Parallel software

The burden is on software

- Hardware and compilers can keep up the pace needed.

- From now on…
  - In shared memory programs:
    - Start a single process and fork threads.
    - Threads carry out tasks.
  - In distributed memory programs:
    - Start multiple processes.
    - Processes carry out tasks.

SPMD – single program multiple data

- A SPMD programs consists of a single executable that can behave as if it were multiple different programs through the use of conditional branches.

```
if (I'm thread process i)
    do this;
else
    do that;
```

Writing Parallel Programs

1. Divide the work among the processes/threads
   (a) so each process/thread gets roughly the same amount of work
   (b) and communication is minimized.
2. Arrange for the processes/threads to synchronize.
3. Arrange for communication among processes/threads.

```
double x[n], y[n];
…
for (i = 0; i < n; i++)
    x[i] += y[i];
```

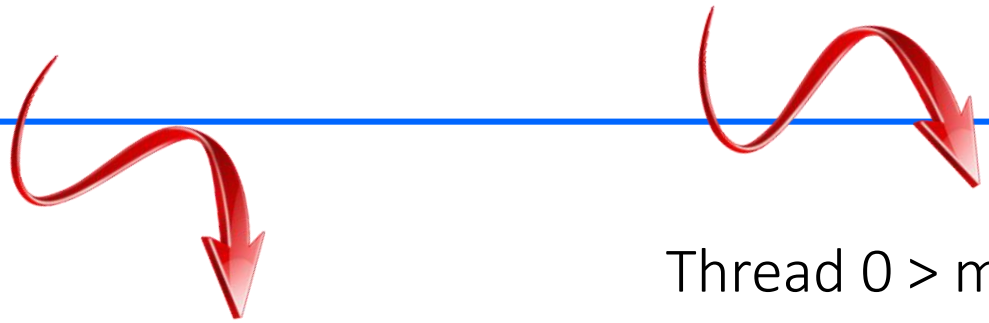
Shared Memory

- **Dynamic threads**
  - Master thread waits for work, forks new threads, and when threads are done, they terminate
  - Efficient use of resources, but thread creation and termination is time consuming.

- **Static threads**
  - Pool of threads are created and allocated work, but do not terminate until cleanup.
  - Better performance, but potential waste of system resources.

Nondeterminism

```
. . .
printf ( "Thread %d > my_val = %d\n" ,
         my_rank , my_x ) ;
. . .
```



Thread 0 > my_val = 7

Thread 1 > my_val = 19

Thread 1 > my_val = 19

Thread 0 > my_val = 7

Nondeterminism

my_val = Compute_val (my_rank) ;

x += my_val ;

Time	Core 0	Core 1
0	Finish assignment to `my_val`	In call to `Compute_val`
1	Load `x = 0` into register	Finish assignment to `my_val`
2	Load `my_val = 7` into register	Load `x = 0` into register
3	Add `my_val = 7` to `x`	Load `my_val = 19` into register
4	Store `x = 7`	Add `my_val` to `x`
5	Start other work	Store `x = 19`

Nondeterminism

- Race condition
- Critical section
- Mutually exclusive
- Mutual exclusion lock (mutex, or simply lock)

```
my_val = Compute_val ( my_rank ) ;
Lock(&add_my_val_lock ) ;
x += my_val ;
Unlock(&add_my_val_lock ) ;
```

busy-waiting

```
my_val = Compute_val ( my_rank ) ;
if ( my_rank == 1)
    while ( ! ok_for_1 ) ;  /* Busy−wait loop */
x += my_val ;  /* Critical section */
if ( my_rank == 0)
    ok_for_1 = true ;  /* Let thread 1 update x */
```

message-passing

```
char message [ 1 0 0 ] ;
. . .
my_rank = Get_rank ( ) ;
if ( my_rank == 1) {
    printf ( message , "Greetings from process 1" ) ;
    Send ( message , MSG_CHAR , 100 , 0 ) ;
} elseif ( my_rank == 0) {
    Receive ( message , MSG_CHAR , 100 , 1 ) ;
    printf ( "Process 0 > Received: %s\n" , message ) ;
}
```

