Introduction to Computational Science

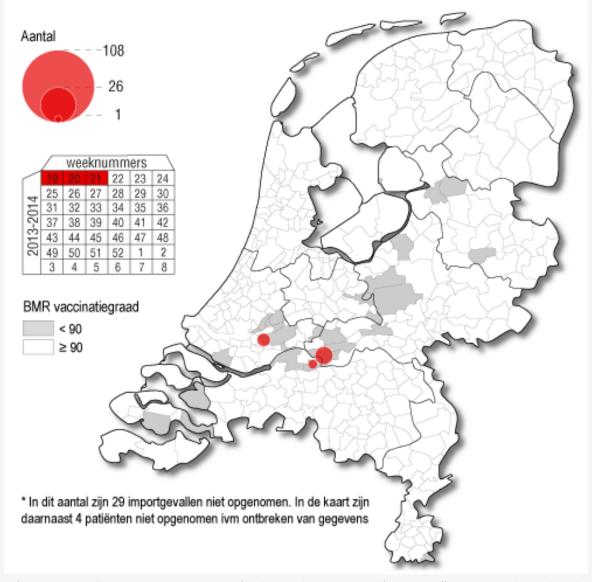
6. Spatial Models - Meta Population Models

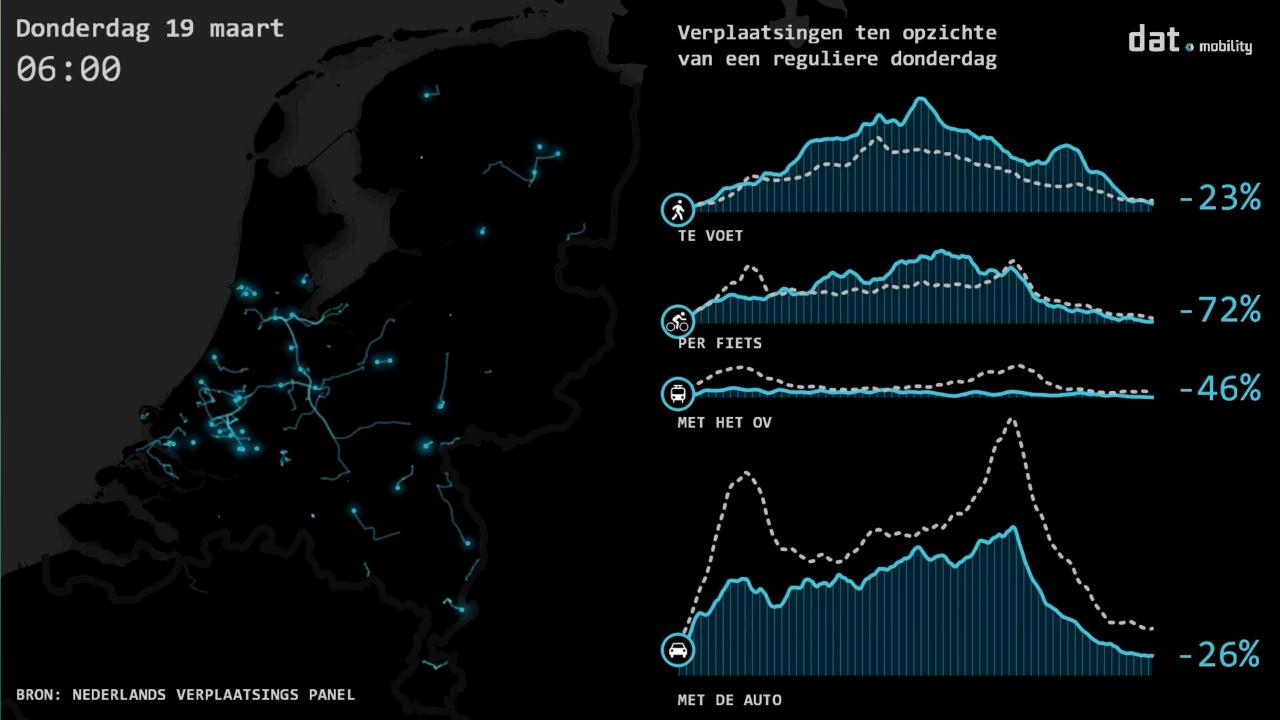
Michael Lees - m.h.lees@uva.nl

- 1. Spatial Model Introduction
- 2. Meta-population Models
- 3. Deterministic vs Stochastic Populations
- 4. Modelling Commuters
- 5. GleamViz state of the art

