

# CHALMERS



A Generator of Divide-and-Conquer  
Lexers

A Tool to Generate an Incremental Lexer from a  
Lexical Specification

*Master of Science Thesis [in the Programme MPALG]*

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## **Abstract**

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# 1

## Introduction

This master-thesis is carried out at Chalmers, on the department of computer science.

### 1.1 Background

Editors normally have regular-expression based parsers, which are efficient and robust, but lack in precision: they are unable to recognize complex structures. Parsers used in compilers are precise, but typically not robust: they fail to recover after an error. They are also not efficient for editing purposes, because they have to parse files from the beginning, even if the user makes incremental changes to the input. More modern IDEs use compilerstrength parsers, but they give delayed feedback to the user. Building a parser with good characteristics is challenging: no system offers such a combination of properties

### 1.2 Scope of work

\*Usage of BNFC \*With help of regexp build a finit state machine that will lex a code string. \*Give finite states with corresponding Monoid data type. \*Flag for errors from the Lexer, give meningfull info to the user, and stop the worklow after lexer, until new updated text. \*If no errors, handel layout \*Parse the Monoid data type tree, AKA integrate the result with an existing parser. \*Smile and be happy!

# 2

## Lexer

A Lexer, lexical analyser, is a pattern matcher. It's job is to find sequence of characters in a larger string. The Lexer is a front end of a syntax analyser. [?] This can be done by using regular expressions, regular sets and finite automata. Which are central concepts in formal language theory. [?] All on which will be described in this chapter.

### 2.1 Lexing vs Parsing

There are several reasons why a compiler should be separated in to lexical analyser and a parser (syntax analyser) phases. Simplicity of design is the most important reason. When dividing the task in to these to sub task, it allows the system to simplify one of these sub-tasks. For example, a parser that has to deal with white-spaces and comments as syntactical units would be more complex then one that can assume white-spaces and comments have already been removed by an lexer. Also when the two tasks are divided into sub-tasks it can lead to cleaner overall design when designing a new language [?] Lexers work as a subprogram to the parser, giving it's result to the syntax analyser. So the only thing the syntax analyser will see is the output from the lexer, tokens and lexemes which will be described later in this chapter. [?] The lexer also skips comments and white-spaces, since these are not relevant for the syntax analyser. [?] Also overall efficiency of the compiler can be improved. When separating the lexical analyser it allows for appliance of specialised techniques that serve only the lexical task. [?] Last compiler portability can be enhanced. That is Input-device-specific peculiarities can be restricted to the lexical analysis. [?] So the lexer can detect syntactical errors in tokens, such as ill-formed floating-points literals, and report these errors to the user. [?] Breaking the compilation before running the syntax analyser, saving computing time.

## 2.2 Token Specification

A lexical analyser job is to translate a human readable string to a abstract computer readable list of tokens. To define these abstract data-types in form of strings the lexer uses different techniques. This section will describe these techniques used when writing rules for the tokens patterns.

### 2.2.1 Languages

An alphabet is an finite set of symbols, such an alphabet is for example the Unicode, which includes approximately 100,000 characters. A language is any countable set of strings over some fixed alphabet. [?] The term formal languages refers to languages which can be described by a body of systematic rules. Like any formal language, a regular language is a set of strings. In other words a sequence of symbols, from a finite set of symbols. Only some formal languages are regular; in fact, regular languages are exactly those that can be defined by regular expressions. [?]

### 2.2.2 Regular Expressions

Say that we want to express the set of valid C identifiers. Use of regular expressions make it very easy, as shown in example 2.2.1.

**Example 2.2.1** (Valid C Idents). [?]

Say we have a element  $letter \in \{a \dots z\} \cup \{A \dots Z\} \cup \{-\}$  and another element  $digit \in \{0 \dots 9\}$  Then with help of regular expressions the definition of all valid C identifiers would look like this:  $letter(letter|digit)^*$ .

