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Q. array \rightarrow arr[] = {1, 2, 3, 4, 5} (sorted)

Insertion sort \rightarrow

for ($j=2$; $j < n$; $j++$)

Key = arr[j]

$i = j - 1$

while ($i > 0$ && Key < arr[i])

{

arr[i+1] = arr[i];

}

arr[i+1] = Key

}

Complexity analysis

	0	1	2	3	4
		1	2	3	4
i			1	2	3
j			2	3	4
Key			2	3	4
Comp			1	1	1
Moved			1	1	1

$$P(n) = 2 + 2 + 2 \dots n = 2(n)$$

$$\text{time complexity} = O(n)$$

The complexity can be reduced by

- 1) Binary search - by using a sorted array & using binary search can reduced the complexity to $O(\log n)$

- 2) By using linked list - complexity of insertion become $O(1)$ & the overall complexity becomes $O(n)$

Q2 Quick sort algorithm

Quick sort ($low, high$)

if ($low \leq high$)

$pi = \text{partition}(low, high)$

Quick sort ($low, pi-1$)

Quick sort ($pi+1, high$)

partition

$n = low, high$

$i = low$

for ($j = high$ to $low-1$)

if ($arr[j] < arr[i]$)

swap ($arr[j], arr[i]$)

$arr[i+1] = arr[i]$

return i

The complexity of best case of

quick sort = $O(n \log n)$

The complexity of quick sort is $T(n) = O(n^2)$

Bubble sort

for $i = 0$ to size

for $j = 0$ to size-1

if $(a[j] > a[j+1])$

temp = $a[j]$

$a[j] = a[j+1]$

$a[j+1] = \text{temp}$

The complexity of bubble sort

best $\Rightarrow O(n^2)$

worst $\Rightarrow O(n^2)$