6.1 Spatial Models Introduction

Remember: Example of a measles wave in the Netherlands in 2013-2014





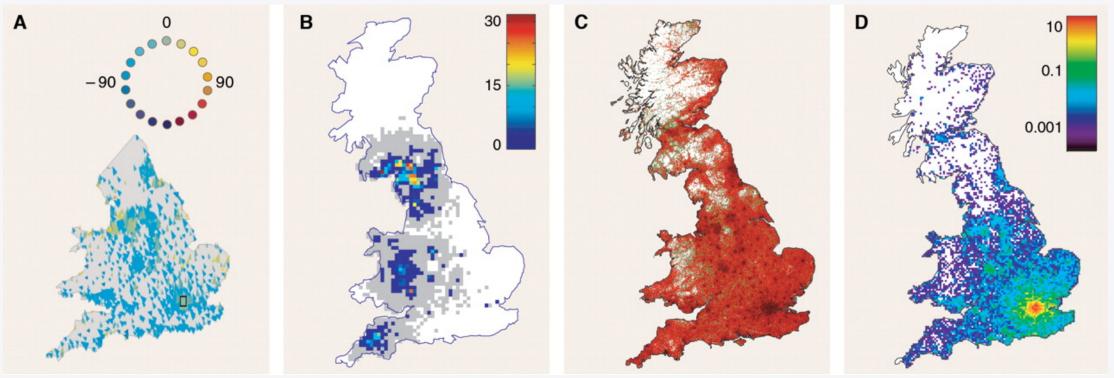
The Spatial Component

- Capturing the spatial component
 - Transmission is a local process
 - Population is usually not evenly spread
 - Individuals move around between population centers

To

- Determine rate of spatial spread
- Understand influence of heterogeneity of population density
- Understand how to use this to optimize control measures

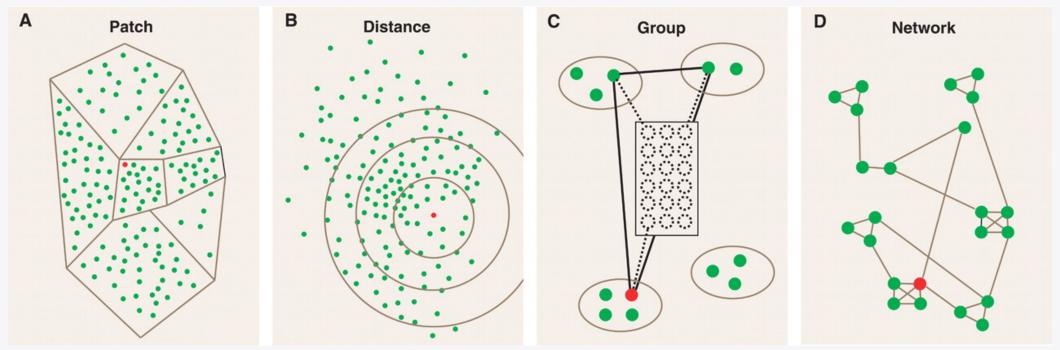
Patterns of disease transmission in the United Kingdom



Patterns of disease transmission in the United Kingdom. (A) Wavelet analysis of prevaccination measles epidemics in 954 locations in England and Wales [reproduced with permission from (15)] shows how London (black box) drove the epidemics in most of the country, with the exception of the Manchester-Liverpool urban concentration (upper left). (B) Simulations show the three high-risk areas [adapted with permission from (21)] for FMD in the United Kingdom in 2001. The key indicates the average number of cases in a 10-by-10-km square from 100 model realizations. (C) A novel strain of influenza [reproduced with permission from (34)] would spread rapidly though the United Kingdom during a global pandemic. Only 75 days after the arrival of the first cases from overseas, the intensity of red color shows the relative concentration of infectious individuals, and green indicates that the epidemic is already over in some small communities. (D) In contrast, even under a pessimistic transmission scenario, 75 days after 10 initial seeds became infectious with smallpox in London [adapted with permission from (31)], there would have been relatively few cases, and the degree of spatial correlation would still be striking [same Science key as in (B) but with 5-by-5-km squares.



Four common abstractions for the spatial transmission of infectious diseases



Four common abstractions for the spatial transmission of infectious diseases. Differences between these approaches are best understood in terms of the FOI, which is location-specific in spatially explicit models. Red dots represent infectious individuals. (A) For patch transmission, all members of the same patch (residents of a town, for example) receive the same FOI, which is a function of the distance from their home patch to other patches and of the prevalence of infection in all patches. (B) Distance transmission is explicitly individual-based. It is assumed that any given infectious individual can infect all susceptible individuals within range. (C) In a pure multigroup model, the FOI is determined entirely by group membership. For example, if an infectious individual shares a household with a susceptible individual (ovals), there is a high probability of transmission occurring between the two. However, if an infectious individual does not share a group with a particular susceptible individual, transmission between the two cannot occur. (D) Network transmission is similar to group transmission in that the FOI experienced by susceptible individuals is zero, unless they share an arc with an infectious individual. In general, computational requirements increase from (A) to (D). Patch models can be implemented effectively on a typical desktop computer because they do not explicitly represent individuals. For population sizes greater than 10 million, individual-based models have been implemented on clusters of large-memory personal computers (26, 31, 34). Detailed microsimulation models (33) have not yet been implemented at scales larger than a city.