In definition 2.2.2 is the formal definition for regular expressions.

**Definition 2.2.2** (Regular Expressions). [?]

1. The following characters are meta characters  $\{'|', '(', ')', '*', '\}$ .
2. A none meta character  $a$  is a regular expression that matches the string  $a$ .
3. If  $r_1$  and  $r_2$  are regular expressions then  $(r_1|r_2)$  is a regular expression that matches any string that matches  $r_1$  or  $r_2$ .
4. If  $r_1$  and  $r_2$  are regular expressions.  $(r_1)(r_2)$  is a regular expression of the form that matches the string  $xy$  iff  $x$  matches  $r_1$  and  $y$  matches  $r_2$ .
5. If  $r$  is a regular expression the  $r^*$  is a regular expression that matches any string of the form  $x_1, x_2, \dots, x_n, n \geq 0$ . Where  $r$  matches  $x_i$  for  $1 \leq i \leq n$ , in particular  $(r)^*$  matches the empty string,  $\epsilon$ .
6. If  $r$  is a regular expression, then  $(r)$  is a regular expression that matches the same string as  $r$ .

Many parentheses can be reduced by adopting the convention that the Kleene closure operator  $*$  has the highest precedence, then concat and then or operator  $|$ . The two binary operators, concat and  $|$  are left left-associative. [? ]

### 2.2.3 Regular Definitions

In a definition of a language it is useful to give regular expressions names, so they can for example be used in other regular expressions, as these names where themselves symbols. If  $\Sigma$  is an alphabet of basic symbols, then a regular definition is a sequence of definitions of the form:

$$\begin{array}{lcl} d_1 & \rightarrow & r_1 \\ d_2 & \rightarrow & r_2 \\ \vdots & \rightarrow & \vdots \\ d_n & \rightarrow & r_n \end{array}$$

where:

1. Each  $d_i$  is a new symbol, not in  $\Sigma$  and not the same as any other of the  $d$ 's.
2. Each  $r_i$  is a regular expression over the alphabet  $\Sigma \cup \{d_1, d_2 \dots d_{i-1}\}$

By restricting  $r_i$  to  $\Sigma$  and previously defined  $d$ 's the regular definitions avoid recursive definitions. [? ]

## 2.3 Tokens, Patterns and Lexemes

When the rules are defined, the lexer needs structures of representing these rules and the result from lexing the code-string. This section will describe the data-structures the lexical analyser works with for representing the abstract data. What the lexer uses them for and what is sent forward to the syntactical analyser.

A lexical analyser uses three different terms. All which is described here below.

**Token** is a pair consisting of a token name and an optional attribute value. The token name is an abstract symbol corresponding to a lexical unit [? ]. For example, a particular keyword, data-type or identifier. The token names is what is given to the parser.

**Pattern** is a description of what form a lexemes of a token may take. [? ] For example, a keyword is just the sequence of characters that forms the keyword, an int is just a sequence consisting of just numbers.

**Lexemes** is a sequence of characters in the code that is being analysed which matches the pattern for a token and is identified by the lexical analyser as an instance of a token. [? ]

As mention before a token consist of token name and a optional attribute value. This attribute is used when one lexeme can match more then one pattern. [?] For example the pattern for a digit token matches both 0 and 1, but it is important for the code generator to know which lexeme was found. Therefore the lexer often return not just the token but also an attribute value that describes the lexeme found in the source program corresponding to this token. [?] A lexer collects chars into logical groups and assign internal codes to these groups. according to there structure.[?] Where the groups of chars are lexemes and the internal codes are tokens. Here follows a example how a small piece of code would be divided.

