

Functional programming from its fundamentals



Whoami



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The goal of today

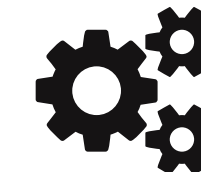
Content



**Fundamentals of
functional
programming**



**Why do we need
functional
programming**



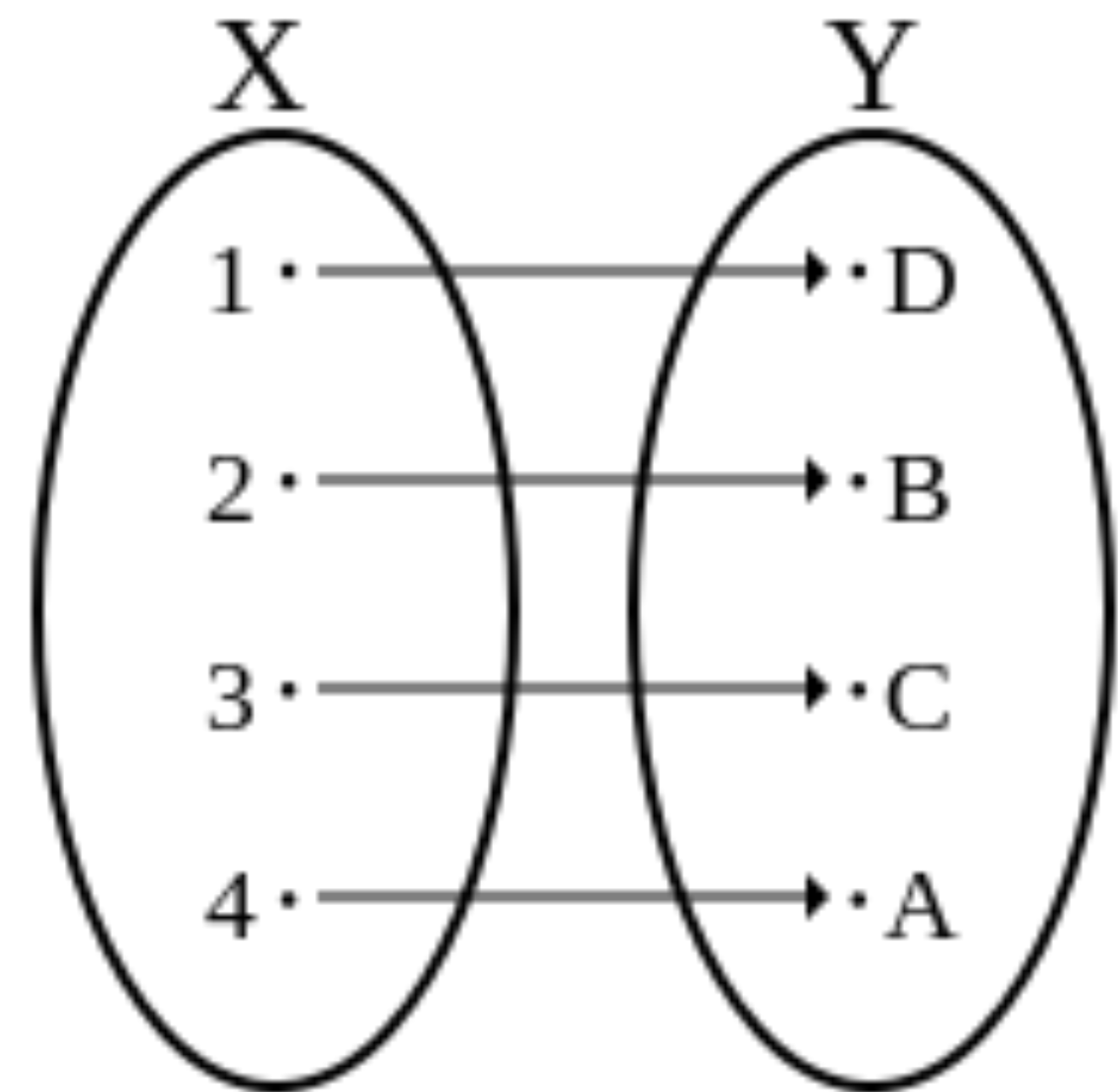
**Common constructs
from the
fundamentals**



What is functional programming

Programming with mathematical functions

A function is a mapping between a domain and a codomain. The only effect of a function is computing the result

