

1 Figure

1.1 Angle2D

1. Definition

Angle2D	<i>type</i> = Angle2D
	<i>center</i>
	<i>start</i>
	<i>end</i>
	<i>height</i>
	<i>right</i>
	<i>key</i>
	<i>key_object</i>
	<i>key_label</i>
	method

2. Method

1	construct						
	CO	<table><tr><td>center</td><td>start</td><td>end</td><td>height</td><td>right</td></tr></table>	center	start	end	height	right
	center	start	end	height	right		
		<table><tr><td>\equiv</td><td>$\left[\begin{array}{l} this \blacktriangleright center \\ center \end{array} \right]$</td></tr></table>	\equiv	$\left[\begin{array}{l} this \blacktriangleright center \\ center \end{array} \right]$			
	\equiv	$\left[\begin{array}{l} this \blacktriangleright center \\ center \end{array} \right]$					
		<table><tr><td>\equiv</td><td>$\left[\begin{array}{l} this \blacktriangleright start \\ start \end{array} \right]$</td></tr></table>	\equiv	$\left[\begin{array}{l} this \blacktriangleright start \\ start \end{array} \right]$			
	\equiv	$\left[\begin{array}{l} this \blacktriangleright start \\ start \end{array} \right]$					
		<table><tr><td>\equiv</td><td>$\left[\begin{array}{l} this \blacktriangleright end \\ end \end{array} \right]$</td></tr></table>	\equiv	$\left[\begin{array}{l} this \blacktriangleright end \\ end \end{array} \right]$			
	\equiv	$\left[\begin{array}{l} this \blacktriangleright end \\ end \end{array} \right]$					
		<table><tr><td>\equiv</td><td>$\left[\begin{array}{l} this \blacktriangleright right \\ right \end{array} \right]$</td></tr></table>	\equiv	$\left[\begin{array}{l} this \blacktriangleright right \\ right \end{array} \right]$			
	\equiv	$\left[\begin{array}{l} this \blacktriangleright right \\ right \end{array} \right]$					
	<table><tr><td>SW</td><td>$this \blacktriangleright right$</td></tr><tr><td>arc</td><td>$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ height \end{array} \right]$</td></tr><tr><td>right</td><td>$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ \frac{1}{\sqrt{2}} \times height \end{array} \right]$</td></tr></table>	SW	$this \blacktriangleright right$	arc	$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ height \end{array} \right]$	right	$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ \frac{1}{\sqrt{2}} \times height \end{array} \right]$
SW	$this \blacktriangleright right$						
arc	$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ height \end{array} \right]$						
right	$\equiv \left[\begin{array}{l} this \blacktriangleright height \\ \frac{1}{\sqrt{2}} \times height \end{array} \right]$						
2	angle	center angle					
	angle						
		<table><tr><td>$angle.start = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright start) \end{array} \right]$</td></tr></table>	$angle.start = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright start) \end{array} \right]$				
	$angle.start = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright start) \end{array} \right]$						
		<table><tr><td>$angle.end = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright end) \end{array} \right]$</td></tr></table>	$angle.end = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright end) \end{array} \right]$				
	$angle.end = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(this \blacktriangleright end) \end{array} \right]$						
RE	$\equiv \left[\begin{array}{l} angle.end \\ angle.start \end{array} \right]$						
3	height.contact	height when <i>object</i> contacts					

height_contact	<div>object</div> <div>type = min</div>
	<div> <div> <div>SW</div> <div>object ► type</div> </div> <div> <div> <div> <div>Rectangle2D = object</div> <div>heights = ∅</div> <div> <div>FE</div> <div> <div>Rectangle2D ► vertices</div> <div>vertex</div> </div> <div> <div>heights ±</div> <div> <div>−</div> <div>this ► center</div> <div>vertex</div> </div> </div> </div> <div> <div>SW</div> <div>type</div> <div> <div>min</div> <div>RE</div> <div>min(heights)</div> </div> <div> <div>max</div> <div>RE</div> <div>max(heights)</div> </div> </div> </div> </div> <div> <div> <div> <div>Label2D</div> <div>Rectangle2D</div> </div> <div> <div>⌈</div> <div>⌋</div> </div> </div> </div> </div> <div> <div>RE</div> <div>max(distances)</div> </div> </div>

4

interval_angle

Interval_angle formed by two edges of this

interval_angle	
	<div> <div> <div>angle_start = this ►</div> <div> <div>center</div> <div>vector_angle(this ► start)</div> </div> </div> </div> <div> <div>RE</div> <div>Interval_angle</div> <div> <div>angle_start</div> <div>this ► angle</div> </div> </div>

5

rotation

rotate around center with angle

rotation	<div>center</div> <div>angle</div>
	<div> <div>this_rotated = this</div> <div> <div> <div>this_rotated ► start = this ►</div> <div> <div>start</div> <div>rotation</div> <div>center</div> <div>angle</div> </div> </div> </div> <div> <div> <div>this_rotated ► end = this ►</div> <div> <div>end</div> <div>rotation</div> <div>center</div> <div>angle</div> </div> </div> </div> </div> <div> <div>RE</div> <div>this_rotated</div> </div>

6

translation

translate with vector

translation	<div>vector</div>
	<div> <div>this_translated = this</div> <div> <div> <div>this_translated ► center =</div> <div> <div>+</div> <div> <div>this ► center</div> <div>vector</div> </div> </div> </div> <div> <div> <div>this_translated ► start =</div> <div> <div>+</div> <div> <div>this ► start</div> <div>vector</div> </div> </div> </div> <div> <div> <div>this_translated ► end =</div> <div> <div>+</div> <div> <div>this ► end</div> <div>vector</div> </div> </div> </div> </div> <div> <div>RE</div> <div>this_translated</div> </div> </div></div></div>

1.2 Arc2D

1. Definition

Arc2D	type = Arc2D
	center
	start
	angle
	measure = ∅
	key
	key_object
	key_label
method	

2. Method

1	construct																					
	CO	<table><tr><td>center</td><td>start</td><td>angle</td><td>measure</td></tr><tr><td>$\left[\begin{array}{c} \text{this} \blacktriangleright \text{cetner} \\ \text{center} \end{array} \right]$</td><td></td><td></td><td></td></tr><tr><td>$\left[\begin{array}{c} \text{this} \blacktriangleright \text{start} \\ \text{start} \end{array} \right]$</td><td></td><td></td><td></td></tr><tr><td>$\left[\begin{array}{c} \text{this} \blacktriangleright \text{angle} \\ \text{angle} \end{array} \right]$</td><td></td><td></td><td></td></tr><tr><td>$\left[\begin{array}{c} \text{this} \blacktriangleright \text{measure} \\ \text{measure} \end{array} \right]$</td><td></td><td></td><td></td></tr></table>	center	start	angle	measure	$\left[\begin{array}{c} \text{this} \blacktriangleright \text{cetner} \\ \text{center} \end{array} \right]$				$\left[\begin{array}{c} \text{this} \blacktriangleright \text{start} \\ \text{start} \end{array} \right]$				$\left[\begin{array}{c} \text{this} \blacktriangleright \text{angle} \\ \text{angle} \end{array} \right]$				$\left[\begin{array}{c} \text{this} \blacktriangleright \text{measure} \\ \text{measure} \end{array} \right]$			
center	start	angle	measure																			
$\left[\begin{array}{c} \text{this} \blacktriangleright \text{cetner} \\ \text{center} \end{array} \right]$																						
$\left[\begin{array}{c} \text{this} \blacktriangleright \text{start} \\ \text{start} \end{array} \right]$																						
$\left[\begin{array}{c} \text{this} \blacktriangleright \text{angle} \\ \text{angle} \end{array} \right]$																						
$\left[\begin{array}{c} \text{this} \blacktriangleright \text{measure} \\ \text{measure} \end{array} \right]$																						
2	center	center																				
	center	<table><tr><td></td><td>$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$</td></tr></table>		$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$																		
	$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$																					
3	end	end																				
	end	<table><tr><td></td><td>$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$</td></tr></table>		$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$																		
	$\left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right) \end{array} \right]$																					
4	interval.angle	Interval.angle formed by start and end angles																				
	interval.angle	<table><tr><td></td><td>$\left(\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$</td></tr></table>		$\left(\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$																		
	$\left(\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$																					
5	is.tangent	check if <i>object</i> is tangent with <i>this</i>																				

is.tangent	object	
	SW	object ► type
	Segment2D	$Segment2D = object$
		$\equiv \left[\begin{array}{l} radius.this \\ this \blacktriangleright radius \end{array} \right]$
		$\equiv \left[\begin{array}{l} angle_Segment2D \\ Segment2D \blacktriangleright vector_angle \end{array} \right]$
		$angle_Segment2D.start = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(Segment2D \blacktriangleright start) \end{array} \right]$
		$angle_Segment2D.end = this \blacktriangleright \left[\begin{array}{l} center \\ vector_angle(Segment2D \blacktriangleright end) \end{array} \right]$
		$sign_Segment2D = \text{sign} \left(\begin{array}{c} \pi - \text{polar} \left(\boxed{-} \left[\begin{array}{l} angle_Segment2D.end \\ angle_segment2D.start \end{array} \right] \right) \\ 1 \end{array} \right)$
		$angle_perpendicular = \boxed{\times} \left[\begin{array}{l} sign_Segment2D \\ angle_Segment2D \end{array} \right] - \frac{\pi}{2}$
		$\equiv \left[\begin{array}{l} interval_angle.this \\ this \blacktriangleright interval_angle \end{array} \right]$
		$\boxed{\text{IF}} \not\in \left[\begin{array}{l} angle_perpendicular \\ interval_angle.this \end{array} \right] \quad \boxed{\text{RE}} \quad \boxed{\text{FA}}$
		$angle.start = \min \left(\begin{array}{c} \boxed{\times} \left[\begin{array}{l} -sign_Segment2D \\ angle_segment2D.start \end{array} \right] \\ \boxed{\times} \left[\begin{array}{l} sign_Segment2D \\ angle_Segment2D.start \end{array} \right] \end{array} \right)$
		$angle.end = \max \left(\begin{array}{c} \boxed{\times} \left[\begin{array}{l} sign_Segment2D \\ angle_segment2D.start \end{array} \right] \\ \boxed{\times} \left[\begin{array}{l} -sign_Segment2D \\ angle_Segment2D.start \end{array} \right] \end{array} \right)$
		$interval_angle.Segment2D = \mathbf{Interval_angle} \left(\begin{array}{c} angle.start \\ \boxed{-} \left[\begin{array}{l} angle.end \\ angle.start \end{array} \right] \end{array} \right)$
		$\boxed{\text{IF}} \not\in \left[\begin{array}{l} angle_perpendicular \\ interval_angle.Segment2D \end{array} \right] \quad \boxed{\text{RE}} \quad \boxed{\text{FA}}$
		$angle.start = \boxed{-} \left[\begin{array}{l} angle_perpendicular \\ interval_angle.Segment2D \blacktriangleright start \end{array} \right]$
		$angle.end = \boxed{-} \left[\begin{array}{l} interval_angle.Segment2D \blacktriangleright end \\ angle_perpendicular \end{array} \right]$
		$distance = \boxed{\div} \left[\begin{array}{c} Segment2D \\ \boxed{+} \left[\begin{array}{l} \tan(angle.start) \\ \tan(angle.end) \end{array} \right] \end{array} \right]$
		$\boxed{\text{RE}} \quad distance \equiv radius.this$

