Solving Rational Equations

Solve each equation. Remember to check for extraneous solutions.

1)
$$\frac{1}{6k^2} = \frac{1}{3k^2} - \frac{1}{k}$$

2)
$$\frac{1}{n^2} + \frac{1}{n} = \frac{1}{2n^2}$$

3)
$$\frac{1}{6h^2} + \frac{1}{6h} = \frac{1}{h^2}$$

4)
$$\frac{b+6}{4b^2} + \frac{3}{2b^2} = \frac{b+4}{2b^2}$$

5)
$$\frac{1}{x} = \frac{6}{5x} + 1$$

$$6) \ \frac{1}{6x^2} = \frac{1}{2x} + \frac{7}{6x^2}$$

7)
$$\frac{1}{v} + \frac{3v + 12}{v^2 - 5v} = \frac{7v - 56}{v^2 - 5v}$$

8)
$$\frac{1}{m^2 - m} + \frac{1}{m} = \frac{5}{m^2 - m}$$

9)
$$\frac{1}{n-8} - 1 = \frac{7}{n-8}$$

10)
$$\frac{1}{r-2} + \frac{1}{r^2 - 7r + 10} = \frac{6}{r-2}$$

11)
$$1 = \frac{v+2}{v-4} + \frac{7v-42}{v-4}$$

12)
$$\frac{r-4}{5r} = \frac{1}{5r} + 1$$

13)
$$1 + \frac{x^2 - 5x - 24}{3x} = \frac{x - 6}{3x}$$

14)
$$1 = \frac{1}{x^2 + 2x} + \frac{x - 1}{x}$$

15)
$$\frac{n+5}{n+8} = 1 + \frac{6}{n+1}$$

16)
$$\frac{r+5}{r^2-2r}-1=\frac{1}{r^2-2r}$$

17)
$$\frac{1}{x^2 - 5x} = \frac{x + 7}{x} - 1$$

18)
$$\frac{a-2}{a+3} - 1 = \frac{3}{a+2}$$

19)
$$\frac{p+5}{p^2+p} = \frac{1}{p^2+p} - \frac{p-6}{p+1}$$

20)
$$\frac{5}{n^3 + 5n^2} = \frac{4}{n+5} + \frac{1}{n^2}$$

Solving Rational Equations

Solve each equation. Remember to check for extraneous solutions.

1)
$$\frac{1}{6k^2} = \frac{1}{3k^2} - \frac{1}{k}$$
 $\left\{\frac{1}{6}\right\}$

2)
$$\frac{1}{n^2} + \frac{1}{n} = \frac{1}{2n^2}$$
 $\left\{ -\frac{1}{2} \right\}$

3)
$$\frac{1}{6b^2} + \frac{1}{6b} = \frac{1}{b^2}$$
 {5}

4)
$$\frac{b+6}{4b^2} + \frac{3}{2b^2} = \frac{b+4}{2b^2}$$

$$5) \frac{1}{x} = \frac{6}{5x} + 1$$

$$\left\{ -\frac{1}{5} \right\}$$

6)
$$\frac{1}{6x^2} = \frac{1}{2x} + \frac{7}{6x^2}$$
$$\{-2\}$$

7)
$$\frac{1}{v} + \frac{3v + 12}{v^2 - 5v} = \frac{7v - 56}{v^2 - 5v}$$
 {21}

8)
$$\frac{1}{m^2 - m} + \frac{1}{m} = \frac{5}{m^2 - m}$$
 {5}

9)
$$\frac{1}{n-8} - 1 = \frac{7}{n-8}$$
 {2}

10)
$$\frac{1}{r-2} + \frac{1}{r^2 - 7r + 10} = \frac{6}{r-2}$$
$$\left\{\frac{26}{5}\right\}$$

11)
$$1 = \frac{v+2}{v-4} + \frac{7v-42}{v-4}$$
$$\left\{\frac{36}{7}\right\}$$

12)
$$\frac{r-4}{5r} = \frac{1}{5r} + 1$$
$$\left\{-\frac{5}{4}\right\}$$

13)
$$1 + \frac{x^2 - 5x - 24}{3x} = \frac{x - 6}{3x}$$
$$\{-3, 6\}$$

14)
$$1 = \frac{1}{x^2 + 2x} + \frac{x - 1}{x}$$
$$\{-1\}$$

15)
$$\frac{n+5}{n+8} = 1 + \frac{6}{n+1}$$
$$\left\{ -\frac{17}{3} \right\}$$

16)
$$\frac{r+5}{r^2-2r} - 1 = \frac{1}{r^2-2r}$$
$$\{4, -1\}$$

17)
$$\frac{1}{x^2 - 5x} = \frac{x + 7}{x} - 1$$

$$\left\{\frac{36}{7}\right\}$$

18)
$$\frac{a-2}{a+3} - 1 = \frac{3}{a+2}$$
 $\left\{-\frac{19}{8}\right\}$

19)
$$\frac{p+5}{p^2+p} = \frac{1}{p^2+p} - \frac{p-6}{p+1}$$
{4, 1}

20)
$$\frac{5}{n^3 + 5n^2} = \frac{4}{n+5} + \frac{1}{n^2}$$
$$\left\{ -\frac{1}{4} \right\}$$