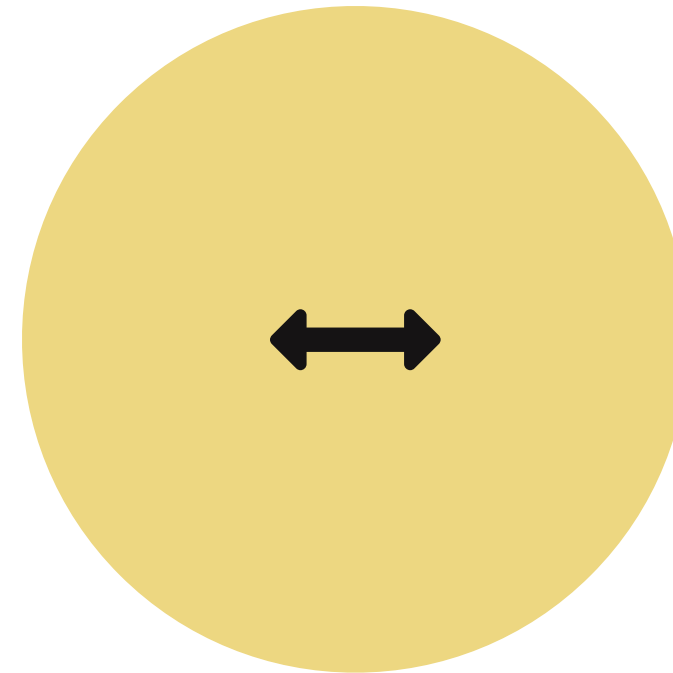


Properties of a function



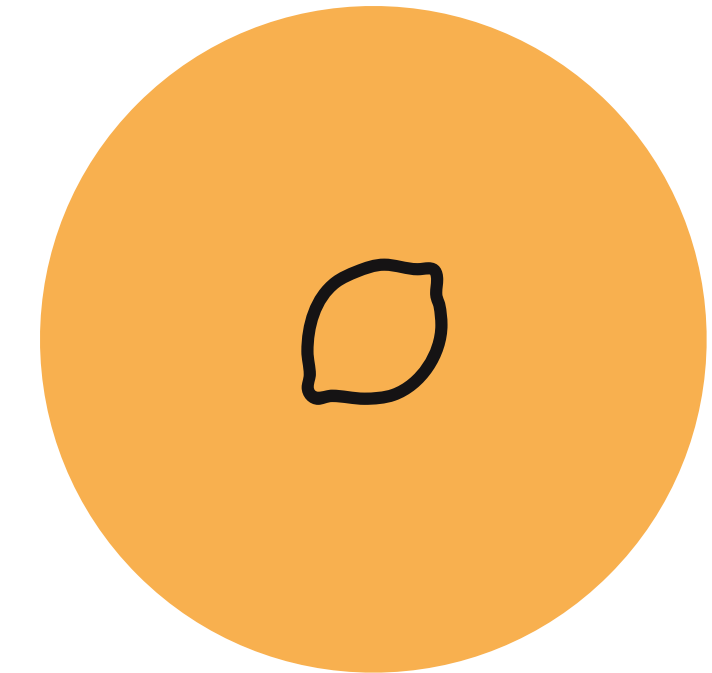
Totality

A function must yield a value for every possible input



Determinism

A function must yield the same result for the same input



Purity

A function's only effect must be the computation of its return value

Referential transparency

Expressions can be replaced with their values without changing the meaning of the program

Integer x = 1

new Pair<Integer, Integer>(x, x)

new Pair<Integer, Integer>(1, 1)

```
public Integer random() { ... }
```

```
Integer x = random();
```

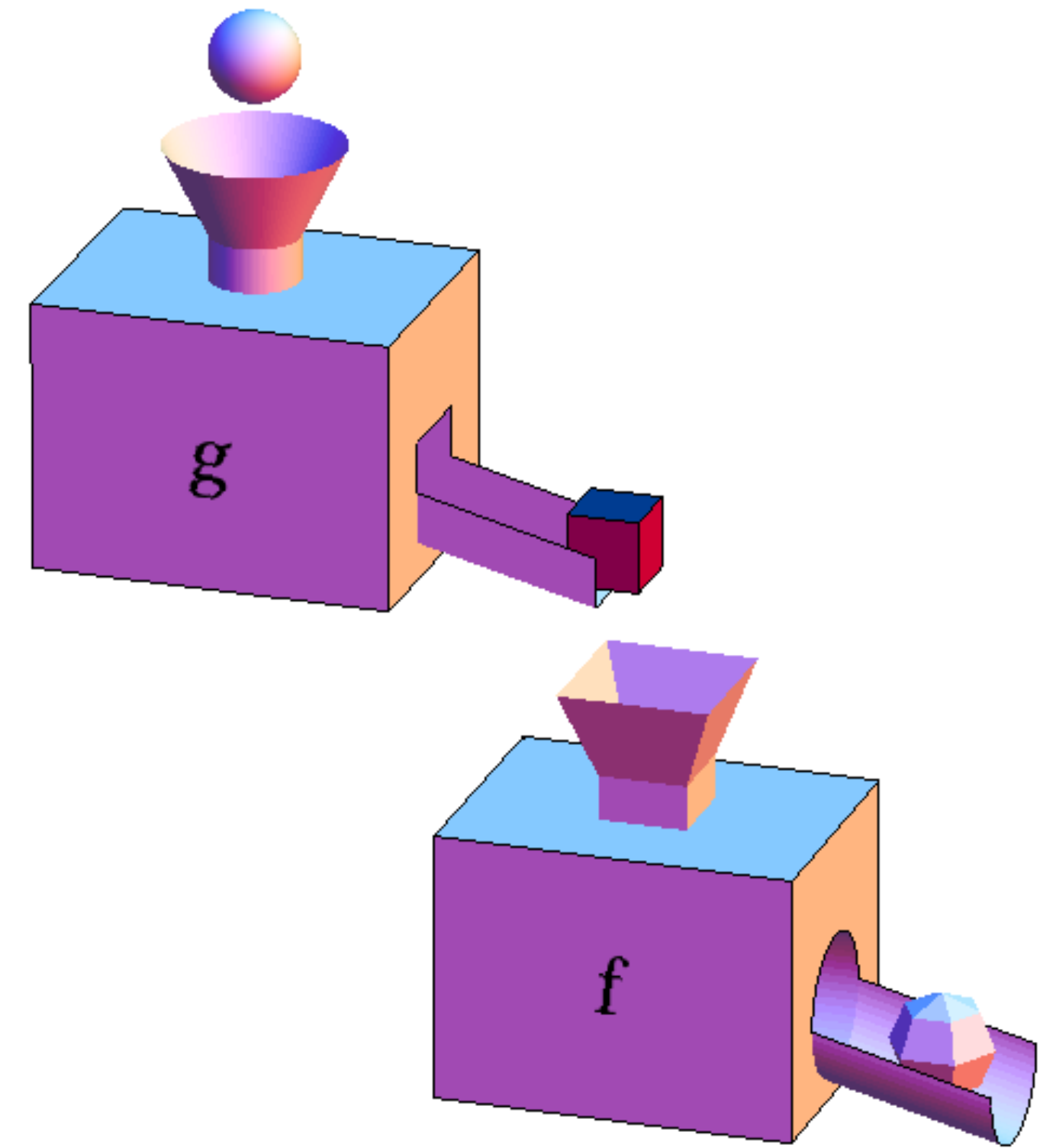
```
new Pair<Integer, Integer>(x, x)
```

```
public Integer random() { ... }
```

```
new Pair<Integer, Integer>(random(), random())
```

