The fibnum package

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Abstract

The package fibnum provides expandable fibonacci numbers for both LaTeX and plain TeX.

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1 Documentation

In the mailing list texhax Jan Abraham asked the question, how to get Fibonacci numbers in T_{EX} [1]:

Write a Macro in TeX that compute the function \mathbf{m} All fibonacci numbers from 1 to m (m < 40).

^{*}Please report any issues at https://github.com/ho-tex/oberdiek/issues

This packages provides an expandable implementation for the calculation of these numbers for a much larger set of indexes. For practical reasons the index is restricted to the same limitations that apply for TEX integer numbers. The range of the Fibonacci numbers, however, are not limited by the algorithm. They are only restricted to memory limitations, if they are hit.

The package is loaded as LATEX package in LATEX:

\usepackage{fibnum}

and as file in plain T_FX:

\input fibnum.sty

The package does not know any options and it provides the macros \fibnum and \fibnumPreCalc.

\fibnum $\{\langle index \rangle\}$

Macro \fibnum expects a TEX number as $\langle index \rangle$ in the official TEX number range from $-(2^{31}-1)$ up to $2^{31}-1$. In exact two expansion steps the macro expands to the Fibnoacci number $F_{\langle index \rangle}$. In case of a negative $\langle index \rangle$, the "negafibonacci" number [2] is used. Formally the Fibonacci number F_n with integer index n, $n \in \mathbb{Z}$ and $n \in [-2147483647, 2147483647]$ that is returned by macro \fibnum with numerical argument n is defined the following way:

$$F_n = \begin{cases} 0 & \text{for } n = 0\\ 1 & \text{for } n = 1\\ F_{n-1} + F_{n-2} & \text{for } n > 1\\ (-1)^{n+1} F_n & \text{for } n < 0 \end{cases}$$
 (1)

Examples:

```
\fibnum{-6}
fibnum{-5}
                   5
\int \int \int dx dx dx = -4
                \rightarrow -3
fibnum{-3}
fibnum\{-2\}
fibnum\{-1\}
\fibnum{0}
\fibnum{1}
fibnum{2}
\fibnum{3}
fibnum{4}
\fibnum{5}
                \rightarrow 5
\fibnum{6}
\fibnum{10}
\final {46}
                \rightarrow 1836311903
\final {100} \rightarrow 354224848179261915075
\verb| fibnum{200}| \ \to \ 280571172992510140037611932413038677189525
fibnum{1000} \rightarrow 434665576869374564356885276750406258025646
                    605173717804024817290895365554179490518904
                    038798400792551692959225930803226347752096
                    896232398733224711616429964409065331879382
                    98969649928516003704476137795166849228875
```

\fibnumPreCalc $\{\langle index \rangle\}$

The package already provides precalculated Fibonacci numbers up to index 46. That means that calculations are not necessary for Fibonacci numbers that fit into the range of TeX numbers. Because macro \fibnum is expandable, it cannot store calculated Fibonacci numbers for later use. Macro definitions are forbidden in expandable contexts. If larger Fibonacci numbers are used more than once, than the compilation time can be shortened by calculating and storing the Fibonacci numbers beforehand. The argument $\langle index \rangle$ is a TeX number and macro \fibnumPreCalc ensures that the Fibonacci numbers F_0 up to $F_{|\langle index \rangle|}$ that are not already known are calculated and stored in internal macros. Internally only non-negative Fibonacci numbers are stored. If $\langle index \rangle$ is negative, then the needed positive Fibonacci numbers are calculated and stored. Example:

```
\fibnumPreCalc{50} % calculates and stores the values for indexes 47..50. % (Values for 0..46 are already stored by the package.) \fibnum{49} % uses the stored value \fibnum{51} % only calculates F_{51} from stored values F_{49} and F_{50} \fibnumPreCalc{100} % calculates and stores the values for indexes 51..100 \fibnum{100} % uses the stored value for F_{100} \fibnum{-100} % uses the stored value for F_{100}
```