Partitioned Global Address Space Languages

```
shared int n = . . . ;
shared double x [ n ] , y [ n ] ;
private int i , my_first_element , my_last_element ;
my_first_element = . . . ;
my_last_element = . . . ;
/ * Initialize x and y  */
. . .
f o r ( i = my_first_element ; i <= my_last_element ; i++)
    x [ i ] += y [ i ] ;
```

Input and Output

- In distributed memory programs, only process 0 will access *stdin*.
- In shared memory programs, only the master thread or thread 0 will access *stdin*.
- In both distributed memory and shared memory programs all the processes/threads can access *stdout* and *stderr*.

Input and Output

- In most cases only a single process/thread will be used for all output to *stdout* other than debugging output.
  - because of the indeterminacy of the order of output to *stdout*

- Debug output should always include the rank or id of the process/thread that's generating the output.

Input and Output

- Only a single process/thread will attempt to access any single file other than stdin, stdout, or stderr.
  - E.g., each process/thread can open its own, private file for reading or writing,

- But no two processes/threads will open the same file.

Performance

Speedup

- Number of cores = p
- Serial run-time = T_{serial}
- Parallel run-time = $T_{parallel}$

linear speedup

$$T_{parallel} = T_{serial} / p$$

Speedup of a parallel program

$$S = \frac{T_{serial}}{T_{parallel}}$$

Efficiency of a parallel program

$$E = \frac{S}{p} = \frac{\left(\frac{T_{serial}}{T_{parallel}}\right)}{p} = \frac{T_{serial}}{p \cdot T_{parallel}}$$

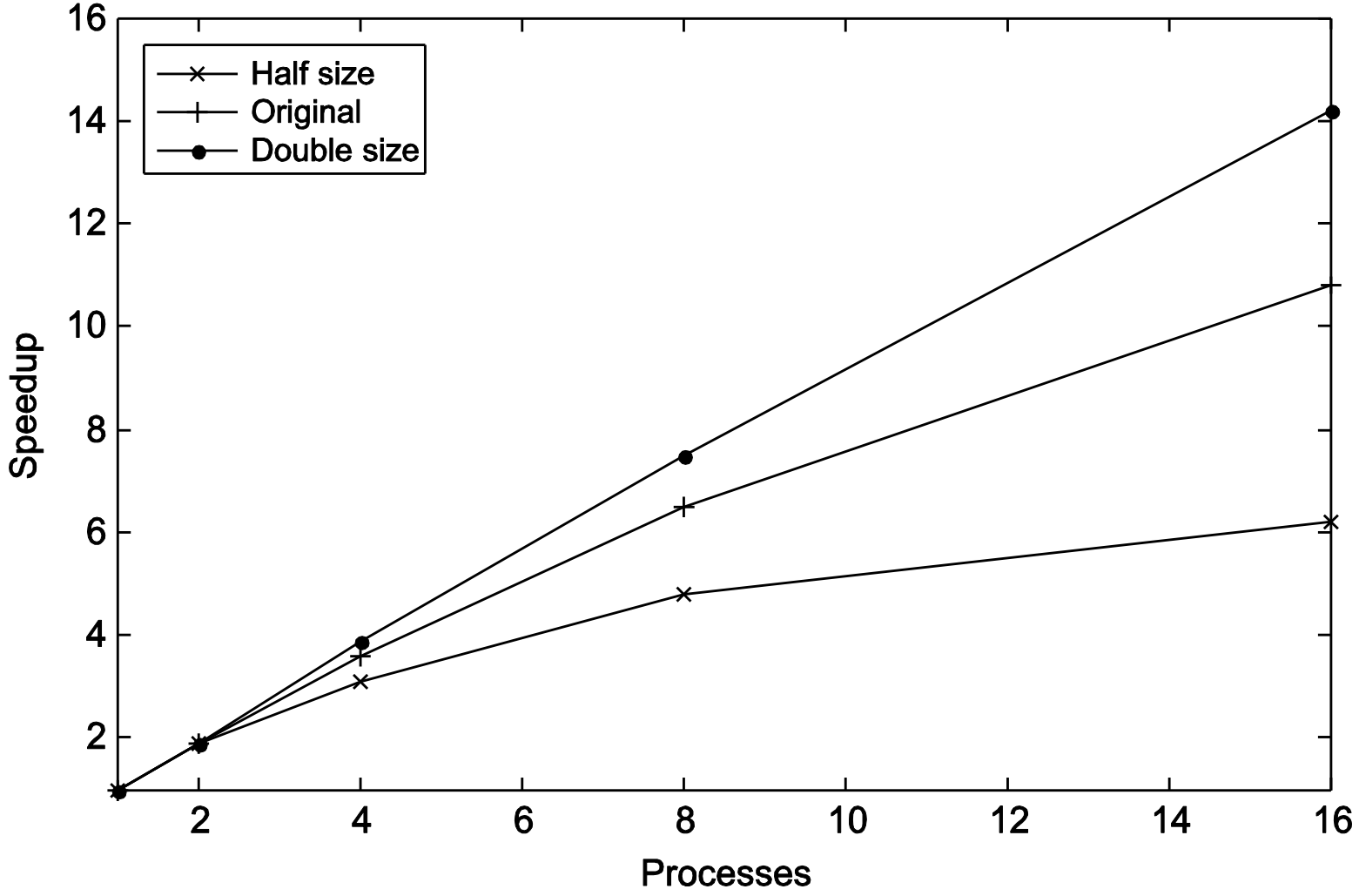
Speedups and efficiencies of a parallel program