Function composition

Creates a new function from two other functions where the **second** function will be called with the result of evaluating the first function



Function composition

```
public static Integer length(String s) {  
    return s.length();  
}
```

```
public static Integer plus2(Integer x) {  
    return x + 2;  
}
```

```
public static Integer lengthPlus2(String s) {  
    return plus2(length(s));  
}
```

Function composition

```
public static <IN, MID, OUT> Function<IN, OUT> compose(Function<IN, MID> fst, Function<MID, OUT> snd) {  
    return (x -> snd.apply(fst.apply(x)));  
}
```


Function composition

```
Main.compose(Main::length, Main::plus2);
```


A blue pushpin is pinned to the top center of the notepad.

Disclaimer

Function composition

$(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow (a \rightarrow c)$

$(.)\ g\ f = \backslash a \rightarrow g\ (f\ a)$

Function composition

```
length :: String -> Int
```

```
plus2 :: Int -> Int
```

```
lengthPlus2 :: String -> Int -- lengthPlus2 "Hello Crowd!" -- 14  
lengthPlus2 = plus2 . length
```

Function composition

```
String -> Int  
      Int -> Int
```


Recap



Referential transparency



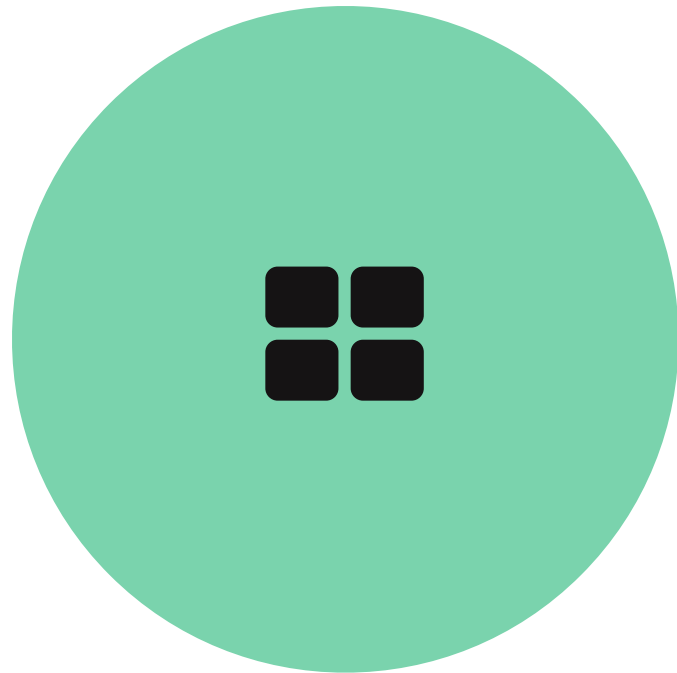
Function composition



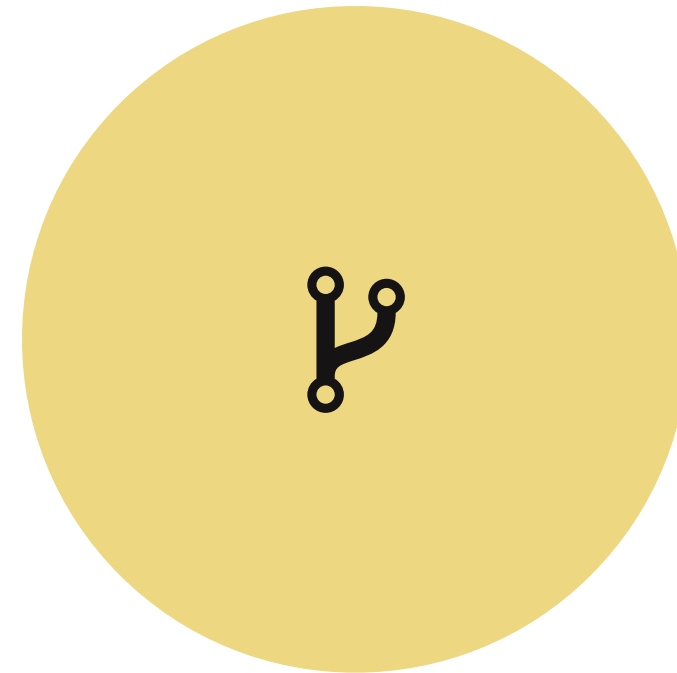


Why do we need functional programming

Why do we need functional programming



Concurrency & Parallelism



Reducing cognitive load



Easier to reason about

Example 1

```
public class Class1 {  
  
    public String head(List<String> list) {  
        if (list.size() <= 0) {  
            return null;  
        }  
  
        return list.get(0);  
    }  
}
```

Example 1

```
public class Class2 {  
  
    public Integer program(List<String> list) {  
  
        // can produce null pointer if list is empty  
        return head(list).length();  
    }  
}
```


Example 2

```
public class Class1 {  
  
    public Optional<String> head(List<String> list) {  
        if (list.size() <= 0) {  
            return Optional.empty();  
        }  
  
        return Optional.of(list.get(0));  
    }  
}
```

Example 2

```
public class Class2 {  
  
    public Optional<Integer> program(List<String> list) {  
        if (head(list).isPresent()) {  
            return Optional.of(head(list).get().length());  
        } else {  
            return Optional.empty();  
        }  
    }  
}
```



