

题目：

Given an unsorted array of integers, find the length of longest increasing subsequence.

For example,

Given `[10, 9, 2, 5, 3, 7, 101, 18]`,

The longest increasing subsequence is `[2, 3, 7, 101]`, therefore the length is `4`. Note that there may be more than one LIS combination, it is only necessary for you to return the length.

Your algorithm should run in $O(n^2)$ complexity.

Follow up: Could you improve it to $O(n \log n)$ time complexity?

1.时间： $O(N^2)$ ；空间： $O(1)$ --> >理解错题意

```
class Solution {
```

```
public:
```

```
    int lengthOfLIS(vector<int>& nums) {  
        if (nums.size() < 2) return nums.size();  
        const int len = nums.size();  
        int maxIncreLen = 0;  
        for (int i = 0; i < len; ++i){  
            int count = 0;  
            for (int k = i + 1; k < len; ++k){  
                if (nums[k] > nums[i]){  
                    count++;  
                }  
            }  
        }  
    }
```

```

        maxIncrLen = std::max(maxIncrLen, count);

    }

    return maxIncrLen;

}

};

```

2.时间 : $O(N^2)$;空间 : $O(1)$ --> N^2 复杂度 , 不高效

```

class Solution {

public:

    int lengthOfLIS(vector<int> & nums) {

        if (nums.size() < 2) return nums.size();

        std::vector<int> dp(nums.size(), 0);

        int maxLen = 0;

        for (int i = 0; i < nums.size(); ++i){

            dp[i] = 1;

            for (int k = 0; k < i; ++k){

                if (nums[i] > nums[k]){

                    dp[i] = std::max(dp[i], dp[k] + 1);

                }

            }

            maxLen = std::max(maxLen, dp[i]);

        }

    }

};

```

```

        return maxLen;

    }

};

```

3.时间 : $O(\log N)$; 空间 : $O(N)$

```

class Solution {

public:

    int lengthOfLIS(vector<int>& nums) {

        if (nums.size() < 2) return nums.size();

        std::vector<int> dp(nums.size(), 0);

        std::vector<int> ends(nums.size(), 0);

        int rIndex = 0; /* ends 有效区[0~rIndex] */


        int maxLen = 1;

        dp[0] = 1;

        ends[0] = nums[0];

        for (int i = 1; i < nums.size(); ++i){

            /* lower_bound : 找到第一个可以插入的位置 */

            auto fIndex = std::lower_bound(ends.begin(), ends.begin() + rIndex + 1,

nums[i]) - ends.begin();

            if (fIndex > rIndex){ /* ends 上未有大于等于 nums[i]的数 */

                ends[++rIndex] = nums[i];

```

```
        dp[i] = rIndex + 1;

    } else{

        dp[i] = fIndex + 1;

        ends[fIndex] = nums[i];

    }

    maxLen = std::max(maxLen, dp[i]);

}

return maxLen;

}

};
```