p	1	2	4	8	16
S	1.0	1.9	3.6	6.5	10.8
$E = S/p$	1.0	0.95	0.90	0.81	0.68

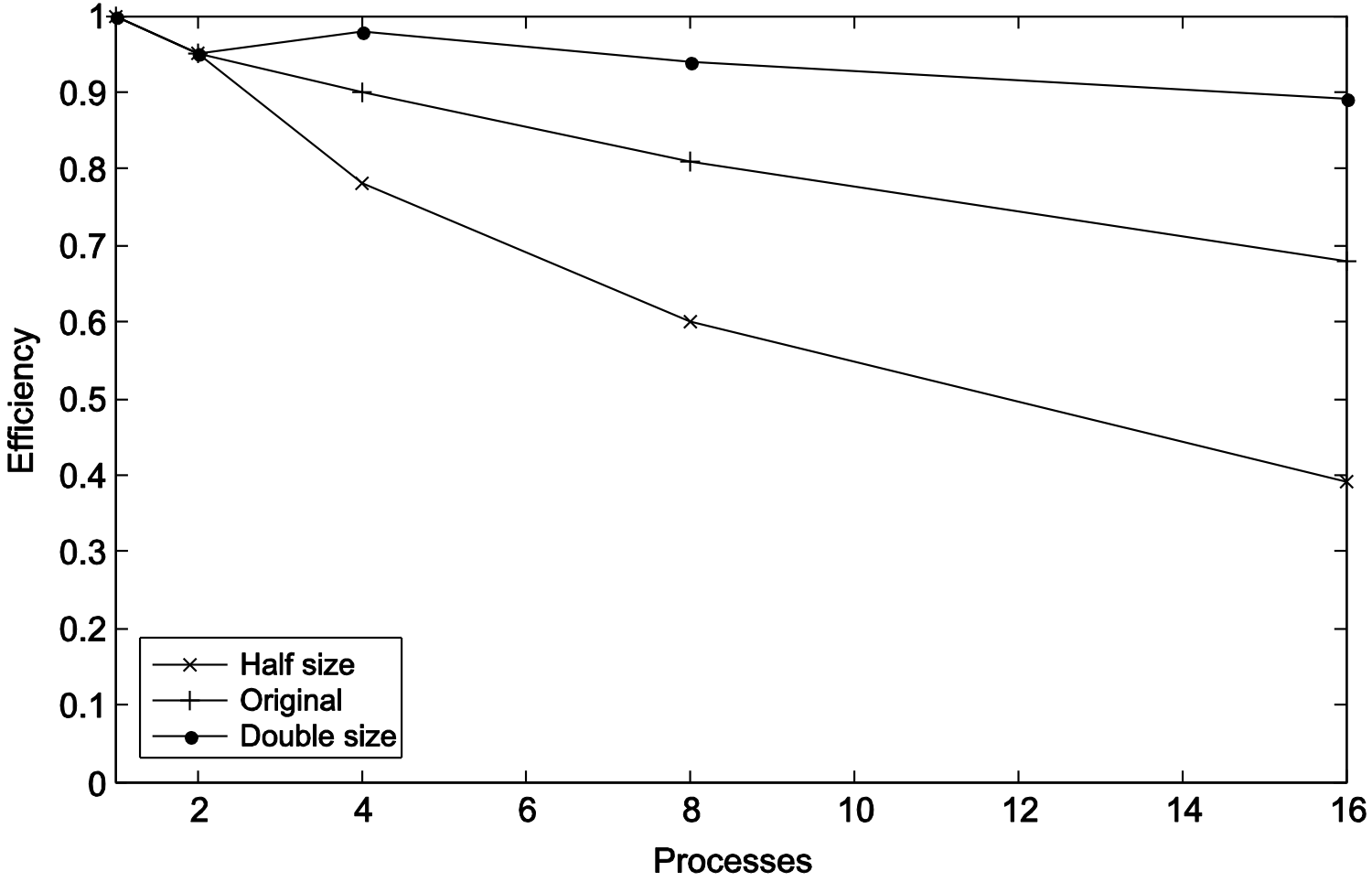
Speedups and efficiencies of parallel program on different problem sizes