Common constructs from the fundamentals

Type classes

A tool to perform ad-hoc polymorphism in a functional programming language



Code duplication

```
-- sortString ["ba", "ab", "cd"] == ["ab", "ba", "cd"]
sortString :: [String] -> [String]
sortString [] = []
sortString (p:xs) =
    (sortString lesser) ++ [p] ++ (sortString greater)
    where
        lesser  = filter (< p) xs
        greater = filter (>= p) xs
```


Code duplication

```
-- sortInteger [1, 3, 2] == [1, 2, 3]
sortInteger :: [Integer] -> [Integer]
sortInteger [] = []
sortInteger (p:xs) =
    (sortInteger lesser) ++ [p] ++ (sortInteger greater)
    where
        lesser = filter (< p) xs
        greater = filter (>= p) xs
```

Ord typeclass

```
class Ord a where
    (<)      :: a -> a -> Bool
    (<=)     :: a -> a -> Bool
    (==)     :: a -> a -> Bool
    (/=)     :: a -> a -> Bool
    (>)      :: a -> a -> Bool
    (>=)     :: a -> a -> Bool
```

Ord instance for Integer

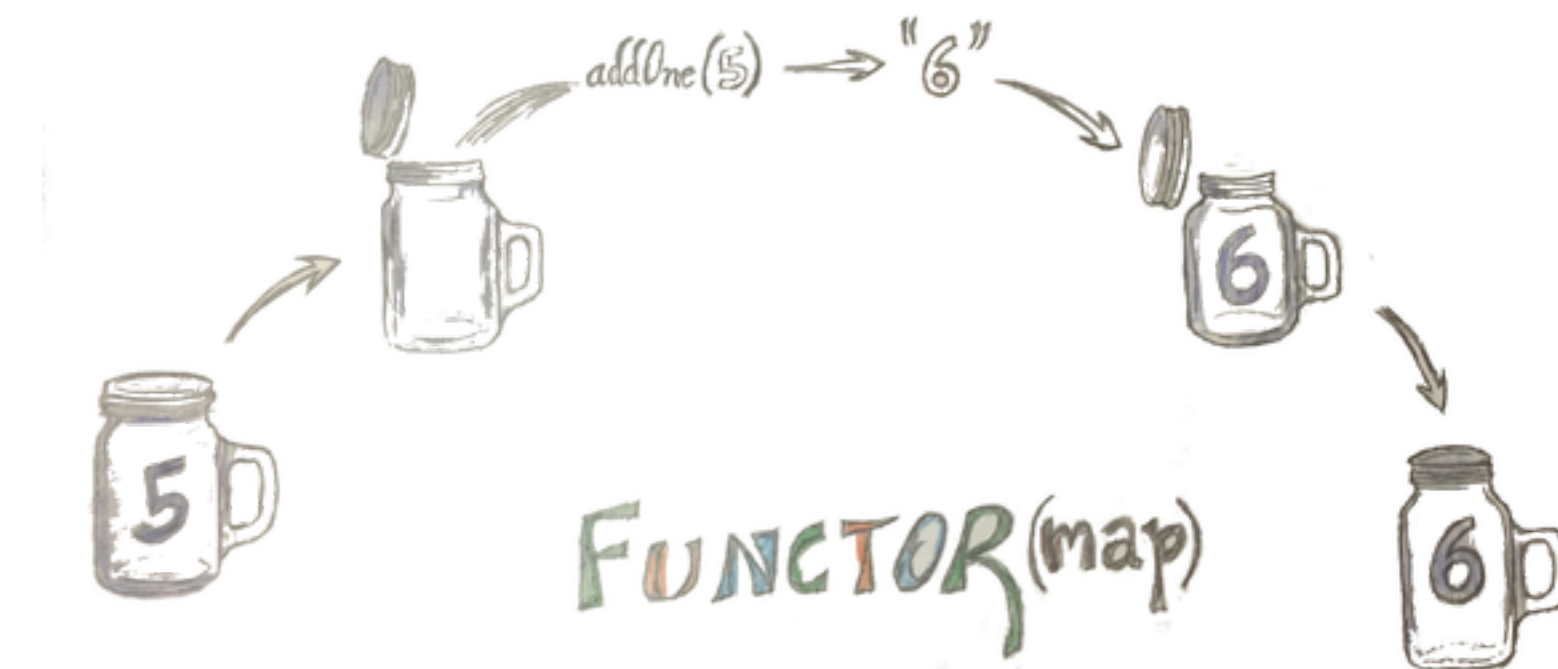
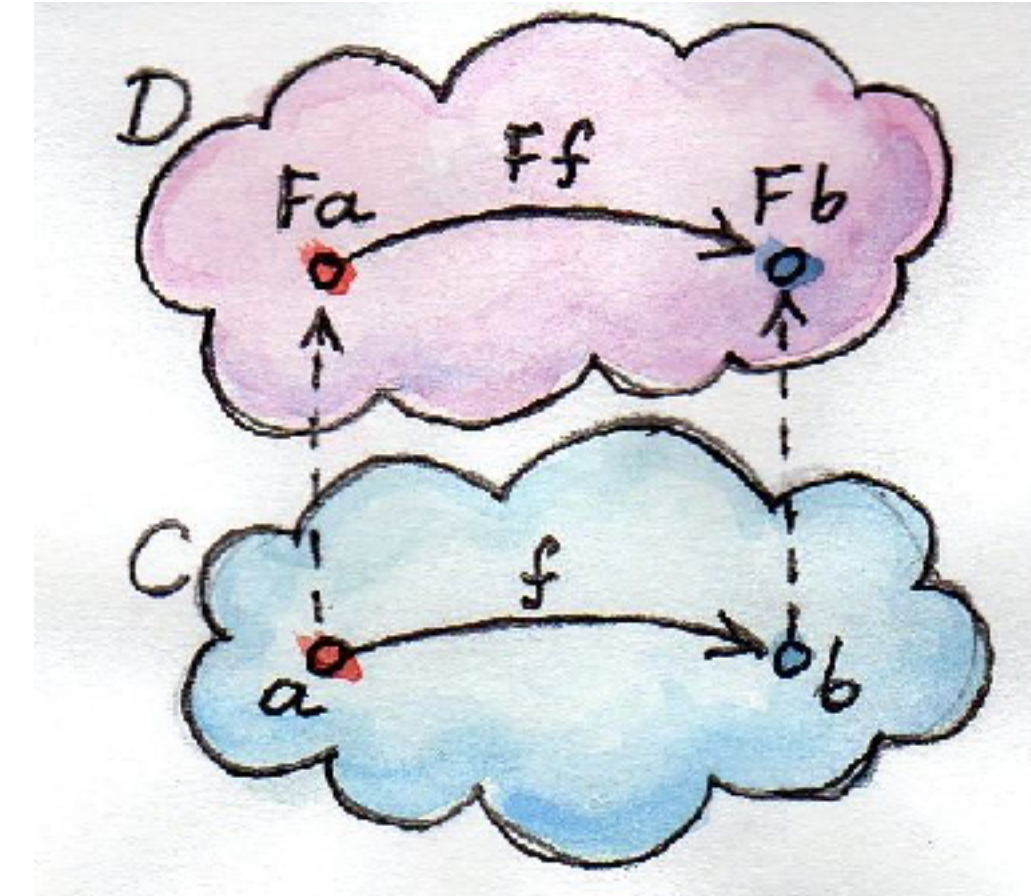
```
instance Ord Integer where
    (<)    a b = ...
    (<=)   a b = ...
    (==)   a b = ...
    (/=)   a b = ...
    (>)    a b = ...
    (>=)   a b = ...
```