**Example 2.3.1** (Logical grouping). [?]

This is the code being lexed:

```
result = oldsum - value /100;
```

This is how it will be divided:

<u>Token</u>	<u>Lexeme</u>
IDENT	result
ASSING_OP	=
IDENT	oldsum
SUB_OP	-
IDENT	value
DIV_OP	/
INT_LIT	100
SEMICOLON	;

## 2.4 Recognition of Tokens

In previous section the topic have been, how to represent a pattern using regular expressions and how these expressions relates to tokens. This section will highlight how to transform a sequence of characters into a sequence of abstract tokens. First some basic understanding with transition diagrams.

### 2.4.1 Transition Diagrams

A state transition diagram, or just transition diagram is a directed graph. Where the nodes are labelled with the state name. Each node represent a state which could occur during the process of scanning the input looking for lexeme that matches one of several patterns.[?] The edges are labelled with the input characters that causes the transition among the states. An edge may also contain actions the lexer must perform when transition is token.[?] Here follows some properties for a transition diagram, One state is said to be initial state. The transition diagram always begins at this state, before

any input symbols have been read. Some states are said to be accepting (final). They indicate that a lexeme has been found. The found token should then be returned with any additional optional values, mentioned in previous section.[?] Transition diagrams of the formed used in lexers are representations of a class of mathematical machines called finite automata. Finite automata can be designed to recognise members of a class of languages called regular languages, mentioned above. [?]

### 2.4.2 Finite Automata

A finite automata are essentially graphs, like transitions diagrams, with some differences:

- Finite automata are recognizers; they simply say "YES" or "NO" about each possible input string.
- Finite automata comes in to different forms:

**Non-deterministic Finite Automata (NFA)** which have no restriction of the edges, several edges can be labelled by the same symbol out from the same state.  $\epsilon$ , the empty string, is a possible label.

**Deterministic Finite Automata (DFA)** for each state and for each symbol of its input alphabet exactly one edge with that symbol leaving that state

Both these forms of finite automate are capable of recognising the same language, called regular languages. These are languages that regular expressions can describe. [?] The formal definition of a finite automata follows:

**Definition 2.4.1** (Finite Automata). [?]

A finite automata is a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$ , where

1.  $Q$  is a finite set called the states,
2.  $\Sigma$  is a finite set called alphabet,
3.  $\delta : Q \times \Sigma \rightarrow Q$  is a transition function,
4.  $q_0 \in Q$  is the start state, and
5.  $F \subseteq Q$  is the set of accept states.

#### Non-deterministic Finite Automata

An NFA accept input  $x$  if and only if there is a path in the transition diagram from the start state to one of the accepting states. Such that the symbols along the way spells out  $x$ . [?]

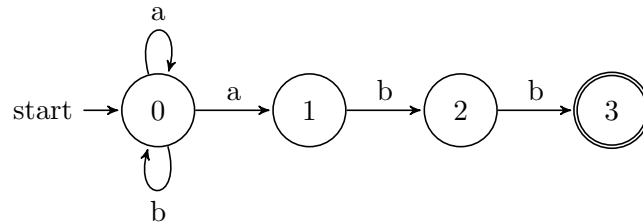
There are two different ways of representing an NFA which this report will describe. One is by transition diagrams, where the regular expression will be represented by a graph structure. Another is by transitions table, where the regular expression will be

converted in to a table of states and the transitions for these states given the input. The following examples shows how the transition diagram and transition table representation will look like for a given regular expression.

**Example 2.4.2** (RegExp to Transition Diagram). [? ]

Given this regular expression:  $(a|b)^*abb$

the transition diagram in fig. 2.1 representing this regular expression.