	p	1	2	4	8	16
Half	S	1.0	1.9	3.1	4.8	6.2
	E	1.0	0.95	0.78	0.60	0.39
Original	S	1.0	1.9	3.6	6.5	10.8
	E	1.0	0.95	0.90	0.81	0.68
Double	S	1.0	1.9	3.9	7.5	14.2
	E	1.0	0.95	0.98	0.94	0.89

Speedup


Half size
Original
Double size
Speedup
Processes
16
14
12
10
8
6
4
2
2
4
6
8
10
12
14
16

Efficiency


Efficiency
Processes
Half size
Original
Double size
0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0.8
0.9
1
2
4
6
8
10
12
14
16

Effect of overhead

$$T_{parallel} = T_{serial} / p + T_{overhead}$$

Amdahl's Law

- Unless virtually all of a serial program is parallelized, the possible speedup is going to be very limited

  — regardless of the number of cores available.

Example

- We can parallelize 90% of a serial program.
- Parallelization is "perfect" regardless of the number of cores *p* we use.
- T_{serial} = 20 seconds
- Runtime of parallelizable part is

$$0.9 \times T_{serial} / p = 18 / p$$

Example (cont.)

- Runtime of "unparallelizable" part is

$$0.1 \times T_{serial} = 2$$

- Overall parallel run-time is

$$T_{parallel} = 0.9 \times T_{serial} / p + 0.1 \times T_{serial} = 18 / p + 2$$

Example (cont.)

- Speed up

$$S = \frac{T_{serial}}{0.9 \times T_{serial} / p + 0.1 \times T_{serial}} = \frac{20}{18 / p + 2}$$

Scalability

- In general, a problem is *scalable* if it can handle ever increasing problem sizes.

- If we increase the number of processes/threads and keep the efficiency fixed without increasing problem size, the problem is *strongly scalable*.

- If we keep the efficiency fixed by increasing the problem size at the same rate as we increase the number of processes/threads, the problem is *weakly scalable*.