MAAAS

Types of Spatial Models

Many options, still developing field

- We will be looking at
 - 1. Metapopulation models
 - Usually using patch transmission
 - Metapopulations usually modelled in a stochastic framework
 - 2. Individual based models
 - Using distance, group
 - Using stochastic simulation setups
 - Network Models or Agent-based Models

Other options (see Keeling and Rohani Ch. 7):

- Lattice based approaches
 Special cases of above, mainly to study in abstract way fundamental processes of disease dynamics
- 2. Continuous PDE based models

Important concepts

Heterogeneity

- Spatial differences in the fundamental forces
 - e.g. different social structures leading to different transmission rates
- Emerging spatial differences
 - Arising from the dynamical processes, stochasticity, different movement patterns, etc.

2. Interaction

- Due to movement of host between populations
- Allows for spreading of a disease
- Modelling interaction is key in including the spatial component
 - E.g. by adding additional force of infection due to infectious individuals in other locations
 - Typically, interaction between two populations should in some way decrease with distance d between them.
 - This is captured by a transmission kernel K
 - e.g. exponential $K \propto \exp(-Ad)$, Gaussian $K \propto \exp(-Ad^2)$, or power law $K \propto d^{-A}$.

Important concepts

3. Isolation

Isolated populations can be protected from infections

4. Local Extinction

- Due to smaller subpopulation sizes in spatial models, local extinctions are common.
- Interaction with larger subpopulations where the disease is endemic (e.g. large cities) then leads to new invasions of the pathogen

5. Scale

- Scale of interactions
 - From metapopulations (but how large/small are they) down to individuals
 - More subtle in lattice based and PDE based models
- Scale of the simulation
 - In real world problems this is clear, e.g. spreading of SARS in USA.
 - But in generic situations this is less clear. It should be large enough so that we can observe all the interesting dynamics.
 - but not too large ...

6.2 Meta Population Models

Metapopulations

- Most applicable to many human diseases
- Concept of metapopulation modelling
 - 1. Subdivide the population in distinct subpopulations
 - Cities, villages, or based on administrative boundaries (counties, districts, etc) leading to patches in which subpopulations live.
 - 2. Each subpopulation has independent dynamics
 - Deterministic, stochastic, with or without seasonal forcing, etc.
 - 3. and a limited form of interaction
 - Implementing some interaction kernel

Metapopulations in the SIR framework

- Assume n subpopulations, and (X_i, Y_i, Z_i) are the number of susceptible, infectious and recovered individuals in subpopulation i.
- Likewise, $N_i = X_i + Y_i + Z_i$ is to total number of individuals in subpopulation i and $N = \sum_{i=1}^{n} N_i$ is the total population size.
- We first model interaction purely due to an additional force of infection

$$\frac{dX_i}{dt} = v_i N_i - \lambda_i X_i - \mu_i X_i$$

$$\frac{dY_i}{dt} = \lambda_i X_i - \gamma_i Y_i - \mu_i Y_i$$

Force of infection

- Relation between force of infection in population i and the number of infectious individuals in population j.
 - Depends highly on assumed mechanism of transmission
 - In general

$$\lambda_i = \beta_i \sum_{j=1}^n \rho_{ij} \underbrace{\frac{Y_j}{N_i}}_{N_i}$$