2 Implementation

2.1 Identification

```
1 (*package)
Reload check, especially if the package is not used with LATEX.
 2 \begingroup\catcode61\catcode48\catcode32=10\relax%
    \catcode13=5 % ^^M
     \endlinechar=13 %
    \catcode35=6 % #
    \catcode39=12 % '
    \catcode44=12 % ,
    \catcode45=12 % -
    \catcode46=12 % .
    \catcode58=12 % :
10
    \catcode64=11 % @
11
     \catcode123=1 % {
12
     \catcode125=2 % }
13
     \expandafter\let\expandafter\x\csname ver@fibnum.sty\endcsname
     \ifx\x\relax % plain-TeX, first loading
     \else
16
17
       \def\empty{}%
18
       \ifx\x\empty % LaTeX, first loading,
         % variable is initialized, but \ProvidesPackage not yet seen
19
20
         \expandafter\ifx\csname PackageInfo\endcsname\relax
21
22
           \def\x#1#2{%}
             \immediate\write-1{Package #1 Info: #2.}%
23
           }%
24
         \else
25
           \def\x#1#2{\PackageInfo{#1}{#2, stopped}}%
26
27
         \x{fibnum}{The package is already loaded}%
28
         \aftergroup\endinput
29
30
31
    \fi
32 \endgroup%
Package identification:
33 \begingroup\catcode61\catcode48\catcode32=10\relax%
     \catcode13=5 % ^^M
34
     \endlinechar=13 %
35
    \catcode35=6 % #
36
    \catcode39=12 % '
37
    \catcode40=12 % (
    \catcode41=12 % )
    \catcode44=12 % ,
40
     \catcode45=12 % -
41
     \colored{catcode46=12 \%} .
42
43
     \catcode47=12 % /
     \catcode58=12 % :
     \catcode64=11 % @
     \catcode91=12 % [
46
47
    \catcode93=12 % ]
48 \catcode123=1 % {
49 \catcode125=2 % }
```

```
\expandafter\ifx\csname ProvidesPackage\endcsname\relax
50
       \def\x#1#2#3[#4]{\endgroup}
51
52
         \immediate\write-1{Package: #3 #4}%
53
         \xdef#1{#4}%
       }%
54
     \else
55
       \def \x#1#2[#3] {\endgroup}
56
         #2[{#3}]%
57
         \ifx#1\@undefined
58
           \xdef#1{#3}%
59
         \fi
60
         \int x#1\relax
61
62
           \xdef#1{#3}%
         \fi
63
       }%
64
65
     \fi
66 \expandafter\x\csname ver@fibnum.sty\endcsname
67 \ProvidesPackage{fibnum}%
     [2016/05/16 v1.1 Fibonacci numbers (HO)]%
69 \begingroup\catcode61\catcode48\catcode32=10\relax%
     \color= 13=5 \% ^M
70
     \endlinechar=13 %
71
72
     \catcode123=1 % {
     \catcode125=2 % }
73
     \catcode64=11 % @
74
75
     \def\x{\endgroup
       \expandafter\edef\csname FibNum@AtEnd\endcsname{%
76
77
         \endlinechar=\the\endlinechar\relax
78
         \catcode13=\the\catcode13\relax
79
         \catcode32=\the\catcode32\relax
         \catcode35=\the\catcode35\relax
80
         \catcode61=\the\catcode61\relax
81
         \catcode64=\the\catcode64\relax
82
         \catcode123=\the\catcode123\relax
83
         \catcode125=\the\catcode125\relax
84
       }%
85
86
87 \x\catcode61\catcode48\catcode32=10\relax%
88 \catcode13=5 % ^^M
89 \endlinechar=13 %
90 \catcode35=6 % #
91 \catcode64=11 % @
92 \catcode123=1 % {
93 \catcode125=2 % }
94 \def\TMP@EnsureCode#1#2{%
     \edef\FibNum@AtEnd{%
95
       \FibNum@AtEnd
96
       \catcode#1=\the\catcode#1\relax
97
     }%
98
99
     \catcode#1=#2\relax
100 }
101 \TMP@EnsureCode{33}{12}%!
102 %\TMP@EnsureCode{36}{3}% $
103 %\TMP@EnsureCode{38}{4}% &
104 \TMP@EnsureCode{40}{12}% (
105 \TMP@EnsureCode{41}{12}% )
106 \TMP@EnsureCode{45}{12}% -
107 \TMP@EnsureCode{46}{12}% .
```

```
108 \TMP@EnsureCode{47}{12}% /
109 \TMP@EnsureCode{58}{12}% :
110 \TMP@EnsureCode{60}{12}% <
111 \TMP@EnsureCode{62}{12}% >
112 \TMP@EnsureCode{91}{12}% [
113 %\TMP@EnsureCode{96}{12}% '
114 \TMP@EnsureCode{93}{12}% '
115 %\TMP@EnsureCode{93}{12}% ]
115 %\TMP@EnsureCode{94}{12}% ^ (superscript) (!)
116 %\TMP@EnsureCode{124}{12}% |
117 \edef\FibNum@AtEnd{\FibNum@AtEnd\noexpand\endinput}
```

