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# Scheduling in Real-Time Operation System

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# Đánh giá môn học

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- Điểm bài tập: Chọn 1 trong những bài báo trong đây để báo cáo, sử dụng nhóm đã lập.
  - Nêu vấn đề
  - Nghiên cứu liên quan
  - Giải pháp
  - Kết luận
- Điểm GK: Lý thuyết, làm bài tại lớp
- Báo cáo cuối kì:

# Đánh giá môn học

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- Điểm Cuối kì (project): Làm sản phẩm ứng dụng RTOS và viết báo cáo
- Mục tiêu: RTOS hoặc FREERTOS, ứng dụng cho y tế, giáo dục .v.v, tham khảo các bài báo đã publish ở link này.
- Yêu cầu:
- Tên đề tài khác với những bài báo trong link
- Khuyến khích apply machine learning hoặc tiny machine learning. hoặc ứng dụng RTOS trong y tế.
- Mỗi nhóm tối đa 4 thành viên, 2 nhóm 5 thành viên.
- Có thể chọn ESP32, ARM, Raspberry, phải sử dụng RTOS, đồng thời lưu ý yêu cầu tên khác với báo báo đã publish.

# Outline

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- Real-time systems
- Real-time scheduling algorithms
  - Fixed-priority algorithm (RM)
  - Dynamic-priority algorithm (EDF)

# Introduction

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- ❑ Why do we need scheduling?
    - There are always more tasks than processors.
    - Multiple tasks run concurrently on uniprocessor system.
  - ❑ Scheduling policy: the criterion to assign the CPU time to concurrent tasks
  - ❑ Scheduling algorithm: the set of rules that determines the order in which tasks are executed
- *What is the main difference between scheduling in RTOS and GPOS?*

# Scheduling algorithms

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- A scheduling algorithm is a scheme that selects what job to run next.
  - Can be preemptive or non-preemptive.
  - Dynamic or static priorities
  - Etc.

**In general, a RTS will use some scheduling algorithm to meet its deadlines.**

# Real-Time Systems

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- Definition
  - Systems whose correctness depends on their **temporal** aspects as well as their **functional** aspects
- Performance measure
  - **Timeliness** on timing constraints (deadlines)
  - Speed/average case performance are less significant.
- Key property
  - **Predictability** on timing constraints

# Terms and definitions

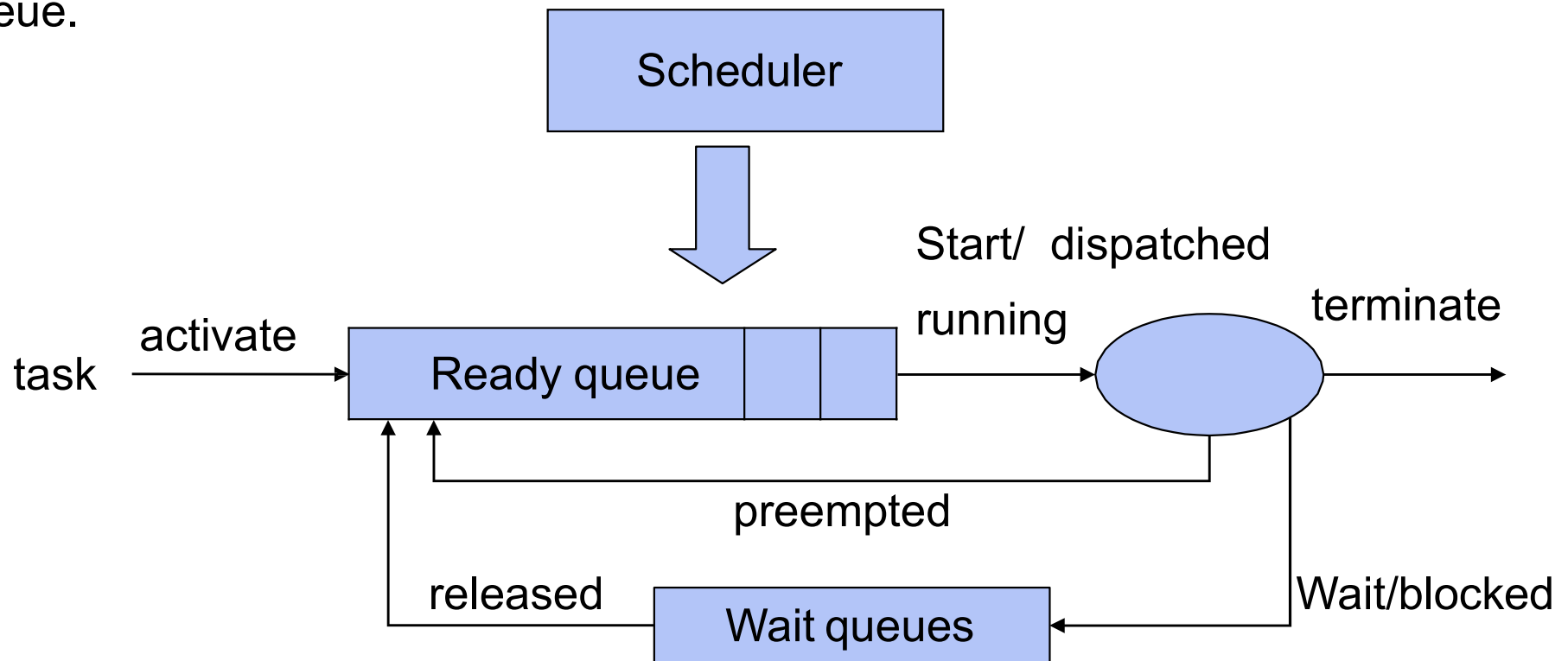
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- ❑ Release time (or ready time): This is the time instant at which a task(process) is ready or eligible for execution
- ❑ Schedule Time: This is the time instant when a task gets its chance to execute
- ❑ Completion time: This is the time instant when task completes its execution
- ❑ Deadline: This is the instant of time by which the execution of task should be completed
- ❑ Runtime: The time taken without interruption to complete the task, after the task is released



# An illustration of scheduling

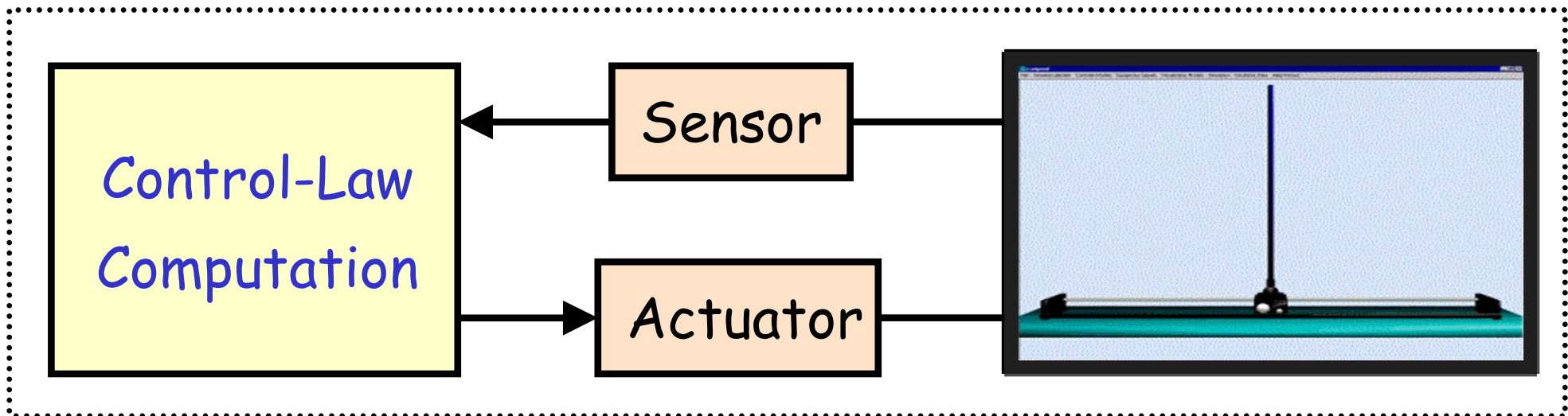
- ❑ All activated tasks enters “ready queue” at first.
- ❑ The scheduler selects one task in the Ready queue according to the tasks’ priorities allocated based on the scheduling algorithm.
- ❑ The selected task is dispatched and becomes in “running” state.
- ❑ After the selected task is completed, it is removed from the Ready queue.



# Real-Time System Example

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- Digital control systems
  - periodically performs the following job:  
  
senses the system status and  
actuates the system according to its current status



# Real-Time System Example

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- Multimedia applications
  - periodically performs the following job:  
*reads, decompresses, and displays* video and audio streams



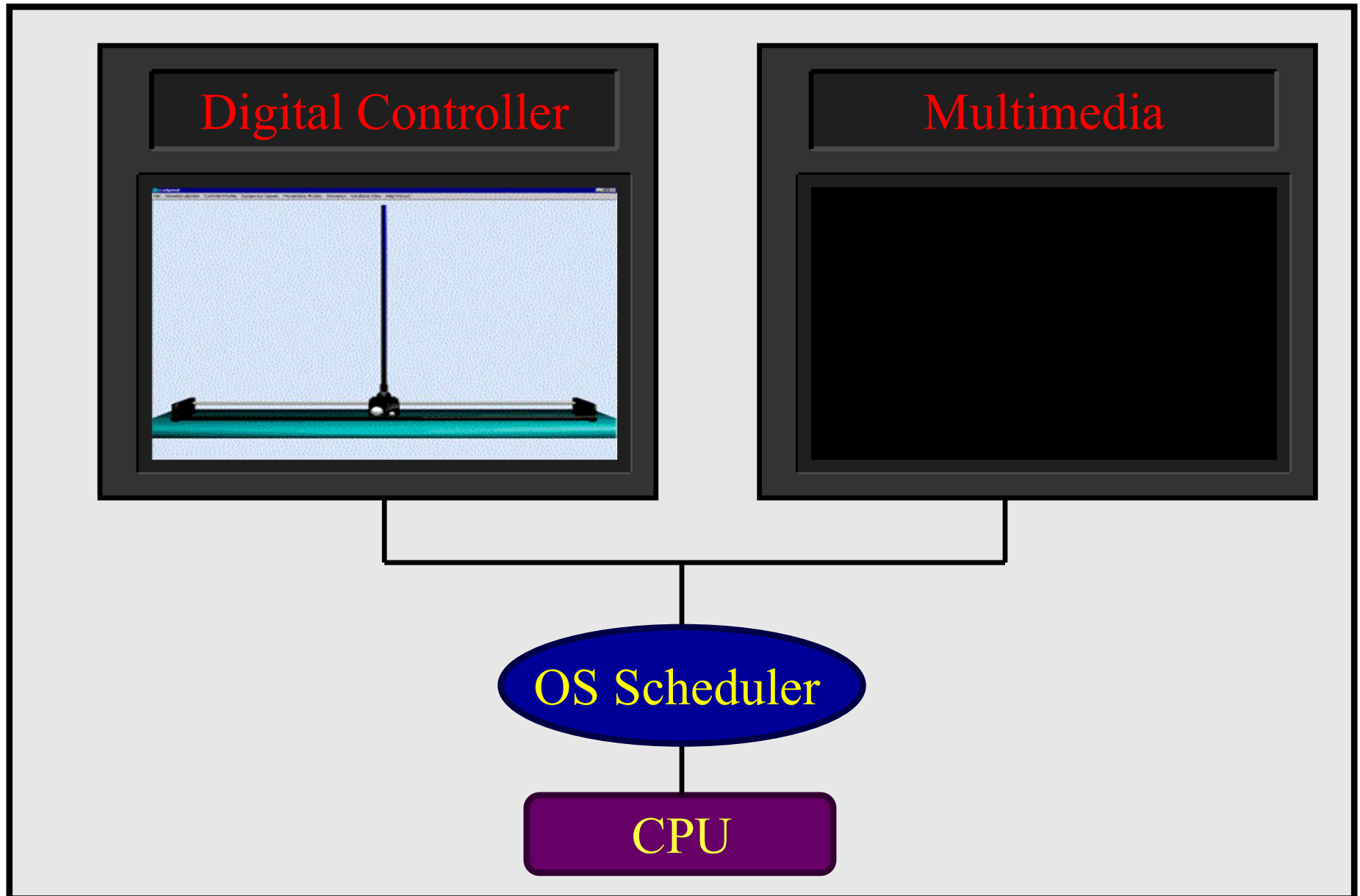
# Fundamental Real-Time Issue

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- To specify the timing constraints of real-time systems
- To achieve predictability on satisfying their timing constraints, possibly, with the existence of other real-time systems

# Scheduling Framework Example

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# Preemption

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- ❑ The running task can be interrupted at any point, so that a more important task that arrives can immediately gain the processor.
- ❑ The to-be-preempted task is interrupted and inserted to the ready queue, while CPU is assigned to the most important ready task which just arrived.