6	radius	radius
	radius	<div> <div> <div>RE</div> <div> <div>-</div> <div> <div>this ► start</div> <div>this ► center</div> </div> </div> </div> </div>
7	rotation	rotate arround center with angle

rotation	<i>center</i>	<i>angle</i>
	<i>this.rotated = this</i>	
	<i>this.rotated</i> ► <i>center = this</i> ► $\left[\begin{array}{c} center \\ rotation \left(\begin{array}{c} center \\ angle \end{array} \right) \end{array} \right]$	
	<i>this.rotated</i> ► <i>start = this</i> ► $\left[\begin{array}{c} start \\ rotation \left(\begin{array}{c} center \\ angle \end{array} \right) \end{array} \right]$	
	RE	<i>this.rotated</i>

8

translation

translate with *vector*

translation	<i>vector</i>
	<i>this.translated = this</i>
	$\left[\begin{array}{c} \pm \\ \pm \end{array} \right] \left[\begin{array}{c} this.rotated \blacktriangleright center \\ vector \end{array} \right]$
	$\left[\begin{array}{c} + \\ \pm \end{array} \right] \left[\begin{array}{c} this.rotated \blacktriangleright start \\ vector \end{array} \right]$
	RE <i>this.translated</i>

1.3 Curve2D

1. Definition

Curve2D	<i>type</i> = Curve2D
	<i>equation</i>
	<i>bounds</i>
	<i>key</i>
	<i>key_object</i>
	<i>key_label</i>
	method

2. Method

1

construct

CO	<i>equation</i>	<i>bounds</i>
$\left[\begin{array}{c} = \\ = \end{array} \right]$	$\left[\begin{array}{c} this \blacktriangleright equation \\ javascript.to.php(equation) \end{array} \right]$	
	$\left[\begin{array}{c} this \blacktriangleright bounds \\ bounds \end{array} \right]$	

2

centroid

centroid

centroid	$\left[\begin{array}{c} = \\ = \end{array} \right] \left[\begin{array}{c} region \\ this \blacktriangleright region \end{array} \right]$	
	<i>x</i> = 0	
	<i>y</i> = 0	
	FE	<i>region</i> <i>rectalgle</i>
	$x \pm rectangle \blacktriangleright \left[\begin{array}{c} center \\ x \end{array} \right]$	
	$y \pm rectangle \blacktriangleright \left[\begin{array}{c} center \\ y \end{array} \right]$	
	<i>x</i> $\overset{\cdot}{\overset{\cdot}{\doteq}} region $	
	<i>y</i> $\overset{\cdot}{\overset{\cdot}{\doteq}} region $	
	RE	$\mathbf{xy} \left(\begin{array}{c} x \\ y \end{array} \right)$

3

region

region

5	translation	translate with <i>vector</i>
	translation	<div> <div> <div><i>vector</i></div> <div> <div><i>this.translated = this</i></div> <div> <div>=</div> <div> <div><i>this.translated ► vertices</i></div> <div>∅</div> </div> </div> </div> </div> <div> <div>FE</div> <div> <div><i>this ► vertices</i></div> <div><i>vertex</i></div> </div> <div> <div><i>this.translated ► vertices ±</i></div> <div>+</div> <div> <div><i>vertex</i></div> <div><i>vector</i></div> </div> </div> </div> </div> <div> <div>RE</div> <div><i>this.translated</i></div> </div>

1.5 Label2D

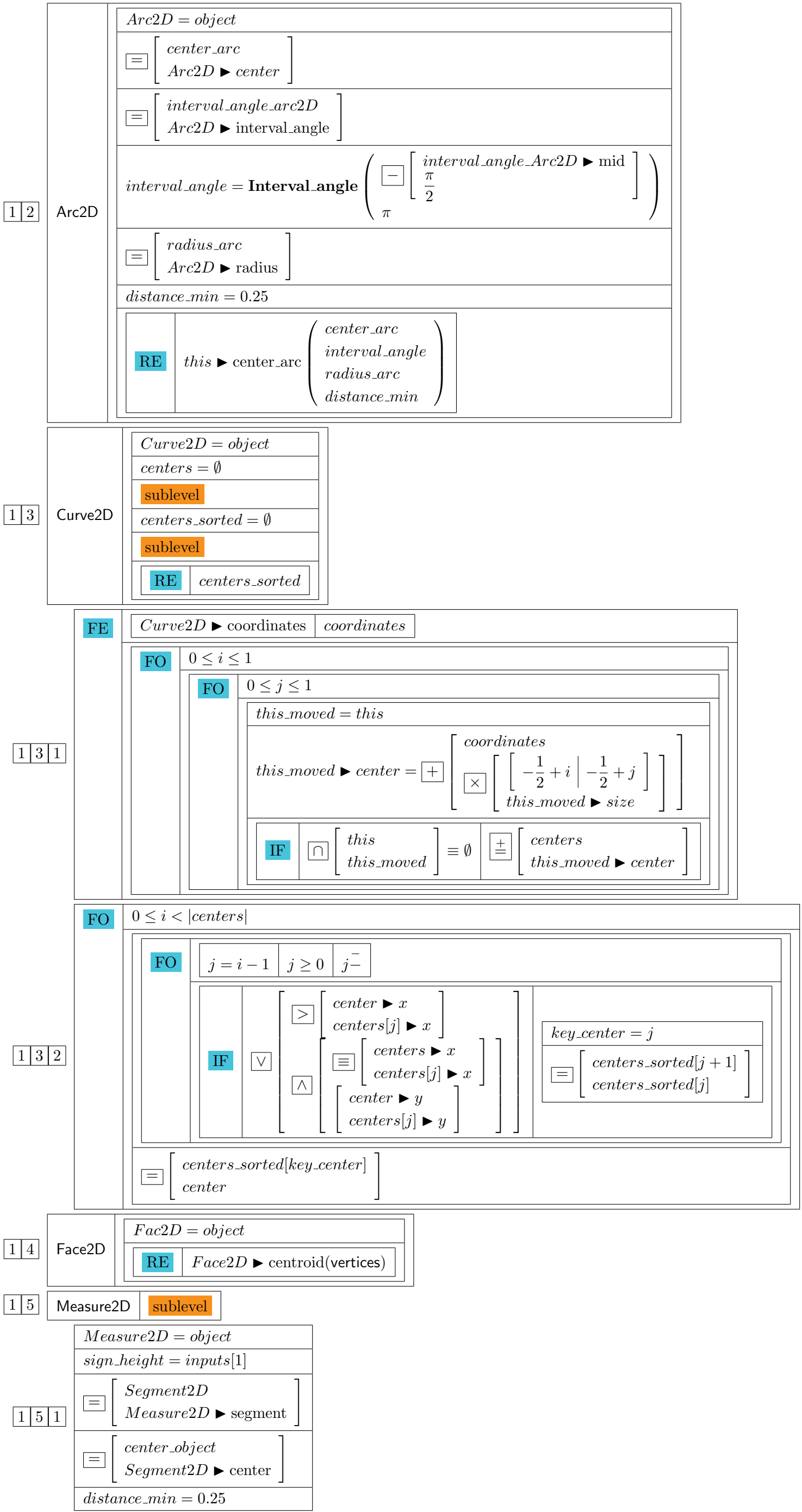
1. Definition

Label2D ◄ Rectangle2D	<i>type</i>	= Label2D
	<i>type_labeled</i>	
	<i>center</i>	
	<i>size</i>	
	<i>rotation</i>	
	<i>target</i>	
	<i>key</i>	
	<i>key_object</i>	
	<i>key_labeled</i>	
	<i>key_labeled_object</i>	
	method	

2. Method

1	center	center
	center	<div> <div>inputs</div> <div> <div><i>object = inputs[0]</i></div> <div> <div>SW</div> <div> <div><i>object ► type</i></div> <div> <div>Angle2D</div> <div>sublevel</div> </div> <div> <div>Arc2D</div> <div>sublevel</div> </div> <div> <div>Curve2D</div> <div>sublevel</div> </div> <div> <div>Face2D</div> <div>sublevel</div> </div> <div> <div>Measure2D</div> <div>sublevel</div> </div> <div> <div>MeasureArc2D</div> <div>sublevel</div> </div> <div> <div>Point2D</div> <div>sublevel</div> </div> <div> <div>Segment2D</div> <div>sublevel</div> </div> </div> </div> </div> </div>

11	Angle2D	<i>Angle2D = object</i>
		<i>center_arc = inputs[1]</i>
		<div> <div>IF</div> <div><i>interval_angle ≡ ∅</i></div> <div>=</div> <div> <div><i>interval_angle</i></div> <div><i>Angle2D ► interval_angle</i></div> </div> </div>
		<i>distance_min = 0.25</i>
		<div> <div>=</div> <div> <div><i>radius_arc</i></div> <div><i>Angle2D ► height</i></div> </div> </div>
		<div> <div>RE</div> <div><i>this ► center_arc</i></div> <div> <div><i>center_arc</i></div> <div><i>interval_angle</i></div> <div><i>radius_arc</i></div> <div><i>distance_min</i></div> </div> </div>



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$angle_Segment2D = \boxed{-} \left[\begin{array}{l} Segment2D \blacktriangleright vector.angle \\ this \blacktriangleright rotation \end{array} \right]$		
$\boxed{\mathbb{F}}$	$sign.height \equiv 0$	$sign.height = \boxed{-} \left[\begin{array}{l} [1 + \text{sign}(Measure2D \blacktriangleright height)] \\ 1 \end{array} \right]$
$angle.rotation = \boxed{+} \left[\begin{array}{l} angle.Segment2D \\ \pi \times sign.height \end{array} \right]$		
$angle.label = \boxed{+} \left[\begin{array}{l} this \blacktriangleright rotation \\ angle.rotation \end{array} \right]$		
$angles.label = \mathbf{index}(\text{direction})$		
$angles.label \blacktriangleright right = \text{mod} \left(\frac{angle.label}{\frac{\pi}{2}} \right)$		
$\boxed{=}\left[\begin{array}{l} angles.label \blacktriangleright left \\ \frac{\pi}{2} - angles.label \blacktriangleright right \end{array} \right]$		
$parity = \text{mod} \left(\frac{\frac{\pi}{2} \times angle.label}{2} \right)$		
$lengths.label = \mathbf{index}(\text{direction})$		
$lengths.label \blacktriangleright left = \boxed{\times} \left[\begin{array}{l} [parity \mid 1 - parity] \\ this \blacktriangleright size \end{array} \right]$		
$lengths.label \blacktriangleright right = \boxed{\times} \left[\begin{array}{l} [1 - parity \mid parity] \\ this \blacktriangleright size \end{array} \right]$		
$widths.label = \mathbf{index}(\text{direction})$		
$widths.label \blacktriangleright left = \boxed{\times} \left[\begin{array}{l} lengths.label \blacktriangleright left \\ \cos(angles.label \blacktriangleright left) \end{array} \right]$		
$widths.label \blacktriangleright right = \boxed{\times} \left[\begin{array}{l} lengths.label \blacktriangleright right \\ \cos(angles.label \blacktriangleright right) \end{array} \right]$		
$heights.label = \mathbf{index}(\text{direction})$		
$heights.label \blacktriangleright left = \boxed{\times} \left[\begin{array}{l} lengths.label \blacktriangleright left \\ \sin(angles.label \blacktriangleright left) \end{array} \right]$		
$heights.label \blacktriangleright right = \boxed{\times} \left[\begin{array}{l} lengths.label \blacktriangleright right \\ \sin(angles.label \blacktriangleright right) \end{array} \right]$		
$angle = \min \left(\begin{array}{l} angles.label \blacktriangleright left \\ angles.label \blacktriangleright right \end{array} \right)$		
$sign = \text{sign} \left(\frac{\boxed{-} \left[\begin{array}{l} angles.label \blacktriangleright left \\ angles.label \blacktriangleright right \end{array} \right]}{1} \right)$		
$length = \boxed{+} \left[\begin{array}{l} \boxed{\times} \left[\begin{array}{l} \max \left(\begin{array}{l} sign \\ 0 \end{array} \right) \\ lengths.label \blacktriangleright left \end{array} \right] \\ \boxed{\times} \left[\begin{array}{l} \min \left(\begin{array}{l} sign \\ 0 \end{array} \right) \\ lengths.label \blacktriangleright right \end{array} \right] \end{array} \right]$		