Generalized

```
sort :: Ord a => [a] -> [a]
sort [] = []
sort (p:xs) = (sort lesser) ++ [p] ++ (sort greater)
    where
        lesser    = filter (< p) xs
        greater   = filter (>= p) xs
```


Functor

Abstract over type constructors that can be mapped over



When function composition doesn't fit

```
-- head ["a", "b", "c"] == "a"  
head :: List String -> Maybe String
```

```
-- Length "hello" == 5  
length :: String -> Int
```

When function composition doesn't fit

`List String -> Maybe`

<code>String</code>
<code>String</code>

`-> Int`

Mapping over the value in a context

```
fmap :: (a -> b) -> (Maybe a -> Maybe b)
```


Mapping over the value in a context

```
fmap :: (a -> b)  
      -> Maybe a -> Maybe b
```

```
head :: List String -> Maybe String
```

```
length :: String -> Int
```

```
-- composed ["test", "b"] == Just 4
```

```
composed :: List String -> Maybe Int
```

```
composed = fmap length . head
```

Lifting a function in a context

```
fmap :: (a -> b)  
      -> Maybe a -> Maybe b
```

```
length :: String -> Int -- length "example" == 7
```

```
-- maybeLength (Just "example") == Just 7
```

```
maybeLength :: Maybe String -> Maybe Int
```

```
maybeLength = fmap length
```

Abstracting over fmap

```
-- fproduct (Just 5) ((+) 1) == Just (5, 6)
fproduct :: Maybe a -> (a -> b) -> Maybe (a, b)
fproduct ma f = fmap (\a -> (a, f a)) ma
```

Abstracting over fmap

```
-- fproduct [1, 2, 3] ((+) 1) == [(1,2), (2, 3), (3, 4)]  
fproduct :: List a -> (a -> b) -> List (a, b)  
fproduct list f = fmap (\a -> (a, f a)) list
```

Abstracting over fmap

```
fproduct :: IO a -> (a -> b) -> IO (a, b)  
fproduct ma f = fmap (\a -> (a, f a)) ma
```


Code duplication

```
fproduct :: List a -> (a -> b) -> List (a, b)  
fproduct ma f = fmap (\a -> (a, f a)) ma
```