❑ Why preemption is needed in real-time systems?

Exception handling of a task

Treating with different criticalities of tasks, permits to anticipate the execution of the most critical activities

Efficient scheduling to improve system responsiveness

# Notation of scheduling (1)

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□  $J = \{J_1, \dots, J_n\}$       A set of tasks

□  $\sigma: \mathbf{R}^+ \rightarrow \mathbf{N}$       A schedule

A function mapping from time to task to assign task to CPU

If  $\sigma(t)=i$  for  $\forall t \in [t_1, t_2)$ , task  $J_i$  is executed during time duration  $[t_1, t_2)$ .

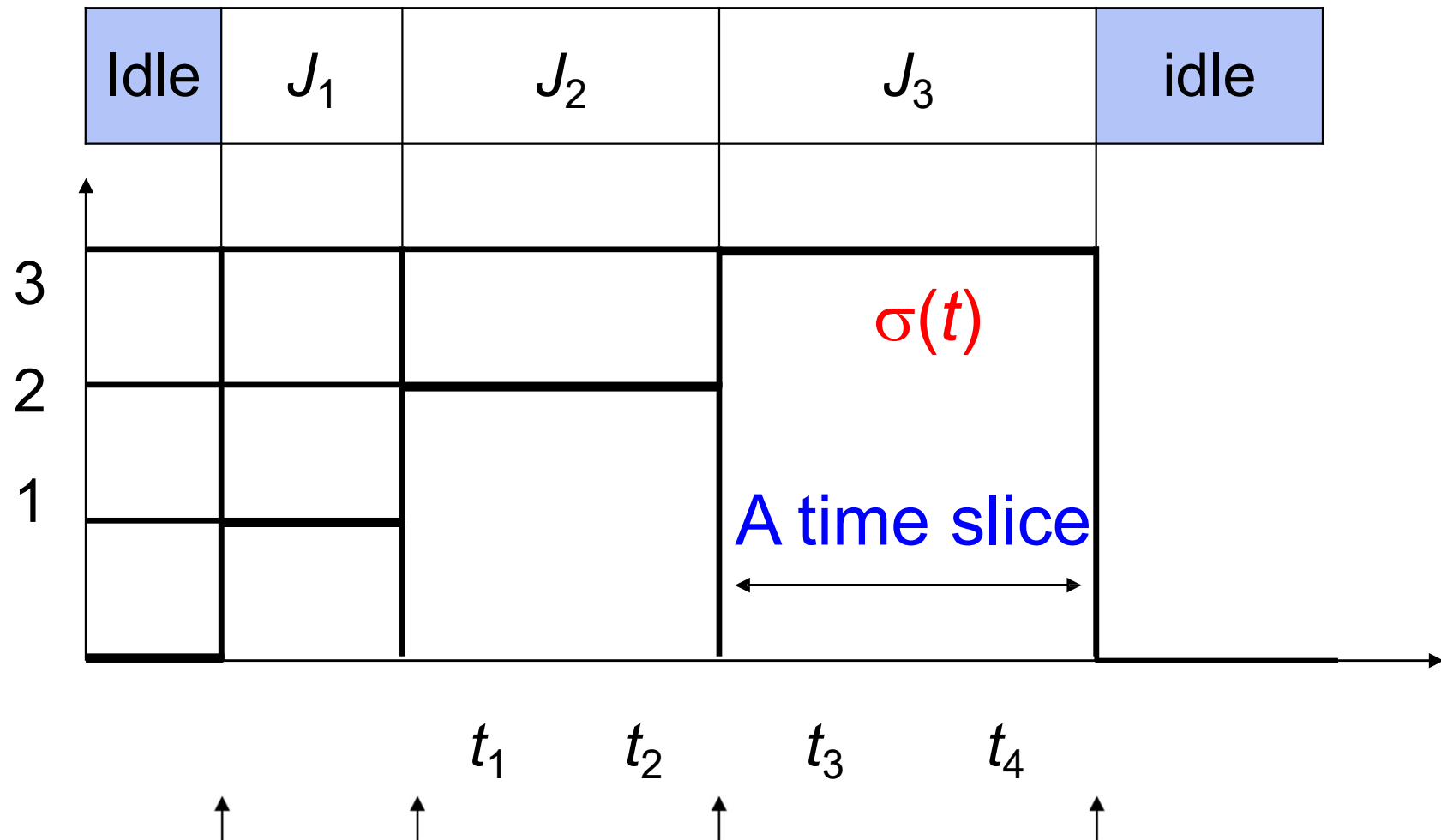
If  $\sigma(t)=0$ , the CPU is *idle*.

□ Simple translation

CPU time is divided in to time slices  $[t_1, t_2)$

During a time slice  $\sigma(t)=\text{const}$ , representing the task that is executed

# Notation of scheduling (2)

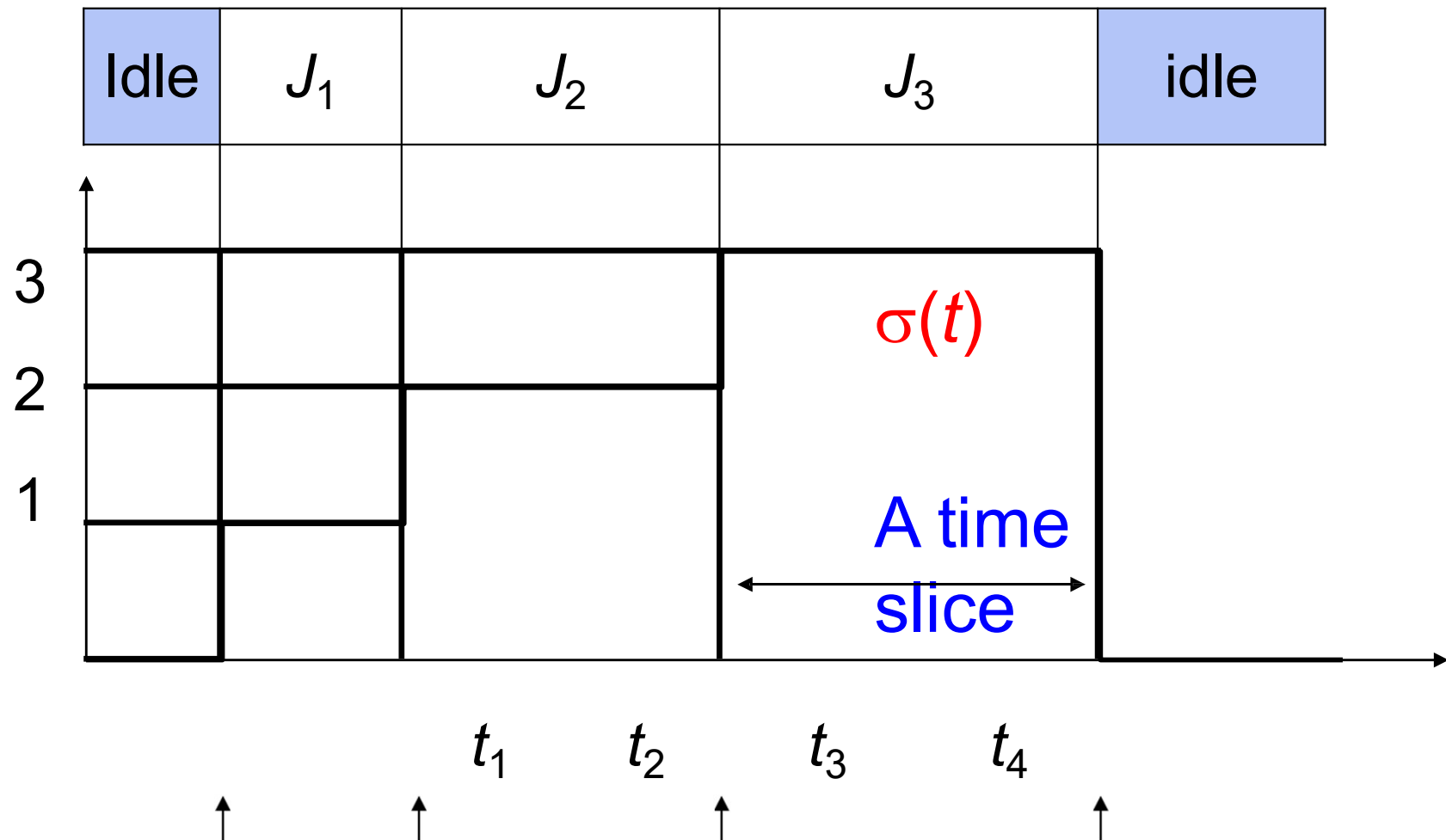


Context switching are performed at these times



# Notation of scheduling (2)

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**Context switching** are performed at these times

# Notation of scheduling (3)

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## □ Preemptive schedule

- A schedule in which the running task can be arbitrarily suspended at any time, to assign the CPU to another task

## □ Feasible schedule

- A schedule that all tasks can be completed according to a set of specified constraints

## □ Schedulable set of tasks

- A set of tasks that has at least one feasible schedule by some scheduling algorithm

