Graphing and Properties of Ellipses

Identify the center, vertices, co-vertices, foci, length of the major axis, and length of the minor axis of each.

$$1) \ \frac{x^2}{49} + \frac{y^2}{169} = 1$$

2)
$$\frac{x^2}{36} + \frac{y^2}{16} = 1$$

3)
$$\frac{x^2}{95} + \frac{y^2}{30} = 1$$

4)
$$\frac{x^2}{169} + \frac{y^2}{64} = 1$$

5)
$$\frac{x^2}{64} + \frac{(y-6)^2}{121} = 1$$

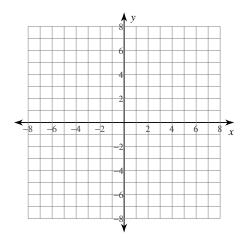
6)
$$\frac{(x+5)^2}{81} + \frac{(y-1)^2}{144} = 1$$

7)
$$\frac{(x-3)^2}{49} + \frac{(y-9)^2}{4} = 1$$

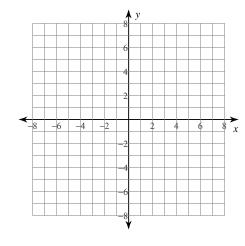
$$8) \ \frac{x^2}{64} + \frac{(y-8)^2}{9} = 1$$

Graph each equation.

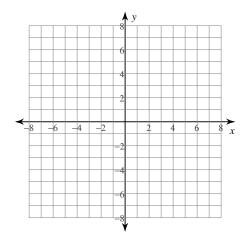
9)
$$\frac{x^2}{4} + \frac{y^2}{9} = 1$$



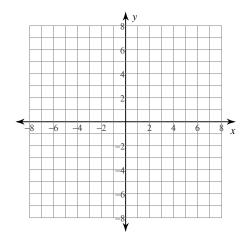
$$10) \ \frac{x^2}{49} + y^2 = 1$$



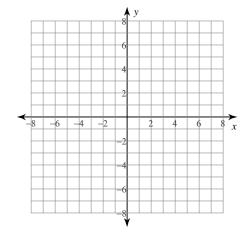
11)
$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$



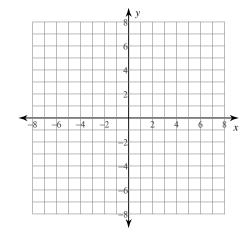
12)
$$\frac{x^2}{9} + \frac{y^2}{49} = 1$$



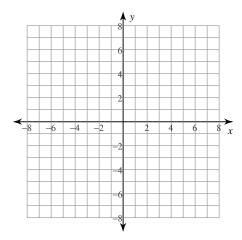
13)
$$\frac{x^2}{49} + \frac{(y-3)^2}{16} = 1$$



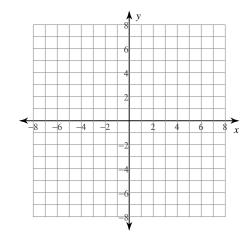
14)
$$\frac{(x-1)^2}{4} + \frac{y^2}{49} = 1$$



15)
$$\frac{x^2}{49} + \frac{(y-1)^2}{9} = 1$$



16)
$$(x+5)^2 + \frac{y^2}{49} = 1$$



Identify the length of the major axis, length of the minor axis, length of the latus rectum, and eccentricity of each.

17)
$$-16y + 52 = -2x^2 - 8x - y^2$$

18)
$$4y^2 - 338x + 32y = -169x^2 + 443$$

19)
$$\frac{(x+4)^2}{4} + \frac{(y+9)^2}{64} = 1$$

20)
$$126y + 9y^2 - 8x - 131 = -4x^2$$

Graphing and Properties of Ellipses

Identify the center, vertices, co-vertices, foci, length of the major axis, and length of the minor axis of each.

1)
$$\frac{x^2}{49} + \frac{y^2}{169} = 1$$

Center: (0, 0)

Vertices: (0, 13), (0, -13)Co-vertices: (7, 0), (-7, 0)

Foci: $(0, 2\sqrt{30}), (0, -2\sqrt{30})$

Major Axis: 26 units Minor Axis: 14 units

$$3) \ \frac{x^2}{95} + \frac{y^2}{30} = 1$$

Center: (0, 0)Vertices: $(\sqrt{95}, 0), (-\sqrt{95}, 0)$ Co-vertices: $(0, \sqrt{30}), (0, -\sqrt{30})$

Foci: $(\sqrt{65}, 0), (-\sqrt{65}, 0)$ Major Axis: $2\sqrt{95}$ units

Minor Axis: $2\sqrt{30}$ units

5)
$$\frac{x^2}{64} + \frac{(y-6)^2}{121} = 1$$

Center: (0, 6)

Vertices: (0, 17), (0, -5)

Co-vertices: (8, 6), (-8, 6)

Foci: $(0, 6 + \sqrt{57}), (0, 6 - \sqrt{57})$

Major Axis: 22 units Minor Axis: 16 units

$$2) \ \frac{x^2}{36} + \frac{y^2}{16} = 1$$

Center: (0, 0)

Vertices: (6, 0), (-6, 0)

Co-vertices: (0, 4), (0, -4)