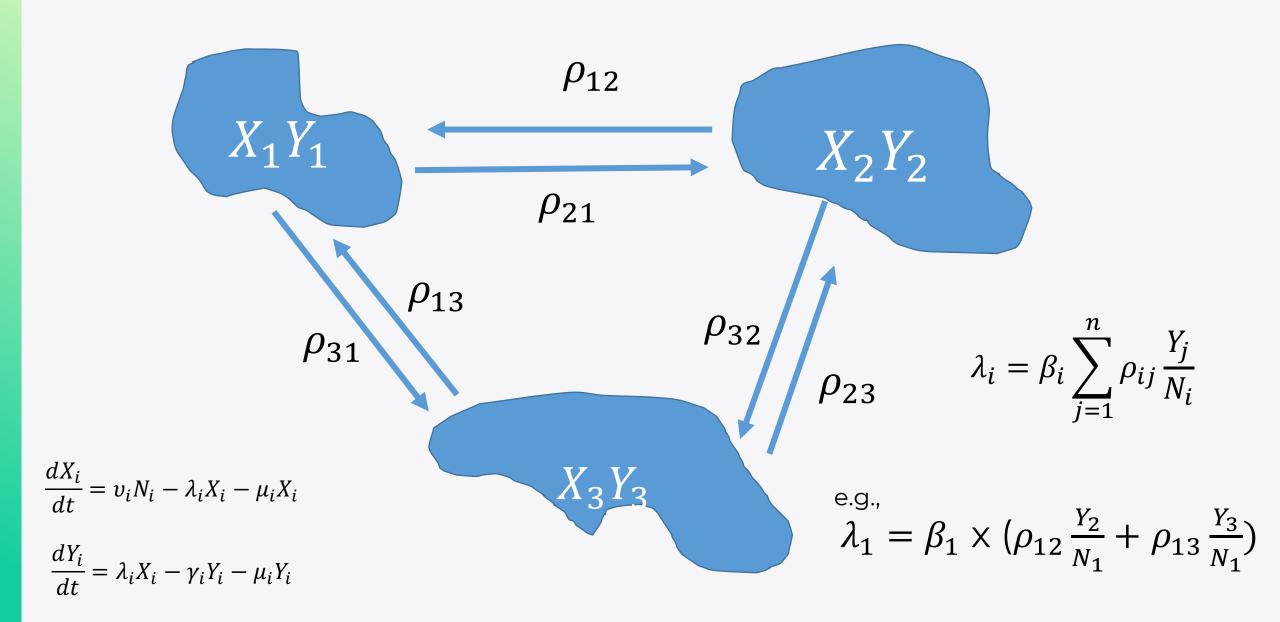
 So, a weighted sum over prevalence in all populations

(ps. note a little mistake equation in book)

- Strength of interaction matrix
- ρ_{ij} is the relative strength of transmission to population i from population j

- Important choice is the precise scaling with the population size.
- Here we assumed that transmission takes place in population i
 - E.g. due to a visit from an infectious individual from j to i
 - So, divide by N_i
- Vice versa,
 - if the model would be that the interaction is due to individual from i picking up an infection in j
 - Then divide by N_i

Metapopulation Schematic



6.3 Deterministic vs Stochastic Populations

Deterministic vs. Stochastic subpopulations

- Consider two subpopulations, n = 2.
 - Both of equal size $N_1 = N_2 = N'$, simplifying the interaction terms
 - Ignore demography
 - Fully susceptible at start
 - Introduce infection in subpopulation 1
 - Only coupling from 1 to 2, specifically, assume $\rho_{ii}=1$, $\rho_{12}=0$, and ρ_{21} is small, to mimic a relative weak coupling
- Model subpopulation 1 with a deterministic model, and subpopulation 2 with either a deterministic or stochastic model.
 - What would be the differences in the dynamics of the spreading of the disease in subpopulation 2, as a function of the interaction strength ρ_{21} ?

Population 2: deterministic

$$\frac{dY_2}{dt} = \beta_2 \rho_{21} \frac{Y_1}{N'} X_2 + \beta_2 \frac{Y_2}{N'} X_2 - \gamma_2 Y_2$$

Divide the equation by N' and consider early dynamics where $S_2 = \frac{X_2}{N'} \approx 1$, leading to

$$\frac{dI_2}{dt} = \beta_2 \rho_{21} I_1 + \beta_2 I_2 - \gamma_2 I_2$$

which can be solved as $I_2(t) = \int_0^t \beta_2 \rho_{21} I_1(s) \exp([\beta_2 - \gamma_2]s) ds$

We observe

- I. The disease is present in population 2 immediate from the start of the epidemic in population 1
- 2. Early very small infections that arrive in population 2 trigger an exponential growth at rate $\beta_2 \gamma_2$.