2.2 Package resources

```
118 \begingroup\expandafter\expandafter\expandafter\endgroup
119 \expandafter\ifx\csname RequirePackage\endcsname\relax
     \def\TMP@RequirePackage#1[#2]{%
121
       \begingroup\expandafter\expandafter\expandafter\endgroup
       \expandafter\ifx\csname ver@#1.sty\endcsname\relax
122
123
         \input #1.sty\relax
       \fi
124
     }%
125
126
     \TMP@RequirePackage{ltxcmds}[2011/04/18]%
127
     \TMP@RequirePackage{intcalc}[2007/09/27]%
128
     \TMP@RequirePackage{bigintcalc}[2007/11/11]%
129 \else
     \RequirePackage{ltxcmds}[2011/04/18]%
130
     \RequirePackage{intcalc}[2007/09/27]%
131
132
     \RequirePackage{bigintcalc}[2007/11/11]%
133 \fi
```

2.3 Setup precalculated values

```
134 \ensuremath{\mbox{\sc 134 \ensuremath{\mbox{\sc 134} \ensuremath{\mbox{\sc 134}}}\xspace} \ensuremath{\mbox{\sc 134} \ensuremath{\mbox{\sc 134}}}\xspace
      \expandafter\def\csname FibNum@#1\endcsname
136 }
137 \catcode46=9 % dots are ignored
138 \FibNum@temp{0}{0}
139 \FibNum@temp{1}{1}
140 \FibNum@temp{2}{1}
141 \FibNum@temp{3}{2}
142 \FibNum@temp{4}{3}
143 \FibNum@temp{5}{5}
144 \FibNum@temp{6}{8}
145 \FibNum@temp{7}{13}
146 \ \text{FibNum@temp}{8}{21}
147 \FibNum@temp{9}{34}
148 \FibNum@temp{10}{55}
149 \FibNum@temp{11}{89}
150 \FibNum@temp{12}{144}
151 \FibNum@temp{13}{233}
152 \FibNum@temp{14}{377}
153 <caption> FibNum@temp{15}{610}
154 \FibNum@temp{16}{987}
155 \FibNum@temp{17}{1.597}
156 \FibNum@temp{18}{2.584}
157 \FibNum@temp{19}{4.181}
158 \FibNum@temp{20}{6.765}
159 \FibNum@temp{21}{10.946}
160 \FibNum@temp{22}{17.711}
161 \FibNum@temp{23}{28.657}
```

```
162 \FibNum@temp{24}{46.368}
                                                                              163 \FibNum@temp{25}{75.025}
                                                                              164 \succ 164 \succ 121.393
                                                                              165 \FibNum@temp{27}{196.418}
                                                                              166 \FibNum@temp{28}{317.811}
                                                                              167 \FibNum@temp{29}{514.229}
                                                                              168 \FibNum@temp{30}{832.040}
                                                                              169 \FibNum@temp{31}{1.346.269}
                                                                              170 \FibNum@temp{32}{2.178.309}
                                                                              171 \FibNum@temp{33}{3.524.578}
                                                                              172 \FibNum@temp{34}{5.702.887}
                                                                              173 \FibNum@temp{35}{9.227.465}
                                                                              174 \FibNum@temp{36}{14.930.352}
                                                                              175 \FibNum@temp{37}{24.157.817}
                                                                              176 \FibNum@temp{38}{39.088.169}
                                                                              177 \succ 177 \succ 177 \leftarrow 177 
                                                                              178 \FibNum@temp{40}{102.334.155}
                                                                              179 \FibNum@temp{41}{165.580.141}
                                                                              180 \FibNum@temp{42}{267.914.296}
                                                                               181 \FibNum@temp{43}{433.494.437}
                                                                              182 \FibNum@temp{44}{701.408.733}
                                                                              183 \FibNum@temp{45}{1.134.903.170}
                                                                              184 \FibNum@temp{46}{1.836.311.903}
                 \FibNum@max
                                                                              185 \def\FibNum@max{46}
                                                                                                            Macros for precalculating values
   \fibnumPreCalc
                                                                              186 \def\fibnumPreCalc#1{%
                                                                                                     \expandafter\expandafter\expandafter
                                                                                                     \FibNum@PreCalc\intcalcNum{#1}/%
                                                                              188
                                                                              189 }
\FibNum@PreCalc
                                                                               190 \def\FibNum@PreCalc#1/{%
                                                                                                     \ifnum#1<\ltx@zero
                                                                              191
                                                                                                               \expandafter\FibNum@PreCalc\ltx@gobble#1/%
                                                                              192
                                                                              193
                                                                                                     \else
                                                                                                               \ifnum#1>\FibNum@max
                                                                              194
                                                                              195
                                                                                                                         \begingroup
                                                                               196
                                                                                                                                  \ltx@LocDimenA=#1sp\relax
                                                                                                                                  \countdef\FibNum@i=255\relax
                                                                               197
                                                                                                                                  \FibNum@i=\FibNum@max\relax
                                                                              198
                                                                                                                                  \edef\FibNum@temp{%
                                                                              199
                                                                                                                                           \csname FibNum@\the\FibNum@i\endcsname/%
                                                                              200
                                                                                                                                 }%
                                                                              201
                                                                              202
                                                                                                                                  \advance\FibNum@i by -1\relax
                                                                                                                                  \edef\FibNum@temp{%
                                                                                                                                           \FibNum@temp
                                                                              204
                                                                              205
                                                                                                                                           \csname FibNum@\the\FibNum@i\endcsname
                                                                                                                                 }%
                                                                              206
                                                                                                                                  \advance\FibNum@i\ltx@two
                                                                              207
                                                                                                                                  \iftrue
                                                                              208
                                                                              209
                                                                                                                                           \expandafter\FibNum@PreCalcAux\FibNum@temp
```

