

- 1) Consider the relation $R(A, B, C, D)$ having the Functional Dependencies: $\{BCD \rightarrow A, A \rightarrow D\}$. Prove your answer to these questions.

- a. Possible minimal keys for R :

$\{BCD\}, \{BCA\}$

There is no way to get BC other than starting with them so it must be in both keys. If you add D , you can use $BCD \rightarrow A$ to get A .

Back to the base of BC , if you add A , you can use $A \rightarrow D$ to get D .

- b. Currently, what is the normal form of R ?

Not 3NF because $A \rightarrow D$ is not a superkey. It is 2NF.

- c. Preserving dependencies, show how to transform R into BCNF if it is not already in BCNF.

It is not BCNF because $A \rightarrow D$ is not a super key.

$R = \{A, B, C, D\}$

Start

$R = \{(A, B, C), (A, D)\}$

$A \rightarrow D$

$R_1 = ABC, R_2 = AD$

- 2) Consider the relation $S(A, B, C, D, E)$ having the Functional Dependencies: $\{AB \rightarrow C, DE \rightarrow C, B \rightarrow D\}$. State any BCNF violations. Then, decompose, as necessary, the relation into a collection of relations that are in BCNF.

Minimal key: $\{ABE\}$

$AB = \{A, B, C, D\} \rightarrow$ violation, not superkey

$DE = \{C, D, E\} \rightarrow$ violation, not superkey

$B = \{B, D\} \rightarrow$ violation, not superkey

$S = R \{A, B, C, D, E\}$

Start

$S = R \{(A, B, D, E), (A, B, C)\}$

$AB \rightarrow C$

$S = R \{(A, B, D, E), (A, B, C), (D, E, C)\}$

$DE \rightarrow C$

$S = R \{(A, B, E), (A, B, C), (D, E, C), (B, D)\}$

$B \rightarrow D$

$R_1 = ABE, R_2 = ABC, R_3 = DEC, R_4 = BD$

3) Consider the relation T (A,B,C,D,E,F)having the Functional Dependencies:
 $\{E \rightarrow CF, CA \rightarrow B, BD \rightarrow E\}$. Prove your answers to these questions.

a. What are all the possible <minimal> keys for T?

Minimal keys: $\{A,D,B\}, \{A,D,C\}, \{A,D,E\}$

b. Is T in BCNF?

No none of the FDs are superkeys

c. Is T in 3NF?

No, for the same reason it is not BCNF, none of the FDs are superkeys.