Population 2: stochastic

- Very different behavior
- The coupling between populations 2 and 1 will trigger events in 2 that lead to introduction of one or more infectious individuals in population 2.
 - However, that happens initially at a small rate
 - And the probability that the disease subsequently goes extinct is $\frac{1}{R_0}$
- Estimate the probability that an epidemic is triggered in population 2

$$P(\text{epidemic}) = \sum_{n=0}^{\infty} P(\text{cases in 1 cause } n \text{ cases in 2}) \times P(n \text{ initial cases lead to epidemic})$$

$$= \sum_{n=1}^{N'} \exp\left(-\beta_2 \rho_{21} \int_0^\infty I_1(s) ds\right) \frac{\left(\beta_2 \rho_{21} \int_0^\infty I_1(s) ds\right)^n}{n!} \times \left[1 - \left(\frac{\gamma}{\beta_2}\right)^n\right]$$

Poisson statistics

Probability that invasion with *n* infecteds in population 2 leads to an epidemic

$$= \exp\left(-\beta_2 \rho_{21} \int_0^\infty I_1(s) ds\right) \left[\exp\left(\beta_2 \rho_{21} \int_0^\infty I_1(s) ds\right) - \exp\left(\gamma \rho_{21} \int_0^\infty I_1(s) ds\right) \right]$$

$$= 1 - \exp\left(-\beta_2 \rho_{21} \left[1 - \frac{\gamma}{\beta_2}\right] \int_0^\infty I_1(s) ds\right) < 1 - \exp\left(-\beta_2 \rho_{21} \left[1 - \frac{\gamma}{\beta_2}\right]\right)$$

Population 2: stochastic

Estimate the probability that an epidemic is triggered in population 2

$$P(\text{epidemic}) < 1 - \exp\left(-\beta_2 \rho_{21} \left[1 - \frac{\gamma}{\beta_2}\right]\right)$$

- We observe
 - 1. If the coupling ho_{21} is small enough, there is a high probability that the disease will not spread in population 2
 - 2. For larger coupling ho_{21} the pathogen can spread, but their can be a significant delay of spreading of the disease in population 2 with respect to the epidemic in population 1
 - In stochastic metapopulation models the spread of infectious disease is slower than for deterministic ones.

Delay between population 1 and 2

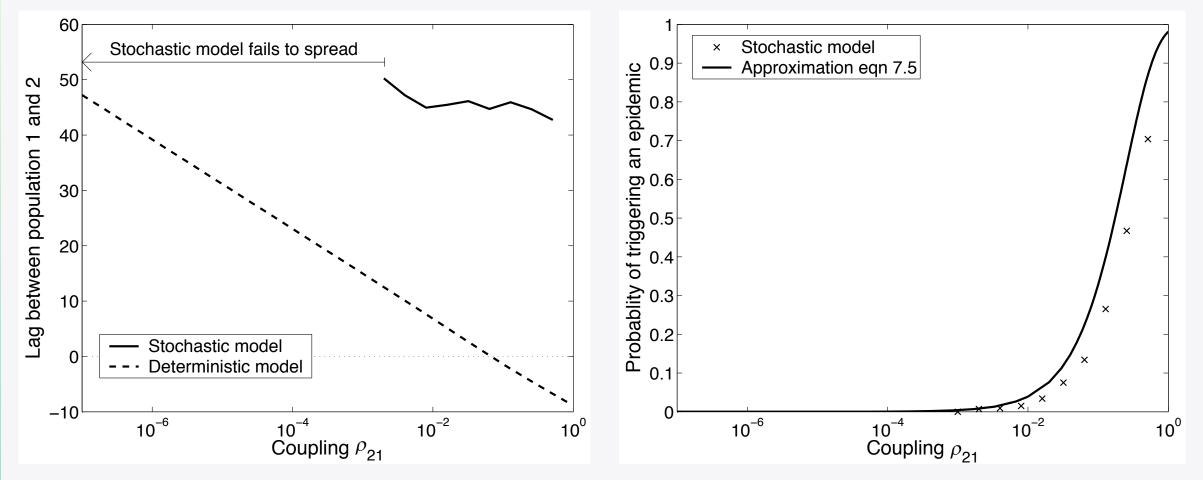


Figure 7.1 from Keeling and Rohani, For a metapopulation with just two populations we examine the effect of coupling ρ_{21} on the dynamics of the epidemic in population 2. Population 1 is modelled deterministically and is initialized with $I_1(0) = 10^{-5}$, $S_1(0) = 1 - I_1(0)$. The left-hand graph shows the delay between the peak of the epidemic in population 1 and the peak in population 2, where population 2 is modeled either stochastically (solid line) or deterministically (dashed line) and is initially disease-free. The right-hand graph is the probability that a major epidemic is triggered in the stochastic population (crosses) compared to the analytical approximation. ($\mu = \nu = 0$, $1/\gamma = 14$ days, $\beta = 0.3571$ per day $R_0 = 5$, $\rho_{ii} = 1$, $\rho_{12} = 0$. Stochastic results are the average of 1,000 realizations, $N_2 = 10^5$).