**Figure 2.1:** Transition Diagram, accepting the pattern  $(a|b)^*abb$

**Example 2.4.3** (RegExp to Transition Table). [? ]

Given the regular expression from example 2.4.2 it can be converted into transition table shown in fig. 2.2

State	a	b	$\epsilon$
0	{0, 1}	{0}	$\emptyset$
1	$\emptyset$	{2}	$\emptyset$
2	$\emptyset$	{3}	$\emptyset$
3	$\emptyset$	$\emptyset$	$\emptyset$

**Figure 2.2:** Transition Table representation of regular expression in example 2.4.2

Transition tables has the advantage that they have an quick lookup time. But instead it will take allot of data space, when the alphabet is large. Most states do not have any moves on most of the input symbols. [? ]

### Deterministic Finite Automata

DFA is a special case of an NFA where,

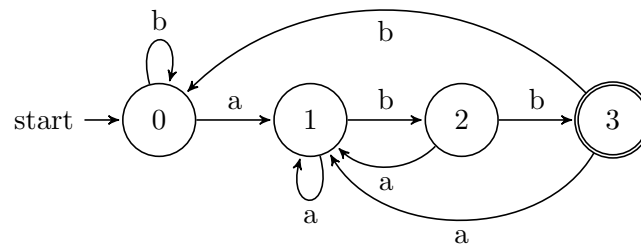
1. there are no moves on input  $\epsilon$  and
2. for each state  $s$  and input symbol  $a$ , there is exactly one edge out of  $s$  labelled with  $a$ .



While NFA is an abstract representation of an algorithm to recognise the string of a language, the DFA is a simple concrete algorithm for recognising strings. Every regular expression can be converted in to a NFA and every NFA can be converted in to a DFA. [?] It is the DFA that is implemented and used when building lexical analysers.

**Example 2.4.4** (DFA representation of RegExp). [?]

A DFA representation of same regular expression from example 2.4.2 is shown in fig. 2.3



**Figure 2.3:** DFA, accepting the regular expression:  $(a|b)^*abb$

# 3

## Divide-and-Conquer Lexer

An incremental lexer works by dividing the sequence, to be lexically analysed, into its smallest part and analyse them; and then combining them. In the base case the lexical analysis is done on a single character. The conquer step is then to combine the smaller tokens into as large tokens as possible. The end result should be a sequence of tokens that represent the code. How this is done will be described below. #Some ref to divide and conquer?

### 3.1 The Structure

For the lexer to be able to represent every possible substring of the code in the same datastructure. There need to be a generic representation for tokens and subtokens. A subtoken is a representing of a lexeme for that subtoken and a list of accepting tokens for that lexeme. The final tokens is a sequence of subtokens the output state for this sequence and an suffix, this suffix can be empty or consist of an alternativ ending for the sequence of tokens. What this is and how it works will be described more in detail in section 3.2. In fig. 3.1 is a code representation of the datastructure

### 3.2 The Power of Suffix

### 3.3 Lexing in the middle attack

When the code is divided the lexer doesn't know if the string (or character) it lexes is the first, last or is somewhere in the middle of a token. Instead of checking what type of token the string will be (if it were to begin from the starting state) it saves all the possible state transitions for that string.

In the examples that follow below state 0 is considered the starting state and state 1 – 6 are considered accepting.

```

type State = Int
type Transition = State -> Tokens — Transition from in state to Tokens
data Tokens    = Tokens {currentSeq :: Seq PartToken
                        ,outState   :: State
                        ,suffix     :: Suffix}
                        deriving Show
data Suffix    = None
                | End {getToks :: Tokens}
                deriving Show
data Size      = Size Int
type LexTree   = FingerTree (Table State Tokens, Size) Char
data PartToken = Token { lexeme      :: String
                        , token_id   :: Accepts}
type Accepts   = [AlexAcc (Posn -> String -> Token) ()]

```

**Figure 3.1:** Datastructure for tokens and lexems.

**Example 3.3.1** (Transition map for a token). A hypothetical transition map for the char 'i'.

'i'	
in	out
0	1
1	1
8	7

In the base case the lexer will map all the transitions for all individual characters in the code and construct partial tokens of them. The conquer step will then combine two of these at a time by checking which possible outgoing states from the first token can be matched with incoming states from the second token. If there are such pairs of outgoing states with incoming states, then a new partial token is created.