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18	Segment2D	$\text{Segment2D} = \text{object}$
		$\text{distance_min} = 0.35$
		$\text{center} = \mathbf{xy} \begin{pmatrix} 0 \\ 0 \end{pmatrix}$
		$\text{Segment2D.rotated} = \text{Segment2D} \blacktriangleright \text{rotation} \begin{pmatrix} \text{center} \\ \text{this} \blacktriangleright \text{rotation} \end{pmatrix}$
		$\text{angle.this.rotated} = \text{mod} \begin{pmatrix} \text{Segment2D.rotated} \blacktriangleright \text{veto.rangle} \\ \pi \end{pmatrix}$
		$\boxed{=} \left[\begin{array}{c} \text{center.Segment2D.rotated} \\ \text{Segment2D.rotated} \blacktriangleright \text{center} \end{array} \right]$
		$\text{vector_Segment2D.rotated.half} = \mathbf{xy} \begin{pmatrix} \frac{1}{2} \times \text{Segment2D.rotated} \\ \text{angle.Segment2D.rotated} \\ \text{polar} \end{pmatrix}$
		$\text{start.Segment2D.rotated} = \boxed{+} \left[\begin{array}{c} \text{center.Segment2D.rotated} \\ \text{vector.Segment2D.rotated.half} \end{array} \right]$
		$\text{angles} = \text{index}(\text{polar})$
		$\text{angles} \blacktriangleright \text{right} = \text{mod} \begin{pmatrix} \text{angle.this.rotated} \\ \frac{\pi}{2} \end{pmatrix}$
		$\boxed{=} \left[\begin{array}{c} \text{angles} \blacktriangleright \text{left} \\ \frac{\pi}{2} - \text{angles} \blacktriangleright \text{right} \end{array} \right]$
		$\text{lengths} = \text{index}(\text{direction})$
		$\text{lengths} \blacktriangleright \text{left} = \boxed{\times} \left[\begin{array}{c} \left[\cos(\text{angles} \blacktriangleright \text{right}) \mid \cos(\text{angles} \blacktriangleright \text{left}) \right] \\ \text{this} \blacktriangleright \text{size} \end{array} \right]$
		$\text{lengths} \blacktriangleright \text{right} = \boxed{\times} \left[\begin{array}{c} \left[\cos(\text{angles} \blacktriangleright \text{left}) \mid \cos(\text{angles} \blacktriangleright \text{right}) \right] \\ \text{this} \blacktriangleright \text{size} \end{array} \right]$
		$\text{radius} = \sqrt{\boxed{-} \left[\begin{array}{c} \left(\boxed{+} \left[\begin{array}{c} \frac{1}{2} \times \text{lengths} \blacktriangleright \text{left} \\ \text{distance_min} \end{array} \right] \right)^2 \\ \left(\boxed{+} \left[\begin{array}{c} \frac{1}{2} \times \text{lengths} \blacktriangleright \text{right} \\ \text{distance_min} \end{array} \right] \right)^2 \end{array} \right]}$
		$\text{sign_angle} = \text{sign} \begin{pmatrix} \cos(\text{angle.this}) \\ 1 \end{pmatrix}$
		$\text{angle.diagonal} = \text{vector.angle} \begin{pmatrix} \boxed{+} \left[\begin{array}{c} \frac{1}{2} \times \text{lengths} \blacktriangleright \text{left} \\ \text{distance_min} \end{array} \right] \\ \boxed{+} \left[\begin{array}{c} \frac{1}{2} \times \text{lengths} \blacktriangleright \text{right} \\ \text{distance_min} \end{array} \right] \end{pmatrix}$
$\text{angle} = \text{sign_angle} \times \left(\boxed{+} \left[\begin{array}{c} -\text{angle.Segment2D.rotated} \\ -\text{angle.diagonal} \end{array} \right] \right)$		
$\text{vector_addition} = \mathbf{xy} \begin{pmatrix} \text{radius} \\ \text{angle} \\ \text{polar} \end{pmatrix}$		
$\boxed{\text{RE}} \boxed{+} \left[\begin{array}{c} \text{start.Segment2D.rotated} \\ \text{vector_addition} \end{array} \right]$		
2	center_arc	center of label whose object is Arc2D or Angle2D

center_arc	<i>center_arc</i>	<i>interval_angle</i>	<i>radius_arc</i>	<i>distance_min</i>
	sublevel			
	sublevel			
	sublevel			
	sublevel			
	sublevel			
	<div><div>RE</div><div>+</div><div><div><i>label_min</i></div><div><i>translation_center</i></div><div><i>center_arc</i></div></div></div>			

$distance_min_center = \boxed{+} \left[\begin{array}{c} distance_min \\ radius_arc \end{array} \right]$	
$\boxed{=}\left[\begin{array}{c} angle.rotation \\ \frac{\pi}{2} - interval_angle \blacktriangleright mid \end{array}\right]$	
$angle_arc = \max \left(\begin{array}{c} 0 \\ polar \left(\boxed{+} \left[\begin{array}{c} interval_angle \blacktriangleright start \\ angle.rotation \end{array} \right] \right) \\ -\pi \end{array} \right)$	
$angle_label = \boxed{+} \left[\begin{array}{c} this \blacktriangleright rotation \\ angle.rotation \end{array} \right]$	
$angles_label \blacktriangleright right = \text{mod} \left(\frac{angle_label}{2} \right)$	
$\boxed{=}\left[\begin{array}{c} angles_label \blacktriangleright left \\ \frac{\pi}{2} - angles_label \blacktriangleright right \end{array}\right]$	

21

interval_angle

22

$parity_label = \text{mod} \left(\left\lfloor \frac{2}{\pi} \times angle_label \right\rfloor \right)$
$lengths_label = \text{index}(\text{direction})$
$lengths_label \blacktriangleright left = \left[\begin{array}{c} \left[\begin{array}{c} \times \\ this \blacktriangleright \left[\begin{array}{c} 1 - parity_label \\ size \\ x \end{array} \right] \end{array} \right] \\ \left[\begin{array}{c} \times \\ this \blacktriangleright \left[\begin{array}{c} parity_label \\ size \\ y \end{array} \right] \end{array} \right] \end{array} \right]$
$lengths_label \blacktriangleright right = \left[\begin{array}{c} \left[\begin{array}{c} \times \\ this \blacktriangleright \left[\begin{array}{c} parity_label \\ size \\ x \end{array} \right] \end{array} \right] \\ \left[\begin{array}{c} \times \\ this \blacktriangleright \left[\begin{array}{c} 1 - parity_label \\ size \\ y \end{array} \right] \end{array} \right] \end{array} \right]$
$widths_label = \text{index}(\text{direction})$
$widths_label \blacktriangleright left = \left[\times \right] \left[\begin{array}{c} lengths_label \blacktriangleright left \\ \cos(angle_label \blacktriangleright left) \end{array} \right]$
$widths_label \blacktriangleright right = \left[\times \right] \left[\begin{array}{c} lengths_label \blacktriangleright right \\ \cos(angle_label \blacktriangleright right) \end{array} \right]$
$heights_label = \text{index}(\text{direction})$
$heights_label \blacktriangleright left = \left[\times \right] \left[\begin{array}{c} lengths_label \blacktriangleright left \\ \sin(angle_label \blacktriangleright left) \end{array} \right]$
$heights_label \blacktriangleright left = \left[\times \right] \left[\begin{array}{c} lengths_label \blacktriangleright right \\ \sin(angle_label \blacktriangleright right) \end{array} \right]$
$widths_label_min = \text{index}(\text{direction})$
$angle_label_min = \max \left(\begin{array}{c} angle_arc \\ angles_label \blacktriangleright left \\ angles_label \blacktriangleright right \end{array} \right)$
$widths_label_min \blacktriangleright left = \left[\begin{array}{c} \left[\begin{array}{c} widths_label \blacktriangleright left \\ heights_label \blacktriangleright left \\ \sin(angle_label_min) \end{array} \right] \end{array} \right]$
$widths_label_min \blacktriangleright right = \left[\begin{array}{c} \left[\begin{array}{c} widths_label \blacktriangleright right \\ heights_label \blacktriangleright right \\ \sin(angle_label_min) \end{array} \right] \end{array} \right]$

	$x_label_min = \boxed{-} \left[\begin{array}{c} widths_label_min \blacktriangleright left \\ widths_label_min \blacktriangleright right \end{array} \right] \times \frac{1}{2}$
	$y_label_min_fit = \boxed{+} \left[\begin{array}{c} \boxed{\times} \left[\begin{array}{c} x_label_min \\ \tan(angle_arc) \end{array} \right] \\ distance_min \end{array} \right]$
	$xs_label = \mathbf{index}(\mathbf{direction})$
	$xs_label \blacktriangleright left = \boxed{-} \left[\begin{array}{c} x_label_min \\ widths_label \blacktriangleright left \end{array} \right]$
	$xs_label \blacktriangleright right = \boxed{+} \left[\begin{array}{c} x_label_min \\ widths_label \blacktriangleright right \end{array} \right]$
$\boxed{2} \boxed{3}$	$y_label_contact_min = \sqrt{\max \left(\begin{array}{c} 0 \\ \boxed{-} \left[\begin{array}{c} (distance_min_center)^2 \\ (x_label_min)^2 \end{array} \right] \end{array} \right)}$
	$ys_label_contact = \mathbf{index}(\mathbf{direction})$
	$ys_label_contact \blacktriangleright left = \sqrt{\max \left(\begin{array}{c} 0 \\ \boxed{-} \left[\begin{array}{c} (distance_min_center)^2 \\ (x_label \blacktriangleright left)^2 \end{array} \right] \end{array} \right)}$
	$ys_label_contact \blacktriangleright right = \sqrt{\max \left(\begin{array}{c} 0 \\ \boxed{-} \left[\begin{array}{c} (distance_min_center)^2 \\ (x_label \blacktriangleright right)^2 \end{array} \right] \end{array} \right)}$
	$y_label_min_contact = \max \left(\begin{array}{c} y_label_contact_min \\ \boxed{-} \left[\begin{array}{c} ys_label_contact \blacktriangleright left \\ heights_label \blacktriangleright left \end{array} \right] \\ \boxed{-} \left[\begin{array}{c} ys_label_contact \blacktriangleright right \\ heights_label \blacktriangleright right \end{array} \right] \end{array} \right)$
	$interval_x_min_contact = \mathbf{Interval} \left(\begin{array}{c} \boxed{\times} \left[\begin{array}{c} -distance_min_center \\ \cos(angles_label \blacktriangleright left) \end{array} \right] \\ \boxed{\times} \left[\begin{array}{c} distance_min_center \\ \cos(angles_label \blacktriangleright right) \end{array} \right] \end{array} \right)$
	$\boxed{=}\left[\begin{array}{c} intervals_x_min_tangent \\ \mathbf{index}(\mathbf{direction}) \end{array} \right]$
$\boxed{2} \boxed{4}$	$intervals_x_min_tangent \blacktriangleright left = \mathbf{Interval} \left(\begin{array}{c} \boxed{-} \left[\begin{array}{c} interval_x_min_contact \blacktriangleright min \\ widths_label \blacktriangleright left \end{array} \right] \\ interval_x_min_contact \blacktriangleright min \end{array} \right)$
	$intervals_x_min_tangent \blacktriangleright right = \mathbf{Interval} \left(\begin{array}{c} interval_x_min \blacktriangleright max \\ \boxed{+} \left[\begin{array}{c} interval_x_min_contact \blacktriangleright max \\ widths_label \blacktriangleright right \end{array} \right] \end{array} \right)$
	$indicators_tangent = \mathbf{index}(\mathbf{direction})$
	$indicators_tangent \blacktriangleright left = intervals_x_min_tangent \blacktriangleright \left[\begin{array}{c} left \\ indicator(x_label_min) \end{array} \right]$
	$indicators_tangent \blacktriangleright right = intervals_x_min_tangent \blacktriangleright \left[\begin{array}{c} right \\ indicator(x_label_min) \end{array} \right]$