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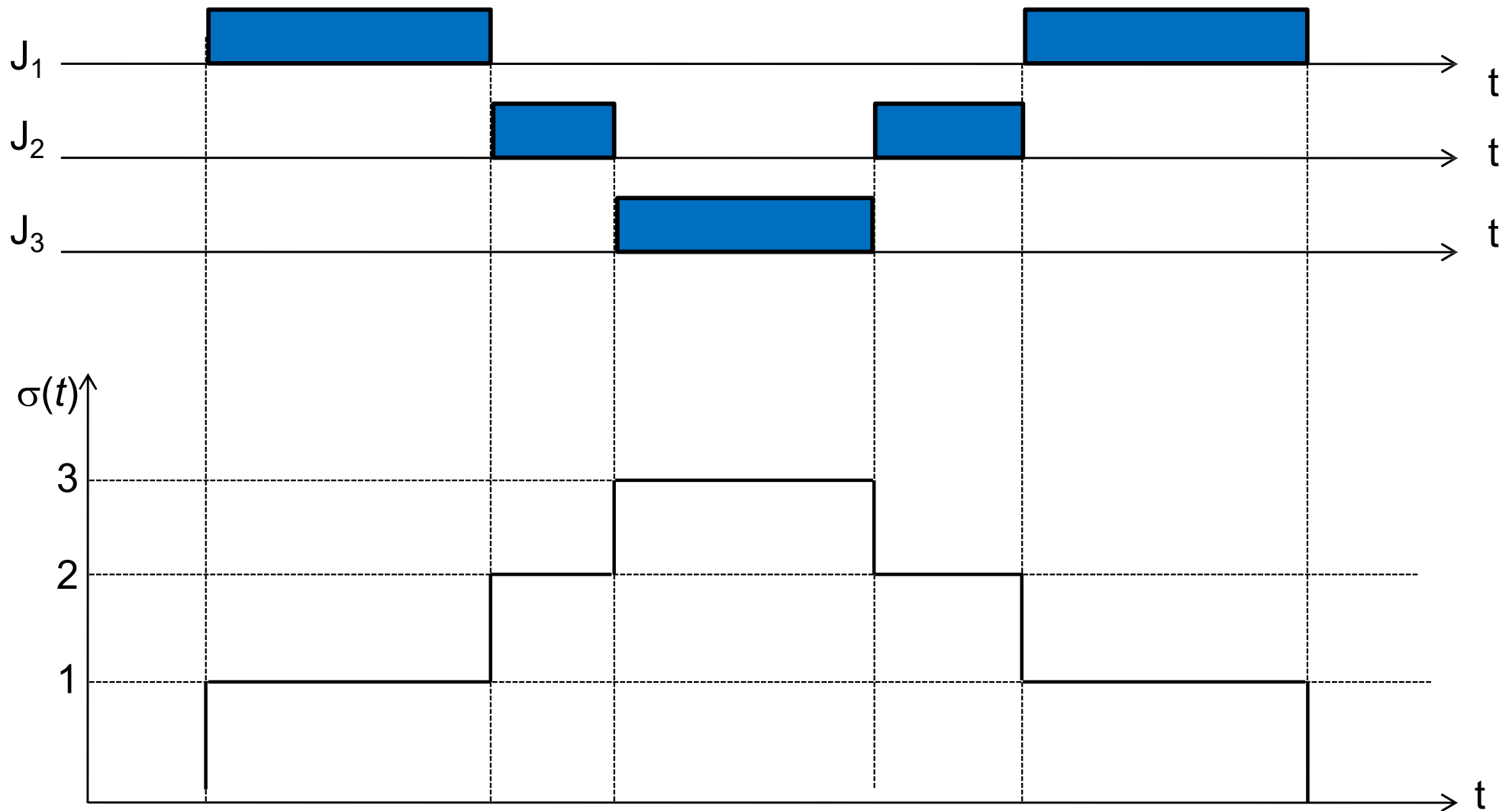
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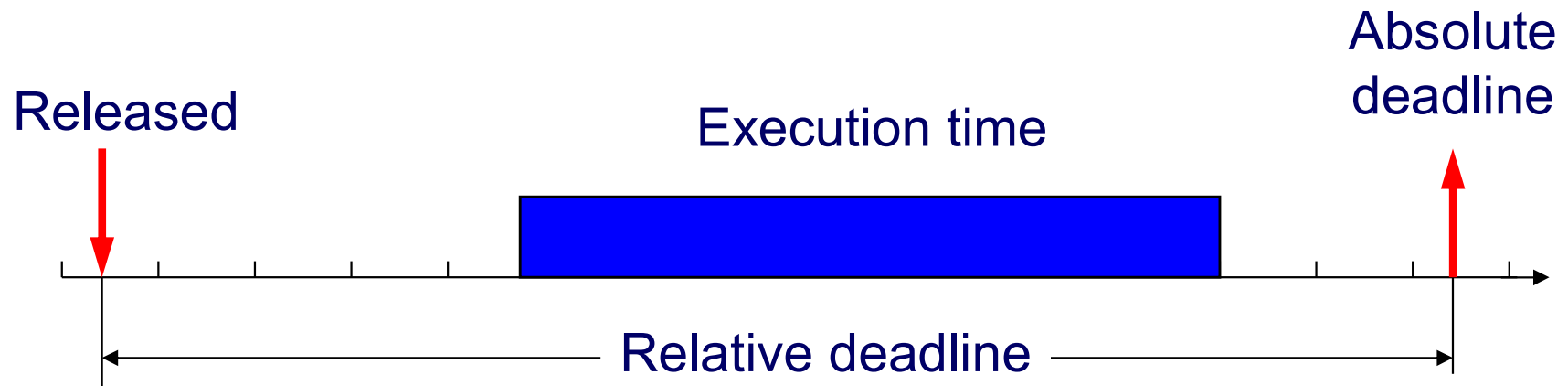
# Example of preemptive schedule



# Real-Time Workload

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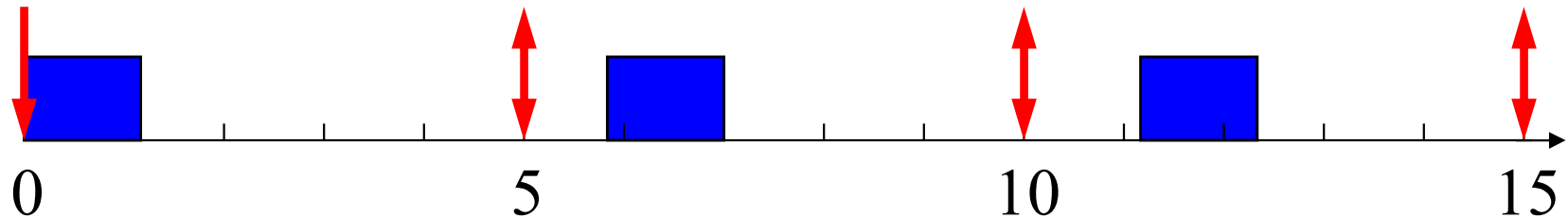
- Job (unit of work)
  - a computation, a file read, a message transmission, etc
- Attributes
  - Resources required to make progress
  - Timing parameters



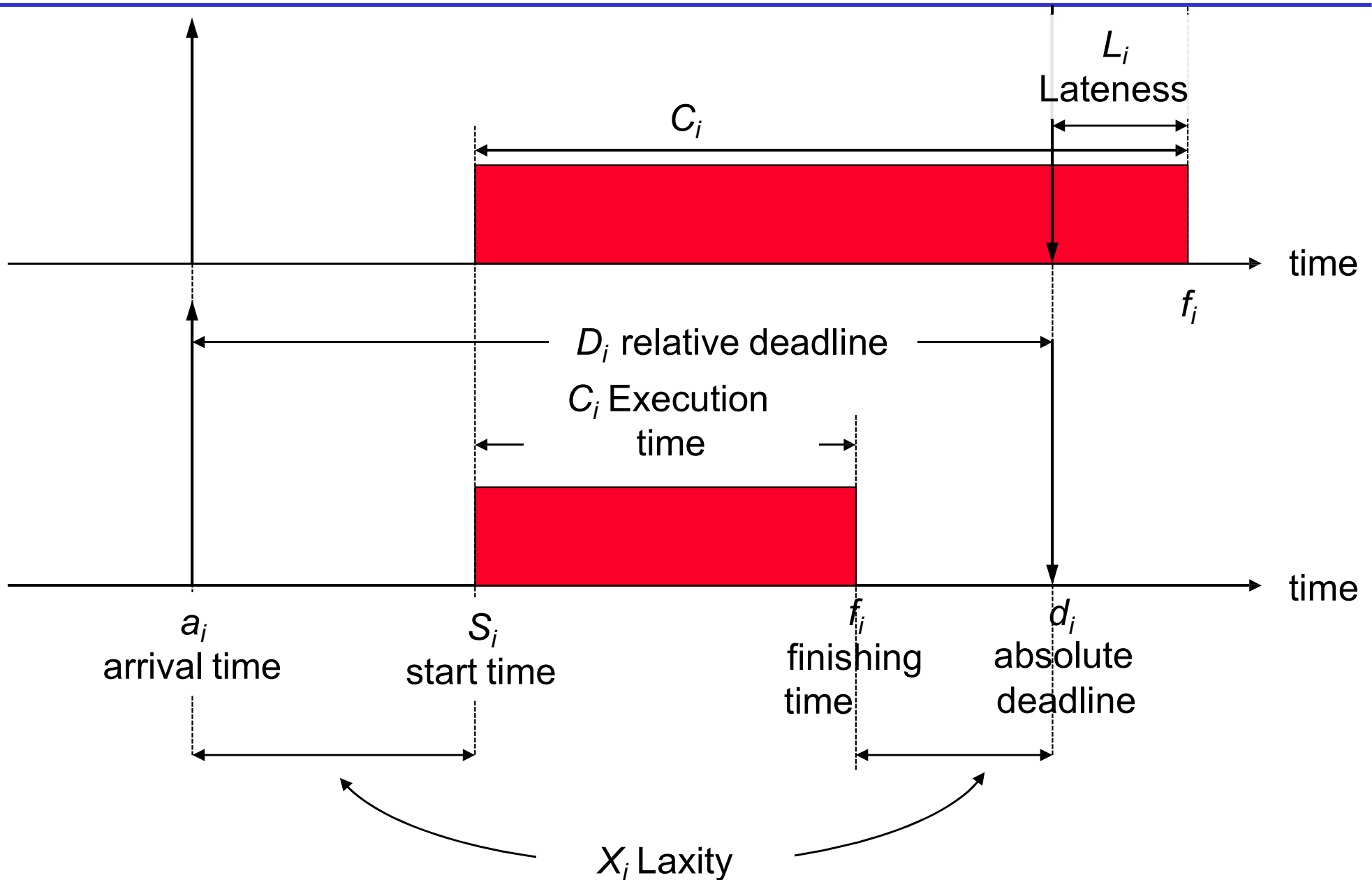
# Real-Time Task

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- Task : a sequence of similar jobs
  - Periodic task ( $p, e$ )
    - Its jobs repeat regularly
    - Period  $p$  = inter-release time ( $0 < p$ )
    - Execution time  $e$  = maximum execution time ( $0 < e < p$ )
    - Utilization  $U = e/p$

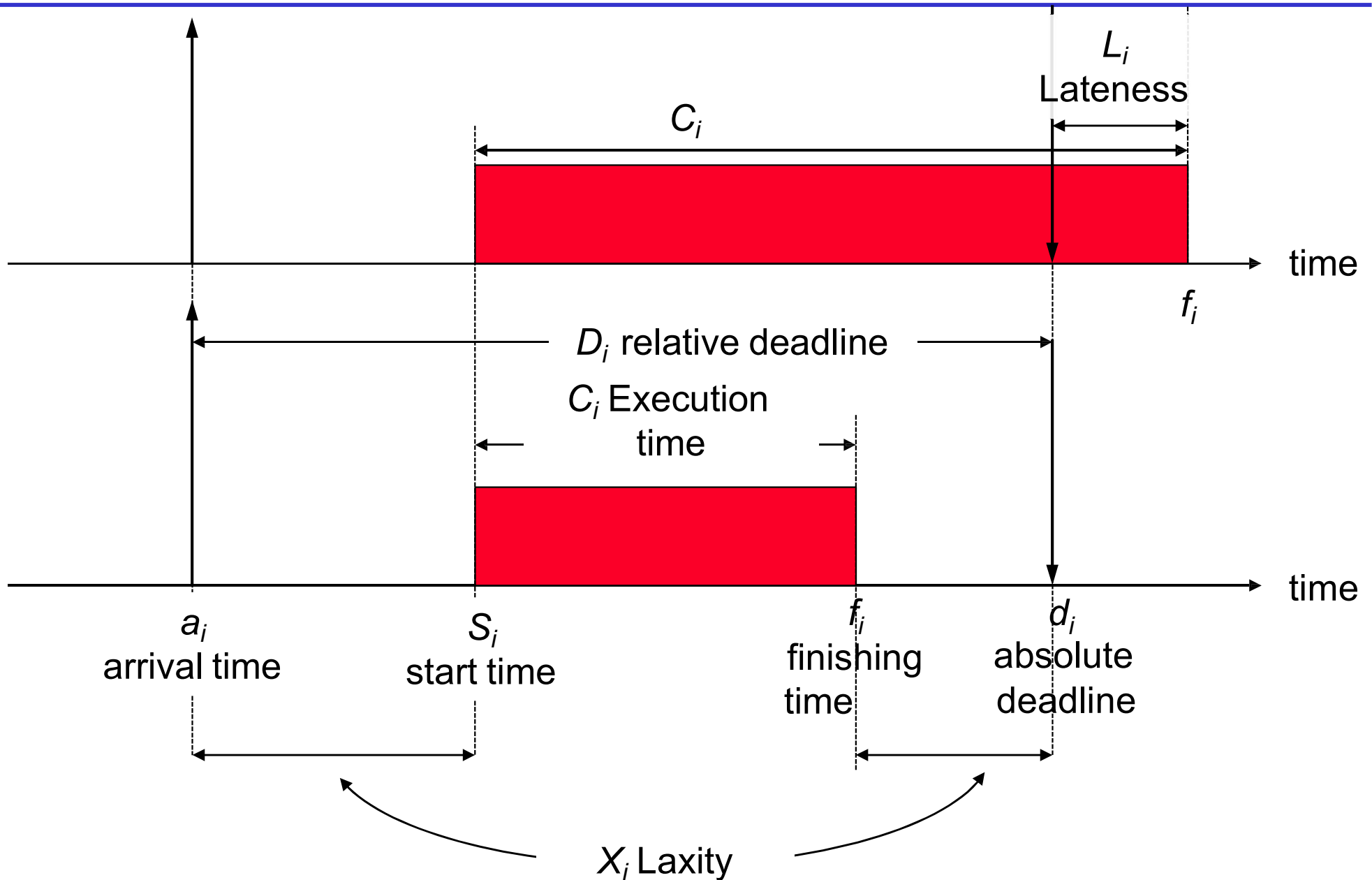


# Task parameters(1)





# Task parameters(1)



# Task parameters(2)

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## ❑ Other task parameters

- Criticality: Hard or Soft
- Value  $v_i$ : relative importance of task with respect to the other tasks
- Lateness: the delay of a task completion with respect to its deadline  $L_i = f_i - d_i$
- Tardiness or *Exceeding time*:  $E_i = \max(0, L_i)$  is the time a task stays active after its deadline.
- Laxity or *Slack time*  $X_i = d_i - a_i - C_i$  is the maximum time a task can be delayed on its activation to complete within its deadline

