = 30;

struct edge

{
    int to, next;
} G[maxn << 1];

int head[maxn], si;

int parent[maxk][maxn]; //注意第一维为小的

int depth[maxn];

void dfs(int u, int p, int d)
{
    parent[0][u] = p;

    depth[u] = d;

    for (int i = head[u]; i != -1; i = G[i].next)
    {
        int v = G[i].to;

        if (v != p) dfs(v, u, d + 1);
    }
}

void init_lca(int _n)

```

```

{

    dfs(1, -1, 0);

    for (int k = 0; k + 1 < maxk; k++)

    {

        for (int u = 1; u <= _n; u++) //注意下标是0~n-1 还是1~n

        {

            if (parent[k][u] < 0) parent[k + 1][u] = -1;

            else parent[k + 1][u] = parent[k][parent[k][u]];

        }

    }

}

int get_lca(int u, int v)

{

    if (depth[u] > depth[v]) swap(u, v);

    for (int k = 0; k < maxk; k++)

    {

        if ((depth[v] - depth[u]) >> k & 1)

        {

            v = parent[k][v];

        }

    }

    if (u == v) return u;

```

```

    for (int k = maxk - 1; k >= 0; k--)
    {
        if (parent[k][u] != parent[k][v])
        {
            u = parent[k][u];
            v = parent[k][v];
        }
    }

    return parent[0][u];
}

```

边双连通分量

```
const int maxn = 2000;
```

```
const int maxm = 550;
```

```
struct edge
```

```
{
```

```
    int to, next;
```

```
}G[maxn << 1];
```

```
int head[maxn], si;
```

```
int pre[maxn], dfs_clock, bridge;
```

```
int par[maxn], n;
```

```
void init(int _n)
```

```
{
```

```
    for (int i = 0; i <= _n; i++)
```

```
        par[i] = i;
```

```
}
```

```
int Find(int x)
```

```
{
```

```
    if (x == par[x]) return x;
```

```
    return par[x] = Find(par[x]);
```

```
}
```

```
void unite(int x, int y)
```

```
{
```

```
    x = Find(x);
```

```
    y = Find(y);
```

```
    if (x == y) return;
```

```
    par[x] = y;
```

```
}
```

```
int Tarjan(int u, int fa)
```

```

{

    int lowu = pre[u] = ++dfs_clock;

    for (int i = head[u]; i != -1; i = G[i].next)

    {

        int v = G[i].to;

        if (v == fa) continue;

        if (pre[v] == 0)

        {

            int lowv = Tarjan(v, u);

            lowu = min(lowu, lowv);

            if (lowv <= pre[u]) unite(u, v);

            // 表示是桥

            else if (lowv > pre[u]) bridge++;

        }

        else lowu = min(lowu, pre[v]);

    }

    return lowu;

}

```

```

void find_bridge(int _n)

```

```

{

    clr(pre, 0);

```

```

    dfs_clock = 0;

    for (int i = 1; i <= n; i++)

        if (!pre[i]) Tarjan(i, -1);

}

```

点双连通分量

```

#include <cstdio>

#include <iostream>

#include <algorithm>

#include <cstring>

#include <vector>

#include <queue>

#define clr(x, y) memset(x, y, sizeof x)

#define inf 1000000000

using namespace std;

typedef long long LL;

const int maxn = 1505;

int pre[maxn], iscut[maxn], bccno[maxn], dfs_clock, bcc_cnt;

vector<int> G[maxn], bcc[maxn];

```



```
int n, m;
```

```
struct edge
```

```
{
```

```
    int st, ed;
```

```
};
```

```
stack<edge> S;
```

```
int dfs(int u, int fa)
```

```
{
```

```
    int lowu = pre[u] = ++dfs_clock;
```

```
    int child = 0;
```

```
    for (int i = 0; i < G[u].size(); i++)
```

```
    {
```

```
        int v = G[u][i];
```

```
        Edge e = (Edge){ u, v };
```

```
        if (!pre[v])
```

```
        {
```

```
            S.push(e);
```

```
            child++;
```

```

int lowv = dfs(v, u);

lowu = min(lowu, lowv);

if (lowv >= pre[u])
{
    iscut[u] = true;

    bcc_cnt++; bcc[bcc_cnt].clear();

    for (;;)
    {
        edge x = S.top(); S.pop();

        if (bccno[x.u] != bcc_cnt)
        {
            bcc[bcc_cnt].push_back(x.u);

            bcc_cnt[x.u] = bcc_cnt;
        }

        if (bccno[x.v] != bcc_cnt)
        {
            bcc[bcc_cnt].push_back(x.v);

            bcc_cnt[x.v] = bcc_cnt;
        }

        if (x.u == u && x.v == v) break;
    }
}

```

```

    }

    else if (pre[v] < pre[u] && v != fa)

    {

        S.push(e);

        lowu = min(lowu, pre[v]);

    }

}

if (fa < 0 && child == 1) iscut[u] = 0;

return lowu;

}

void find_bcc(int n)

{

    clr(pre, 0); clr(iscut, 0); clr(bccno, 0);

    dfs_clock = bcc_cnt = 0;

    for (int i = 0; i < n; i++)

    {

        if (!pre[i]) dfs(i, -1);

