

YES Calculator is permitted. Show your work and box your answers when appropriate. ROUNDING RULES: Round money to the nearest penny. Round Bacteria to nearest whole. Round any rate to the at least three decimal places. Do not round in the middle of a problem, only at the end of the problem. Provide exact values when requested.

1. Find the amount that results when \$1500 is invested at 8% compounded monthly after a period of 14 years.	2. Find the amount that results when \$375 is invested at 4% compounded continuously after a period of 3 years.
3. Find the principal needed now (present value) to get \$13,000 after 5 years at 9% compounded quarterly.	4. Find the effective interest rate of interest for 8.5% compounded continuously.
5. How long does it take for an investment to double in value if it is invested at 3% compounded monthly?	6. How many years will it take for an initial investment of \$25,000 to grow to \$80,000? Assume a rate of 7% interest compounded continuously.
<p>7. A skillet is removed from an oven whose temperature is 450° and placed in a room whose temperature is 70°. After 5 minutes, the temperature of the skillet is 400°.</p> <p>a. Write a formula to model the temperature of the skillet after t seconds. Use an exact value for k.</p> <p>b. How long will it be until the skillet is 150°?</p>	<p>8. A culture of bacteria obeys the laws of uninhibited growth.</p> <p>a. Write a formula if 600 bacteria are present initially, and there are 790 after 1 hour.</p> <p>b. How many bacteria will be present after 12 hours?</p>

<p>9. A colony of bacteria grows according to the law of uninhibited growth where $N(t) = 100e^{0.054t}$ Where N is measured in grams and t is measured in days.</p> <p>a. Determine the initial amount of bacteria</p> <p>b. What is the growth rate of the bacteria?</p> <p>c. What is the population after 5 days?</p> <p>d. How long will it take for the population to reach 140 grams?</p>	<p>10. A piece of charcoal is found to contain 25% of the carbon 14 that it originally had. When did the tree from which the charcoal came from die? Remember the half-life of Carbon 14 is about 5600 years. (Do not round any value until the end!)</p>
<p>11. The normal healing of wounds can be modeled by an exponential function. If A_0 represents the original area of the wound and if A equals the area of the wound, then the function $A(n) = A_0e^{-0.35n}$ describes the area of a wound after n days following an injury when no infection is present to slow healing. Suppose a wound is initially 80 square millimeters.</p> <p>a. After how many days will the wound be half its original size?</p> <p>b. How long before the wound is 10% of its original size.</p>	
<p>12. Solve. You do not have to show work if calculator is your method.</p> $\log_2 x + \log_4 x = \log_3(2 - x)$	<p>13. Solve. Round answer to three decimal places</p> $e^x - \ln 5 = 2 - x^2$
<p>14. State the domain $y = \log_5(x^2 - 2x - 15)$</p>	<p>15. $f(x) = \log_7(7 - x)$</p> <p>a. Solve $f(x) = 0$</p> <p>b. Evaluate $f(0)$</p>

11/26/2018

Honors Precalculus Applications of Logarithms & Exponential Functions Name

KEY 2018

YES Calculator is permitted. Show your work and box your answers when appropriate. ROUNDING RULES: Round money to the nearest penny. Round Bacteria to nearest whole. Round any rate to the at least three decimal places. Do not round in the middle of a problem, only at the end of the problem. Provide exact values when requested.

