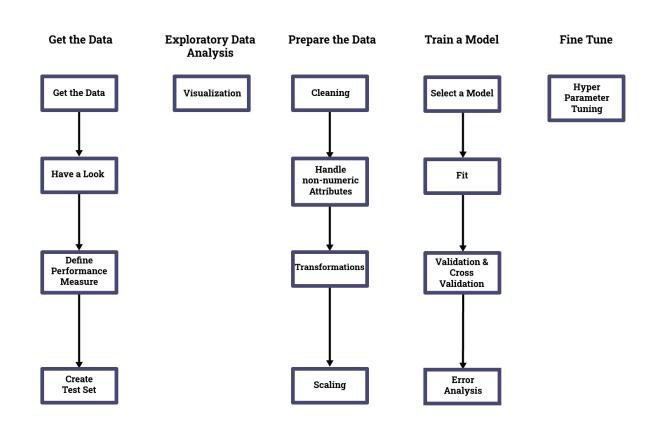
Prepare data: transformations

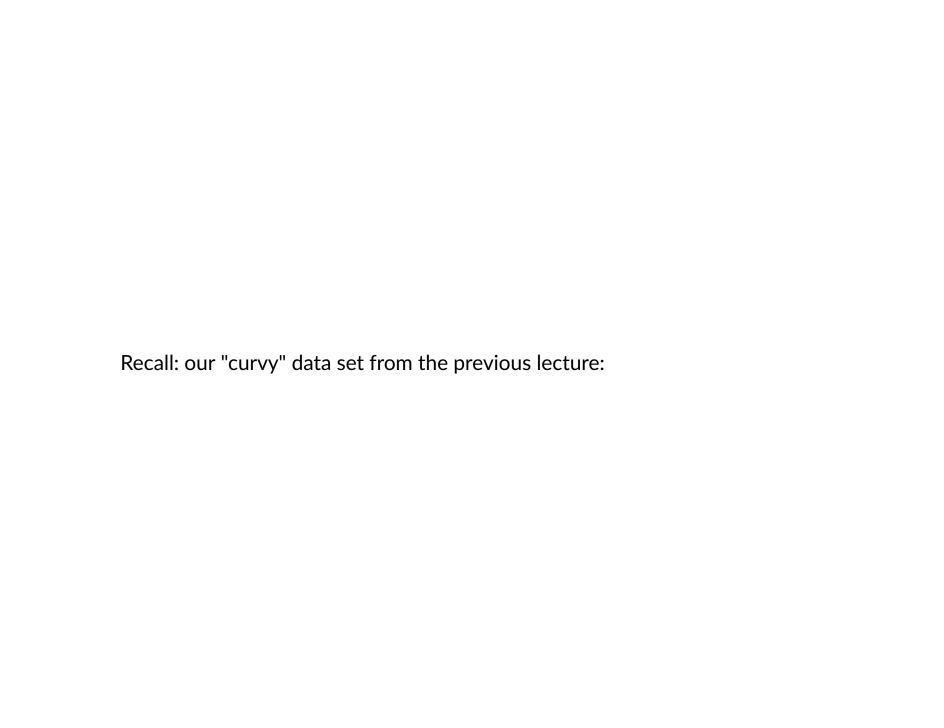
Transforming data (Recipe C.3) may be **the most important** step of the multi-step Recipe

Recipe for Machine Learning

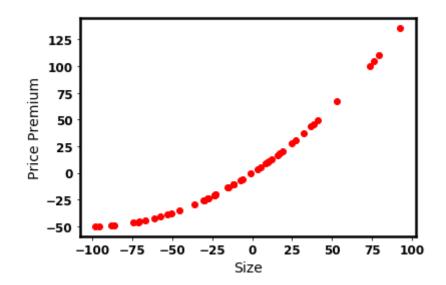


It is often the case that the "raw" features given to us don't suffice

- we may need to create "synthetic" features.
- This is called **feature engineering**.



