Section 3-10: Implicit Differentiation

For problems 1-3 do each of the following.

- (a) Find y' by solving the equation for y and differentiating directly.
- **(b)** Find y' by implicit differentiation.
- (c) Check that the derivatives in (a) and (b) are the same.

1.
$$\frac{x}{v^3} = 1$$

2.
$$x^2 + y^3 = 4$$

3.
$$x^2 + y^2 = 2$$

For problems 4-9 find y' by implicit differentiation.

4.
$$2y^3 + 4x^2 - y = x^6$$

5.
$$7y^2 + \sin(3x) = 12 - y^4$$

6.
$$e^x - \sin(y) = x$$

7.
$$4x^2y^7 - 2x = x^5 + 4y^3$$

8.
$$\cos(x^2 + 2y) + xe^{y^2} = 1$$

9.
$$\tan(x^2y^4) = 3x + y^2$$

For problems 10 & 11 find the equation of the tangent line at the given point.

10.
$$x^4 + y^2 = 3$$
 at $(1, -\sqrt{2})$.

11.
$$y^2 e^{2x} = 3y + x^2$$
 at $(0,3)$.

For problems 12 & 13 assume that x = x(t), y = y(t) and z = z(t) and differentiate the given equation with respect to t.

12.
$$x^2 - y^3 + z^4 = 1$$

13.
$$x^2 \cos(y) = \sin(y^3 + 4z)$$