强可扩展性（Strongly Scalable）

- **定义**：在**问题规模（即任务大小）固定**的情况下，通过增加计算资源（如处理器数量）来**缩短计算时间**。
- **目标**：提高计算速度，使任务更快完成。
- **关键点**：**问题规模不变，资源增加，计算时间减少**。
- **理想情况**：资源增加一倍，计算时间减半（线性加速）。

- **例子**：假设你需要对一个固定大小的矩阵（例如1000x1000）进行矩阵乘法运算：
  - 使用 **1 个处理器**，计算时间为 100 秒。
  - 使用 **2 个处理器**，计算时间减少到 50 秒。
  - 使用 **4 个处理器**，计算时间减少到 25 秒。

弱可扩展性（Weakly Scalable）

- **定义**：在**增加计算资源的同时，问题规模也按比例增加**，目标是保持每个处理器的负载不变，**计算时间基本稳定**。
- **目标**：在资源增加的情况下，能够处理更大规模的问题，同时保持效率。
- **关键点**：**问题规模与资源同步增加，计算时间不变**。
- **理想情况**：资源增加一倍，问题规模也增加一倍，计算时间保持不变

- **例子**：假设你需要对一个矩阵进行乘法运算（对于方阵n×n，运算量为n^3次乘法），但矩阵的大小会随着处理器数量的增加而增加：
  - 使用 **1 个处理器**，计算一个 100x100 的矩阵，时间为 10 秒。
  - 使用 **8 个处理器**，计算一个 200x200 的矩阵，时间仍为 10 秒。
  - 使用**64个处理器**，计算一个 400x400 的矩阵，时间仍为 10 秒。

区别总结

特性	强可扩展性	弱可扩展性
问题规模	固定	随资源增加而增加
资源增加	资源增加，问题规模不变	资源增加，问题规模同步增加
目标	缩短计算时间	处理更大规模的问题，保持计算时间稳定
适用场景	计算密集型任务（如固定规模的科学计算）	数据密集型任务（如大数据处理）

- **强可扩展性**关注的是在固定问题规模下，通过增加资源来加速计算。
- **弱可扩展性**关注的是在资源增加的同时，能够处理更大规模的问题，同时保持计算效率。

Taking Timings

- What is time?
- Start to finish?
- A program segment of interest?
- CPU time?
- Wall clock time?

Taking Timings

```
double start, finish;
. . .
start = Get_current_time();
/* Code that we want to time */
. . .
finish = Get_current_time();
printf("The elapsed time = %e seconds\n", finish-start);
```

theoretical function

MPI_Wtime

omp_get_wtime

Taking Timings

```
private double start, finish;
. . .
start = Get_current_time();
/* Code that we want to time */
. . .
finish = Get_current_time();
printf("The elapsed time = %e seconds\n", finish-start);
```

Taking Timings

```
shared double global_elapsed;
private double my_start, my_finish, my_elapsed;
. . .
/* Synchronize all processes/threads */
Barrier();
my_start = Get_current_time();

/* Code that we want to time */
. . .

my_finish = Get_current_time();
my_elapsed = my_finish - my_start;

/* Find the max across all processes/threads */
global_elapsed = Global_max(my_elapsed);
if (my_rank == 0)
   printf("The elapsed time = %e seconds\n", global_elapsed);
```

Parallel program design

Foster's methodology

1. Partitioning: divide the computation to be performed and the data operated on by the computation into small tasks.

   The focus here should be on identifying tasks that can be executed in parallel.

Foster's methodology

2. Communication: determine what communication needs to be carried out among the tasks identified in the previous step.

Foster's methodology

3. Agglomeration or aggregation: combine tasks and communications identified in the first step into larger tasks.

   For example, if task A must be executed before task B can be executed, it may make sense to aggregate them into a single composite task.