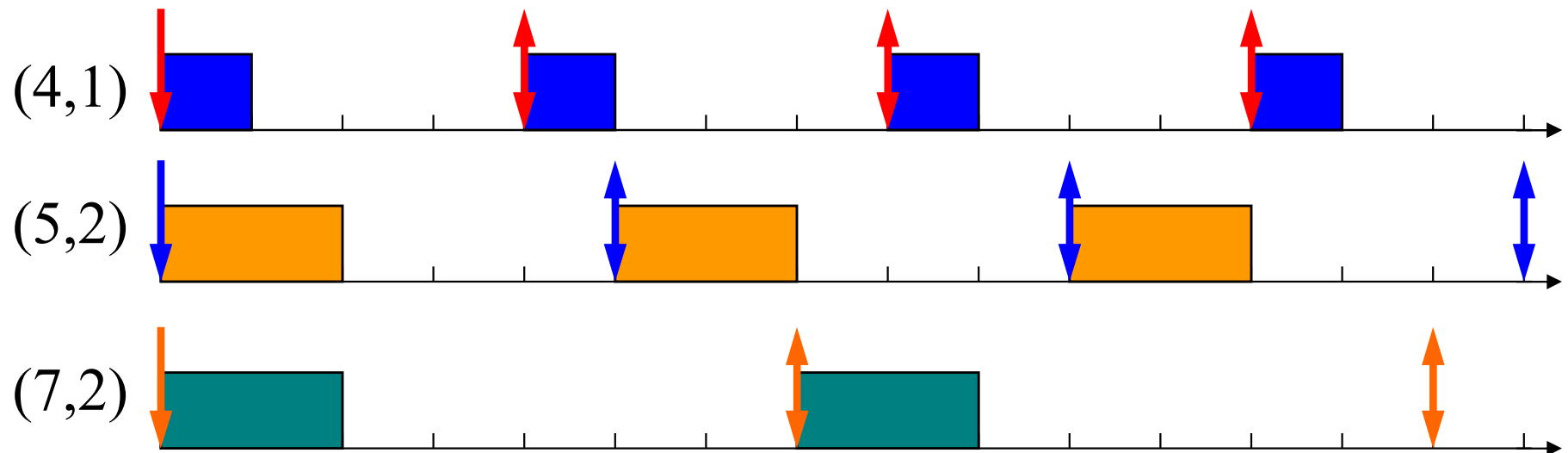
# Deadlines: Hard vs. Soft

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- **Hard** deadline
  - Disastrous or very serious consequences may occur if the deadline is missed
  - Validation is essential : can **all** the deadlines be met, even under worst-case scenario?
  - Deterministic guarantees
- **Soft** deadline
  - Ideally, the deadline should be met for maximum performance. The performance degrades in case of deadline misses.
  - Best effort approaches / statistical guarantees

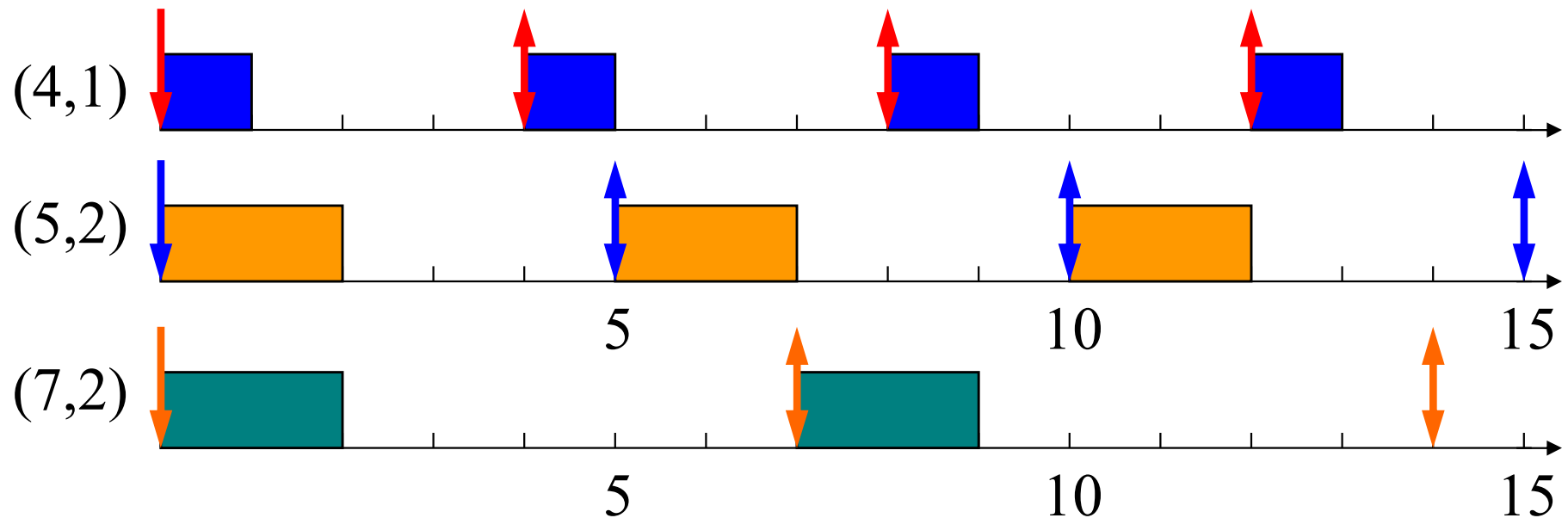
# Schedulability

- Property indicating whether a real-time system (a set of real-time tasks) can meet their deadlines



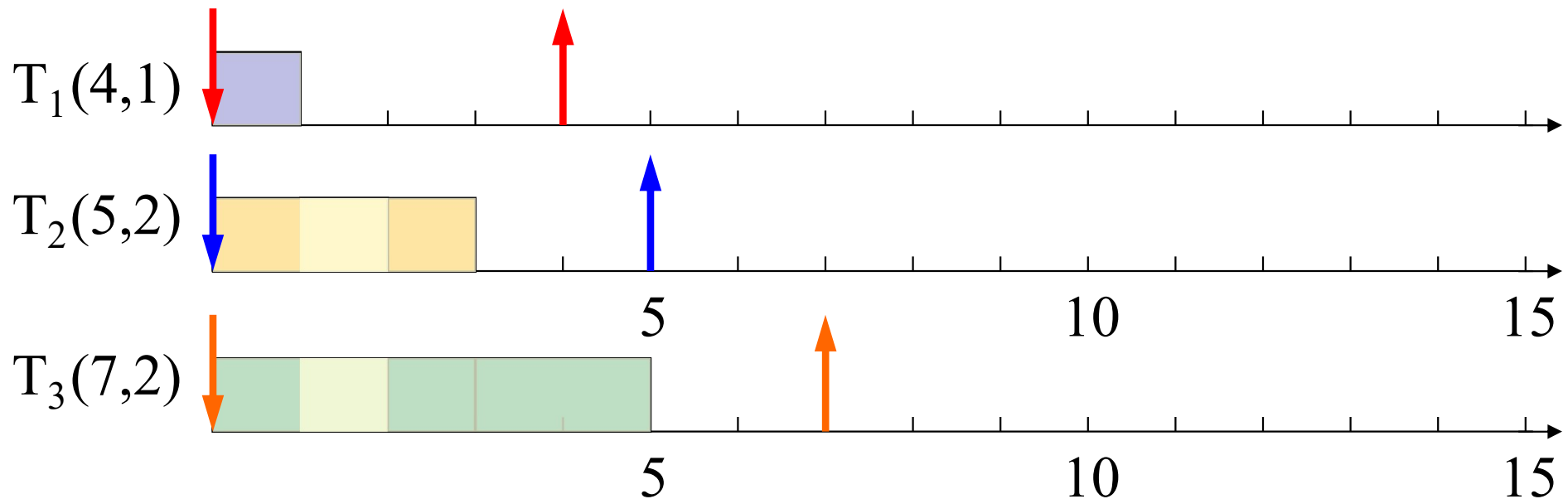
# Real-Time Scheduling

- Determines the order of real-time task executions
- Static-priority scheduling
- Dynamic-priority scheduling



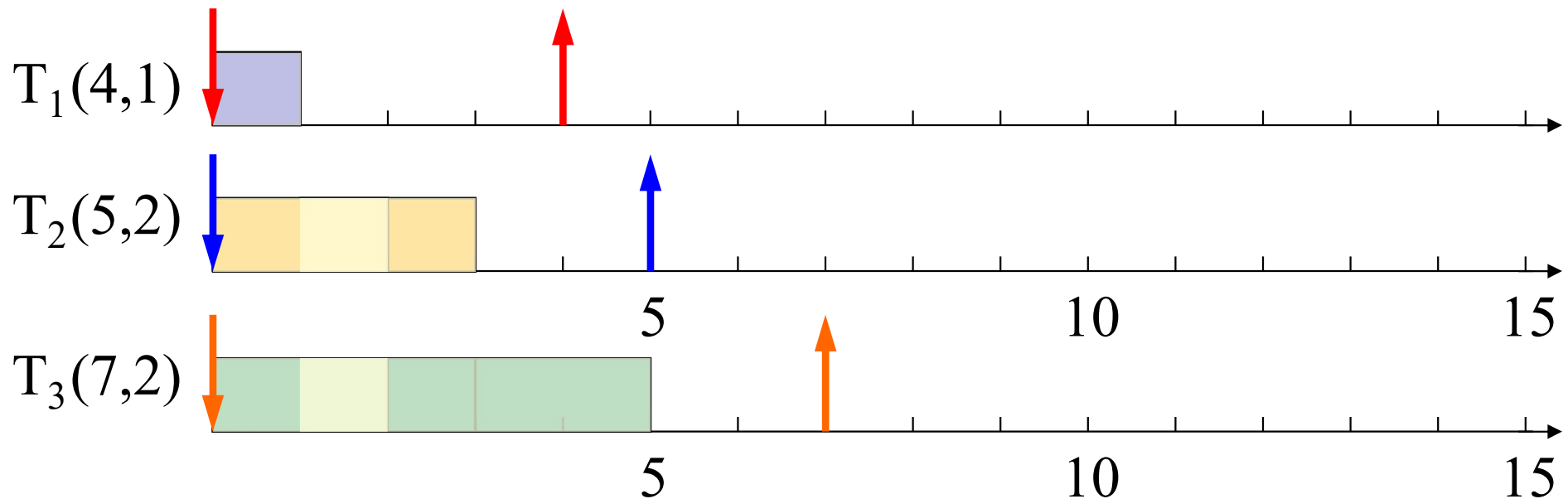
# RM (Rate Monotonic)