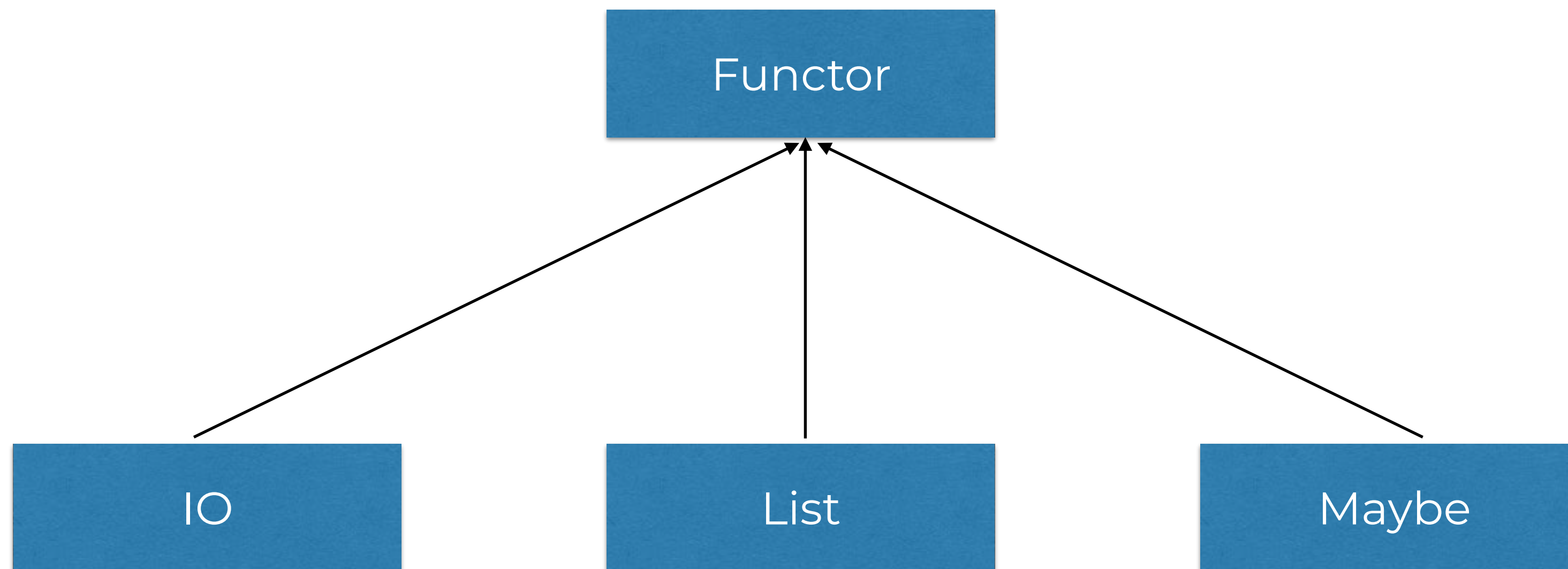
```
fproduct :: Maybe a -> (a -> b) -> Maybe (a, b)  
fproduct ma f = fmap (\a -> (a, f a)) ma
```

```
fproduct :: IO a -> (a -> b) -> IO (a, b)  
fproduct ma f = fmap (\a -> (a, f a)) ma
```

Functor typeclass

```
class Functor f where  
  fmap :: (a -> b) -> f a -> f b
```

Hierarchy



Functor for optionality

```
instance Functor Maybe where
  fmap :: (a -> b) -> Maybe a -> Maybe b
  fmap f (Just x) = Just $ f x
  fmap f Nothing = Nothing
```

Functor for List

```
instance Functor List where
  fmap :: (a -> b) -> List a -> List b
  fmap f [] = []
  fmap f (x:xs) = f x : fmap f xs
```

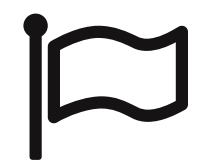

Generalizing fproduct function

```
fproduct :: Functor f => f a -> (a -> b) -> f (a, b)
fproduct ma f = fmap (\a -> (a, f a)) ma
```

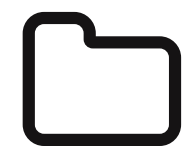
Impossible in Java

```
class Functor<F<>> {  
}
```