 $\frac{210}{211}$

\endgroup

```
212
                           \fi
                    213
                         \fi
                    214 }
\FibNum@PreCalcAux
                    215 \def\FibNum@PreCalcAux#1/#2\fi{%
                    216
                         \fi
                    217
                         \edef\FibNum@temp{\BigIntCalcAdd#1!#2!}%
                         \global\expandafter
                    218
                         \let\csname FibNum@\the\FibNum@i\endcsname\FibNum@temp
                    219
                         \ifnum\FibNum@i=\ltx@LocDimenA
                    220
                           \xdef\FibNum@max{\the\FibNum@i}%
                    221
                         \else
                    222
                           \advance\FibNum@i\ltx@one
                    223
                    224
                           \expandafter\FibNum@PreCalcAux\FibNum@temp/#1%
                    225
                    226 }
                    2.5
                           Expandable calculations
           \fibnum
                    227 \def\fibnum#1{%
                         \romannumeral
                         \expandafter\expandafter\FibNum@Do\intcalcNum{#1}/%
                    230 }
        \FibNum@Do
                    231 \def\FibNum@Do#1/{\%}
                    232
                         \ifnum#1<\ltx@zero
                           \FibNum@ReturnAfterElseFiFi{%
                    233
                             \ifodd#1 %
                    234
                               \expandafter\expandafter\ltx@zero
                    235
                    236
                    237
                                \expandafter\expandafter\expandafter\ltx@zero
                                \expandafter\expandafter\expandafter-%
                    238
                    239
                             \romannumeral
                    240
                             \expandafter\FibNum@Do\ltx@gobble#1/%
                    241
                           }%
                    ^{242}
                    243
                           \ifnum\FibNum@max<#1 %
                    244
                             \ltx@ReturnAfterElseFi{%
                    245
                                \expandafter
                    246
                                \FibNum@ExpCalc\number\expandafter\IntCalcInc\FibNum@max!%
                    247
                                \expandafter\expandafter\expandafter/%
                    248
                    249
                                \csname FibNum@\FibNum@max
                                \expandafter\expandafter\expandafter\endcsname
                    250
                                \expandafter\expandafter\expandafter/%
                    251
                                \csname FibNum@\expandafter\IntCalcDec\FibNum@max!%
                    252
                               \endcsname/%
                    253
                    254
                               #1%
                             }%
                    255
                    256
                           \else
                             \expandafter\expandafter\ltx@zero
                    257
                    258
                             \csname FibNum@#1\expandafter\expandafter\expandafter\endcsname
                           \fi
                    259
                         \fi
                    260
```

261 }

262 \def\FibNum@ReturnAfterElseFiFi#1\else#2\fi\fi{\fi#1}

\FibNum@ExpCalc

```
263 \def\FibNum@ExpCalc#1/#2/#3/#4\fi{%
264
     \ifnum#1=#4 %
265
       \ltx@ReturnAfterElseFi{%
266
         \expandafter\expandafter\expandafter\ltx@zero
267
         \BigIntCalcAdd#2!#3!%
268
269
       }%
270
       \expandafter\FibNum@ExpCalc
271
       \number\IntCalcInc#1!%
272
       \expandafter\expandafter\%
273
       \BigIntCalcAdd#2!#3!/%
274
       #2/#4%
275
276
     \fi
277 }
278 \FibNum@AtEnd%
279 (/package)
```

3 Installation

3.1 Download

Package. This package is available on CTAN¹:

CTAN:macros/latex/contrib/oberdiek/fibnum.dtx The source file.