- Optimal static-priority scheduling
- It assigns priority according to period
- A task with a shorter period has a higher priority
- Executes a job with the shortest period



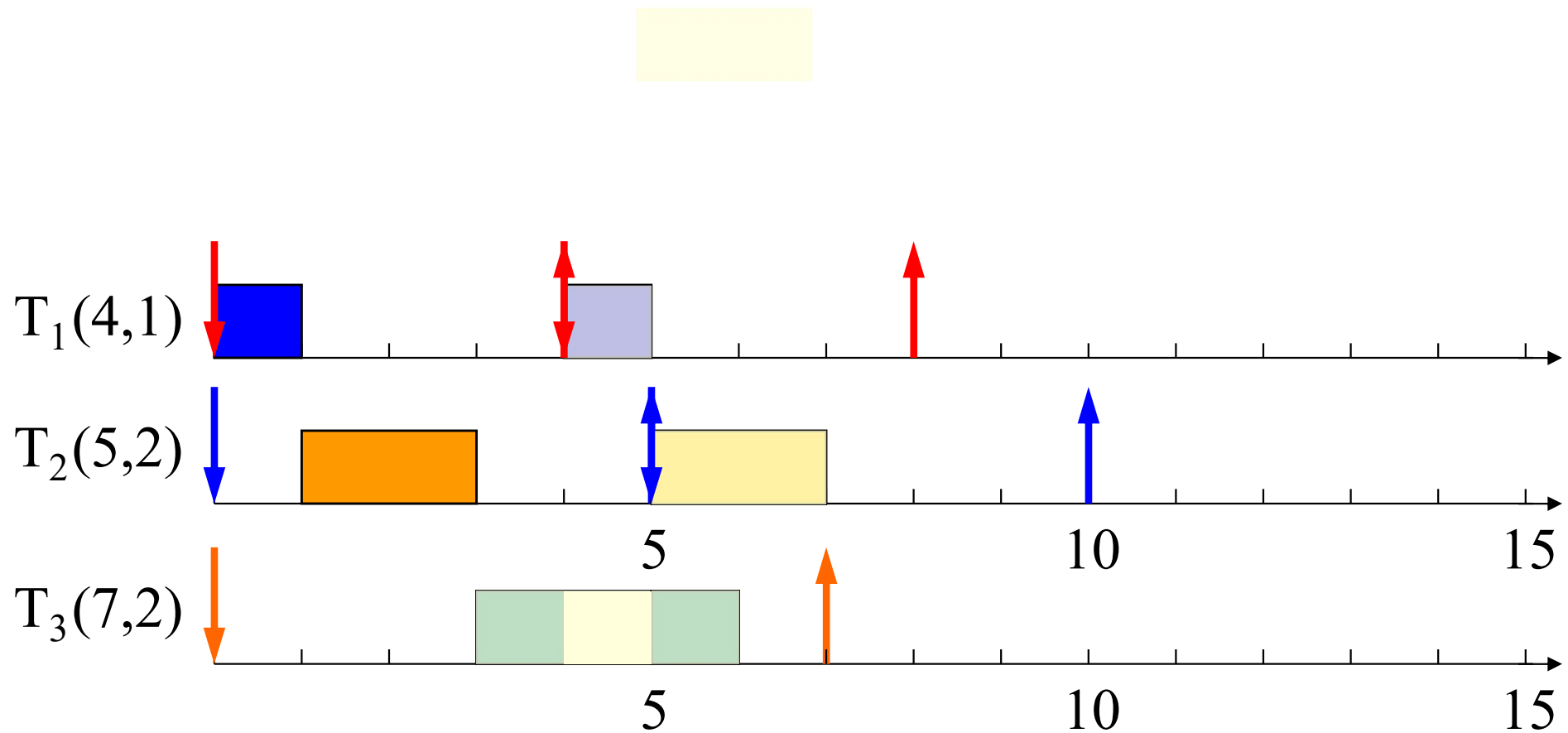
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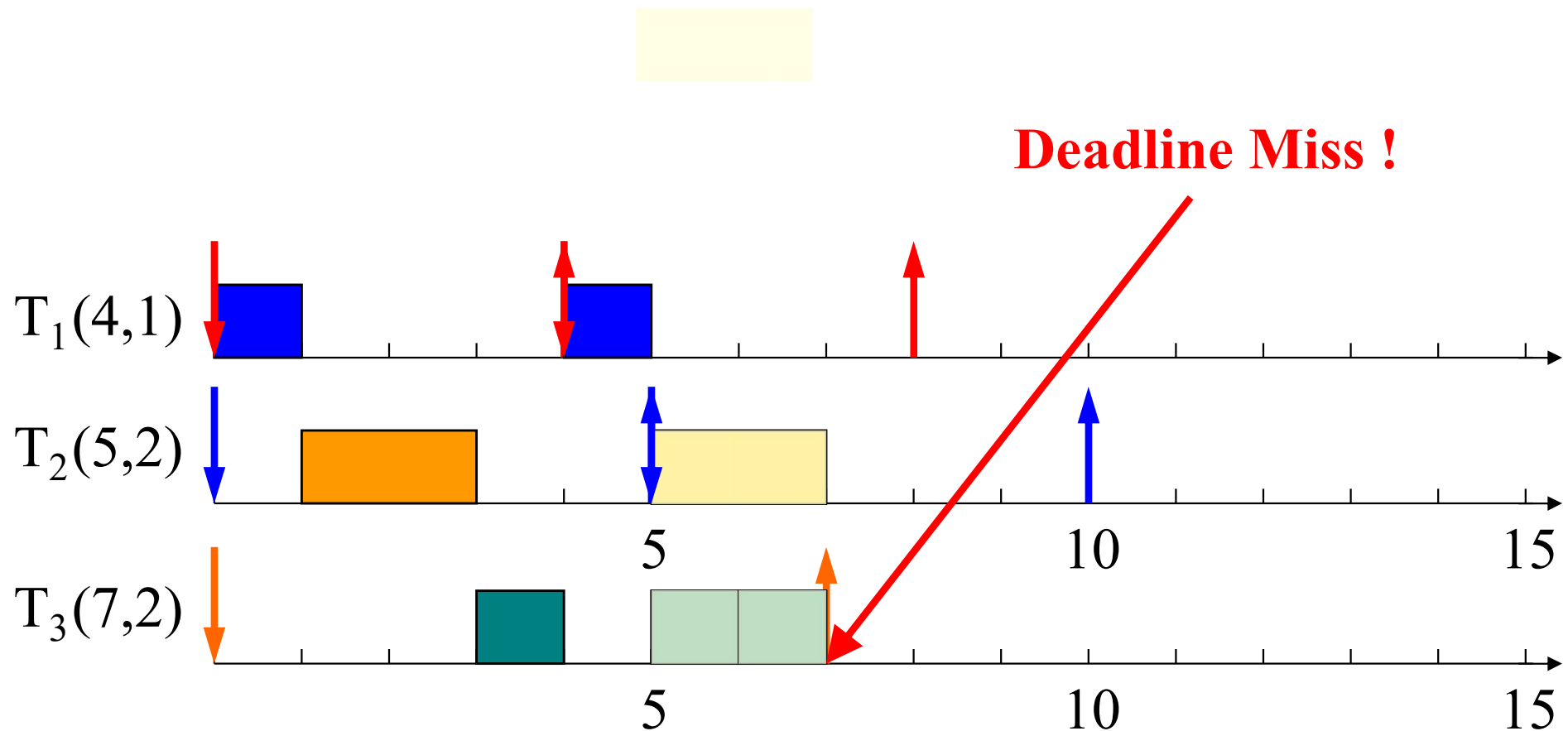
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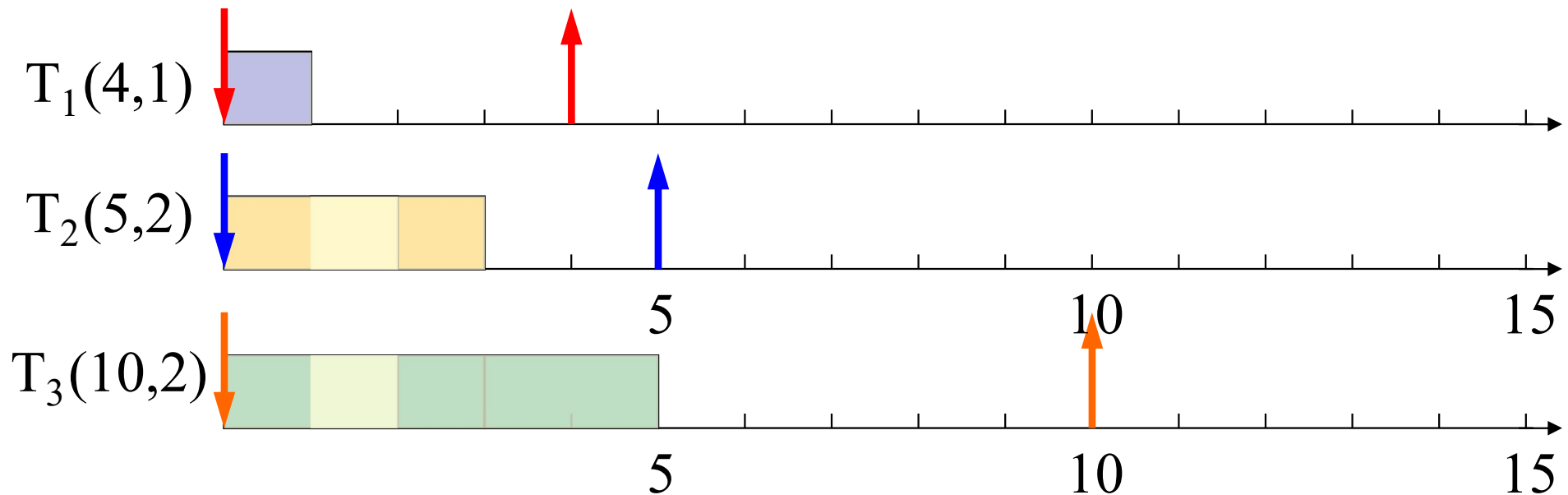
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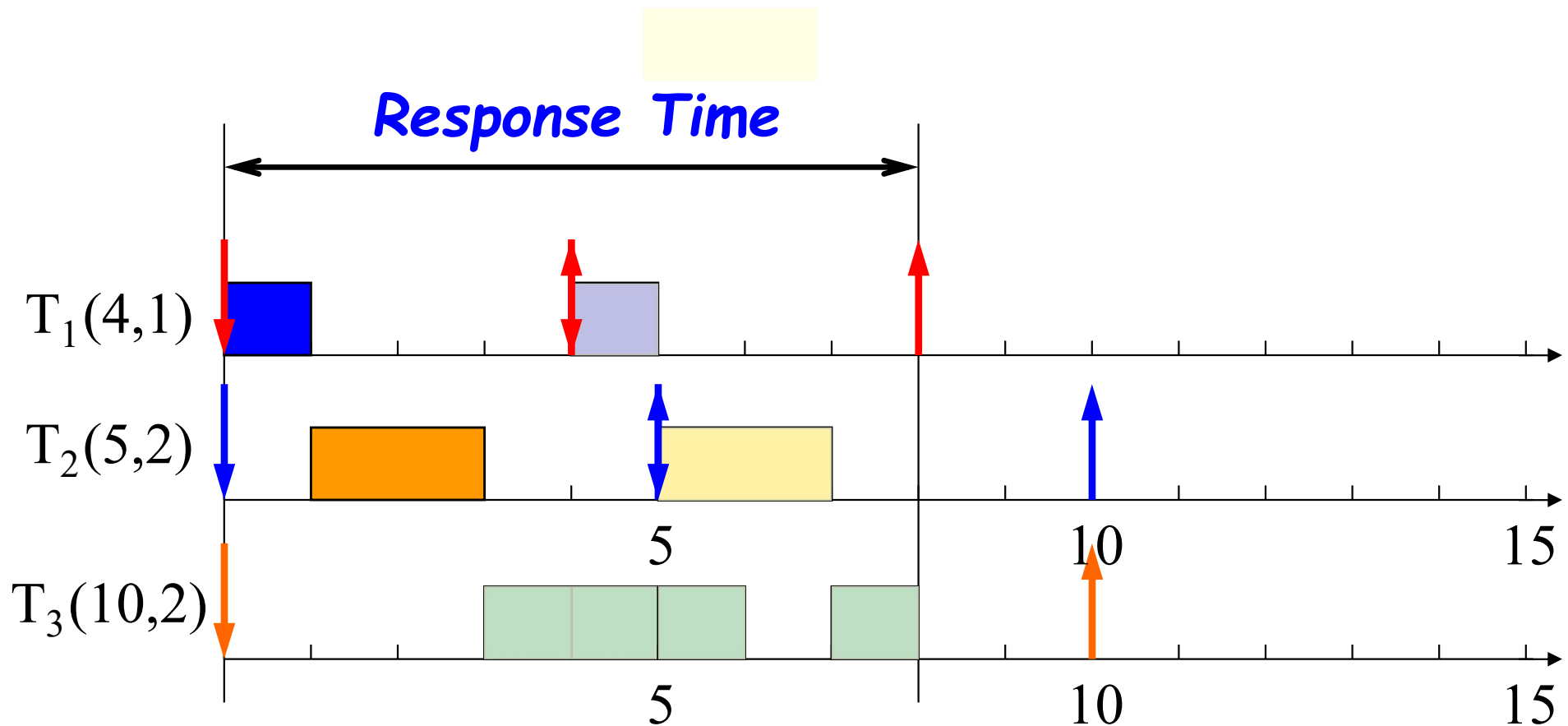
# Response Time