Recap



**Transforming values in
context**

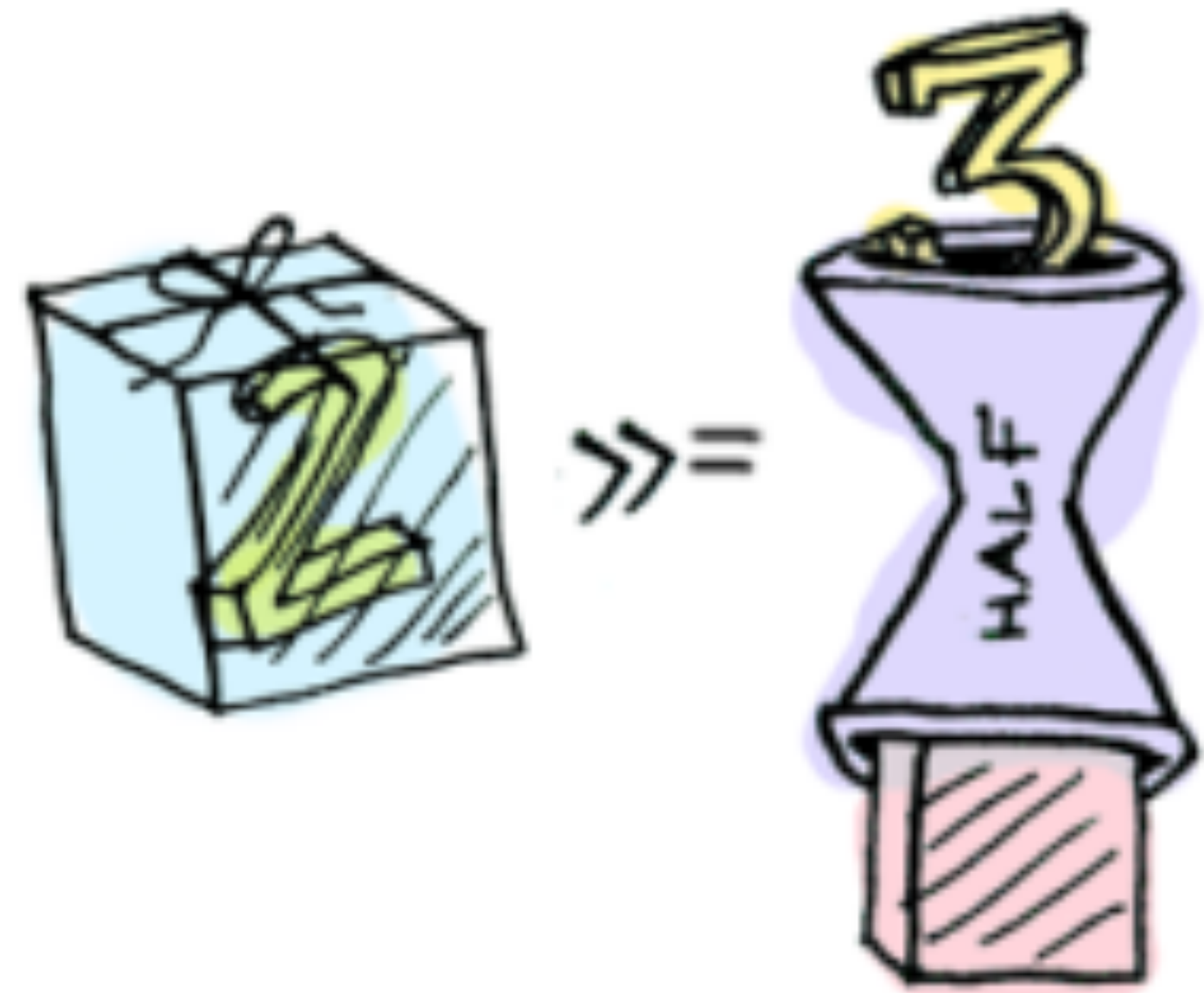


**Functor typeclass allows
polymorphism**



Monad

Combine computations that depend on each other



Monad

When functor is not enough

```
head :: List Int -> Maybe Int  
head [] = Nothing  
head (x:xs) = Just x
```

```
-- fiveDivBy 2 == Just 2.5  
-- fiveDivBy 0 == Nothing  
fiveDivBy :: Int -> Maybe Int  
fiveDivBy 0 = Nothing  
fiveDivBy x = Just (5 / x)
```

Map over f with g resulting in context

`List Int -> Maybe`

<code>Int</code>
<code>Int</code>

`-> Maybe Int`

When functor is not enough

```
composed list = fmap fiveDivBy (head list)
```

When functor is not enough

```
composed :: List Int -> Maybe (Maybe Int)
composed list = fmap fiveDivBy (head list)
```

```
-- composed [1, 2] == Just (Just 5)
-- composed [] == Nothing
-- composed [0, 3] == Just (Nothing)
```

When functor is not enough

```
composed :: List Int -> Maybe Int
composed list = flatten (fmap fiveDivBy (head list))

-- composed [1, 2] == Just 5
-- composed [] == Nothing
-- composed [0, 3] == Nothing
```

The Monad typeclass

```
class Monad m where  
  return :: a -> m a  
  fmap  :: (a -> b) -> m a -> m b  
  flatten :: m (m a) -> m a
```

The Monad typeclass

```
class Monad m where  
  return :: a -> m a  
  (>>=) :: m a -> (a -> m b) -> m b
```

The Monad typeclass

```
class Monad m where
  return :: a -> m a
  fmap :: (a -> b) -> m a -> m b
  flatten :: m (m a) -> m a

  (>>=) :: m a -> (a -> m b) -> m b
  (>>=) ma f = flatten (fmap f ma)
```


The Monad typeclass

```
instance Monad Maybe where
```

```
  return :: a -> Maybe a
```

```
  return x = Just x
```

```
  fmap :: (a -> b) -> Maybe a -> Maybe b
```

```
  fmap f (Just x) = Just (f x)
```

```
  fmap f Nothing = Nothing
```

```
  flatten :: Maybe (Maybe a) -> Maybe a
```

```
  flatten (Just (Just x)) = Just x
```

```
  flatten _ = Nothing
```

Composing with Monads

```
head :: List Int -> Maybe Int  
head [] = Nothing  
head (x: xs) = Just x
```

```
fiveDivBy :: Int -> Maybe Int  
fiveDivBy 0 = Nothing  
fiveDivBy x = Just (5 / x)
```

Composing with Monads

Head

List Int -> Maybe

Int
Int

 -> Maybe Int

fiveDivBy

Composing with Monads

```
composed :: List Int -> Maybe Int
composed list = flatten (fmap fiveDivBy (head list))
```

Composing with Monads

```
composed :: List Int -> Maybe Int
composed list = (head list) >>= fiveDivBy

-- composed [1, 2] == Just 5
-- composed [] == Nothing
-- composed [0, 3] == Nothing
```

Abstracting function composition with effects

Head

List Int -> Maybe

Int
Int

 -> Maybe Int

fiveDivBy

Abstracting function composition with effects

f

$a \rightarrow \text{Maybe } \boxed{\begin{smallmatrix} b \\ b \end{smallmatrix}} \rightarrow \text{Maybe } c$

g

Abstracting function composition with effects

f

a -> List

b
b

 -> List c

g

Abstracting function composition with effects

f

$a \rightarrow \text{IO } \boxed{\begin{smallmatrix} b \\ b \end{smallmatrix}} \rightarrow \text{IO } c$

g

Abstracting function composition with effects


```
maybeComposition :: (a -> Maybe b) -> (b -> Maybe c) -> (a -> Maybe c)
maybeComposition f g = \a -> (f a) >>= g
```

Abstracting function composition with effects

```
listComposition :: (a -> List b) -> (b -> List c) -> (a -> List c)
listComposition f g = \a -> (f a) >>= g
```

Abstracting function composition with effects

```
ioComposition :: (a -> IO b) -> (b -> IO c) -> (a -> IO c)  
ioComposition f g = \a -> (f a) >>= g
```



```
listComposition :: (a -> List b) -> (b -> List c) -> (a -> List c)
```


```
listComposition f g = \a -> (f a) >>= g
```

```
maybeComposition :: (a -> Maybe b) -> (b -> Maybe c) -> (a -> Maybe c)
```

```
maybeComposition f g = \a -> (f a) >>= g
```

```
ioComposition :: (a -> IO b) -> (b -> IO c) -> (a -> IO c)
```


```
ioComposition f g = \a -> (f a) >>= g
```



```
listComposition :: (a -> List b) -> (b -> List c) -> (a -> List c)
listComposition f g = \a -> (f a) >>= g
```

```
maybeComposition :: (a -> Maybe b) -> (b -> Maybe c) -> (a -> Maybe c)
maybeComposition f g = \a -> (f a) >>= g
```

```
ioComposition :: (a -> IO b) -> (b -> IO c) -> (a -> IO c)
ioComposition f g = \a -> (f a) >>= g
```

```
listComposition :: (a -> m b) -> (b -> m c) -> (a -> m c)
listComposition f g = \a -> (f a) >>= g
```

```
maybeComposition :: (a -> m b) -> (b -> m c) -> (a -> m c)
maybeComposition f g = \a -> (f a) >>= g
```

```
ioComposition :: (a -> m b) -> (b -> m c) -> (a -> m c)
ioComposition f g = \a -> (f a) >>= g
```

