Differentiation - Logs and Exponentials

Differentiate each function with respect to x.

1)
$$y = 4^{4x^4}$$

2)
$$y = 4^{-5x^3}$$

$$3) \quad y = \log_3 3x^2$$

4)
$$y = \log_2 4x^2$$

5)
$$y = \log_3 (3x^5 + 5)^5$$

6)
$$y = \log_5 (-5x^3 - 2)^3$$

7)
$$y = (4^{x^3} + 2)^3$$

8)
$$y = 3^{(x^4 + 1)^3}$$

9)
$$y = 3^{\cos 3x^4}$$

$$10) \ \ y = \log_5 \tan 4x^4$$

Differentiation - Logs and Exponentials

Differentiate each function with respect to x.

1)
$$y = 4^{4x^4}$$

$$\frac{dy}{dx} = 4^{4x^4} \ln 4 \cdot 16x^3$$

$$= x^3 \cdot 4^{4x^4 + 2} \ln 4$$

3)
$$y = \log_3 3x^2$$

$$\frac{dy}{dx} = \frac{1}{3x^2 \ln 3} \cdot 6x$$

$$= \frac{2}{x \ln 3}$$

5)
$$y = \log_3 (3x^5 + 5)^5$$

$$\frac{dy}{dx} = \frac{1}{(3x^5 + 5)^5 \ln 3} \cdot 5(3x^5 + 5)^4 \cdot 15x^4$$

$$= \frac{75x^4}{\ln 3 \cdot (3x^5 + 5)}$$

7)
$$y = (4^{x^3} + 2)^3$$

$$\frac{dy}{dx} = 3(4^{x^3} + 2)^2 \cdot 4^{x^3} \ln 4 \cdot 3x^2$$

$$= 9x^2(4^{x^3} + 2)^2 \cdot 4^{x^3} \ln 4$$

9)
$$y = 3^{\cos 3x^4}$$

$$\frac{dy}{dx} = 3^{\cos 3x^4} \ln 3 \cdot -1\sin 3x^4 \cdot 12x^3$$

$$= -4x^3 \cdot 3^{\cos 3x^4 + 1} \sin 3x^4 \cdot \ln 3$$

2)
$$y = 4^{-5x^3}$$

$$\frac{dy}{dx} = 4^{-5x^3} \ln 4 \cdot -15x^2$$

$$= -\frac{15x^2 \ln 4}{4^{5x^3}}$$

4)
$$y = \log_2 4x^2$$

$$\frac{dy}{dx} = \frac{1}{4x^2 \ln 2} \cdot 8x$$

$$= \frac{2}{x \ln 2}$$

6)
$$y = \log_5 (-5x^3 - 2)^3$$

$$\frac{dy}{dx} = \frac{1}{(-5x^3 - 2)^3 \ln 5} \cdot 3(-5x^3 - 2)^2 \cdot -15x^2$$

$$= -\frac{45x^2}{\ln 5 \cdot (-5x^3 - 2)}$$

8)
$$y = 3^{(x^4 + 1)^3}$$

$$\frac{dy}{dx} = 3^{(x^4 + 1)^3} \ln 3 \cdot 3(x^4 + 1)^2 \cdot 4x^3$$

$$= 4x^3 \cdot 3^{(x^4 + 1)^3 + 1} \cdot (x^4 + 1)^2 \ln 3$$

10)
$$y = \log_5 \tan 4x^4$$

$$\frac{dy}{dx} = \frac{1}{\tan 4x^4 \cdot \ln 5} \cdot \sec^2 4x^4 \cdot 16x^3$$

$$= \frac{16x^3 \cdot \sec^2 4x^4}{\tan 4x^4 \cdot \ln 5}$$