6.4 Modelling Commuters

Modelling commuters

- Commuters live in one population, say j, but travel occasionally to another population, say i.
- Let's formulate an SIR framework including commuters
- X_{ij} , Y_{ij} , and N_{ij} are the number of susceptibles, infecteds, and total hosts currently in population i that live in population.

$$\frac{dX_{ii}}{dt} = v_{ii}N_{ii} - \beta_i X_{ii} \frac{\sum_{j} Y_{ij}}{\sum_{j} N_{ij}} - \sum_{j} l_{ji} X_{ii} + \sum_{j} r_{ji} X_{ji} - \mu_{ii} X_{ii}$$

$$\frac{dX_{ij}}{dt} = v_{ij}N_{ij} - \beta_i X_{ij} \frac{\sum_j Y_{ij}}{\sum_j N_{ij}} + l_{ij}X_{jj} - r_{ij}X_{ij} - \mu_{ij}X_{ij}$$

$$\frac{dY_{ii}}{dt} = \beta_i X_{ii} \frac{\sum_j Y_{ij}}{\sum_j N_{ij}} - \gamma Y_{ii} - \sum_j l_{ji} Y_{ii} + \sum_j r_{ji} Y_{ji} - \mu_{ii} Y_{ii}$$

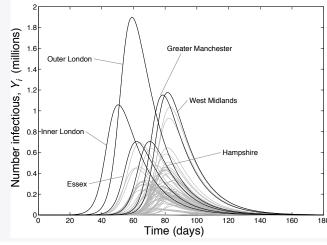
$$\frac{dY_{ij}}{dt} = \beta_i X_{ij} \frac{\sum_{j} Y_{ij}}{\sum_{i} N_{ij}} - \gamma Y_{ij} + l_{ij} Y_{jj} - r_{ij} Y_{ij} - \mu_{ij} Y_{ij}$$

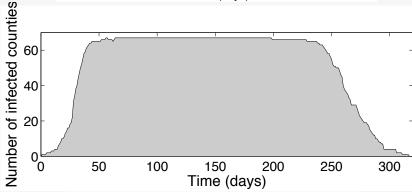
$$\frac{dN_{ii}}{dt} = v_{ii}N_{ii} - \sum_{j} l_{ji}N_{ii} + \sum_{j} r_{ji}N_{ji} - \mu_{ii}N_{ii}$$

$$\frac{dN_{ij}}{dt} = v_{ij}N_{ij} + l_{ij}N_{jj} - r_{ij}N_{ij} - \mu_{ij}N_{ij}$$

- l_{ij}: rate at which individuals leave their home j and commute to i
- r_{ij} : return rate, so from i back to home j
- l and r can be found from detailed data on populations, commuting, etc.
- We use frequency transmission with $\sum_{i} N_{ij}$ the total individuals in population i
- Full mechanistic description, but at expense of $3n^2$ equations for n populations
- Approximations exist (see 7.2.1.4 in book)

Spreading in 67 counties in England





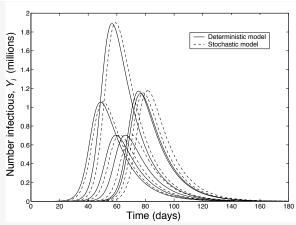


Figure 7.2 from Keeling and Rohani, Deterministic and stochastic results for an infection spread through the 67 counties of Great Britain. The epidemic is initialized with 10 cases in Inner London, and is spread by commuter movements. The population size and rate of commuting is taken from the 1991 census database, and all trips are considered to be of short duration, 1/r = 0.5 days. The top figure shows the county level epidemics from a single stochastic iteration, with six counties highlighted. The middle graph shows the number of counties with infection from the same stochastic model. The bottom graph compares the deterministic solution (solid line) with the stochastic model (dashed line) for the six counties highlighted in the top graph. $(\mu = \nu = 0, 1/\gamma = 14 \text{ days}, \beta = 0.3571 \text{ per day} \Rightarrow R_0 = 5).$

- Some results not so surprising
 - First major epidemic in innner London
 - Next and largest peak in outer London
- Some maybe more surprising
 - E.g. late peak in greater Manchester
- Within 50 days infection reached all counties
 - After that time commuting plays a minor role
- Disease stays around until after 300 days
 - Despite very low levels
- In stochastic dynamics the epidemic is delayed.

