Animation of n-queens problem in JavaScript

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Study report

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Mannheim, March 6, 2019

Koen Logmann & Jessica Roth

Abstract

Animation of n-queens problem in JavaScript

Todo

Animation des N-Damen Problems in JavaScript

TODO

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Chapter 1

Introduction

Figure 1.1: DHBW-Logo [**lin1973**]

Chapter 2

Scientific Basics

The aim of this work is to visualize the Davis Putman algorithm that solves the so-called n queens problem.
Therefore a general understanding of this algorithm and the mathematical problem has to be created.
For this reason, this chapter summarizes this fundamental knowledge in order to create a basis for further development. Among other things, the declaration of the mathematical problem plays a role here, so that it can be solved by the Davis Putman algorithm.

2.1 Davis Putnam algorithm

The Davis Putman algorithm is a method for calculating a solution of logical clause sets. With very small clause sets this can be easily determined, as can be seen in the following two examples.

$$K_1 = \{\ \{r\},\ \{\neg s\},\ \{t\},\ \{\neg u\},\ \{\neg v\}\ \}$$

K_1 can also be written as a statement logic formula.

$$r \wedge \neg s \wedge t \wedge \neg u \wedge \neg v.$$

It is recognizable that this formula is solvable by r and t "true" and s, u and v having the value "false". As a counter example K_2 is to be considered. $K_1 = \{\ \{r\},\ \{\},\ \{t\}\ \}$

An empty parenthesis means a falsum in the statement logic, making K_2 impossible to fulfill. With very large clause sets it is usually no longer visible at first glance, so

that algorithms like this are used. But to be able to set a step lower, two definitions have to be introduced first. [1]

Unit clause A clause C is a unit clause if it consists of only one literal, i.e. a statement variable.

trivial clause sets A trivial set of clauses can only occur if one of the two cases occurs.

1. K contains the empty clause and is therefore unfulfillable
2. The unit clauses always contain different statement variables, so that only the clause $\{p\}$ or $\{\neg p\}$ can occur. If this is the case, a solution for the clause set can be determined.

In order for one of these two cases to occur, the clause sets must be simplified with the help of the following three options so that they consist only of unit clauses.

1. Schnittregel
2. Subsumption
3. Fallunterscheidung

2.1.1 Vereinfachung mit Schnittregel

2.1.2 Vereinfachung mit Subsumption

2.1.3 Vereinfachung mit Fallunterscheidung

The following sentence forms the basis for the principle of case differentiation.

Satz The clause set K can be fulfilled if the clause $K \cup \big\{\{p\}\big\}$ or $K \cup \big\{\{\neg p \neg p\}\big\}$ can be fulfilled.

For simplification, a statement variable p is selected at the beginning, which occurs in the clause set. Then the two clause sets mentioned above are formed and an attempt is made to find a solution for one of them. If this attempt is successful, the result is automatically the solution of K. If none is found, K is unsolvable.

2.1.4 Vorgehen des Algorithmus

The knowledge base that was previously created now makes it possible to sketch the procedure of the Davis Putman algorithm. With the help of the intersection rule and the subsumption, the clause set K is simplified as far as possible. If already after this step K is trivial, the procedure is finished. Otherwise a statement logical variable p is selected, which occurs in K. Then a recursive attempt is made to solve the clause set $K \cup \{\{p\}\}$ in order to find a solution for K. If no solution was found here either, the same is tried with the negated p. If this attempt also fails, K is unsolvable.[1], [2]

2.2 N Queens Problem

The n queen problem is the generalized mathematical problem related to a chessboard that consists of $n \times n$ squares. A special example would be the 8 queens problem, which is related to the standardized chessboard. In general, the problem is to place n queens on an $n \times n$ chessboard so that none would be obstructed in their turn. A queen in a normal game of chess can move diagonally, vertically and horizontally. This move pattern can be seen in Figure 2.1. In summary, this means that there is only one queen allowed on her vertical, horizontal and diagonal line at a time so that they do not interfere with each other. In this problem it is assumed that any queen can attack any other queen and the field colors are ignored. This problem can be solved by several algorithms such as the Davis Putman algorithm. [3], [4], [5, pp. 146 sq.], [2]

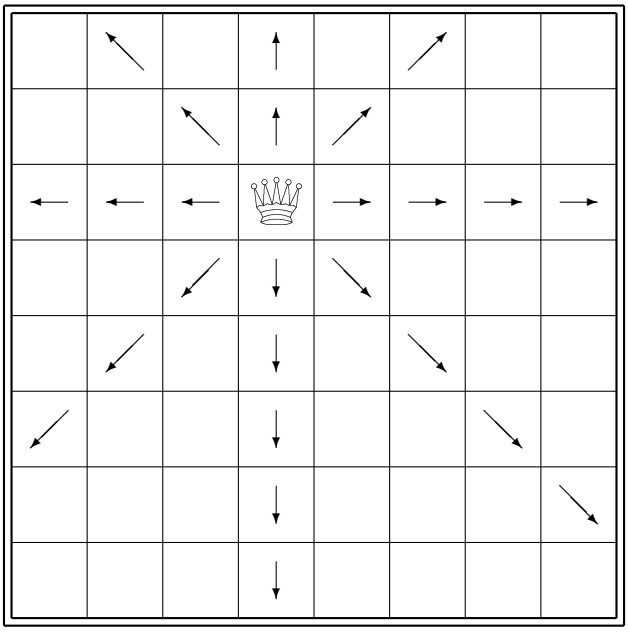

Figure 2.1: Das 8-Damen-Problem [6]

Chapter 3

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