    }

}

```

LCT 动态树

```
/*  
包含最基本的加入操作，删除操作，询问两个点是否联通  
*/
```

```
#include <cstdio>
```

```
#include <cstring>
```

```
#include <algorithm>
```

```
using namespace std;
```

```
const int MAXN = 10005;
```

```
struct Node* null;
```

```
struct Node {
```

```
    Node* c[2];
```

```
    Node* f;
```

```
    int flip;
```

```
void newnode() {
```

```
    c[0] = c[1] = f = null;
```

```
        flip = 0;
    }
}
```

```
void reverse() {
    if (this == null) return;

    swap(c[0], c[1]);

    flip ^= 1;
}
```

```
void link_child(Node* o, int d) {
    c[d] = o;

    o->f = this;
}
```

```
int is_root() {
    return f == null || f->c[0] != this && f->c[1] != this;
}
```

```
void push_down() {
    if (flip) {
        c[0]->reverse();
        c[1]->reverse();
    }
}
```

```

        flip = 0;

    }

}

```

```

void sign_down() {

    if (!is_root()) f->sign_down();

    push_down();

}

```

```

void rotate(int d) {

    Node* p = f;

    Node* g = p->f;

    p->link_child(c[d], !d);

    if (!p->is_root()) {

        if (p == g->c[0]) g->link_child(this, 0);

        else g->link_child(this, 1);

    }

    else f = g;

    this->link_child(p, d);

}

```

```

void splay() {

```

```

sign_down();

while (!is_root()) {

    if (f->is_root()) rotate(this == f->c[0]);

    else {

        if (f == f->f->c[0]) {

            if (this == f->c[0]) f->rotate(1), rotate(1);

            else rotate(0), rotate(1);

        }

        else {

            if (this == f->c[1]) f->rotate(0), rotate(0);

            else rotate(1), rotate(0);

        }

    }

}

```

```

void access() {

    Node* o = this;

    Node* x = null;

    while (o != null) {

        o->splay();

        o->link_child(x, 1);
    }
}

```

```

        x = o;

        o = o->f;

    }

    splay();

}

```

```

Node* find_root() {

    access();

    Node* o = this;

    while (o->c[0] != null) o = o->c[0];

    return o;

}

```

```

void make_root() {

    access();

    reverse();

}

```

```

void cut() {

    access();

    c[0]->f = null;

    c[0] = null;
}

```



```
}
```

```
void cut(Node* o) {
```

```
    if (o->find_root() != find_root()) return;
```

```
    make_root();
```

```
    o->cut();
```

```
}
```

```
void link(Node* o) {
```

```
    if (o == this || o->find_root() == find_root()) return;
```

```
    make_root();
```

```
    f = o;
```

```
}
```

```
void query(Node* o) {
```

```
    if (o->find_root() == find_root()) printf("Yes\n");
```

```
    else printf("No\n");
```

```
}
```

```
};
```

```
Node pool[MAXN];
```

```
Node* node[MAXN];
```

```
Node* cur;
```

```
int n, m;
```

```
void clear() {
```

```
    cur = pool;
```

```
    null = cur++;
```

```
    null->newnode();
```

```
}
```

```
void solve() {
```

```
    char s[20];
```

```
    int x, y;
```

```
    clear();
```

```
    for (int i = 1; i <= n; ++i) {
```

```
        node[i] = cur++;
```

```
        node[i]->newnode();
```

```
    }
```

```
    while (m--) {
```

```
        scanf("%s%d%d", s, &x, &y);
```

```
        if (s[0] == 'C') node[x]->link(node[y]);
```

```
        if (s[0] == 'D') node[x]->cut(node[y]);
```

```

        if (s[0] == 'Q') node[x]->query(node[y]);

    }

}

int main() {

    while (~scanf("%d%d", &n, &m)) solve();

    return 0;

}

```

强连通分量缩环

```

const int maxn = 1000;

struct edge

{

    int to, next;

}G[maxn << 1];

int head[maxn], si;

int pre[maxn], lowlink[maxn], sccno[maxn], dfs_clock, scc_cnt;

stack<int> S;

void Tarjan(int u)

```

```

{

    pre[u] = lowlink[u] = ++dfs_clock;

    S.push(u);

    for (int i = head[u]; i != -1; i = G[i].next)
    {

        int v = G[i].to;

        if (!pre[v])

        {

            Tarjan(v);

            lowlink[u] = min(lowlink[u], lowlink[v]);

        }

        else if (!sccno[v])

        {

            lowlink[u] = min(lowlink[u], pre[v]);

        }

    }

    if (lowlink[u] == pre[u])

    {

        scc_cnt++;

        while (1)

        {

            int x = S.top(); S.pop();

```

```

        sccno[x] = scc_cnt;

        if (x == u) break;

    }

}

}

void find_scc(int _n)

{

    dfs_clock = scc_cnt = 0;

    clr(sccno, 0); clr(pre, 0);

    for (int i = 0; i < _n; i++)

        if (!pre[i]) Tarjan(i);

}

```

二分图匹配

/*

二分图匹配模板

跑点数较少的一侧点，复杂度为 $O(VE)$

对于一般图匹配，将可以将点数乘以2建成二分图，通过二分图匹配可以求出来正确的答案(ans/2)

*/

```
const int maxn = 3000;
```

```

vector<int> G[maxn];

int match[maxn], used[maxn];

bool dfs(int u, int mark)
{
    used[u] = mark;

    for (int i = 0; i < G[u].size(); i++)
    {
        int v = G[u][i];

        int w = match[v];

        if (w < 0 || used[w] != mark && dfs(w, mark))
        {
            match[v] = u;

            match[u] = v;

            return true;
        }
    }

    return false;
}

int bipartite_matching(int _n)

```

```
{  
  
    int res = 0;  
  
    clr(match, -1);  
  
    for (int u = 0; u < _n; u++)  
    {  
        if (match[u] < 0)  
        {  
            if (dfs(u, u)) res++;  
        }  
    }  
  
    return res;  
}
```