- Response time
  - Duration from released time to finish time



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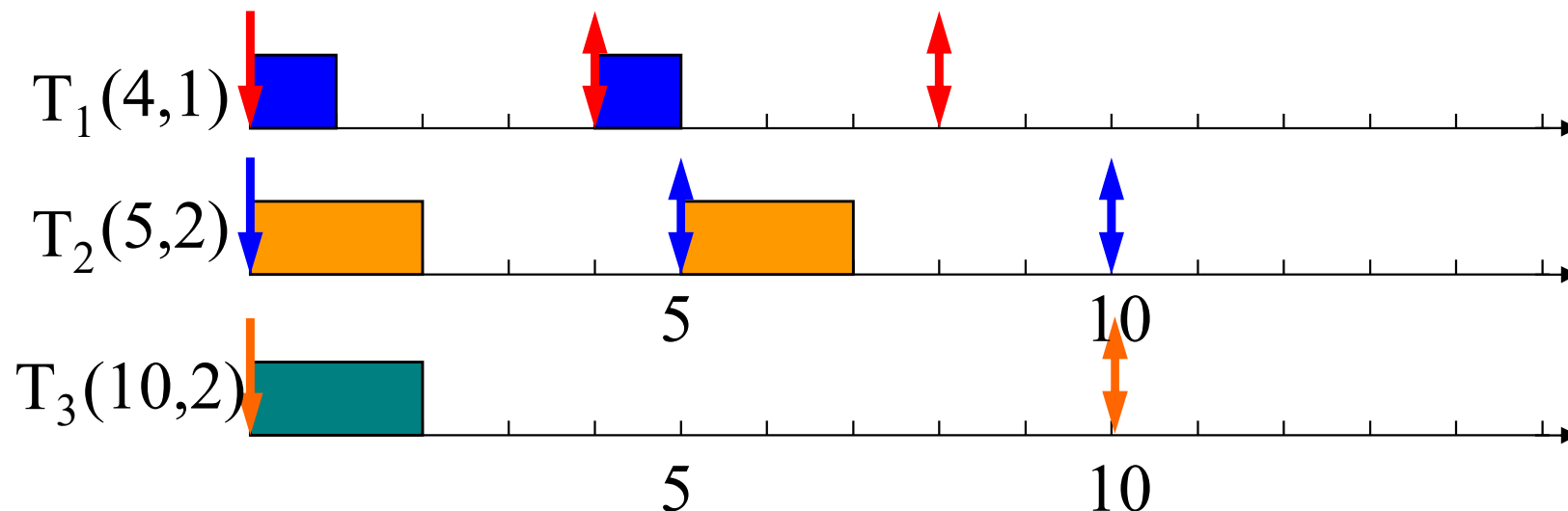


# Response Time

- Response Time ( $r_i$ ) [Audsley et al., 1993]

$$r_i = e_i + \sum_{T_k \in HP(T_i)} \left\lceil \frac{r_i}{p_k} \right\rceil \cdot e_k$$

- $HP(T_i)$  : a set of higher-priority tasks than  $T_i$

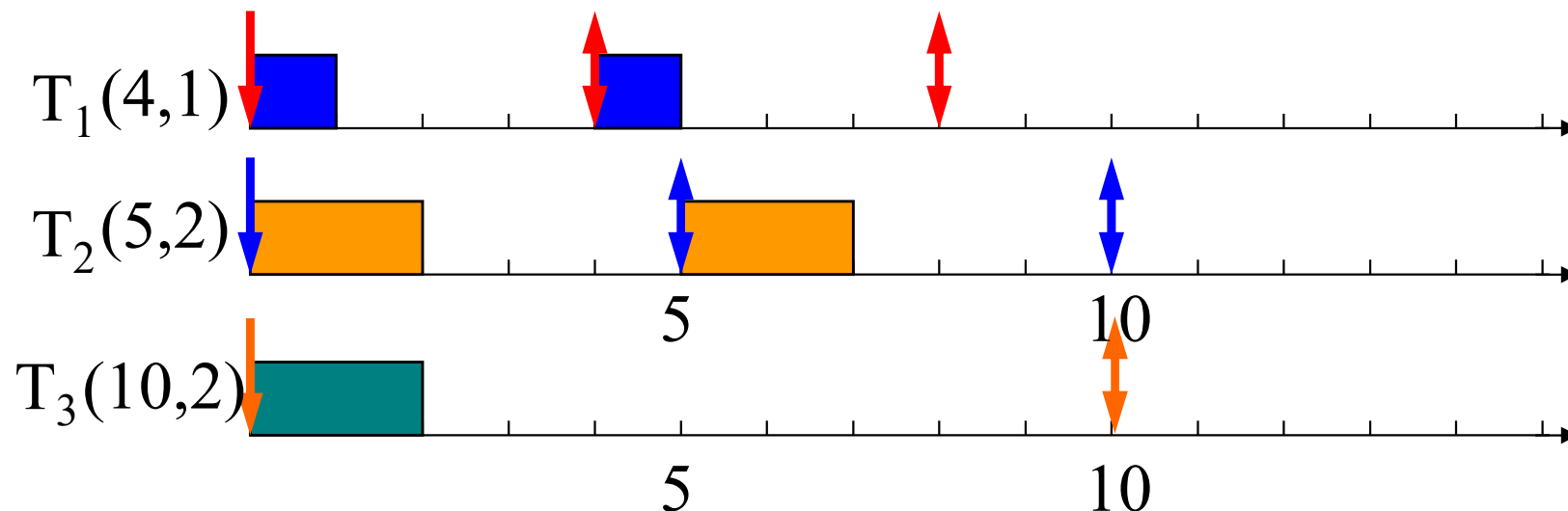


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# RM - Schedulability Analysis

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- Real-time system is schedulable under RM  
if and only if  $r_i \leq p_i$  for all task  $T_i(p_i, e_i)$

Joseph & Pandya,

“Finding response times in a real-time system”,  
The Computer Journal, 1986.

# RM – Utilization Bound

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- Real-time system is schedulable under RM if
$$\sum U_i \leq n (2^{1/n} - 1)$$

Liu & Layland,

“Scheduling algorithms for multi-programming in a hard-real-time environment”, *Journal of ACM*, 1973.

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# RM – Utilization Bound

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- Real-time system is schedulable under RM if
$$\sum U_i \leq n (2^{1/n} - 1)$$

- Example:  $T_1(4,1)$ ,  $T_2(5,1)$ ,  $T_3(10,1)$ ,

$$\begin{aligned}\sum U_i &= 1/4 + 1/5 + 1/10 \\ &= 0.55\end{aligned}$$

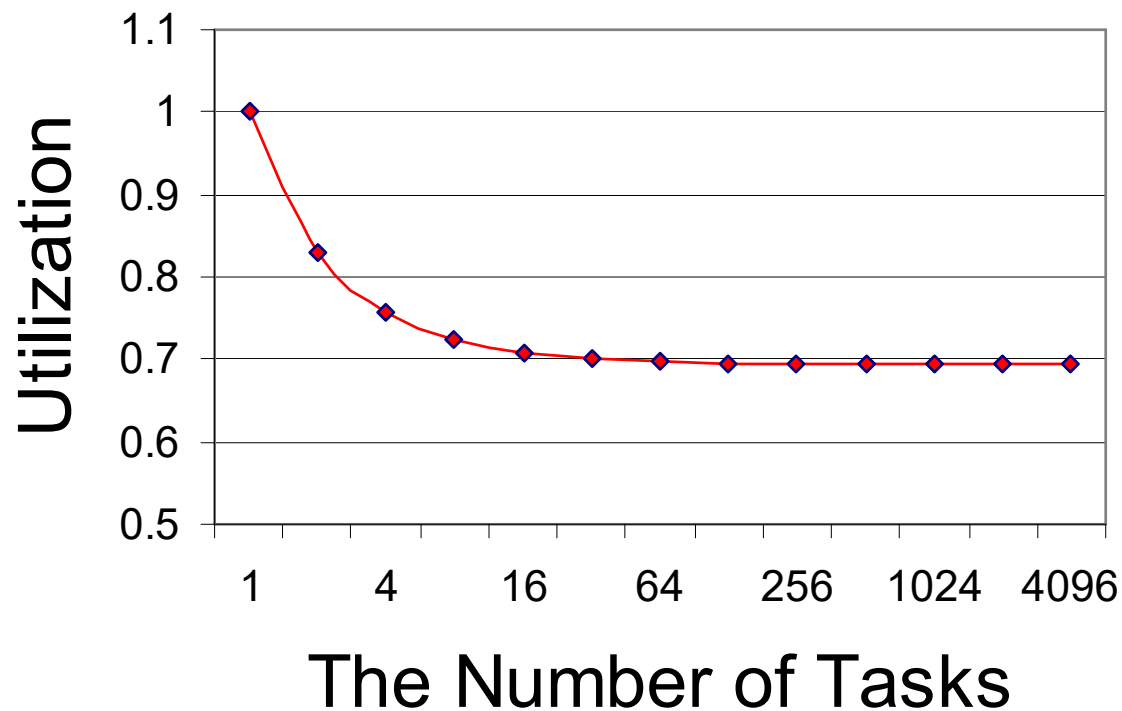
$$3 (2^{1/3} - 1) \approx 0.78$$

Thus,  $\{T_1, T_2, T_3\}$  is schedulable under RM.