Foci: $(2\sqrt{5}, 0), (-2\sqrt{5}, 0)$

Major Axis: 12 units Minor Axis: 8 units

4)
$$\frac{x^2}{169} + \frac{y^2}{64} = 1$$

Center: (0, 0)

Vertices: (13, 0), (-13, 0)

Co-vertices: (0, 8), (0, -8)

Foci: $(\sqrt{105}, 0), (-\sqrt{105}, 0)$

Major Axis: 26 units Minor Axis: 16 units

6)
$$\frac{(x+5)^2}{81} + \frac{(y-1)^2}{144} = 1$$

Center: (-5, 1)

Vertices: (-5, 13), (-5, -11)

Co-vertices: (4, 1), (-14, 1)

Foci: $(-5, 1 + 3\sqrt{7}), (-5, 1 - 3\sqrt{7})$

Major Axis: 24 units Minor Axis: 18 units

7)
$$\frac{(x-3)^2}{49} + \frac{(y-9)^2}{4} = 1$$

Center: (3, 9)

Vertices: (10, 9), (-4, 9)

Co-vertices: (3, 11), (3, 7)Foci: $(3 + 3\sqrt{5}, 9), (3 - 3\sqrt{5}, 9)$

Major Axis: 14 units Minor Axis: 4 units

8)
$$\frac{x^2}{64} + \frac{(y-8)^2}{9} = 1$$

Center: (0, 8)

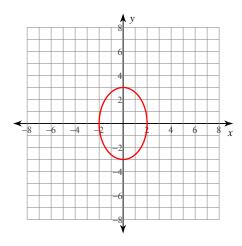
Vertices: (8, 8), (-8, 8)

Co-vertices: (0, 11), (0, 5)Foci: $(\sqrt{55}, 8), (-\sqrt{55}, 8)$

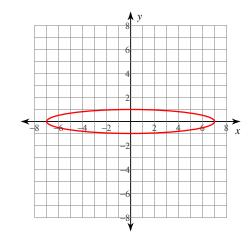
Major Axis: 16 units Minor Axis: 6 units

Graph each equation.

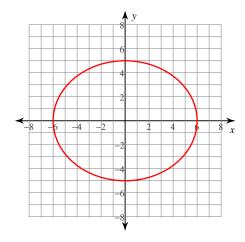
9)
$$\frac{x^2}{4} + \frac{y^2}{9} = 1$$



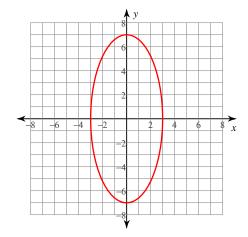
$$10) \ \frac{x^2}{49} + y^2 = 1$$



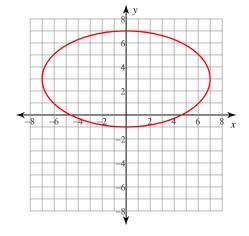
11)
$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$



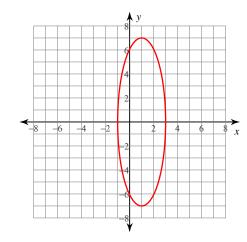
12)
$$\frac{x^2}{9} + \frac{y^2}{49} = 1$$



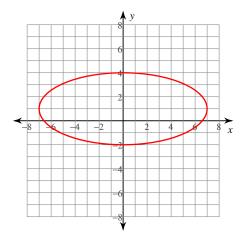
13)
$$\frac{x^2}{49} + \frac{(y-3)^2}{16} = 1$$



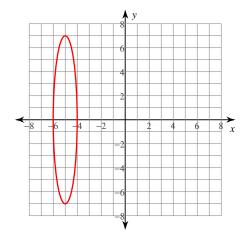
14)
$$\frac{(x-1)^2}{4} + \frac{y^2}{49} = 1$$



15)
$$\frac{x^2}{49} + \frac{(y-1)^2}{9} = 1$$



16)
$$(x+5)^2 + \frac{y^2}{49} = 1$$



Identify the length of the major axis, length of the minor axis, length of the latus rectum, and eccentricity of each.

17)
$$-16y + 52 = -2x^2 - 8x - y^2$$

Major Axis: $4\sqrt{5}$ units Minor Axis: $2\sqrt{10}$ units Latus Rectum: $2\sqrt{5}$ units

Eccentricity: $\frac{\sqrt{2}}{2} \approx 0.707$

18)
$$4y^2 - 338x + 32y = -169x^2 + 443$$

Major Axis: 26 units Minor Axis: 4 units

Latus Rectum: $\frac{8}{13}$ units

Eccentricity: $\frac{\sqrt{165}}{13} \approx 0.988$

19)
$$\frac{(x+4)^2}{4} + \frac{(y+9)^2}{64} = 1$$

Major Axis: 16 units Minor Axis: 4 units Latus Rectum: 1 unit

Eccentricity: $\frac{\sqrt{15}}{4} \approx 0.968$

20)
$$126y + 9y^2 - 8x - 131 = -4x^2$$

Major Axis: 24 units Minor Axis: 16 units

Latus Rectum: $\frac{32}{3}$ units Eccentricity: $\frac{\sqrt{5}}{3} \approx 0.745$