	$ys.tangent = \mathbf{index}(\mathbf{direction})$
	$ys.tangent \blacktriangleright left = \boxed{\times} \left[\begin{array}{c} distance.min.center \\ \sin(angles.label \blacktriangleright left) \end{array} \right]$
	$ys.tangent \blacktriangleright right = \boxed{\times} \left[\begin{array}{c} distance.min.center \\ \sin(angles.label \blacktriangleright right) \end{array} \right]$
	$y.label.min.tangent = \left[\begin{array}{c} \boxed{\times} \left[\begin{array}{c} indicators.tangent \blacktriangleright left \\ ys.tangent \blacktriangleright left \end{array} \right] \\ \boxed{\times} \left[\begin{array}{c} indicators.tangent \blacktriangleright right \\ ys.tangent \blacktriangleright right \end{array} \right] \end{array} \right]$
	$y.label.min = \max \left(\begin{array}{c} y.label.min.fit \\ y.label.min.contact \\ y.label.min.tangent \end{array} \right)$
<div>25</div>	$length.diagonal.half = \frac{1}{2} \times \sqrt{\boxed{-} \left[\begin{array}{c} (lengths.label \blacktriangleright left)^2 \\ (lengths.label \blacktriangleright right)^2 \end{array} \right]}$
	$angle.diagonal = \mathbf{vector.angle} \left(\begin{array}{c} lengths.label \blacktriangleright right \\ lengths.label \blacktriangleright left \end{array} \right)$
	$label.min = \mathbf{xy} \left(\begin{array}{c} x.label.min \\ y.label.min \end{array} \right)$
	$translation = \mathbf{xy} \left(\begin{array}{c} length.diagonal.half \\ \boxed{+} \left[\begin{array}{c} angles.label \blacktriangleright right \\ angle.diagonal \end{array} \right] \end{array} \right)_{\mathbf{polar}}$
	$center.rotation = \mathbf{xy} \left(\begin{array}{c} 0 \\ 0 \end{array} \right)$
	$translation.center = \boxed{+} \left[\begin{array}{c} label.min \\ translation \end{array} \right] \blacktriangleright \mathbf{rotation} \left(\begin{array}{c} center.rotation \\ -angle.rotation \end{array} \right)$

1.6 Line2D

1. Definition

Line2D	$type = \mathbf{Line2D}$
	a
	b
	c
method	

2. Method

1 construct

CO	a	b	c
	$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright a \\ a \end{array} \right]$	
	$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright b \\ b \end{array} \right]$	
	$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright c \\ c \end{array} \right]$	

2 coordinate coordinate when other *axis value* is given

coordinate	value	axis = x	
	SW	axis	
	x	<div><div>IF</div><div><div>≠</div><div><div><div>this ▶ b</div><div>0</div></div></div></div></div>	<div><div>RE</div><div><div>÷</div><div><div><div>+</div><div><div><div>×</div><div><div><div>-this ▶ a</div><div>value</div></div><div><div>-this ▶ c</div></div></div></div><div>this ▶ b</div></div></div></div></div></div>
		<div><div>RE</div><div>IN</div></div>	
y	<div><div>IF</div><div><div>≠</div><div><div><div>this ▶ a</div><div>0</div></div></div></div></div>	<div><div>RE</div><div><div>÷</div><div><div><div>+</div><div><div><div>×</div><div><div><div>-this ▶ b</div><div>value</div></div><div><div>-this ▶ c</div></div></div></div><div>this ▶ a</div></div></div></div></div></div>	
<div><div>RE</div><div>IN</div></div>			
evaluation	evaluation with given coordinates		
evaluation	coordinates		
	<div><div>RE</div><div><div>+</div><div><div><div>×</div><div><div><div>this ▶ a</div><div>coordinates ▶ x</div></div><div><div>this ▶ b</div><div>coordinates ▶ y</div></div></div></div><div>this ▶ c</div></div></div></div>		

1.7 Measure2D

1. Definition

Measure2D	<i>type</i> = Measure2D
	<i>start</i>
	<i>end</i>
	<i>height</i>
	<i>key_object</i>
	<i>key_label</i>
	method

2. Method

1	construct	
	CO	<div> <div>start</div> <div>end</div> <div>height</div> </div>
		<div> <div> <div>≡</div> <div> <div>this ► start</div> <div>start</div> </div> </div> <div> <div> <div>this ► end</div> <div>end</div> </div> <div> <div> <div>this ► height</div> <div>height</div> </div> </div> </div> </div>
2	angles.height	start and end angles formed by height

angles.height	
	$angles = \mathbf{index}(\mathbf{position})$ $\boxed{=} \left[\begin{array}{l} angles \blacktriangleright start \\ \mathbf{index}(\mathbf{sign}) \end{array} \right]$ $\boxed{=} \left[\begin{array}{l} angles \blacktriangleright end \\ \mathbf{index}(\mathbf{sign}) \end{array} \right]$ $angle = \mathbf{vector_angle} \left(\begin{array}{l} \frac{1}{2} \times this \\ this \blacktriangleright height \end{array} \right)$ $angles \blacktriangleright \left[\begin{array}{l} start \\ positive \end{array} \right] = \max \left[\begin{array}{l} 0 \\ angle \end{array} \right]$ $angles \blacktriangleright \left[\begin{array}{l} start \\ negative \end{array} \right] = \min \left(\begin{array}{l} 0 \\ angle \end{array} \right)$ $angles \blacktriangleright \left[\begin{array}{l} end \\ positve \end{array} \right] = angles \blacktriangleright \left[\begin{array}{l} start \\ positive \end{array} \right]$ $angles \blacktriangleright \left[\begin{array}{l} end \\ negative \end{array} \right] = angles \blacktriangleright \left[\begin{array}{l} start \\ negative \end{array} \right]$ $\boxed{\mathbf{RE}} \quad angles$

3	Bezeir	equation in the form of Bezier curve
---	--------	--------------------------------------

Bezier	
	$\boxed{\mathbf{RE}} \quad \mathbf{Bezier} \left(\begin{array}{l} this \blacktriangleright start \\ this \blacktriangleright center \\ this \blacktriangleright end \end{array} \right)$

4	center	center
---	--------	--------

center	
	$angle = this \blacktriangleright \left[\begin{array}{l} start \\ \mathbf{vector_angle}(this \blacktriangleright end) \end{array} \right]$ $angle.height = \boxed{+} \left[\begin{array}{l} angle \\ \frac{\pi}{2} \times \mathbf{sign}(this \blacktriangleright height) \end{array} \right]$ $translation = \mathbf{xy} \left(\begin{array}{l} this \blacktriangleright height \\ angle.height \\ \mathbf{polar} \end{array} \right)$ $\boxed{\mathbf{RE}} \quad \boxed{+} \left[\begin{array}{l} \boxed{+} \left[\begin{array}{l} this \blacktriangleright start \\ this \blacktriangleright end \end{array} \right] \times \frac{1}{2} \\ translation \end{array} \right]$

5	height	height
---	--------	--------

height	$angle$ $angle = \min \left(\begin{array}{l} angle \\ \frac{\pi}{2} \end{array} \right)$ $\boxed{\mathbf{RE}} \quad \boxed{\times} \left[\begin{array}{l} \frac{1}{2} \times \left[\begin{array}{l} this \blacktriangleright start \\ this \blacktriangleright end \end{array} \right] \\ \tan(angle) \end{array} \right]$
--------	---

6	height.contact	height when <i>this</i> contacts <i>label.this</i>
---	----------------	--

height_contact

<i>object</i>	<i>label.this</i>	<i>type</i> = max
<i>heights</i> = index(sign)		
\equiv	$\left[\begin{array}{l} \textit{Segment2D.this} \\ \textit{this} \blacktriangleright \textit{segment} \end{array} \right]$	
\equiv	$\left[\begin{array}{l} \textit{translation} \\ \textit{Segment2D.this} \blacktriangleright \textit{center} \end{array} \right]$	
$\textit{center_rotation} = \mathbf{xy} \begin{pmatrix} 0 \\ 0 \end{pmatrix}$		
\equiv	$\left[\begin{array}{l} \textit{angle_rotation} \\ -\textit{Segment2D.this} \blacktriangleright \textit{vector_angle} \end{array} \right]$	
$\textit{Segment2D.this.moved} = \textit{Segment2D.this} \blacktriangleright \left[\begin{array}{l} \textit{translation}(\textit{translation}) \\ \textit{rotation} \begin{pmatrix} \textit{center_rotation} \\ \textit{angle_rotation} \end{pmatrix} \end{array} \right]$		
\equiv	$\left[\begin{array}{l} \textit{interval.x.this} \\ \textit{Segment2D.this.moved} \blacktriangleright \textit{interval(x)} \end{array} \right]$	
$\textit{interval.x.label.this} = \mathbf{Interval} \begin{pmatrix} -\textit{label.this} \blacktriangleright \left[\begin{array}{l} \textit{size} \\ x \end{array} \right] \times \frac{1}{2} \\ \textit{label.this} \blacktriangleright \left[\begin{array}{l} \textit{size} \\ x \end{array} \right] \times \frac{1}{2} \end{pmatrix}$		
<i>distance</i> = 0		
SW	<i>object</i> \blacktriangleright <i>type</i>	
	\sqsubset	$\left[\begin{array}{l} \text{Label2D} \\ \text{Rectangle2D} \end{array} \right]$ sublevel
	Measure2D sublevel	
	Segment2D sublevel	
	xy sublevel	