Coarse Graining the Commuter model

Fully detailed commuter model

$$\frac{dX_{ii}}{dt} = v_{ii}N_{ii} - \beta_{i}X_{ii} \frac{\sum_{j}Y_{ij}}{\sum_{j}N_{ij}} - \sum_{j}l_{ji}X_{ii} + \sum_{j}r_{ji}X_{ji} - \mu_{ii}X_{ii}$$

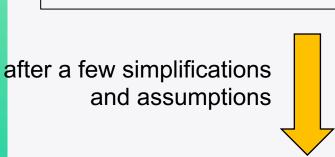
$$\frac{dX_{ij}}{dt} = v_{ij}N_{ij} - \beta_{i}X_{ij} \frac{\sum_{j}Y_{ij}}{\sum_{j}N_{ij}} + l_{ij}X_{jj} - r_{ij}X_{ij} - \mu_{ij}X_{ij}$$

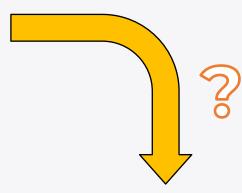
$$\frac{dY_{ii}}{dt} = \beta_{i}X_{ii} \frac{\sum_{j}Y_{ij}}{\sum_{j}N_{ij}} - \gamma Y_{ii} - \sum_{j}l_{ji}Y_{ii} + \sum_{j}r_{ji}Y_{ji} - \mu_{ii}Y_{ii}$$

$$\frac{dY_{ij}}{dt} = \beta_{i}X_{ij} \frac{\sum_{j}Y_{ij}}{\sum_{j}N_{ij}} - \gamma Y_{ij} + l_{ij}Y_{jj} - r_{ij}Y_{ij} - \mu_{ij}Y_{ij}$$

$$\frac{dN_{ii}}{dt} = v_{ii}N_{ii} - \sum_{j}l_{ji}N_{ii} + \sum_{j}r_{ji}N_{ji} - \mu_{ii}N_{ii}$$

$$\frac{dN_{ij}}{dt} = v_{ij}N_{ij} + l_{ij}N_{jj} - r_{ij}N_{ij} - \mu_{ij}N_{ij}$$





Generic metapopulation model

$$\frac{dX_i}{dt} = v_i N_i - \left(\beta_i \sum_{j=1}^n \rho_{ij} \frac{Y_j}{N_i}\right) X_i - \mu_i X_i$$

$$\frac{dY_i}{dt} = \left(\beta_i \sum_{j=1}^n \rho_{ij} \frac{Y_j}{N_i}\right) X_i - \gamma_i Y_i - \mu_i Y_i$$



$$\frac{dX_{i}}{dt} = \mu N - \beta \frac{X_{i}}{N} [(1 - (n - 1)\rho)Y_{i} + \rho \sum_{k \neq i} Y_{k}] - \mu X_{i}$$

$$\frac{dY_{i}}{dt} = \beta \frac{X_{i}}{N} [(1 - (n - 1)\rho)Y_{i} + \rho \sum_{k \neq i} Y_{k}] - \gamma Y_{i} - \mu Y_{i}$$

For all detailed derivations (study them!) see notes 'Module 6 – Modelling Commuters I'.

Coarse Graining the Commuter model II

- 5 assumptions
 - 1. All parameters do not depend on i, j $\Rightarrow v, \mu, \beta, l, r$
 - 2. $v = \mu$
 - 3. All metapopulations of equal size $\Rightarrow N_i = N \ \forall i$.
 - 4. Dynamics of commuting is fast, reaches equilibrium fast (and with $\alpha = \frac{l}{r}$)

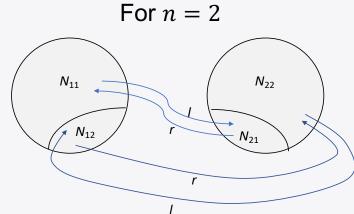
$$\Rightarrow N_{ii} = \frac{1}{1 + \alpha(n-1)} N$$

$$\Rightarrow N_{ij} = \frac{\alpha}{1 + \alpha(n-1)} N$$

5. Dynamics of commuting is much faster than dynamics of disease and demography

$$\Rightarrow X_{ij} = \frac{\alpha}{1 + \alpha(n-1)} X_i$$

$$\Rightarrow Y_{ij} = \frac{\alpha}{1 + \alpha(n-1)} Y_i$$



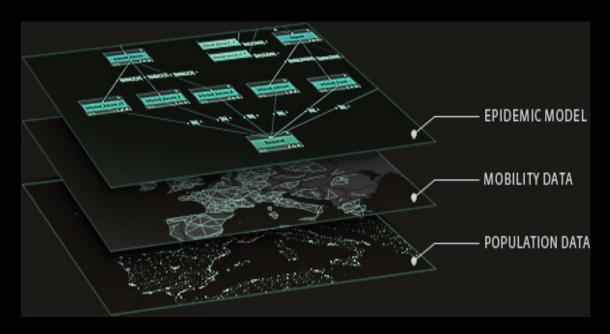
For all detailed derivations (study them!) see notes 'Module 6 – Modelling Commuters I'. Also see 'Module 6 – Modelling Commuters II' for limits of ρ .

