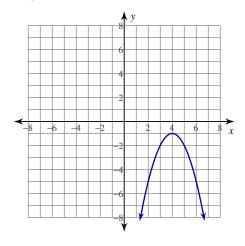
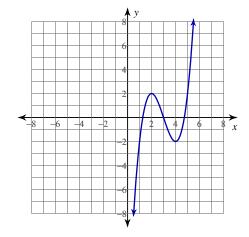
Mean Value Theorem

For each problem, find the values of c that satisfy the Mean Value Theorem.

1)
$$y = -x^2 + 8x - 17$$
; [3, 6]



2)
$$y = x^3 - 9x^2 + 24x - 18$$
; [2, 4]



3)
$$y = -\frac{x^2}{2} + x - \frac{1}{2}$$
; [-2, 1]

4)
$$y = \frac{x^2}{2} - 2x - 1$$
; [-1, 1]

5)
$$y = x^3 + 3x^2 - 2$$
; [-2, 0]

6)
$$y = -x^3 + 4x^2 - 3$$
; [0, 4]

7)
$$y = \frac{x^2 - 9}{3x}$$
; [1, 4]

8)
$$y = \frac{x^2}{2x - 4}$$
; [-4, 1]

9) $y = -(-2x+6)^{\frac{1}{2}}$; [-2, 3]

10) $y = -(-5x + 25)^{\frac{1}{2}}$; [3, 5]

For each problem, determine if the Mean Value Theorem can be applied. If it can, find all values of c that satisfy the theorem. If it cannot, explain why not.

11)
$$y = -\frac{x^2}{4x+8}$$
; [-3, -1]

12)
$$y = \frac{-x^2 + 9}{4x}$$
; [1, 3]

13)
$$y = -(6x + 24)^{\frac{2}{3}}$$
; [-4, -1]

14)
$$y = (x-3)^{\frac{2}{3}}$$
; [1, 4]

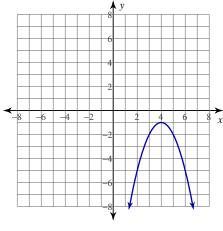
Critical thinking question:

15) Use the Mean Value Theorem to prove that $\left| \sin a - \sin b \right| \le \left| a - b \right|$ for all real values of a and b where $a \ne b$.

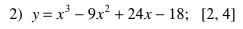
Mean Value Theorem

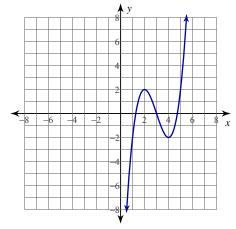
For each problem, find the values of c that satisfy the Mean Value Theorem.

1)
$$y = -x^2 + 8x - 17$$
; [3, 6]



$$\left\{\frac{9}{2}\right\}$$





$$\left\{\frac{9+\sqrt{3}}{3}, \frac{9-\sqrt{3}}{3}\right\}$$

3)
$$y = -\frac{x^2}{2} + x - \frac{1}{2}$$
; [-2, 1]

$$\left\{-\frac{1}{2}\right\}$$

4)
$$y = \frac{x^2}{2} - 2x - 1$$
; [-1, 1] {0}

5)
$$y = x^3 + 3x^2 - 2$$
; $[-2, 0]$
$$\left\{ \frac{-3 + \sqrt{3}}{3}, \frac{-3 - \sqrt{3}}{3} \right\}$$

6)
$$y = -x^3 + 4x^2 - 3$$
; [0, 4] $\left\{\frac{8}{3}\right\}$

7)
$$y = \frac{x^2 - 9}{3x}$$
; [1, 4]

8)
$$y = \frac{x^2}{2x - 4}$$
; [-4, 1] $\{2 - \sqrt{6}\}$

9)
$$y = -(-2x+6)^{\frac{1}{2}}$$
; [-2, 3] $\left\{\frac{7}{4}\right\}$

10)
$$y = -(-5x + 25)^{\frac{1}{2}}$$
; [3, 5] $\left\{\frac{9}{2}\right\}$

For each problem, determine if the Mean Value Theorem can be applied. If it can, find all values of c that satisfy the theorem. If it cannot, explain why not.

11)
$$y = -\frac{x^2}{4x+8}$$
; [-3, -1]

12)
$$y = \frac{-x^2 + 9}{4x}$$
; [1, 3]

The function is not continuous on [-3, -1]

$$\{\sqrt{3}\}$$

13)
$$y = -(6x + 24)^{\frac{2}{3}}$$
; [-4, -1] $\left\{-\frac{28}{9}\right\}$

14)
$$y = (x-3)^{\frac{2}{3}}$$
; [1, 4]

The function is not differentiable on (1, 4)

Critical thinking question:

15) Use the Mean Value Theorem to prove that $\left| \sin a - \sin b \right| \le \left| a - b \right|$ for all real values of a and b where $a \ne b$.

Let $f(x) = \sin x$. Use the interval [a,b]. By the MVT, we know that there is at least one c such that $\frac{\sin b - \sin a}{b - a} = \cos c$. We know $\cos c \le 1$ for all c. Therefore, $\frac{\sin b - \sin a}{b - a} \le 1$, $\frac{\left|\sin a - \sin b\right|}{\left|a - b\right|} \le 1$, and $\left|\sin a - \sin b\right| \le \left|a - b\right|$.

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