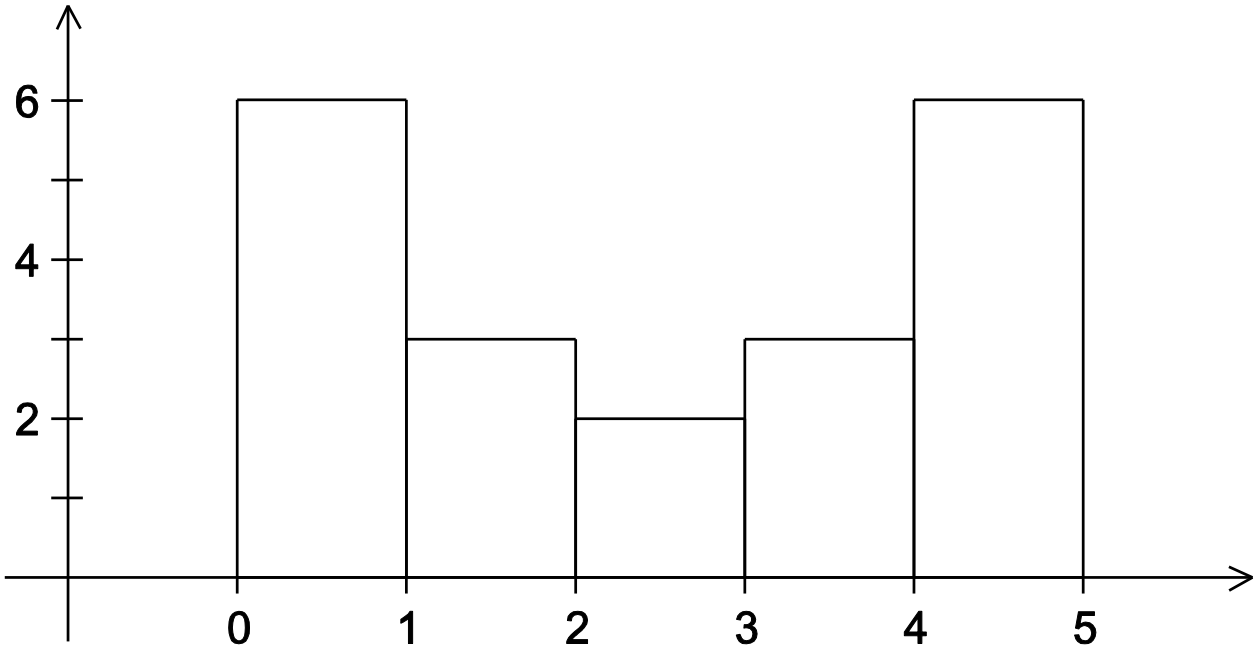
Foster's methodology

4. Mapping: assign the composite tasks identified in the previous step to processes/threads.

   This should be done so that communication is minimized, and each process/thread gets roughly the same amount of work.

Example - histogram

- 1.3,2.9,0.4,0.3,1.3,4.4,1.7,0.4,3.2,0.3,4.9,2.4,3.1,4.4,3.9,0.4,4.2,4.5,4.9,0.9



Serial program - input

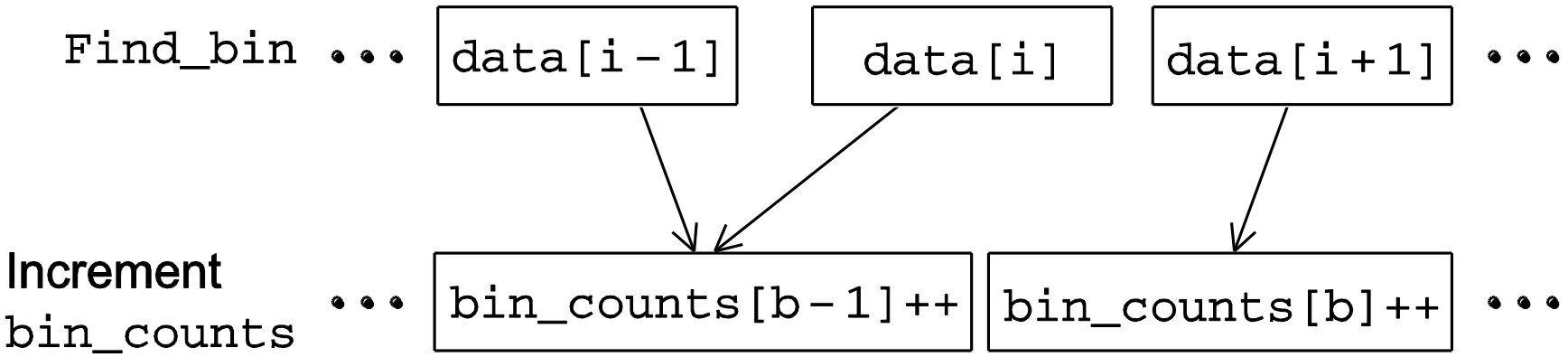
1. The number of measurements: data_count
2. An array of data_count floats: data
3. The minimum value for the bin containing the smallest values: min_meas
4. The maximum value for the bin containing the largest values: max_meas
5. The number of bins: bin_count