<div> <div> <div>6</div> <div>1</div> </div> <div> <div>⌊</div> <div> <div>Label2D</div> <div>Rectangle2D</div> </div> <div>⌋</div> </div> </div>	<div> <div> <div>Rectangle2D = object</div> </div> <div> <div>Rectangle2D = Rectangle2D ►</div> <div> <div>translation(translation)</div> <div>rotation $\begin{pmatrix} center \\ angle \end{pmatrix}$</div> </div> <div>⌋</div> </div> <div> <table> <tr> <td>SW</td><td><i>type</i></td></tr> <tr> <td>min</td><td>sublevel</td></tr> <tr> <td>max</td><td>sublevel</td></tr> </table> </div> </div>	SW	<i>type</i>	min	sublevel	max	sublevel
SW	<i>type</i>						
min	sublevel						
max	sublevel						

611	min	$\models \left[\begin{array}{l} heights \blacktriangleright positive \\ 0 \end{array} \right]$	
		$\models \left[\begin{array}{l} heights \blacktriangleright negative \\ 0 \end{array} \right]$	
		$Rectangle2D = Rectangle2D \blacktriangleright \left[\begin{array}{l} translation(translation) \\ rotation \left(\begin{array}{l} center \\ -angle \end{array} \right) \end{array} \right]$	
		$\text{IF} \leq \left[\begin{array}{l} Sement2D.this \\ Rectangle2D \blacktriangleright \left[\begin{array}{l} center \\ x \end{array} \right] \end{array} \right]$	$\text{RE} heights$
		$\text{IF} \sqcap \left[\begin{array}{l} Rectangle2D \blacktriangleright interval(x) \\ interval.x.label.this \end{array} \right] \neq \emptyset$	$sign_height = \text{sign} \left(\begin{array}{l} Rectangle2D \blacktriangleright \left[\begin{array}{l} center \\ y \end{array} \right] \\ 1 \end{array} \right)$
			$height_abs = \max \left(\begin{array}{l} 0 \\ \left[\begin{array}{l} Rectangle2D \blacktriangleright \left[\begin{array}{l} center \\ y \end{array} \right] \\ \frac{1}{2} \times Rectangle2D \blacktriangleright \left[\begin{array}{l} size \\ y \end{array} \right] \\ label.this \blacktriangleright \left[\begin{array}{l} size \\ y \end{array} \right] \\ -distance \end{array} \right] \end{array} \right)$
			$heights_positive = \max \left(\begin{array}{l} 0 \\ \left[\begin{array}{l} sign_height \\ height_abs \end{array} \right] \end{array} \right)$
			$heights_negative = \max \left(\begin{array}{l} 0 \\ \left[\begin{array}{l} -sign_height \\ height_abs \end{array} \right] \end{array} \right)$
		$\text{FO} \left[\begin{array}{l} Rectangle2D \blacktriangleright vertices \\ vertex \end{array} \right]$	$height = \left[\begin{array}{l} \left[\begin{array}{l} \left[\begin{array}{l} vertex \blacktriangleright y \\ (2 \times vertex \blacktriangleright x)^2 \end{array} \right] \\ Segment2D.this ^2 \end{array} \right] \\ - \\ \left[\begin{array}{l} (2 \times vertex \blacktriangleright x)^2 \end{array} \right] \end{array} \right]$
		$sign_height = \text{sign} \left(\begin{array}{l} height \\ 1 \end{array} \right)$	
$heights \blacktriangleright positive = \max \left(\begin{array}{l} heights \blacktriangleright positive \\ \left[\begin{array}{l} sign_height \\ height \end{array} \right] \end{array} \right)$			
$heights \blacktriangleright negative = \max \left(\begin{array}{l} heights \blacktriangleright negative \\ \left[\begin{array}{l} -sign_height \\ height \end{array} \right] \end{array} \right)$			
$\text{RE} heights$			
6112	max	sublevel	
		$height_Segment2D = \text{IN}$	
61121	$height_Rectangle2D = \text{sign} \left(\begin{array}{l} Rectangle2D \blacktriangleright \left[\begin{array}{l} center \\ y \end{array} \right] \end{array} \right)$		
		$\models \left[\begin{array}{l} vertices \\ Rectangle2D \blacktriangleright vertices \end{array} \right]$	

FO				0 ≤ i < 4							
IF ⊆ ⌊ vertices[i] (interval.x.this)° ⌋				IF ⊆ ⌊ vertices[i] ▶ x interval.x.label.this ⌋				height_Rectangle2D = min ⎛ height_Rectangle2D 0 ⎛ ⌊			

7 2 2

\equiv	$\left[\begin{array}{l} heights \blacktriangleright positive \\ \text{IN} \end{array} \right]$
\equiv	$\left[\begin{array}{l} heights \blacktriangleright negative \\ \text{IN} \end{array} \right]$
$Measure2D.moved = \left[\begin{array}{c} + \\ \left[\begin{array}{l} Measure2D \\ translation \end{array} \right] \end{array} \right] \blacktriangleright \text{rotation} \left(\begin{array}{l} center \\ angle \end{array} \right)$	
\equiv	$\left[\begin{array}{l} Segment2D.moved \\ Measure2D.moved \blacktriangleright \text{segment} \end{array} \right]$
\equiv	$\left[\begin{array}{l} Bezier \\ Segment2D.moved \blacktriangleright \text{Bezier} \end{array} \right]$
$interval.t = \mathbf{Interval} \left(\begin{array}{c} 0 \\ 1 \end{array} \right)$	
\equiv	$\left[\begin{array}{l} quadratic.x \\ Bezier \blacktriangleright \text{quadratic}(x) \end{array} \right]$
\equiv	$\left[\begin{array}{l} interval.x \\ quadratic.x \blacktriangleright \text{image}(interval.t) \end{array} \right]$
IF	$\left \left[\begin{array}{l} interval.x \\ interval.x.this \end{array} \right] \right \equiv 0 \quad \text{RE} \quad heights$
$interval.t.intersection = \left[\begin{array}{c} \cap \\ \left[\begin{array}{l} quadratic.x \blacktriangleright \text{preimage}(interval.x.this) \\ interval.t \end{array} \right] \end{array} \right]$	
IF	$\equiv \left[\begin{array}{l} interval.t.intersection \\ \emptyset \end{array} \right] \quad \text{RE} \quad heights$
\equiv	$\left[\begin{array}{l} quadratic.y \\ Bezier \blacktriangleright \text{quadratic}(y) \end{array} \right]$
\equiv	$\left[\begin{array}{l} ts.y \\ quadratic \blacktriangleright \text{solution}(0) \end{array} \right]$
FE	$\left[\begin{array}{c} ts.y \quad t \\ \left[\begin{array}{c} \text{IF} \quad \in \quad \left[\begin{array}{l} t \\ interval.t.intersection \end{array} \right] \quad \text{RE} \quad heights \end{array} \right] \end{array} \right]$

$ts_bound = \emptyset$		
$\left[\begin{smallmatrix} + \\ \pm \end{smallmatrix}\right]$	$\left[\begin{smallmatrix} ts_bound \\ interval.t.intersection \blacktriangleright min \end{smallmatrix}\right]$	
$\left[\begin{smallmatrix} + \\ \pm \end{smallmatrix}\right]$	$\left[\begin{smallmatrix} ts_bound \\ interval.t.intersection \blacktriangleright max \end{smallmatrix}\right]$	
$\left[\begin{smallmatrix} = \\ \pm \end{smallmatrix}\right]$	$\left[\begin{smallmatrix} ts.x \\ quadratic.x \blacktriangleright solution(0) \end{smallmatrix}\right]$	
<div><div><div>FE</div><div><div>$ts.x$</div><div>t</div></div><div><div><div><div>IF</div><div>\in</div><div>$\left[\begin{smallmatrix} t \\ interval.t.intersection \end{smallmatrix}\right]$</div></div><div>$ts_bound \pm t$</div></div></div></div></div>		
$t.apex.y = \left[\begin{smallmatrix} \div \end{smallmatrix}\right] \left[\begin{smallmatrix} -quadratic.y \blacktriangleright b \\ 2 \times quadratic.y \blacktriangleright a \end{smallmatrix}\right]$		
$\left[\begin{smallmatrix} 7 \\ 2 \\ 3 \end{smallmatrix}\right]$	$\left[\begin{smallmatrix} IF \\ \in \end{smallmatrix}\right] \left[\begin{smallmatrix} t.apex.y \\ interval.t.intersection \end{smallmatrix}\right]$	$\left[\begin{smallmatrix} \pm \\ \equiv \end{smallmatrix}\right] \left[\begin{smallmatrix} ts_bound \\ t.apex.y \end{smallmatrix}\right]$
<div><div><div>FE</div><div><div>ts_bound</div><div>t</div></div><div><div><div><div><div>$\left[\begin{smallmatrix} \times \\ \div \end{smallmatrix}\right] \left[\begin{smallmatrix} (interval.x.this \blacktriangleright max)^2 \\ quadratic.y \blacktriangleright evaluation(t) \end{smallmatrix}\right]$</div><div>$\left[\begin{smallmatrix} - \\ \div \end{smallmatrix}\right] \left[\begin{smallmatrix} (interval.x.this \blacktriangleright max)^2 \\ (quadratic.x \blacktriangleright evaluation(5))^2 \end{smallmatrix}\right]$</div></div></div><div>$height =$</div><div>$\left[\begin{smallmatrix} \div \end{smallmatrix}\right]$</div></div><div>$height \blacktriangleright positive = \min \left(\begin{smallmatrix} heights \blacktriangleright positive \\ \max \left(\frac{1}{e^{height}} \right) \end{smallmatrix} \right)$</div><div>$height \blacktriangleright negative = \min \left(\begin{smallmatrix} heights \blacktriangleright positive \\ \max \left(\frac{1}{e^{-height}} \right) \end{smallmatrix} \right)$</div></div></div></div>		
<div><div>RE</div><div>$heights$</div></div>		

8

Segment2D

sublevel

$Segment2D = object$		
$Segment2D.moved = \begin{bmatrix} + \\ \equiv \end{bmatrix} \begin{bmatrix} Segment2D \\ translation \end{bmatrix} \blacktriangleright rotation \left(\begin{array}{l} center \\ angle \end{array} \right)$		
$\begin{bmatrix} IF \\ \vee \end{bmatrix}$	$\begin{bmatrix} \equiv \\ \subseteq \end{bmatrix} \begin{bmatrix} Segment2D.intersection \\ \emptyset \\ Segment2D.intersection \blacktriangleright interval(x) \\ interval.x.this \end{bmatrix}$	<div> <div> <div>\equiv</div> <div>$heights \blacktriangleright positive$</div> <div>IN</div> </div> <div> <div>\equiv</div> <div>$heights \blacktriangleright negative$</div> <div>IN</div> </div> <div> <div>RE</div> <div>$heights$</div> </div> </div>
$\begin{bmatrix} = \\ \equiv \end{bmatrix} \begin{bmatrix} interval.y.Segment2D \\ Segment2D.intersection \blacktriangleright interval(y) \end{bmatrix}$		
$\begin{bmatrix} 8 \\ 1 \end{bmatrix}$	$sign.y = sign \left(\begin{array}{l} \times \left[\begin{array}{l} interval.y.segment2D \blacktriangleright min \\ interval.y.Segment2D \blacktriangleright max \end{array} \right] \end{array} \right)$	
$\begin{bmatrix} IF \\ \vee \end{bmatrix}$	$sign.y \leq 0$	<div> <div> <div> $heights \blacktriangleright positive = \max \left(\begin{array}{l} 0 \\ -sign \left(\begin{array}{l} interval.y.Segment2D \blacktriangleright max \\ -1 \end{array} \right) \end{array} \right)$ </div> <div>IN</div> </div> <div> $heights \blacktriangleright negative = \max \left(\begin{array}{l} 0 \\ -sign \left(\begin{array}{l} interval.y.Segment2D \blacktriangleright min \\ -1 \end{array} \right) \end{array} \right)$ </div> <div>IN</div> </div> <div> <div>RE</div> <div>$heights$</div> </div>