CTAN:macros/latex/contrib/oberdiek/fibnum.pdf Documentation.

Bundle. All the packages of the bundle 'oberdiek' are also available in a TDS compliant ZIP archive. There the packages are already unpacked and the documentation files are generated. The files and directories obey the TDS standard.

```
CTAN:install/macros/latex/contrib/oberdiek.tds.zip
```

TDS refers to the standard "A Directory Structure for TEX Files" (CTAN:pkg/tds). Directories with texmf in their name are usually organized this way.

3.2 Bundle installation

Unpacking. Unpack the oberdiek.tds.zip in the TDS tree (also known as texmf tree) of your choice. Example (linux):

```
unzip oberdiek.tds.zip -d ~/texmf
```

3.3 Package installation

Unpacking. The .dtx file is a self-extracting docstrip archive. The files are extracted by running the .dtx through plain T_EX:

```
tex fibnum.dtx
```

¹CTAN:pkg/fibnum

TDS. Now the different files must be moved into the different directories in your installation TDS tree (also known as texmf tree):

```
\label{fibnum.sty} {\tt fibnum.sty} \to {\tt tex/generic/oberdiek/fibnum.sty} \\ {\tt fibnum.pdf} \to {\tt doc/latex/oberdiek/fibnum.pdf} \\ {\tt fibnum.dtx} \to {\tt source/latex/oberdiek/fibnum.dtx} \\
```

If you have a docstrip.cfg that configures and enables docstrip's TDS installing feature, then some files can already be in the right place, see the documentation of docstrip.

3.4 Refresh file name databases

If your TEX distribution (TEX Live, MiKTEX, ...) relies on file name databases, you must refresh these. For example, TEX Live users run texhash or mktexlsr.

3.5 Some details for the interested

Unpacking with LATEX. The .dtx chooses its action depending on the format:

plain T_FX: Run docstrip and extract the files.

LATEX: Generate the documentation.

If you insist on using LATEX for docstrip (really, docstrip does not need LATEX), then inform the autodetect routine about your intention:

```
latex \let\install=y\input{fibnum.dtx}
```

Do not forget to quote the argument according to the demands of your shell.

Generating the documentation. You can use both the .dtx or the .drv to generate the documentation. The process can be configured by the configuration file ltxdoc.cfg. For instance, put this line into this file, if you want to have A4 as paper format:

\PassOptionsToClass{a4paper}{article}

An example follows how to generate the documentation with pdfIAT_FX:

```
pdflatex fibnum.dtx
bibtex fibnum.aux
makeindex -s gind.ist fibnum.idx
pdflatex fibnum.dtx
makeindex -s gind.ist fibnum.idx
pdflatex fibnum.dtx
```

4 References

- [1] Jan Abraham. [texhax] Beginner in TEX MACRO to compute functions. 2012-04-07. URL: https://tug.org/pipermail/texhax/2012-April/019146.html (visited on 2012-04-08).
- [2] Wikipedia contributors. Fibonacci numbers. Version 486266088. Wikipedia, The Free Encyclopedia. 2012-04-08. URL: https://en.wikipedia.org/w/index.php?title=Fibonacci_number&oldid=486266088 (visited on 2012-04-08).

5 History

[2012/04/08 v1.0]

• First version.

[2016/05/16 v1.1]

• Documentation updates.

6 Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; plain numbers refer to the code lines where the entry is used.

Symbols \Qundefined	143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160,
A \advance	161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184,
\BigIntCalcAdd 217, 268, 274	199, 203, 204, 209, 217, 219, 224 \fibnumPreCalc
$ \begin{array}{c} \textbf{C} \\ \texttt{\catcode} & \ldots & \ldots & 2, 3, \\ 5, 6, 7, 8, 9, 10, 11, 12, 13, 33, \\ 34, 36, 37, 38, 39, 40, 41, 42, 43, \\ 44, 45, 46, 47, 48, 49, 69, 70, 72, \\ 73, 74, 78, 79, 80, 81, 82, 83, 84, \\ 87, 88, 90, 91, 92, 93, 97, 99, 137 \\ \texttt{\countdef} & \ldots & \ldots & 197 \\ \texttt{\csname} & 14, 21, 50, 66, 76, 119, 122, \\ 135, 200, 205, 219, 249, 252, 258 \\ \end{array} $	I \ifnum 191, 194, 220, 232, 244, 265 \ifodd 234 \iftrue 208 \ifx 15, 18, 21, 50, 58, 61, 119, 122 \immediate 23, 52 \input
E \empty 17, 18 \endcsname 14, 21, 50, 66, 76, 119, 122,	L \ltx@gobble
\empty	\ltx@gobble