6.5 GleamViz

State of the art Metapopulation Model

The Global Epidemic and Mobility Model

http://www.gleamviz.org



- Structured metapopulation model
 - Subpopulation are population areas around major airports
 - Mobility data based on transportation data (e.g. from IATA)
 - Advanced disease models for each subpopulation





VISION

As the growing worldwide population becomes more mobile and urbanized, the risks that infectious diseases epidemic and their associated threats may reach global proportions are constantly increasing

To effectively limit the social and economic damage caused by infectious diseases, the public health communities need to be in the position to anticipate the spatial and temporal evolution of epidemics and evaluate the potential impact of available containment and prevention strategies.

The global epidemic and mobility model, GLEAM, combines real-world data on populations and human mobility with elaborate stochastic models of disease transmission to deliver analytic and forecasting power to address the challenges faced in developing intervention strategies that minimize the impact of potentially devastating epidemics.

LATEST NEWS

Updated release of the GLEAMviz simulator!

Posted on September 25th, 2017, under News,

Dear users, we are glad to announce a new release of our simulator client: version 6.8 includes some important refactoring of the visualization components and bug-fixes, together with a few new powerful features for analyzing the simulations' output results. The updated map widget allows to select an arbitrary region by pressing the Ctrl/Command key and while holding it down clicking and dragging with the mouse. This results in opening an Analyzer widget showing the epidemic curves for the selected area. Another very useful feature is the possibility to click on a data series within an Analyzer

GLEAM IN ACTION



Relevant papers focusing on importance of airlines as major interaction

- V. Colizza, A. Barrat, M. Barthélemy, A. Vespignani, The Modeling of Global Epidemics: Stochastic Dynamics and Predictability, Bulletin of Mathematical Biology (2006) 68: 1893–1921
- 2. Duygu Balcan, Vittoria Colizza, Bruno Gonçalves, Hao Hu, José J. Ramasco, and Alessandro Vespignani, *Multiscale mobility networks and the spatial spreading of infectious diseases*, PNAS (2009) 51: 21484–21489
- 3. Vittoria Colizza, Alain Barrat, Marc Barthélemy, and Alessandro Vespignani, The role of the airline transportation network in the prediction and predictability of global epidemics, PNAS (2006) 103: 2015–2020
- 4. Colizza V, Barrat A, Barthelemy M, Valleron AJ, Vespignani A (2007) *Modeling the Worldwide Spread of Pandemic Influenza: Baseline Case and Containment Interventions*. PLOS Medicine 4(1): e13
- Available via blackboard, as background material. Good reading!

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RESEARCH ARTICLE



The effect of travel restrictions on the spread of the 2019 novel coronavirus (COVID-19) outbreak



Matteo Chinazzi¹, Jessica T. Davis¹, Marco Ajelli², Corrado Gioannini³, D Maria Litvinova³, Stefano Merler², Ana Pastore y Piontti¹, Kunpeng Mu¹, Luca Rossi³, (a) Kaiyuan Sun⁴, (b) Cécile Viboud⁴, Xinyue Xiong¹, (b) Hongjie Yu⁵, (c) M. Elizabeth Halloran^{6,7}, In Ira M. Longini Jr. 8,*, Alessandro Vespignani^{1,3,*}



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- Hide authors and affiliations

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Article

Figures & Data

Info & Metrics

eLetters



Outbreak to pandemic

In response to global dispersion of severe acute respiratory syndrome-coronavirus 2 (SARS-CoV-2), guarantine measures have been implemented around the world. To understand how travel and quarantine influence the dynamics of the spread of this novel human virus, Chinazzi et al. applied a global metapopulation disease transmission model to epidemiological data from China. They concluded that the travel quarantine introduced in Wuhan on 23 January 2020 only delayed epidemic progression by 3 to 5 days within China, but international travel restrictions did help to slow spread elsewhere in the world until mid-February. Their results suggest that early detection, hand washing, self-isolation, and household guarantine will likely be more effective than travel restrictions at mitigating this pandemic.

Science, this issue p. 395



Science

Vol 368, Issue 6489 24 April 2020

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EpiRisk



Infected entiti	ies				
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Welcome to EpiRisk

disease outbreak to other areas in the world through the airline

- · Exported cases: the tool computes the probability P(n) of exporting a given
- · Relative importation risk: for each location Y the platform evaluates the

By interacting with the map, the user can inspect the relative risk and the probability distribution of imported cases for single locations. In addition,

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