Kleisli composition

```
(>=>) :: Monad m => (a -> m b) -> (b -> m c) -> (a -> m c)  
(>=>) f g = \a -> (f a) >>= g
```

Kleisli examples

```
head :: [a] -> Maybe a  
head [] = Nothing  
head (x:xs) = Just x
```

```
fiveDivBy :: Double -> Maybe Double  
fiveDivBy 0 = Nothing  
fiveDivBy x = Just (5 / x)
```

Kleisli examples

```
composed :: [Double] -> Maybe Double  
composed = head >=> fiveDivBy
```

Kleisli examples

```
composed :: [Double] -> Maybe Double  
composed = head >=> fiveDivBy
```

```
-- composed [1.0, 2.0, 3.0] == Just 5.0  
-- composed [0.0, 1.0, 2.0] == Nothing  
-- composed [] == Nothing
```

Kleisli examples

```
composed :: [Double] -> Maybe Double
composed list = case head list of
    Just x -> fiveDivBy x
    Nothing -> Nothing
```

Kleisli examples

```
composed :: [Double] -> Maybe Double  
composed = head >=> fiveDivBy
```

```
another :: Double -> Maybe String
```


Kleisli examples

```
newComposed :: [Double] -> Maybe String  
newComposed = head >=> fiveDivBy >=> another
```

Kleisli examples

```
newComposed :: [Double] -> Maybe String
newComposed list = case head list of
  Just x -> case fiveDivBy x of
    Just y -> another y
    Nothing -> Nothing
  Nothing -> Nothing
```

Recap



Monad allows sequencing of computations



Monad typeclass for abstracting over monads



Kleisli composition as function composition with embellished types





Gabriel Gonzalez @GabrielG439 · 14 apr.



Using "the right tool for job" requires learning the available tools. Expand your horizons by trying a typed and/or functional language if you haven't already

 Tweet vertalen



6



80



178



Beauty of functional programming



We start with function composition

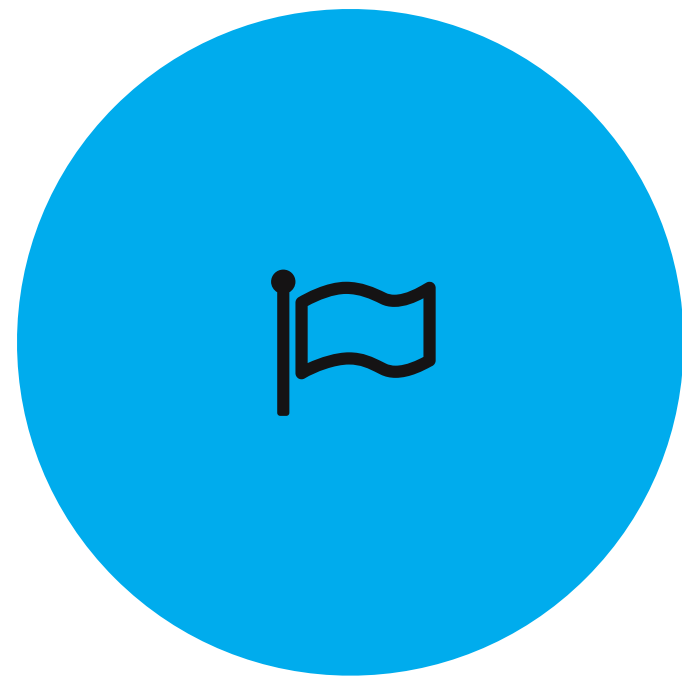


Function composition doesn't fit all requirements anymore



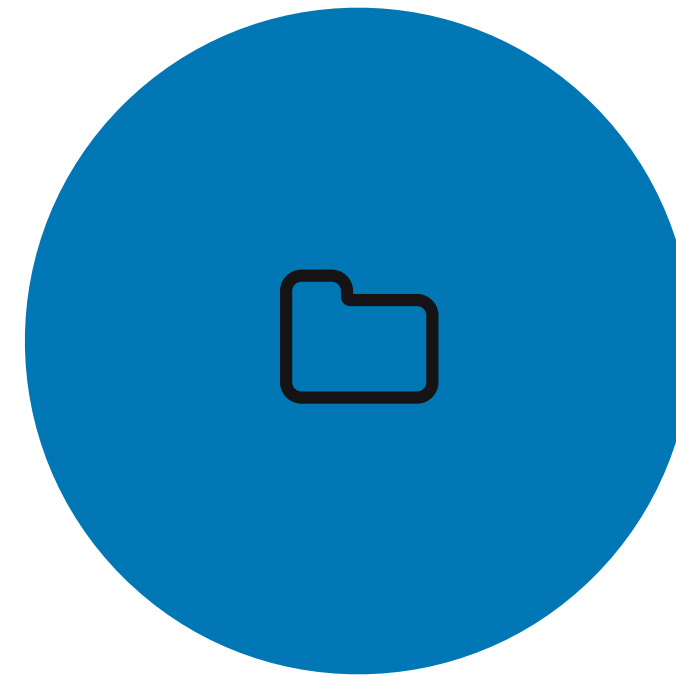
Beautiful abstractions to fit the new requirements

Let's connect



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