

01-12-23

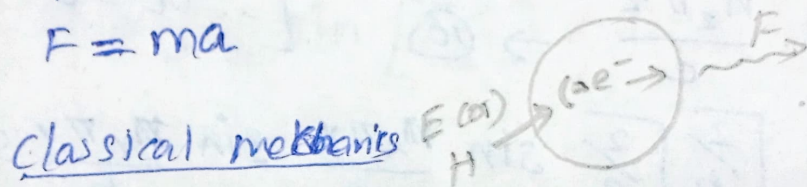
Applied Quantum Mechanics

Day 58

$$F = -Kx$$

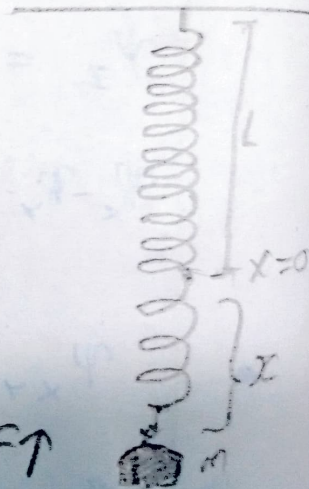
$$F = ma$$

Classical mechanics



- Harmonic motion - displacement of particles \rightarrow moves \rightarrow restoring force \rightarrow back to origin.

\Rightarrow Harmonic Oscillator of Quantum mech is similar to classical mechanics.



$$\frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2} (E - V) \psi = 0 \rightarrow (1)$$

$$\Rightarrow P.E = \frac{1}{2} KX \rightarrow (2)$$

$$\frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2} [E - \frac{1}{2} KX] \psi = 0 \rightarrow (3)$$

$$\therefore h = h/2\pi \text{ (or)} h^2 = h^2/4\pi^2, \therefore \frac{8\pi^2 m E}{h^2} = \alpha.$$

$$\Rightarrow \frac{d^2\psi}{dx^2} [a - \beta^2 x^2] \psi = 0 \rightarrow (5) \quad \therefore \left[\frac{4\pi^2 m K}{h^2} \right]^{1/2} = \beta$$

$$\therefore y = x \sqrt{\beta} \quad (or) \quad x = y/\sqrt{\beta} \quad (or) \quad x^2 = y^2/\beta \rightarrow (6)$$

$$\frac{dx}{dy} = \sqrt{\beta} \rightarrow (8) \quad \therefore \text{diff wrt } 'x':$$

$$\frac{d\psi}{dx} = \frac{d\psi}{dy} \cdot \frac{dy}{dx} \rightarrow (9)$$

$$\frac{d^2\psi}{dx^2} = \beta \frac{d^2\psi}{dy^2} \rightarrow (10)$$

$$\frac{d^2\psi}{dy^2} + \left[\frac{\alpha}{\beta} - y^2 \right] \psi = 0 \quad \therefore \text{Sub eqn (9) and (10) in (5)} \rightarrow (11)$$

function:

$$\psi = f(x) e^{-y^2/2}$$

$$\psi_n(y) = N H_n(y) e^{-y^2/2}$$

Eigen values (Energy)

$$E_n = (n + \frac{1}{2}) h\nu$$

$$E_n = n^2 h^2 / 8ma^2$$