$\equiv \left[\begin{array}{l} line_Segment2D \\ Segment2D_moved \blacktriangleright line \end{array} \right]$	
$\equiv \left[\begin{array}{l} sign_height \\ sign(interval_y_Segment2D \blacktriangleright max) \end{array} \right]$	
$Segment2D_intersection_label.this = \sqcap \left[\begin{array}{l} Segment2D_intersection \\ interval.x.label.this \end{array} \right]$	
IF	$\wedge \left[\begin{array}{l} \left[\begin{array}{l} \neq \\ \emptyset \end{array} \right] \left[\begin{array}{l} Segment2D_intersection_label.this \\ Segment2D_intersection_label.this \blacktriangleright interval(y) \end{array} \right] \\ \left[\begin{array}{l} \neq \\ 0 \end{array} \right] \end{array} \right] \left height_label.this = \max \left(\begin{array}{l} 0 \\ \sqcap \left[\begin{array}{l} Segment2D_intersection_label.this \blacktriangleright interval(y) \\ distance \end{array} \right] \end{array} \right) \right.$
$height_Segment2D_start = \left \begin{array}{l} \div \\ \left[\begin{array}{l} \times \left[\begin{array}{l} Segment2D_intersection \blacktriangleright start \\ (interval.x.this \blacktriangleright max)^2 \end{array} \right] \\ \sqcap \left[\begin{array}{l} (interval.x.this \blacktriangleright max)^2 \\ \left(Segment2D_intersection \blacktriangleright \begin{array}{l} start \\ x \end{array} \end{array} \right)^2 \end{array} \right] \end{array} \right]$	
$height_Segment2D_end = \left \begin{array}{l} \div \\ \left[\begin{array}{l} \times \left[\begin{array}{l} Segment2D_intersection \blacktriangleright end \\ (interval.x.this \blacktriangleright max)^2 \end{array} \right] \\ \sqcap \left[\begin{array}{l} (interval.x.this \blacktriangleright max)^2 \\ \left(Segment2D_intersection \blacktriangleright \begin{array}{l} end \\ x \end{array} \end{array} \right)^2 \end{array} \right] \end{array} \right]$	
$\equiv \left[\begin{array}{l} height_Segment2D_tangent \\ \text{IN} \end{array} \right]$	
IF	$\neq \left[\begin{array}{l} line_Segment2D \blacktriangleright b \\ 0 \end{array} \right]$ <div> <div> <div> $A = \sqcap \left[\begin{array}{l} -line_Segment2D \blacktriangleright a \\ line_Segment2D \blacktriangleright b \end{array} \right]$ </div> <div> $C = \sqcap \left[\begin{array}{l} -line_Segment2D \blacktriangleright c \\ line_Segment2D \blacktriangleright b \end{array} \right]$ </div> <div> $D_height = \sqcap \left[\begin{array}{l} C^2 \\ A \times (interval.x.this \blacktriangleright max)^2 \end{array} \right]$ </div> </div> <div> <div> IF </div> <div> $D_height \geq 0$ </div> <div> $sign.C = \text{sign} \left(\begin{array}{l} C \\ 1 \end{array} \right)$ $x = \sqcap \left[\begin{array}{l} A \times (interval.x.this \blacktriangleright max)^2 \\ \times \left[\begin{array}{l} sign.C \\ \sqrt{D_height} \end{array} \right] + C \end{array} \right]$ <div> IF $\in \left[\begin{array}{l} x \\ Segment2D_intersection \blacktriangleright interval(x) \end{array} \right]$ $height_Segment2D_tangent = \frac{1}{2} \times \left \times \left[\begin{array}{l} sign.C \\ \sqrt{D_height} \end{array} \right] + C \right$ </div> </div> </div> </div>
$height_Segment2D = \min \left(\begin{array}{l} height_Segment2D_start \\ height_Segment2D_end \\ height_Segment2D_tangent \end{array} \right)$	
$height_abs = \min \left(\begin{array}{l} height_label.this \\ height_Segment2D \end{array} \right)$	
$heights \blacktriangleright positive = \max \left(\begin{array}{l} 0 \\ \times \left[\begin{array}{l} sign_height \\ height_abs \end{array} \right] \end{array} \right)$	
$heights \blacktriangleright negative = \max \left(\begin{array}{l} 0 \\ \times \left[\begin{array}{l} -sign_height \\ height_abs \end{array} \right] \end{array} \right)$	
RE	$heights$

	$xy = object$								
	$xy.moved = \boxed{+} \left[\begin{array}{c} xy \\ translation \end{array} \right] \blacktriangleright rotation \left(\begin{array}{c} center.rotation \\ angle.rotation \end{array} \right)$								
	<table><tr><td>$\boxed{\text{IF}} \quad \boxed{\notin} \left[\begin{array}{c} xy.moved \blacktriangleright x \\ (interval.x.this)^{\circ} \end{array} \right]$</td><td><table><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{\text{RE}}$</td><td>$heights$</td></tr></table></td></tr></table>	$\boxed{\text{IF}} \quad \boxed{\notin} \left[\begin{array}{c} xy.moved \blacktriangleright x \\ (interval.x.this)^{\circ} \end{array} \right]$	<table><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{\text{RE}}$</td><td>$heights$</td></tr></table>	$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$	$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$	$\boxed{\text{RE}}$	$heights$
$\boxed{\text{IF}} \quad \boxed{\notin} \left[\begin{array}{c} xy.moved \blacktriangleright x \\ (interval.x.this)^{\circ} \end{array} \right]$	<table><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{=}$</td><td>$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$</td></tr><tr><td>$\boxed{\text{RE}}$</td><td>$heights$</td></tr></table>	$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$	$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$	$\boxed{\text{RE}}$	$heights$		
$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright positive \\ \boxed{\text{IN}} \end{array} \right]$								
$\boxed{=}$	$\left[\begin{array}{c} heights \blacktriangleright negative \\ \boxed{\text{IN}} \end{array} \right]$								
$\boxed{\text{RE}}$	$heights$								
xy	$\boxed{\text{IF}} \quad \boxed{\in} \left[\begin{array}{c} xy \blacktriangleright x \\ interval.x.label.this \end{array} \right]$	$height = \boxed{\times} \max \left(\begin{array}{c} \text{sign}(xy.moved \blacktriangleright y) \\ 0 \\ \boxed{+} \left(\begin{array}{c} xy.moved \blacktriangleright y \\ -\frac{1}{2} \times label.this \blacktriangleright \left[\begin{array}{c} size \\ y \end{array} \right] \\ -distance \end{array} \right) \end{array} \right)$							
	$height = \boxed{\div} \left[\begin{array}{c} \boxed{\times} \left[\begin{array}{c} xy.moved \blacktriangleright y \\ (interval.x.this \blacktriangleright max)^2 \end{array} \right] \\ \boxed{-} \left[\begin{array}{c} (interval.x.this \blacktriangleright max)^2 \\ (xy.moved \blacktriangleright x)^2 \end{array} \right] \end{array} \right]$								
	$sign.height = \text{sign} \left(\begin{array}{c} height \\ 1 \end{array} \right)$								
	$heights \blacktriangleright positive = \max \left(\begin{array}{c} 0 \\ \boxed{\times} \left[\begin{array}{c} sign.height \\ height \end{array} \right] \end{array} \right)$								
	$heights \blacktriangleright negative = \max \left(\begin{array}{c} 0 \\ \boxed{\times} \left[\begin{array}{c} -sign.height \\ height \end{array} \right] \end{array} \right)$								
	$\boxed{\text{RE}} \quad heights$								
	segment	compute Segment2D of this							
	segment								
	$\boxed{\text{RE}} \quad \text{Segment2D} \left(\begin{array}{c} this \blacktriangleright start \\ this \blacktriangleright end \end{array} \right)$								

1.8 MeasureArc2D

1. Definition

$MeasureArc2D \blacktriangleleft Arc2D$	$type = MeasureArc2D$
	$center$
	$start$
	$angle$
	$height$
	key_object
	key_label
	method

2. Method

1	construct	
---	-----------	--

$\boxed{\text{CO}}$	$center$	$start$	$angle$	$height$
$\boxed{=}$	$\begin{bmatrix} this \blacktriangleright center \\ center \end{bmatrix}$			
	$\begin{bmatrix} this \blacktriangleright start \\ start \end{bmatrix}$			
	$\begin{bmatrix} this \blacktriangleright angle \\ angle \end{bmatrix}$			
	$\begin{bmatrix} this \blacktriangleright height \\ height \end{bmatrix}$			

2	arc	Arc2D of this																
	arc	<table><tr><td>RE</td><td>Arc2D</td><td>$\left(\begin{array}{l} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$</td></tr></table>	RE	Arc2D	$\left(\begin{array}{l} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$													
RE	Arc2D	$\left(\begin{array}{l} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \\ \text{this} \blacktriangleright \text{angle} \end{array} \right)$																
3	center	center of this																
	center	<table><tr><td colspan="3">$\text{radius} = + \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right] \\ \text{height} \end{array} \right]$</td></tr><tr><td colspan="3">$\text{angle} = + \left[\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right]$</td></tr><tr><td>RE</td><td>xy</td><td>$\left(\begin{array}{l} \text{radius} \\ \text{angle} \\ \text{polar} \end{array} \right)$</td></tr></table>	$\text{radius} = + \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right] \\ \text{height} \end{array} \right]$			$\text{angle} = + \left[\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right]$			RE	xy	$\left(\begin{array}{l} \text{radius} \\ \text{angle} \\ \text{polar} \end{array} \right)$							
$\text{radius} = + \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right] \\ \text{height} \end{array} \right]$																		
$\text{angle} = + \left[\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{center} \\ \text{vector_angle}(\text{this} \blacktriangleright \text{start}) \end{array} \right] \\ \frac{1}{2} \times \text{this} \blacktriangleright \text{angle} \end{array} \right]$																		
RE	xy	$\left(\begin{array}{l} \text{radius} \\ \text{angle} \\ \text{polar} \end{array} \right)$																
4	height_contact	height of this when this contacts object																
	height_contact	<table><tr><td>object</td><td>type = max</td></tr><tr><td colspan="2">$\text{radius.this} = \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right]$</td></tr><tr><td>SW</td><td>object \blacktriangleright type</td></tr><tr><td>∇</td><td><table><tr><td>Label2D</td><td>Rectangle2D</td><td>sublevel</td></tr></table></td></tr></table>	object	type = max	$\text{radius.this} = \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right]$		SW	object \blacktriangleright type	∇	<table><tr><td>Label2D</td><td>Rectangle2D</td><td>sublevel</td></tr></table>	Label2D	Rectangle2D	sublevel					
object	type = max																	
$\text{radius.this} = \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{this} \blacktriangleright \text{start} \end{array} \right]$																		
SW	object \blacktriangleright type																	
∇	<table><tr><td>Label2D</td><td>Rectangle2D</td><td>sublevel</td></tr></table>	Label2D	Rectangle2D	sublevel														
Label2D	Rectangle2D	sublevel																
4	1	$\nabla \left[\begin{array}{l} \text{Label2D} \\ \text{Rectangle2D} \end{array} \right]$																
		<table><tr><td colspan="2">Rectangle = object</td></tr><tr><td>SW</td><td>type</td></tr><tr><td colspan="2">max</td></tr><tr><td colspan="2">$\text{heights} = \emptyset$</td></tr><tr><td colspan="2">$= \left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{Label2D} \blacktriangleright \text{vertices} \end{array} \right]$</td></tr><tr><td>FE</td><td>$\left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{vertex} \end{array} \right]$</td></tr><tr><td colspan="2">$\text{heights} \pm \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{vertex} \end{array} \right] \\ \text{radius.this} \end{array} \right]$</td></tr><tr><td>RE</td><td>max(heights)</td></tr></table>	Rectangle = object		SW	type	max		$\text{heights} = \emptyset$		$= \left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{Label2D} \blacktriangleright \text{vertices} \end{array} \right]$		FE	$\left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{vertex} \end{array} \right]$	$\text{heights} \pm \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{vertex} \end{array} \right] \\ \text{radius.this} \end{array} \right]$		RE	max(heights)
Rectangle = object																		
SW	type																	
max																		
$\text{heights} = \emptyset$																		
$= \left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{Label2D} \blacktriangleright \text{vertices} \end{array} \right]$																		
FE	$\left[\begin{array}{c} \text{Rectangle2D.vertices} \\ \text{vertex} \end{array} \right]$																	
$\text{heights} \pm \left[\begin{array}{c} \left[\begin{array}{c} \text{this} \blacktriangleright \text{center} \\ \text{vertex} \end{array} \right] \\ \text{radius.this} \end{array} \right]$																		
RE	max(heights)																	