# RM – Utilization Bound

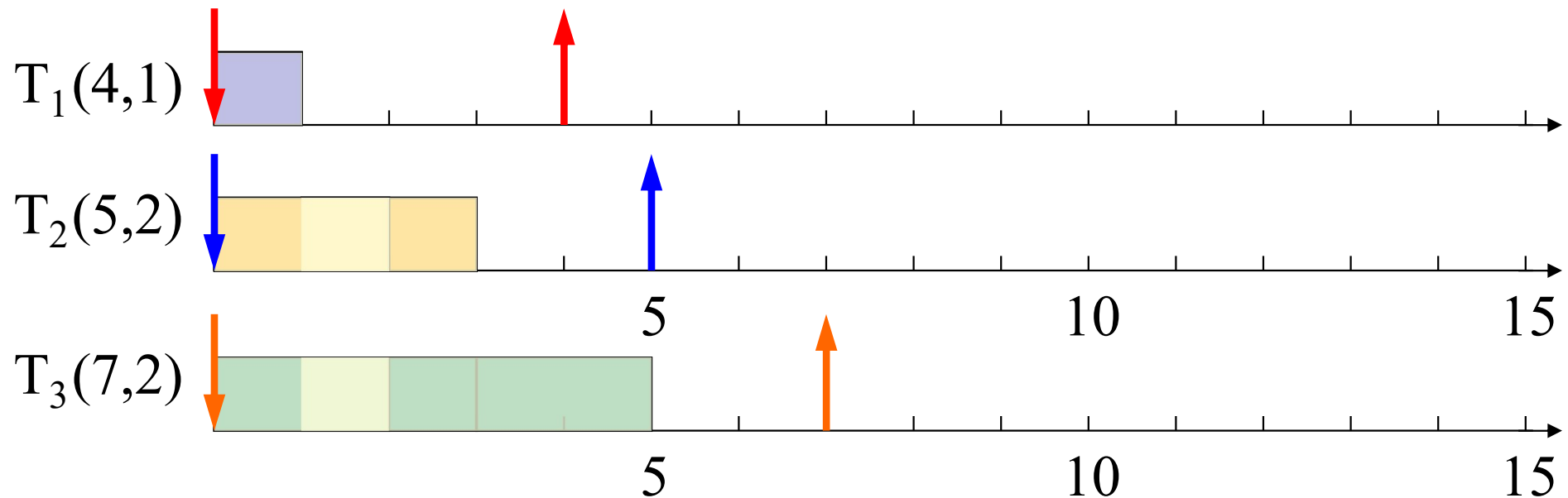
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## RM Utilization Bounds



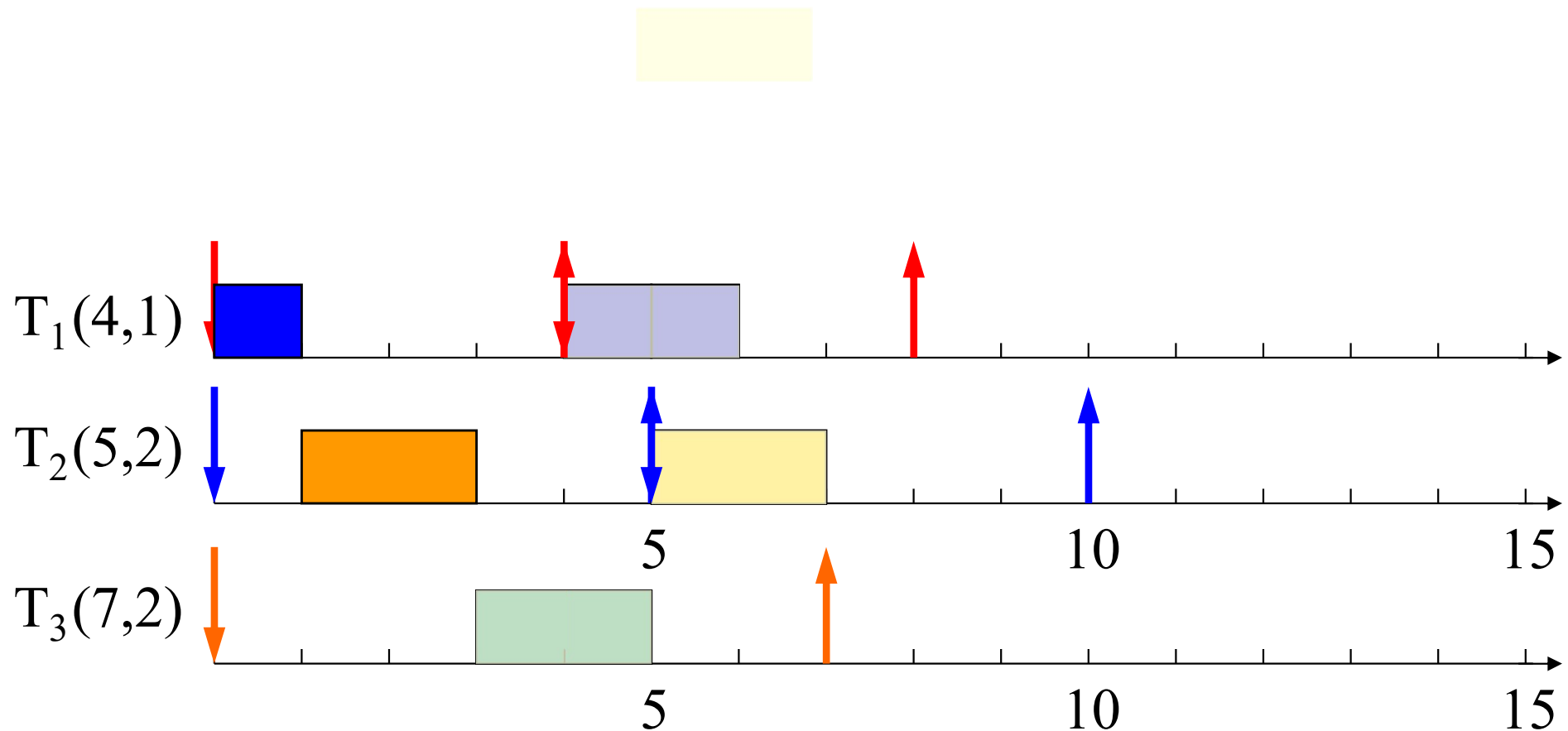
# EDF (Earliest Deadline First)

- Optimal dynamic priority scheduling
- A task with a shorter deadline has a higher priority
- Executes a job with the earliest deadline



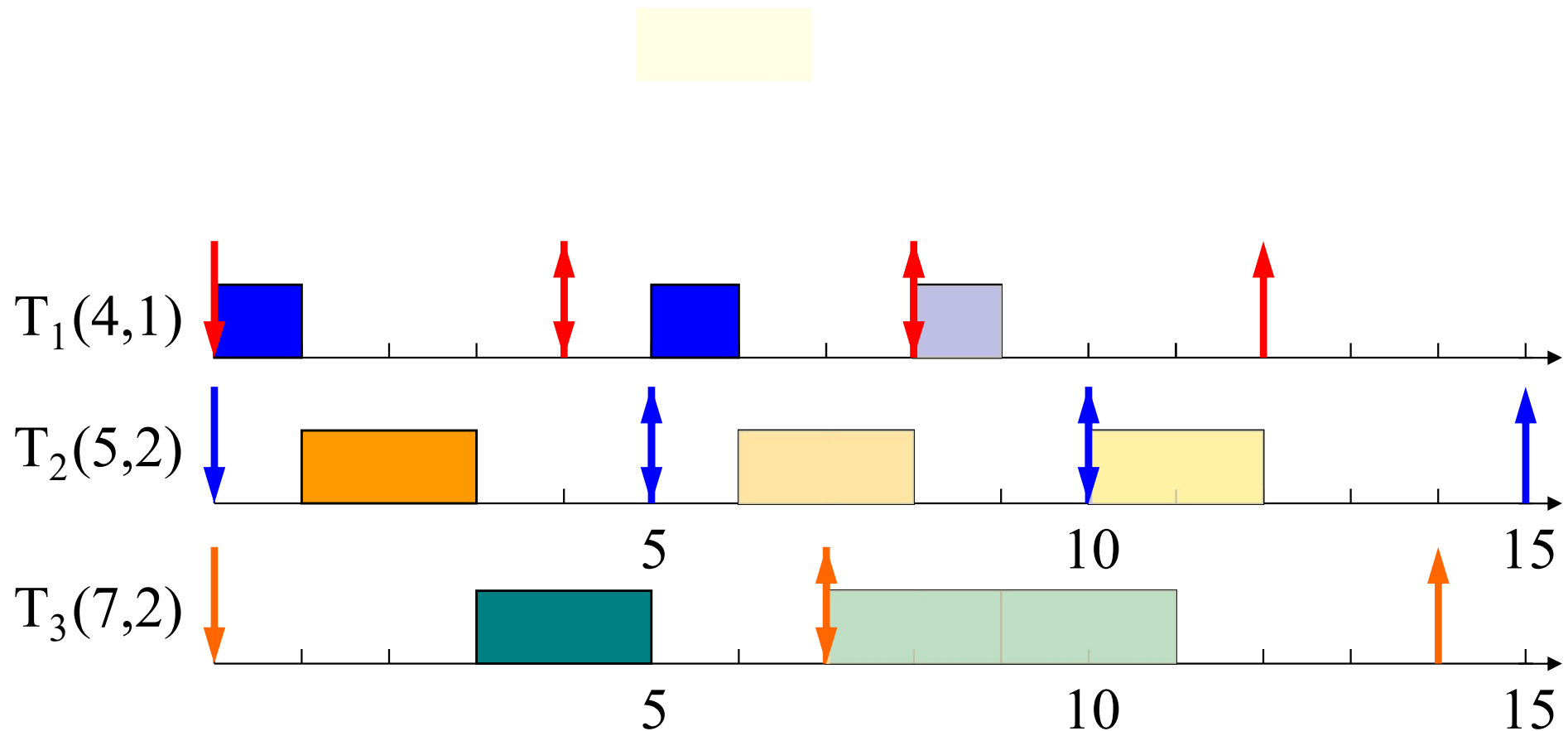
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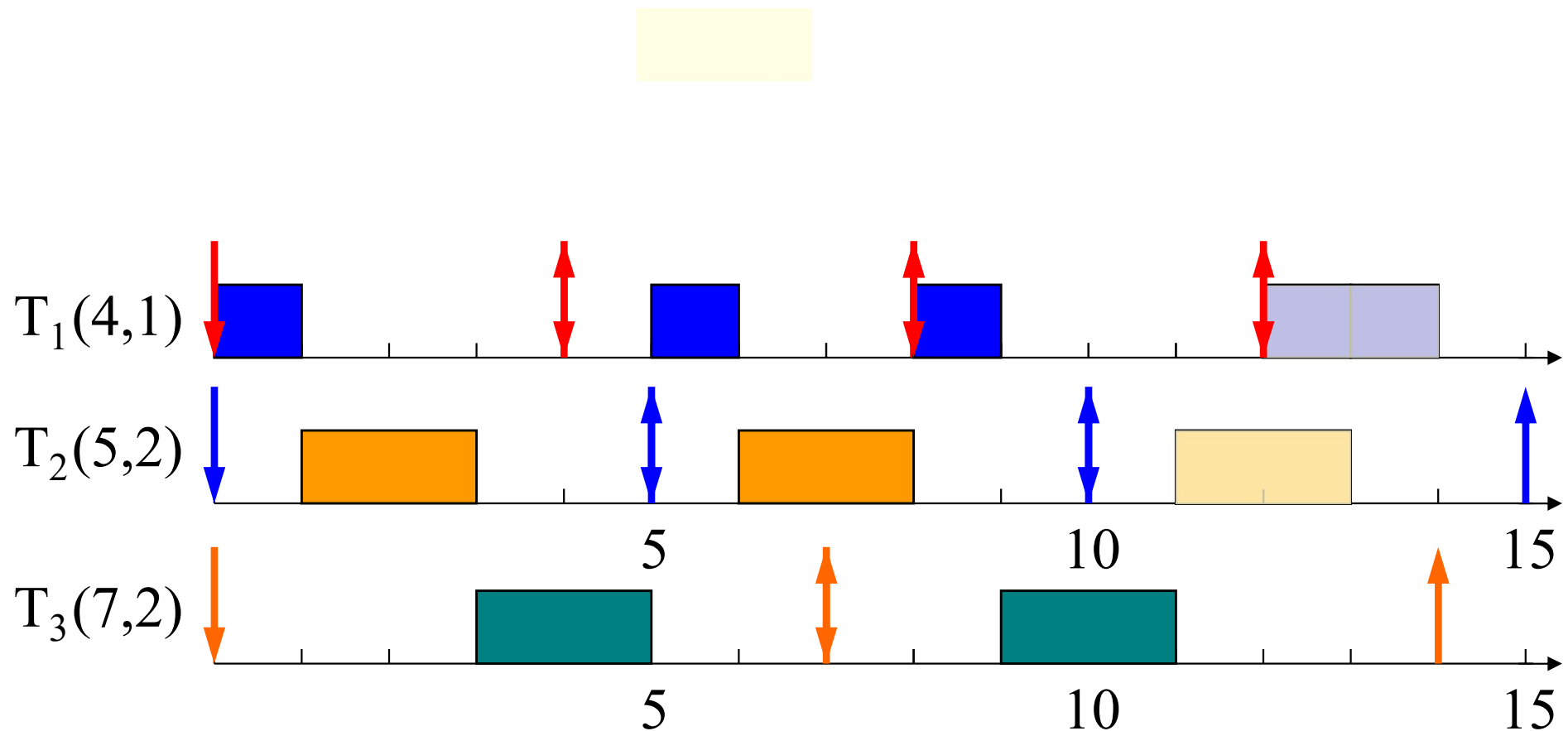
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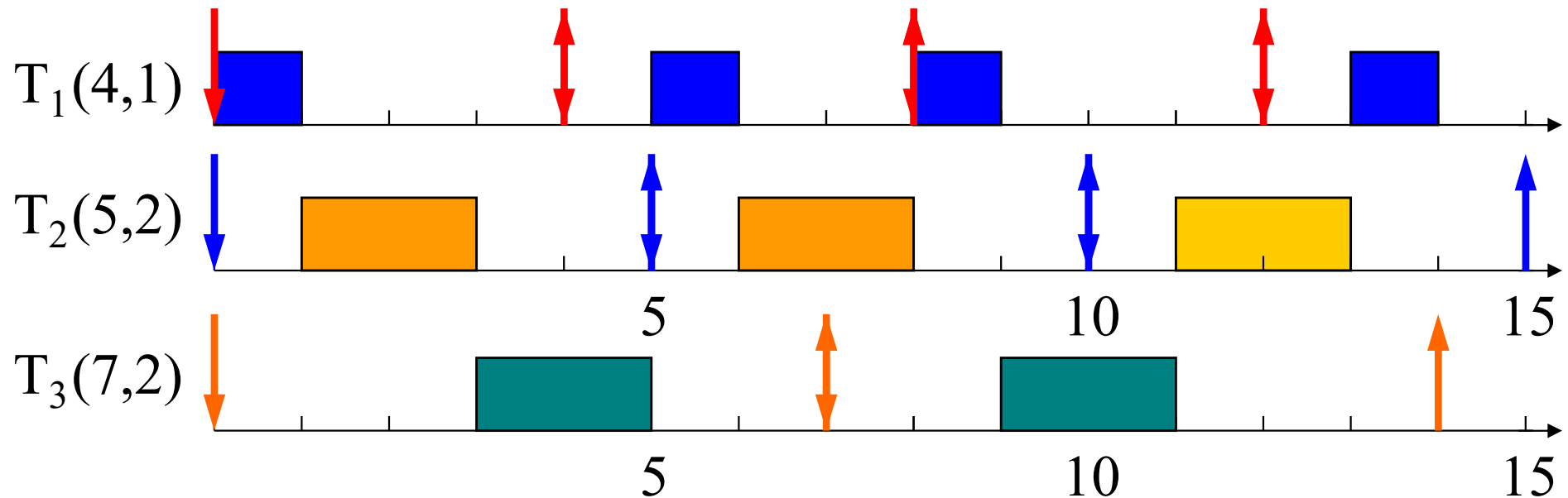
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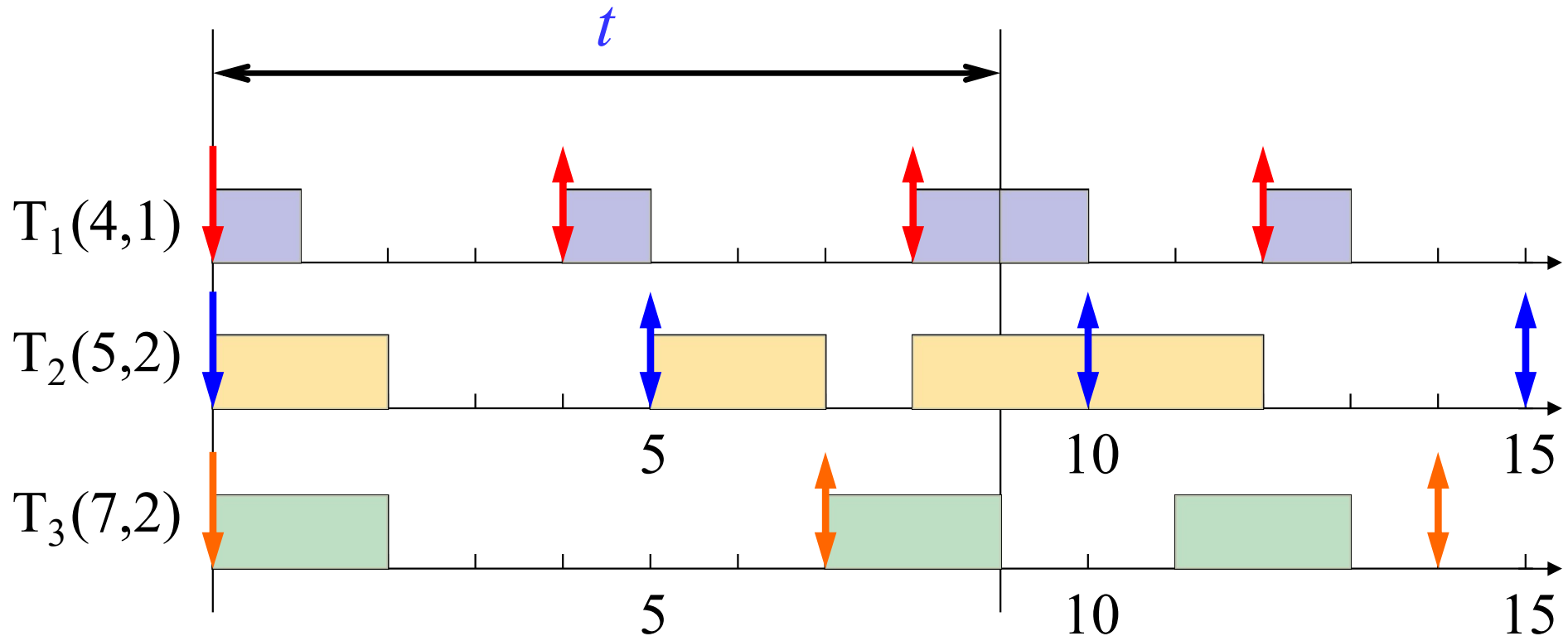
# EDF (Earliest Deadline First)

