

# Greatest Integer Function Worksheet

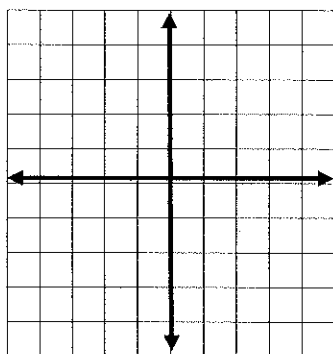
Name \_\_\_\_\_

Evaluate the following:

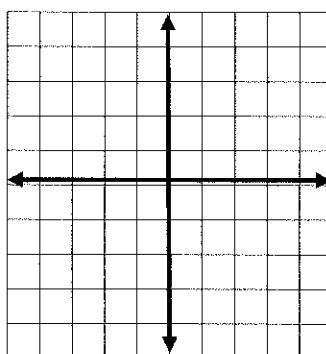
1.  $\lceil 7.1 \rceil$       2.  $\lceil 1.8 \rceil$       3.  $\lceil \pi \rceil$       4.  $\lceil -6.8 \rceil$       5.  $\lceil -2.1 \rceil$       6.  $\lceil 0 \rceil$

Graph the translation in 7 and 8. Then describe the translations and how they differ.

7.  $f(x) = \lceil x \rceil + 2$

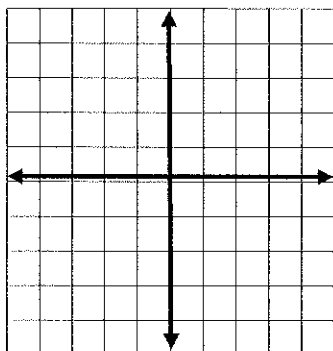


8.  $g(x) = \lceil x + 2 \rceil$

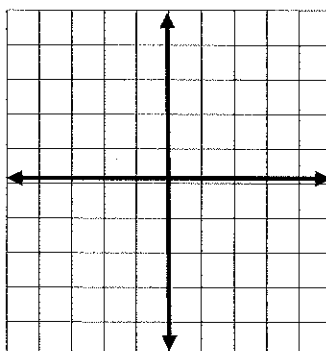


Graph the dilations in 9 and 10. Then describe the dilations and they differ.

9.  $f(x) = 2\lceil x \rceil$

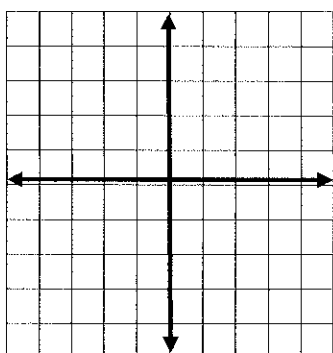


10.  $g(x) = \lceil 2x \rceil$

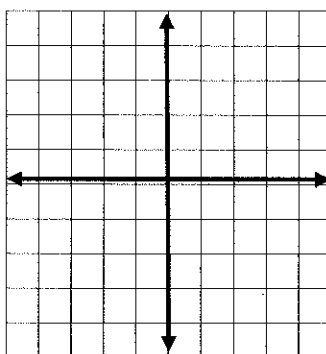


Graph the reflections in 11 and 12. Then describe the reflection and they differ

11.  $f(x) = -\lceil x \rceil$



12.  $g(x) = \lceil -x \rceil$

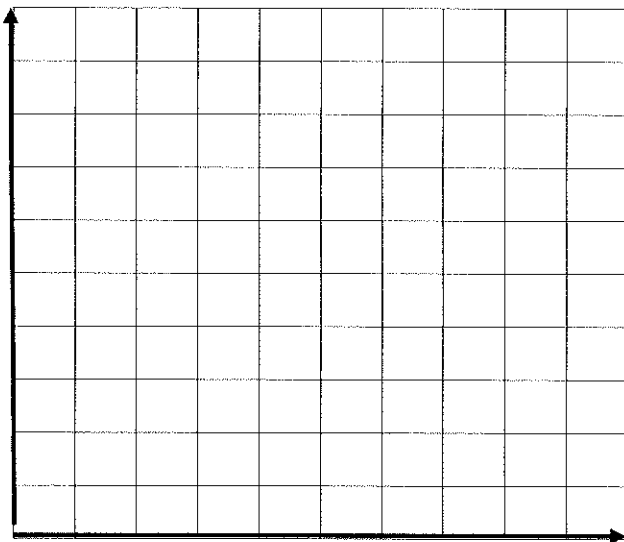


**Real World Application of Step Functions:**

Prior to September, 2000, taxi fares from Washington DC to Maryland were as follows:  
\$2.00 for up to and including the first  $\frac{1}{2}$  mile, + \$0.50 for each additional  $\frac{1}{2}$  mile increment.

Describe the independent and dependent variables and explain your choices.

Graph the fares for the first 2 miles: *(Make sure to label the axes.)*



Explain why this is a step function.

How is it different from the greatest integer parent function  $f(x) = \lfloor x \rfloor$

Write the function that is modeled by this graph.

Preview for tomorrow: Write the piecewise function for 0 to 2 miles.

$$f(x) = \begin{cases} \$2.00 & \text{if } 0 \leq x \leq 0.5 \\ \$2.50 & \text{if } 0.5 < x \leq 1.0 \\ \$3.00 & \text{if } 1.0 < x \leq 1.5 \\ \$3.50 & \text{if } 1.5 < x \leq 2.0 \end{cases}$$