Serial program - output

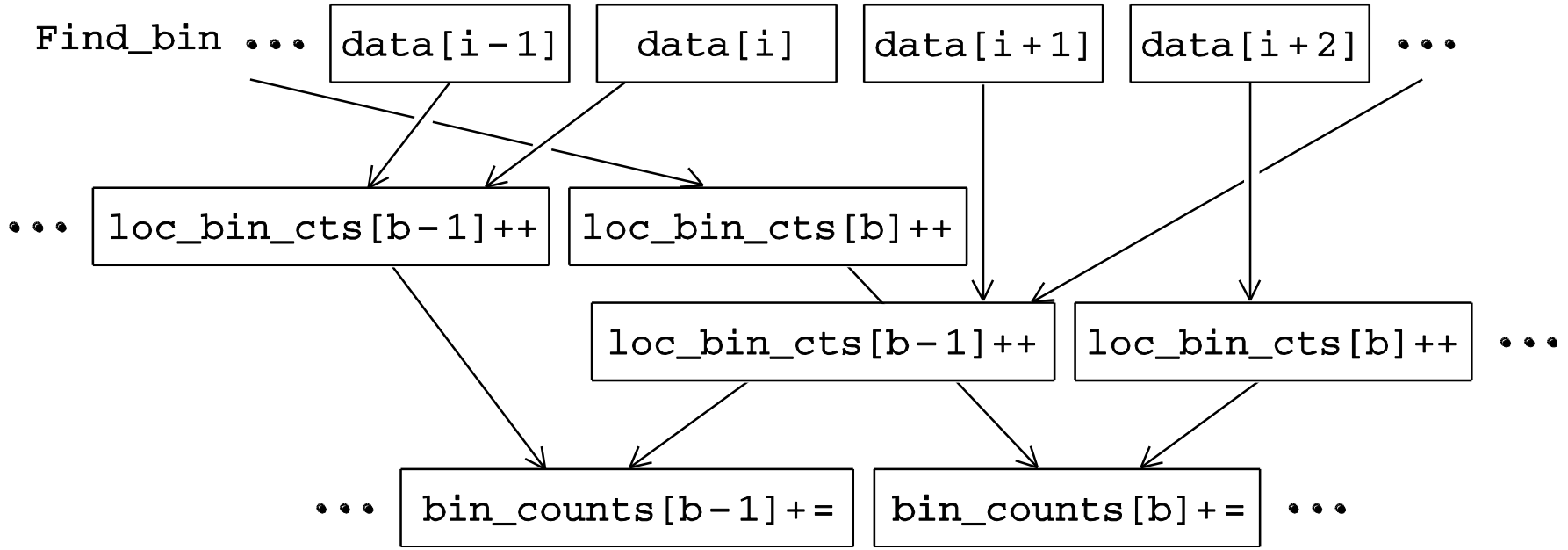
1. bin_maxes : an array of bin_count floats