- Optimal scheduling algorithm
  - if there is a schedule for a set of real-time tasks, EDF can schedule it.



# Processor Demand Bound

- Demand Bound Function :  $dbf(t)$ 
  - the **maximum processor demand** by workload over any interval of length  $t$





# EDF - Schedulability Analysis

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- Real-time system is schedulable under EDF  
if and only if  $\text{dbf}(t) \leq t$  for all interval  $t$

Baruah et al.

“Algorithms and complexity concerning the preemptive scheduling of periodic, real-time tasks on one processor”, Journal of Real-Time Systems, 1990.

- Demand Bound Function :  $\text{dbf}(t)$ 
  - the maximum processor demand by workload over any interval of length  $t$

# EDF – Utilization Bound

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- Real-time system is schedulable under EDF if and only if

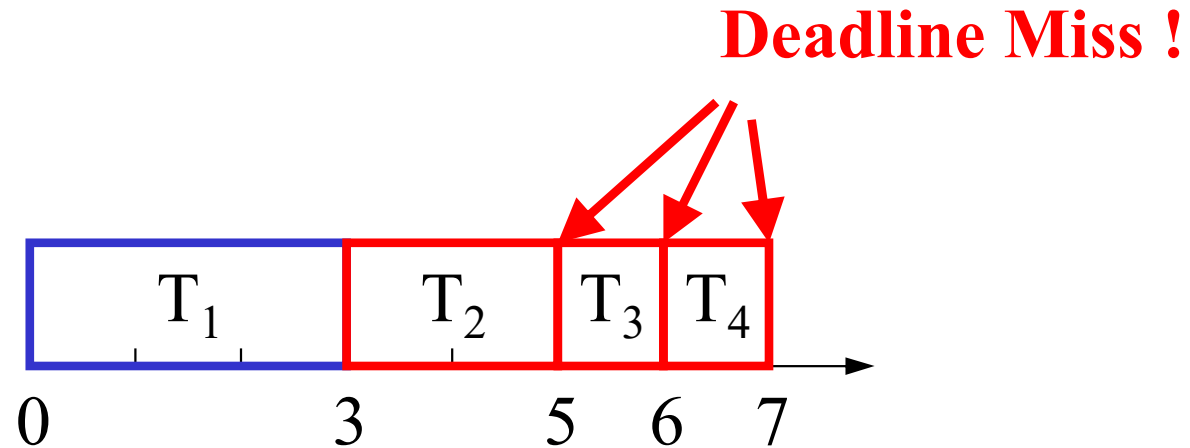
$$\sum U_i \leq 1$$

Liu & Layland,

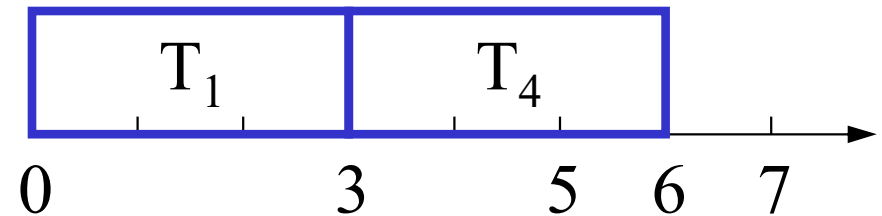
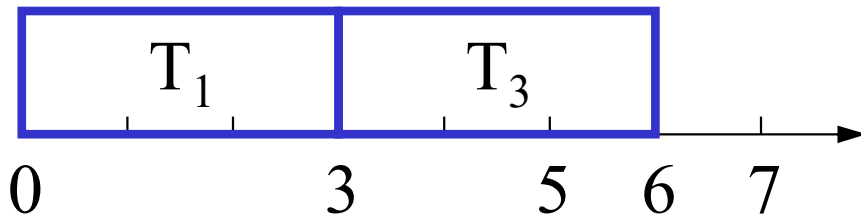
“Scheduling algorithms for multi-programming in a hard-real-time environment”, *Journal of ACM*, 1973.

# EDF – Overload Conditions

- Domino effect during overload conditions
  - Example:  $T_1(4,3)$ ,  $T_2(5,3)$ ,  $T_3(6,3)$ ,  $T_4(7,3)$



Better schedules :



# Two common scheduling schemes

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- **Rate monotonic (RM)**
  - Static priority scheme
  - Preemption required
  - Simple to implement
  - Nice properties
- **Earliest deadline first (EDF)**
  - Dynamic priority scheme
  - Preemption required
  - Harder to implement
  - Very nice properties

# Sharing resources

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- Need some kind of a lock on a resource.
  - If a high priority task finds a resource is locked, it goes to sleep until the resource is available.
  - Task is woken up when resource is freed by lower priority task.
  - Sounds reasonable, but leads to problems.
- More formally stated on next slide.

# Priority Inversion

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- In a preemptive priority based real-time system, sometimes tasks may need to access resources that cannot be shared.
  - The method of ensuring exclusive access is to guard the critical sections with binary semaphores.
  - When a task seeks to enter a critical section, it checks if the corresponding semaphore is locked.
  - If it is not, the task locks the semaphore and enters the critical section.
  - When a task exits the critical section, it unlocks the corresponding semaphore.
- This could cause a high priority task to be waiting on a lower priority one.
  - Even worse, a medium priority task might be running and cause the high priority task to not meet its deadline!

# Example: Priority inversion

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- Low priority task "C" locks resource "Z".
- High priority task "A" preempts "C" then requests resource "Z"
  - Deadlock, but solvable by having "A" sleep until resource is unlocked.
- But if medium priority "B" were to run, it would preempt C, thus effectively making C and A run with a lower priority than B.
  - Thus priority *inversion*.

# Solving Priority inversion

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- Priority Inheritance
  - When a high priority task sleeps because it is waiting on a lower priority task, have it boost the priority of the blocking task to its own priority.