1.9 Point2D

1. Definition

Point2D ◀ xy	type = Point2D
	key
	key_object
	key_label
	method

2. Method

1	distance	distance between <i>this</i> and <i>object</i>												
	distance	<i>object</i>												
		<table><tr><td>SW</td><td><i>object</i> ▶ <i>type</i></td></tr><tr><td></td><td><table><tr><td></td><td><i>Segment2D</i> = <i>object</i></td></tr><tr><td>=</td><td>$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$</td></tr><tr><td>Segment2D</td><td><table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table></td></tr></table></td></tr></table>	SW	<i>object</i> ▶ <i>type</i>		<table><tr><td></td><td><i>Segment2D</i> = <i>object</i></td></tr><tr><td>=</td><td>$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$</td></tr><tr><td>Segment2D</td><td><table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table></td></tr></table>		<i>Segment2D</i> = <i>object</i>	=	$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$	Segment2D	<table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table>	RE	$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$
SW	<i>object</i> ▶ <i>type</i>													
	<table><tr><td></td><td><i>Segment2D</i> = <i>object</i></td></tr><tr><td>=</td><td>$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$</td></tr><tr><td>Segment2D</td><td><table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table></td></tr></table>		<i>Segment2D</i> = <i>object</i>	=	$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$	Segment2D	<table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table>	RE	$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$					
	<i>Segment2D</i> = <i>object</i>													
=	$\left[\begin{array}{c} \textit{line} \\ \textit{Segment2D} \blacktriangleright \textit{line} \end{array} \right]$													
Segment2D	<table><tr><td>RE</td><td>$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$</td></tr></table>	RE	$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$											
RE	$\div \left[\begin{array}{c} \textit{ine} \blacktriangleright \textit{evaluation}(\textit{this}) \\ \sqrt{\left[\begin{array}{c} (\textit{line} \blacktriangleright a)^2 \\ (\textit{line} \blacktriangleright b)^2 \end{array} \right]} \end{array} \right]$													

3	1	FO	$0 \leq i < Measure2Ds_contained $		
		$angle.i = Measure2Ds_contained[i] \blacktriangleright \left[\begin{array}{l} start \\ vector_angle(Measure2D_contained[i] \blacktriangleright end) \end{array} \right]$			
		\equiv	$\left[\begin{array}{l} sign.i \\ sign(Measure2Ds_contained[i] \blacktriangleright height) \end{array} \right]$		
		FO	$0 \leq j < i$		
		$angle.j = Measure2Ds_contained[j] \blacktriangleright \left[\begin{array}{l} start \\ vector_angle(Measure2Ds_contained[i] \blacktriangleright end) \end{array} \right]$			
		\equiv	$\left[\begin{array}{l} sign.j \\ sign(Measure2Ds_contained[j] \blacktriangleright height) \end{array} \right]$		
		\equiv	$\left[\begin{array}{l} number_directions_different \\ 0 \end{array} \right]$		
		IF	\wedge	$\left[\begin{array}{l} angle.i \neq angle.j \\ angle.i \neq -angle.j \end{array} \right]$	$+number_directions_different$
			\wedge	$\left[\begin{array}{l} angle.i \equiv angle.j \\ sign.i \neq sign.j \end{array} \right]$	$+number_directions_different$
			\wedge	$\left[\begin{array}{l} angle.i \equiv -angle.j \\ sign.i \equiv sign.j \end{array} \right]$	$+number_directions_different$
IF	\equiv	$\left[\begin{array}{l} number_directions_different \\ i - 1 \end{array} \right]$	$+number_directions$		

1.10 Rectangle2D

1. Definition

Rectangle	$type = Rectangle2D$
	$center$
	$size$
	$rotation$
	method

2. Method

1	construct													
	CO	<table><tr><td><i>center</i></td><td><i>size</i></td><td><i>rotation</i></td></tr><tr><td>\equiv</td><td colspan="2">$\left[\begin{array}{l} \textit{this} \triangleright \textit{center} \\ \textit{center} \end{array} \right]$</td></tr><tr><td>$\equiv$</td><td colspan="2">$\left[\begin{array}{l} \textit{this} \triangleright \textit{size} \\ \textit{size} \end{array} \right]$</td></tr><tr><td>$\equiv$</td><td colspan="2">$\left[\begin{array}{l} \textit{this} \triangleright \textit{rotation} \\ \textit{rotation} \end{array} \right]$</td></tr></table>	<i>center</i>	<i>size</i>	<i>rotation</i>	\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{center} \\ \textit{center} \end{array} \right]$		\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{size} \\ \textit{size} \end{array} \right]$		\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{rotation} \\ \textit{rotation} \end{array} \right]$	
<i>center</i>	<i>size</i>	<i>rotation</i>												
\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{center} \\ \textit{center} \end{array} \right]$													
\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{size} \\ \textit{size} \end{array} \right]$													
\equiv	$\left[\begin{array}{l} \textit{this} \triangleright \textit{rotation} \\ \textit{rotation} \end{array} \right]$													
2	interval	Interval of given <i>axis</i>												

interval	<i>axis</i>	
	<div> <div>SW</div> <div><i>axis</i></div> </div>	
	<div> <div>x</div> <div> <div>RE</div> <div>Interval</div> <div> $\begin{pmatrix} \boxed{-} & \begin{matrix} this \blacktriangleright center \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright x \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright x \end{matrix} \\ \boxed{+} & \begin{matrix} this \blacktriangleright center \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright x \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright x \end{matrix} \end{pmatrix}$ </div> </div> </div>	
	<div> <div>y</div> <div> <div>RE</div> <div>Interval</div> <div> $\begin{pmatrix} \boxed{-} & \begin{matrix} this \blacktriangleright center \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright y \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright y \end{matrix} \\ \boxed{+} & \begin{matrix} this \blacktriangleright center \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright y \\ \frac{1}{2} \times this \blacktriangleright size \\ this \blacktriangleright y \end{matrix} \end{pmatrix}$ </div> </div> </div>	

3	rotation	rotate arround $\begin{bmatrix} 0 & 0 \end{bmatrix}$ wwith <i>angle</i>
---	----------	---

rotation	angle	
	<i>this_rotated</i> = <i>this</i>	
	<i>center_rotation</i> = $\mathbf{xy} \begin{pmatrix} 0 \\ 0 \end{pmatrix}$	
	<i>this_rotated</i> \blacktriangleright <i>center</i> = <i>this</i> \blacktriangleright $\begin{bmatrix} center \\ rotation \begin{pmatrix} center_rotation \\ -this \blacktriangleright rotation \end{pmatrix} \end{bmatrix}$	
	<i>this_rotated</i> \blacktriangleright <i>target</i> = <i>this</i> \blacktriangleright $\begin{bmatrix} target \\ rotation \begin{pmatrix} center_rotation \\ -this \blacktriangleright rotation \end{pmatrix} \end{bmatrix}$	
	$\boxed{\pm} \begin{bmatrix} this_rotated \blacktriangleright angle \\ angle \end{bmatrix}$	
	RE	<i>this_rotated</i>

4	translation	translate with <i>vector</i>
---	-------------	------------------------------

translation	<i>vector</i>	
	<i>this_translation</i> = <i>this</i>	
	<i>this_translated</i> \blacktriangleright <i>center</i> = $\boxed{+} \begin{bmatrix} this \blacktriangleright center \\ vector \end{bmatrix}$	
	<i>this_translated</i> \blacktriangleright <i>target</i> = $\boxed{+} \begin{bmatrix} this \blacktriangleright target \\ vector \end{bmatrix}$	
	RE	<i>this_translated</i>

5	vertices	vertices
---	----------	----------

vertices	$vertices.0 = \emptyset$	
	$vertices.0 \stackrel{\pm}{=} \boxed{+}$	$\left[\begin{array}{c} this \blacktriangleright center \\ \boxed{\times} \left[t \left[\begin{array}{c c} -\frac{1}{2} & -\frac{1}{2} \end{array} \right] \right] \\ this \blacktriangleright size \end{array} \right]$
	$vertices.0 \stackrel{\pm}{=} \boxed{+}$	$\left[\begin{array}{c} this \blacktriangleright center \\ \boxed{\times} \left[\left[\begin{array}{c c} -\frac{1}{2} & \frac{1}{2} \end{array} \right] \right] \\ this \blacktriangleright size \end{array} \right]$
	$vertices.0 \stackrel{\pm}{=} \boxed{+}$	$\left[\begin{array}{c} this \blacktriangleright center \\ \boxed{\times} \left[\left[\begin{array}{c c} \frac{1}{2} & \frac{1}{2} \end{array} \right] \right] \\ this \blacktriangleright size \end{array} \right]$
	$vertices.0 \stackrel{\pm}{=} \boxed{+}$	$\left[\begin{array}{c} this \blacktriangleright center \\ \boxed{\times} \left[\left[\begin{array}{c c} \frac{1}{2} & -\frac{1}{2} \end{array} \right] \right] \\ this \blacktriangleright size \end{array} \right]$
	$vertices = \emptyset$	
	<div>FE<div>vertices.0vertex</div></div> <div>$vertices \stackrel{\pm}{=} vertex \blacktriangleright \text{rotation} \left(\begin{array}{c} this \blacktriangleright center \\ this \blacktriangleright rotation \end{array} \right)$</div>	
	RE <div>vertices</div>	