2. bin_counts : an array of bin_count ints

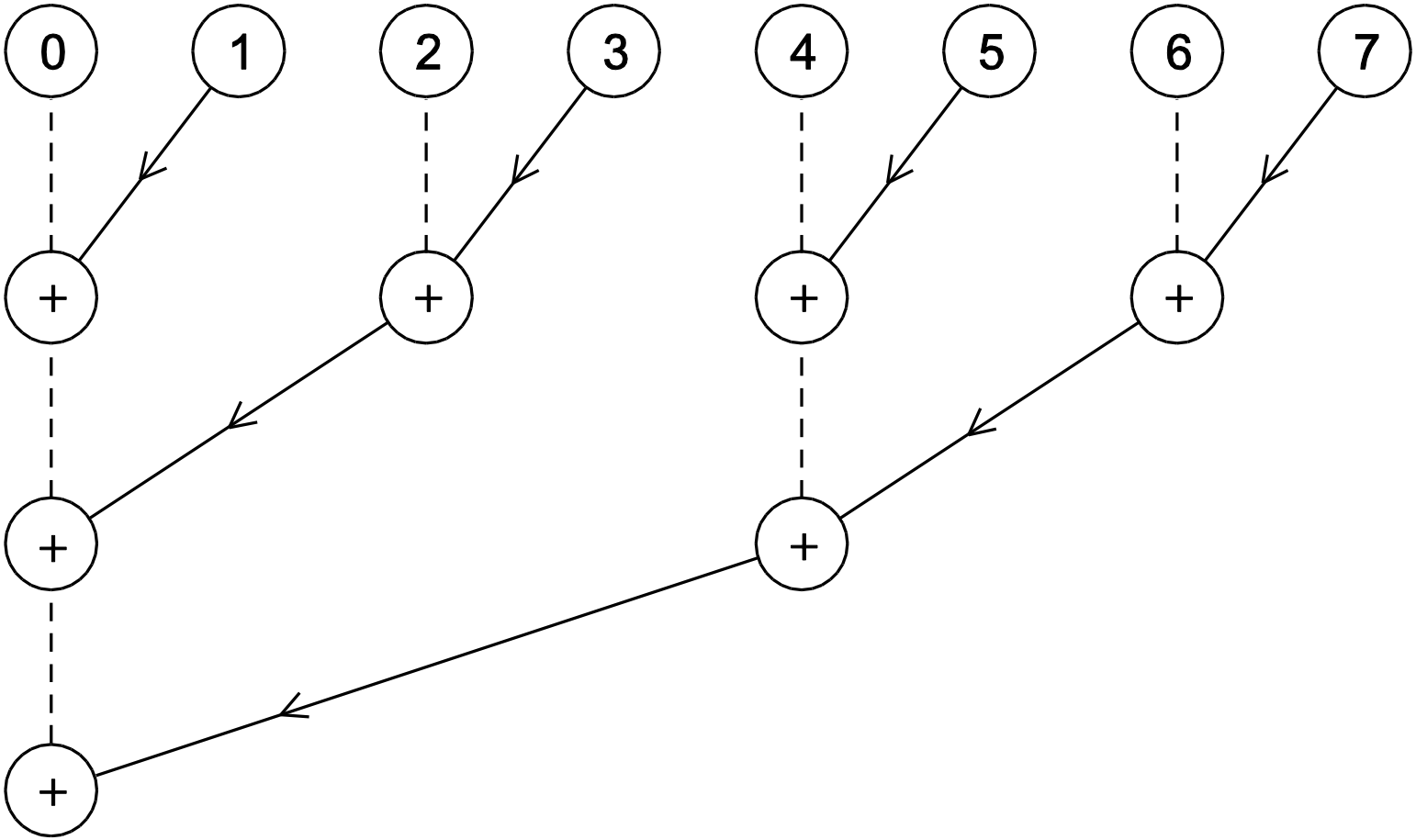
First two stages of Foster's Methodology



Alternative definition of tasks and communication



Adding the local arrays



Concluding Remarks (1)

- Serial systems
  - The standard model of computer hardware has been the von Neumann architecture.
- Parallel hardware
  - Flynn's taxonomy.
- Parallel software
  - We focus on software for homogeneous MIMD systems, consisting of a single program that obtains parallelism by branching.
  - SPMD programs.

Concluding Remarks (2)

- Input and Output
  - We'll write programs in which one process or thread can access stdin, and all processes can access stdout and stderr.
  - However, because of nondeterminism, except for debug output we'll usually have a single process or thread accessing stdout.

Concluding Remarks (3)

- Performance
  - Speedup
  - Efficiency
  - Amdahl's law
  - Scalability
- Parallel Program Design
  - Foster's methodology