

题目：

A sequence of numbers is called a **wiggle sequence** if the differences between successive numbers strictly alternate between positive and negative. The first difference (if one exists) may be either positive or negative. A sequence with fewer than two elements is trivially a wiggle sequence.

For example, `[1,7,4,9,2,5]` is a wiggle sequence because the differences (6,-3,5,-7,3) are alternately positive and negative. In contrast, `[1,4,7,2,5]` and `[1,7,4,5,5]` are not wiggle sequences, the first because its first two differences are positive and the second because its last difference is zero.

Given a sequence of integers, return the length of the longest subsequence that is a wiggle sequence. A subsequence is obtained by deleting some number of elements (eventually, also zero) from the original sequence, leaving the remaining elements in their original order.

**Examples:**

**Input:** `[1,7,4,9,2,5]`

**Output:** 6

The entire sequence is a wiggle sequence.

**Input:** `[1,17,5,10,13,15,10,5,16,8]`

**Output:** 7

There are several subsequences that achieve this length. One is `[1,17,10,13,10,16,8]`.

**Input:** `[1,2,3,4,5,6,7,8,9]`

**Output:** 2

1.时间 :  $O(N)$ ; 空间 :  $O(N)$

```
class Solution {
```

```
public:
```

```
    int wiggleMaxLength(vector<int> & nums) {
```

```
        if (nums.size() < 2) return nums.size();
```

```
        std::vector<int> dp(nums.size(), 0);
```

```
        std::vector<int> diff(nums.size(), 0);
```

```
        for (int i = 1; i < nums.size(); ++i){
```

```
            if (nums[i] == nums[i - 1]) {
```

```
                diff[i] = diff[i - 1]; /* 1, 0, 1 这个应该返回 1 , 而不
```

```
                是 2 , 因为 0 去掉后变成 1,1 */
```

```
            } else
```

```
                diff[i] = nums[i] - nums[i - 1] > 0 ? 1 : -1;
```

```
        }
```

```
        dp[0] = 1;
```

```
        for (int i = 1; i < nums.size(); ++i){
```

```
            if (diff[i] == 0 || diff[i] == diff[i-1]) dp[i] = dp[i - 1];
```

```
            else dp[i] = dp[i - 1] + 1;
```

```
        }
```

```
        return dp.back();
```

```
    }
```

```
};
```

2.时间 :  $O(N)$ ; 空间 :  $O(1)$  --> isInit 的判断和赋值操作导致运行时间相比 1 大幅增加

```
class Solution {
```

```
public:
```

```
    int wiggleMaxLength(vector<int> & nums) {
```

```
        if (nums.size() < 2) return nums.size();
```

```
        int count = 1;
```

```
        /* isInit 用于解决 isInc 在开始不确定的情形 例如 3,3,3,1,2 ,
        这里在 0~2 的下标区间中 isInc 是无法确定的 ,count 计数也无法确定 */
```

```
        bool isInc = false, isInit = false;;
```

```
        for (int i = 1; i < nums.size(); ++i){
```

```
            if (nums[i] > nums[i - 1] && (!isInit || !isInc)){
```

```
                count++;
```

```
                isInc = true;
```

```
                isInit = true;
```

```
            } else if (nums[i] < nums[i - 1] && (!isInit || isInc)){
```

```
                count++;
```

```
                isInc = false;
```

```
                isInit = true;
```

```
            }
```

```
        }
```

```

        return count;
    }
};

```

3.时间 :  $O(N)$ ; 空间 :  $O(1)$  --> 相比 2 , 优化掉 isInit , 运行时间和 1 相同 , 但没有额外空间消耗

```

class Solution {
public:
    int wiggleMaxLength(vector<int> & nums) {
        if (nums.size() < 2) return nums.size();
        int startIndex = 1;
        while (nums[startIndex] == nums[startIndex - 1]){
            startIndex++;
        }
        int count = 1;
        bool isInc = nums[startIndex] > nums[startIndex - 1] ?
true : false;
        isInc = !isInc; /* 保证 startIndex 可以正确计算 */

        for (int i = startIndex; i < nums.size(); ++i){
            if (nums[i] > nums[i - 1] && !isInc){
                count++;
                isInc = true;
            }
        }
    }
};

```

```
    } else if (nums[i] < nums[i - 1] && isInc){  
        count++;  
        isInc = false;  
    }  
}  
return count;  
}  
};
```