<p>1. Find the amount that results when \$1500 is invested at 8% compounded monthly after a period of 14 years.</p> $1500 \left(1 + \frac{.08}{12}\right)^{168}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">\$ 4580.23</div>	<p>2. Find the amount that results when \$375 is invested at 4% compounded continuously after a period of 3 years.</p> $375 e^{(.04 \cdot 3)}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">\$ 422.81</div>
<p>3. Find the principal needed now (present value) to get \$13,000 after 5 years at 9% compounded quarterly.</p> $13,000 = P \left(1 + \frac{.09}{4}\right)^{20}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">\$ 8330.61</div>	<p>4. Find the effective interest rate of interest for 8.5% compounded continuously.</p> $r = 1 - e^{-.085}$ $= 1 - e^{-.085}$ $.088717067$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">8.871%</div>
<p>5. How long does it take for an investment to double in value if it is invested at 3% compounded monthly?</p> $2 = \left(1 + \frac{.03}{12}\right)^{12t}$ $\ln 2 = 12t \ln \left(1 + \frac{.03}{12}\right)$ $t \approx 23.133773$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">About 23.134 years</div>	<p>6. How many years will it take for an initial investment of \$25,000 to grow to \$80,000? Assume a rate of 7% interest compounded continuously.</p> $80,000 = 25000 e^{.07t}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">About 16.616 years</div>
<p>7. A skillet is removed from an oven whose temperature is 450° and placed in a room whose temperature is 70°. After 5 minutes, the temperature of the skillet is 400°.</p> $T(t) = T_s + (T_0 - T_s)e^{-kt}$ <p>a. Write a formula to model the temperature of the skillet after t seconds. Use an exact value for k.</p> $T(t) = 70 + (450 - 70)e^{-kt}$ $T(t) = 70 + 380e^{-kt} \quad \text{use } (5, 400)$ $400 = 70 + 380e^{-5k}$ $\ln\left(\frac{33}{38}\right) = -5k$ $k = \frac{\ln\left(\frac{33}{38}\right)}{-5}$ $T(t) = 70 + 380e^{+.2 \ln\left(\frac{33}{38}\right)t}$ <p>b. How long will it be until the skillet is 150°?</p> $150 = 70 + 380e^{+.2 \ln\left(\frac{33}{38}\right)t}$ $\ln\left(\frac{4}{19}\right) = +.2 \ln\left(\frac{33}{38}\right)t$ 55.22257 <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">About 55.223 minutes</div>	<p>8. A culture of bacteria obeys the laws of <u>uninhibited</u> growth.</p> <p>a. Write a formula if 600 bacteria are present initially, and there are 790 after 1 hour.</p> $A = A_0 e^{rt}$ $790 = 600 e^r$ $\frac{790}{600} = e^r$ $r = \ln\left(\frac{79}{60}\right)$ $A = 600 e^{\ln\left(\frac{79}{60}\right)t}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">\$ A = 600 e^{\ln\left(\frac{79}{60}\right)t} <p>b. How many bacteria will be present after 12 hours?</p> 16287.75925 <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;">About 16288 bacteria</div> </div>

9. A colony of bacteria grows according to the law of uninhibited growth where $N(t) = 100e^{0.054t}$ Where N is measured in grams and t is measured in days.

a. Determine the initial amount of bacteria

100 Bacteria

b. What is the growth rate of the bacteria?

5.4%

c. What is the population after 5 days?

130.9964 About 131 Bacteria

d. How long will it take for the population to reach 140 grams?

$$\frac{140}{100} = e^{0.054t}$$

$$t \approx 6.230967$$

About 6 to 7 days
6.231 days

10. A piece of charcoal is found to contain 25% of the carbon 14 that it originally had. When did the tree from which the charcoal came from die? Remember the half-life of Carbon 14 is about 5600 years. (Do not round any value until the end!)

$$.25 = e^{\frac{\ln(1/2)}{5600}K}$$

$$\ln(.25) = \frac{\ln(1/2)}{5600}K$$

About 11,200 years

$$\begin{aligned} \frac{1}{2} &= e^{K \cdot 5600} \\ \ln\left(\frac{1}{2}\right) &= 5600K \\ K &\approx \frac{\ln(1/2)}{5600} \\ K &\approx -0.000123776 \dots \end{aligned}$$

11. The normal healing of wounds can be modeled by an exponential function. If A_0 represents the original area of the wound and if A equals the area of the wound, then the function $A(n) = A_0e^{-0.35n}$ describes the area of a wound after n days following an injury when no infection is present to slow healing. Suppose a wound is initially 80 square millimeters.

a. After how many days will the wound be half its original size?

$$0.5 = e^{-0.35n}$$

$$n \approx 1.98042$$

About 1.980 or 2 days

b. How long before the wound is 10% of its original size.

$$0.10 = e^{-0.35n}$$

$$\ln(.1) = -0.35n$$

$$n \approx 6.5788$$

About 6.579 days or 7 days

12. Solve. You do not have to show work if calculator is your method.

$$\log_2 x + \log_4 x = \log_3(2-x)$$

$$\text{In calculator}$$

$$Y_1 = \frac{\ln x}{\ln 2} + \frac{\ln x}{\ln 4}$$

$$Y_2 = \frac{\ln(2-x)}{\ln 3}$$

X=1

X=1

13. Solve. Round answer to three decimal places

$$e^x - \ln 5 = 2 - x^2 \quad \text{use calculator}$$

$$Y_1 = e^x - \ln 5$$

$$Y_2 = 2 - x^2$$

$$x \approx -1.858$$

$$\text{or}$$

$$x \approx 0.977$$

14. State the domain $y = \log_5(x^2 - 2x - 15)$

$$x^2 - 2x - 15 > 0$$

$$(x-5)(x+3) > 0$$

$$\begin{array}{c} -3 \quad 5 \\ + \quad | \quad | \quad + \\ + \quad - \quad + \end{array}$$

$(-\infty, -3) \cup (5, \infty)$

15. $f(x) = \log_7(7-x)$

$$7^0 = 7-x$$

a. Solve $f(x) = 0$

$$0 = \log_7(7-x)$$

$$1 = 7-x$$

$$x = 6$$

b. Evaluate $f(0)$

$$\log_7(7-0)$$

$$\log_7 7 = 1$$