1.11 Sector2D

1. Definition

Sector2D	Sector2D
	center
	start
	angle
	method

2. Method

1

construct

CO	center	start	angle
$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright center \\ center \end{array} \right]$		
$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright start \\ start \end{array} \right]$		
$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright angle \\ angle \end{array} \right]$		

2

endend

end			
RE	this	$\left[\begin{array}{c} start \\ \text{rotation} \left(\begin{array}{c} this \blacktriangleright center \\ this \blacktriangleright angle \end{array} \right) \end{array} \right]$	

3

radiusradius

radius			
RE	$\boxed{=}$	$\left[\begin{array}{c} this \blacktriangleright center \\ this \blacktriangleright start \end{array} \right]$	

4

rotationrotate around center with angle

	rotation	<div>centerangle</div>
		<div><div>this_rotated = REthis</div></div>
		<div><div><div>this_rotated ► center = this ►</div><div><div>center</div><div>rotation $\left(\begin{array}{c} this \blacktriangleright center \\ angle \end{array} \right)$</div></div></div></div>
		<div><div><div>this_rotated ► start = this ►</div><div><div>start</div><div>rotation $\left(\begin{array}{c} this \blacktriangleright center \\ angle \end{array} \right)$</div></div></div></div>
		<div><div>REthis_translated</div></div>
5	translation	<div>translate with vector</div>
	translation	<div><div>vector</div><div><div><div>this_translated = this</div></div><div><div><div>this_translated ► center = +</div><div><div>this ► center</div><div>vector</div></div></div></div></div><div><div><div>this_translated ► start = +</div><div><div>this ► start</div><div>vector</div></div></div></div></div> <div><div>REthis_translated</div></div>

1.12 Segment2D

1. Definition

Segment2D	<div>type = Segment2D</div>
	<div>start</div>
	<div>end</div>
	<div>measure = 0</div>
	<div>key</div>
	<div>key_object</div>
	<div>key_label</div>
	<div>method</div>

2. Method

1	construct	
	CO	<div><div>startendmeasure</div><div><div><div><div>≡</div><div><div>this ► start</div><div>start</div></div></div></div><div><div><div><div>≡</div><div><div>this ► end</div><div>end</div></div></div></div><div><div><div><div>≡</div><div><div>this ► measure</div><div>measure</div></div></div></div></div></div></div></div>
2	center	<div>center</div>
	center	<div><div><div>RE</div><div><div><div>+</div><div><div>this ► start</div><div>this ► end</div></div></div><div>$\times \frac{1}{2}$</div></div></div></div>
3	coordinate	<div>coordinate when other axis value is given</div>

coordinate	<i>value</i> <i>axis</i> = x																		
	<div><div>=</div><div><div><div>line</div><div>this ▶ line</div></div></div></div>																		
	$coordinate = line \blacktriangleright coordinate \left(\begin{array}{c} value \\ axis \end{array} \right)$																		
	<div>IF</div>	<div>$coordinate \equiv \emptyset$</div> <div><div>RE</div><div><i>coordinate</i></div></div>																	
	<div>SW</div>	<div><i>axis</i></div> <table><tr><td rowspan="2">x</td><td><div>IF</div></td><td><div>\neq</div><div><div><div><i>coordinate</i></div><div>this ▶ interval(x)</div></div></div></td><td><div>RE</div></td><td><div>\emptyset</div></td></tr><tr><td><div>RE</div></td><td colspan="3"><div><i>coordinate</i></div></td></tr><tr><td rowspan="2">y</td><td><div>IF</div></td><td><div>\neq</div><div><div><div><i>coordinate</i></div><div>this ▶ interval(y)</div></div></div></td><td><div>RE</div></td><td><div>\emptyset</div></td></tr><tr><td><div>RE</div></td><td colspan="3"><div><i>coordinate</i></div></td></tr></table>	x	<div>IF</div>	<div>\neq</div> <div><div><div><i>coordinate</i></div><div>this ▶ interval(x)</div></div></div>	<div>RE</div>	<div>\emptyset</div>	<div>RE</div>	<div><i>coordinate</i></div>			y	<div>IF</div>	<div>\neq</div> <div><div><div><i>coordinate</i></div><div>this ▶ interval(y)</div></div></div>	<div>RE</div>	<div>\emptyset</div>	<div>RE</div>	<div><i>coordinate</i></div>	
x	<div>IF</div>	<div>\neq</div> <div><div><div><i>coordinate</i></div><div>this ▶ interval(x)</div></div></div>		<div>RE</div>	<div>\emptyset</div>														
	<div>RE</div>	<div><i>coordinate</i></div>																	
y	<div>IF</div>	<div>\neq</div> <div><div><div><i>coordinate</i></div><div>this ▶ interval(y)</div></div></div>	<div>RE</div>	<div>\emptyset</div>															
	<div>RE</div>	<div><i>coordinate</i></div>																	

4	interval	Interval for given <i>axis</i>	
	interval	<i>axis</i> = x	
		SW <i>axis</i>	
		x	<div><div>RE</div><div>Interval</div><div><div><div>min</div><div><div><div>this ▶</div><div><div>start</div><div>x</div><div>end</div></div></div><div><div>this ▶</div><div><div>start</div><div>x</div><div>end</div></div></div><div>max</div><div><div>this ▶</div><div><div>start</div><div>x</div><div>end</div></div><div>this ▶</div><div><div>start</div><div>x</div><div>end</div></div></div></div></div></div></div>
		y	<div><div>RE</div><div>Interval</div><div><div><div>min</div><div><div><div>this ▶</div><div><div>start</div><div>y</div><div>end</div></div></div><div><div>this ▶</div><div><div>start</div><div>y</div><div>end</div></div></div><div>max</div><div><div>this ▶</div><div><div>start</div><div>y</div><div>end</div></div><div>this ▶</div><div><div>start</div><div>y</div><div>end</div></div></div></div></div></div></div>

5	is_chord	check if <i>this</i> is chord of <i>Arc2D</i>
---	----------	---

is.chord	<i>Arc2D</i>	
	$distance.this.start = \left - \left[\begin{array}{l} Segment2D \blacktriangleright center \\ this \blacktriangleright start \end{array} \right] \right $	
	<div>IF</div> <div> \neq $\left[\begin{array}{l} Arc2D \blacktriangleright radius \\ distance.this.start \end{array} \right]$ </div> <div> <div>RE</div> <div>FA</div> </div>	
	$distance.this.end = \left - \left[\begin{array}{l} Arc2D \blacktriangleright center \\ this \blacktriangleright end \end{array} \right] \right $	
	<div>IF</div> <div> \neq $\left[\begin{array}{l} Arc2D \blacktriangleright radius \\ distance.this.end \end{array} \right]$ </div> <div> <div>RE</div> <div>FA</div> </div>	
	$angle_Arc2D.start = Arc2D \blacktriangleright \left[\begin{array}{l} center \\ vector.angle(Arc2D \blacktriangleright start) \end{array} \right]$	
	$angle_Arc2D.end = \left[+ \left[\begin{array}{l} angle_Arc2D.start \\ Arc2D \blacktriangleright angle \end{array} \right] \right]$	
	<div>IF</div> <div> \equiv $\left[\begin{array}{l} angle_Arc2D.start \\ angle_Arc2D.end \end{array} \right]$ </div> <div> <div>RE</div> <div>TR</div> </div>	
	$angle.this.start = Arc2D \blacktriangleright \left[\begin{array}{l} center \\ vector.angle(this \blacktriangleright start) \end{array} \right]$	
	$\equiv \left[\begin{array}{l} interval_angle_Arc2D \\ Arc2D \blacktriangleright interval_angle \end{array} \right]$	
6	is.equal.direction	check if vector directions of <i>this</i> and <i>Segment2D</i> are equal
	is.equal.direction	<i>Segment2D</i> <div> <div>RE</div> <div> \equiv $\left[\begin{array}{l} this \blacktriangleright vector.angle \\ Segment2D \blacktriangleright vector.angle \end{array} \right]$ </div> </div>
7	is.equal.direction	check if vector directions of <i>this</i> and <i>Segment2D</i> are opposite
	is.opposite.direction	<i>Segment2D</i> <div> <div>RE</div> <div> \equiv $\left[\begin{array}{l} this \blacktriangleright vector.angle \\ -Segment2D \blacktriangleright vector.angle \end{array} \right]$ </div> </div>
8	is.tangent	check if <i>this</i> and <i>object</i> are tangent
	is.tangent	<i>object</i> <div> <div>SW</div> <div> $object \blacktriangleright type$ </div> <div> <div>Arc2D</div> <div> $Arc2 = object$ <div> <div>RE</div> <div> $Arc2D \blacktriangleright is.tangent(this)$ </div> </div> </div> </div> </div>
9	line	Line2D containing <i>this</i>

line		
	$a = \boxed{-} \left[\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{end} \\ y \\ \text{start} \end{array} \right] \\ \text{this} \blacktriangleright y \end{array} \right]$	
	$b = \boxed{-} \left[\begin{array}{c} \text{this} \blacktriangleright \left[\begin{array}{c} \text{start} \\ x \\ \text{end} \end{array} \right] \\ \text{this} \blacktriangleright x \end{array} \right]$	
$c = \boxed{\times} \left[\begin{array}{c} \left[\begin{array}{c c} -a & b \end{array} \right] \\ \text{this} \blacktriangleright \text{start} \end{array} \right]$		
<div> <div>RE</div> <div>line $\left(\begin{array}{c} a \\ b \\ c \end{array} \right)$</div> </div>		
10	rotation	rotate around <i>center</i> with <i>angle</i>
rotation	<div> <div><i>center</i></div> <div><i>angle</i></div> </div>	
	<i>this_rotated</i> = <i>this</i>	
	$\text{this_rotated} \blacktriangleright \text{start} = \text{this} \blacktriangleright \left[\begin{array}{c} \text{start} \\ \text{rotation} \left(\begin{array}{c} \text{center} \\ \text{angle} \end{array} \right) \end{array} \right]$	
	$\text{this_rotated} \blacktriangleright \text{end} = \text{this} \blacktriangleright \left[\begin{array}{c} \text{end} \\ \text{rotation} \left(\begin{array}{c} \text{center} \\ \text{angle} \end{array} \right) \end{array} \right]$	
<div> <div>RE</div> <div><i>this_rotated</i></div> </div>		
11	translation	translate with <i>vector</i>
translation	<i>vector</i>	
	<i>this_translated</i> = <i>this</i>	
	$\text{this_translated} \blacktriangleright \text{start} = \boxed{+} \left[\begin{array}{c} \text{this} \blacktriangleright \text{start} \\ \text{vector} \end{array} \right]$	
	$\text{this_translated} \blacktriangleright \text{end} = \boxed{+} \left[\begin{array}{c} \text{this} \blacktriangleright \text{end} \\ \text{vector} \end{array} \right]$	
<div> <div>RE</div> <div><i>this_translated</i></div> </div>		
12	vector	vector
vector		
	<div> <div>RE</div> <div> <div>$\boxed{-}$</div> <div> $\left[\begin{array}{c} \text{this} \blacktriangleright \text{end} \\ \text{this} \blacktriangleright \text{start} \end{array} \right]$ </div> </div> </div>	
13	vector_angle	angle of vector
vector_angle		
	<div> <div>RE</div> <div> <div><i>this</i></div> <div> $\blacktriangleright \left[\begin{array}{c} \text{start} \\ \text{vector_angle} \end{array} \right]$ </div> </div> </div>	