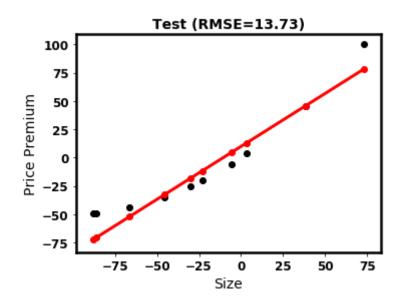
```
In [45]: (xlabel, ylabel) = ("Size", "Price Premium")
v1, a1 = 1, .005
v2, a2 = v1, a1*2
curv = recipe_helper.Recipe_Helper(v = v2, a = a2)
X_curve, y_curve = curv.gen_data(num=50)
_= curv.gen_plot(X_curve,y_curve, xlabel, ylabel)
```

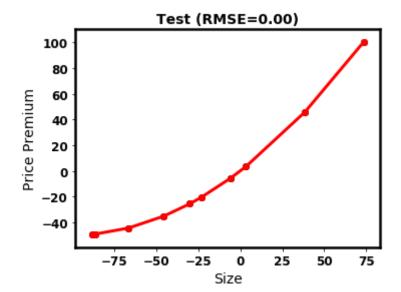


And compare the out of sample performance on this data set

- On a linear model (single, raw feature)
- On a model with a second feature (squared version of raw feature)

In [46]: model_results = curv.compare_regress(X_curve, y_curve, xlabel=xlabel, ylabel=yla
bel, visible=True, plot_train=False)







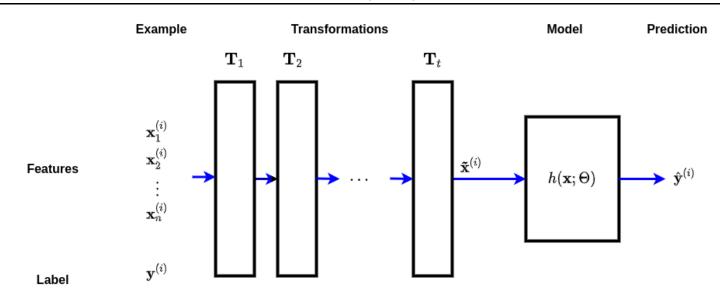
Feature engineering, or transformations

- takes an example: vector $\mathbf{x^{(i)}}$ with n features
- produces a new vector $\tilde{\mathbf{x}}^{(\mathbf{i})}$, with n' features

We ultimately fit the model with the transformed training examples.

We can apply multiple transformations, each

- Adding new synthetic features
- Further transforming synthetic features



- Missing data inputation
- Standardization
- Discretization
- Categorical variable encoding

The above diagram shows multiple transformations

ullet organized as a sequence (sometimes called a *pipeline*) of independent transformations T_1, T_2, \ldots, T_t

$$egin{aligned} ilde{\mathbf{x}}_{(1)} &= T_1(\mathbf{x}) \ ilde{\mathbf{x}}_{(2)} &= T_2(ilde{\mathbf{x}}_{(1)}) \ dots \ ilde{\mathbf{x}}_{(l+1)} &= T_{(l+1)}(ilde{\mathbf{x}}_{(l)}) \end{aligned}$$

We write the final transformed $\tilde{\mathbf{x}}$ as a function T that is the composition of each transformation function

$$\tilde{\mathbf{x}} = T(\mathbf{x}) = T_t(T_{t-1}(\dots T_1(\mathbf{x})\dots))$$

The length of the final transformed vector $\tilde{\mathbf{x}}$ may differ from the n, the length of the input \mathbf{x} • may add features • may drop features

The predictions are now a function of $\tilde{\mathbf{x}}$ rather than \mathbf{x}

$$\hat{\mathbf{y}} = h_{\Theta}(ilde{\mathbf{x}})$$

Example transformation: Missing data imputation

The first transformation we encountered added a feature (\mathbf{x}^2 term) that improved prediction.

Some transformations alter existing features rather than adding new ones.

Transformations in detail will be the subject of a separate lecture but let's cover the basics.

Let's consider a second reason for transformation: filling in (imputing) missing data for a feature.

#	$\mathbf{x_1}$	$\mathbf{x_2}$
1	1.0	10
2	2.0	20
:	:	:
i	2.0	NaN
:	:	:
m		

In the above: feature ${f x}_2$ is missing a value in example i: ${f x}_2^{({f i})}={
m NaN}$

We will spend more time later discussing the various ways to deal with missing data imputation.

For now: let's adopt the common strategy of replacing it with the median of the defined values:

$$\operatorname{median}(\mathbf{x}_2) = \operatorname{median}(\{\mathbf{x}_2^{(\mathbf{i})} | 1 \leq i \leq m, \mathbf{x}_2^{(\mathbf{i})} \neq \operatorname{NaN}\})$$

This imputation is a kind of data transformation: replacing an undefined value.

Without this transformation: the algorithm that implements our model

- May fail
- May impute a less desirable value, since it lacks specific knowledge of our problem

"Fitting" transformations

The behavior of our models for prediction have parameters Θ .

It might not be obvious that transformations have parameters $\Theta_{\mathrm{transform}}$ as well

$$ilde{\mathbf{x}} = T_{\Theta_{ ext{transform}}}(\mathbf{x})$$

For example: when missing data imputation for a feature substitutes the mean/median feature value

• $\Theta_{
m transform}$ stores this value

We use the term "fitting" to describe the process of solving for $\Theta_{transform}$

- Unlike $\Theta,$ one doesn't usually find a "optimal" value for $\Theta_{transform}$

Our prediction is thus

$$egin{array}{lll} \hat{\mathbf{y}} &=& h_{\Theta}(ilde{\mathbf{x}}) \ &=& h_{\Theta}(\,T_{\Theta_{ ext{transform}}}(\mathbf{x})\,) \end{array}$$

The process of Transformations is similar to fitting a model and predicting.

The parameters in $\Theta_{transform}$

- ullet are "fit" by examining all training data $oldsymbol{X}$
- once fit, we can transform ("predict") *any* example (whether it be training/validation or test)

Applying transformations consistently

Since the prediction is now

$$\hat{\mathbf{y}} = h_{\Theta}(\, ilde{\mathbf{x}} \,) \quad ext{where } ilde{\mathbf{x}} = T_{\Theta_{ ext{transform}}}(\mathbf{x})$$

each and every input ${f x}$ must be transformed

- Training examples
- Test examples

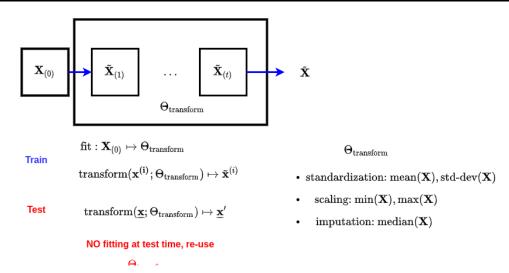
That is: the source	e transformation is applied consistently across all examples, regardless of their
If we didn't	t apply the same transformation to both training and test examples
• We	would violate the Fundamental Assumption of Machine Learning

However

- $\Theta_{transform}$ is fit **only** to training examples
- It is **not** recalculated on a set of test examples

Here's the picture

Feature engineering: fit, then transform



There are several reasons not to re-fit on test examples

- It would be a kind of "cheating" to see all test examples (required to fit)
- You should assume that you only encounter one test example at a time, not as a group

Using pipelines to avoid cheating in cross validation

Although we start off with the best intentions, it is easy to accidentally "cheat"

- When we combine transformations and cross-validation (to measure out of sample performance)
- Is surprisingly common!

k-fold cross-validation:

- ullet Divides the training examples into k "folds"
- A model is fit k times
- Each fit
 - Uses (k-1) folds for training
 - The remaining fold is considered "out of sample" for that fit
- ullet This gives us k Performance Metrics: a distribution of out of sample performance



Consider the difference between fitting $\Theta_{\mathrm{transform}}$

- Once, on all the training examples, before applying cross-validation
- ullet Separately for each of the k fits of Cross-Validation
 - ullet Using the (k-1) folds used for training in this fit

For example, when Fold_k is out of sample

 $\Theta_{ ext{transform}} = f([ext{Fold}_1, ext{Fold}_2, \dots ext{Fold}_{k-1}, ext{Fold}_k])$

versus

 $\Theta_{ ext{transform}} = f([ext{Fold}_1, ext{Fold}_2, \dots ext{Fold}_{k-1})$

In the first case, we are cheating!

- Fold k is out of sample for this fit
- And should **not** influence $\Theta_{\text{transform}}$

The second case avoids this problem

- With seemingly a lot more work
- Fitting $\Theta_{transform}$ multiple times

Perhaps the increase in effort is one reason this subtle cheating is overlooked.

Fortunately, a good toolkit for ML (e.g., sklearn) can facilitate proper transformation fitting without extra effort.

Let's explore <u>Transformation pipelines in sklearn (Transformations Pipelines.ipynb)</u>

We will see this in action within the notebook for Classification.

```
In [2]: print("Done")
```

Done