**Example 3.3.2** (Combining two tokens). 'if' can be an ident (state 1) or part of 'else if' (state 5).

'i'		'f'		'if'	
in	out	in	out	in	out
0	1	0	1	0	1
1	1	1	1	8	5
8	7	7	5		

If there are no pairs of outgoing states which match the incomming states the lexer will try to combine the first token with as much of the second token as possible. In this case there will be a remainder of the second token, The lexer can now be sure that the begining of the remainder is the begining of a token and that the merged part is the end of the token before. Since the lexer knows the remainder is the begining of a token it strips all transitions but the one that has incomming state as starting state. Since the start token is the end of a Token it strips all but the transitions ending in an accepting state.

**Example 3.3.3** (Combining a token a part of the second token). 'ie' ends in the accepting state for ident (1) and '\_' starts in the starting state.

$$\begin{array}{rcccl}
 & & 'e' & & ' ' \\
 & & in & out & in & out \\
 'e' & & 0 & 11 & & \\
 in & out = & 1 & 1 & 'combineToken' & 0 & 2 \\
 10 & 8 & 6 & 1 & & 2 & 2 \\
 & & 10 & 9 & & 9 & 8 \\
 \\
 'i' & & & & 'ie' & & ' ' \\
 in & out & & & in & out & in & out \\
 0 & 1 & 'combineToken' & in & out = & 0 & 1 & + & + & 0 & 2 \\
 1 & 1 & & 10 & 8 & 1 & 1 & & & & \\
 8 & 7 & & & & & & & & & 
 \end{array}$$

# Perhaps remove this part

However the remainder may not have the start state as a possible incomming state. In this case the lexer tries to find the largest possible token (that has the starting state as incomming state) and tries to construct a token of the rest of the remainder, repeating this procedure until the entire remainder has been split into acceptable tokens. All the tokens except the one that is on the very end of the sequence will have all but their accepting states stripped. This case does occur quite frequently since most languages has comments and strings which can contain anything.

**Example 3.3.4** (Handling the remainder). '\_' starts in the starting states and ends in an accepting state and 'e' starts in the starting state, it doesn't have to end in an accepting state.

$$\begin{array}{rcccl}
 & & ' ' & & 'i' \\
 & & in & out & in & out \\
 'i' & & 0 & 2 & 'combineToken' & 0 & 1 \\
 in & out = & 2 & 2 & & 1 & 1 \\
 9 & 7 & 9 & 8 & & 8 & 7
 \end{array}$$

$$checkRemainder \left( \begin{array}{cc} 'i' & \\ in & out \\ 9 & 7 \end{array} \right) = \begin{array}{cc} ' & ' \\ in & out \\ 0 & 2 \end{array} ++ \begin{array}{cc} 'i' & \\ in & out \\ 0 & 1 \end{array}$$

When all partial tokens has been combined in this way the resulting sequence of tokens represents the the code the lexer was run on.

### 3.3.1 Pitfalls

The above rules will work for very simple languages. When comments are introduced you will get the problem that the whole code can be one long partial comment token. To remedy this you can add two rules:

- Every time you combine two tokens you only do so if the combination has a transition from the starting state.
- If two tokens can be combined completely, check if the next token can be combined aswell.

This ensures that every token starts in the starting state and that each token is as long as it can be.

This also has some problems though. When keywords like “else if” are introduced the lexer will start to lex like in example 3.3.5. To solve this the lexer checks when two tokens are completely uncombinable if the first of these have an accepting state as outgoing state. If the token don’t have an accepting out state, the lexer tries to break up the token until it does. The exception to this rule is single characters which are permitted to not have no accepting out states.

**Example 3.3.5** (else if lexing). Somewhere in the middle of the code “... 1 else 0 ...”

String	Type
1	<i>Number</i>
–	<i>Space</i>
else_	<i>Nothing</i>
0	<i>Number</i>

### 3.3.2 The rules

To sum up the rules that lexer needs to follow are the following:

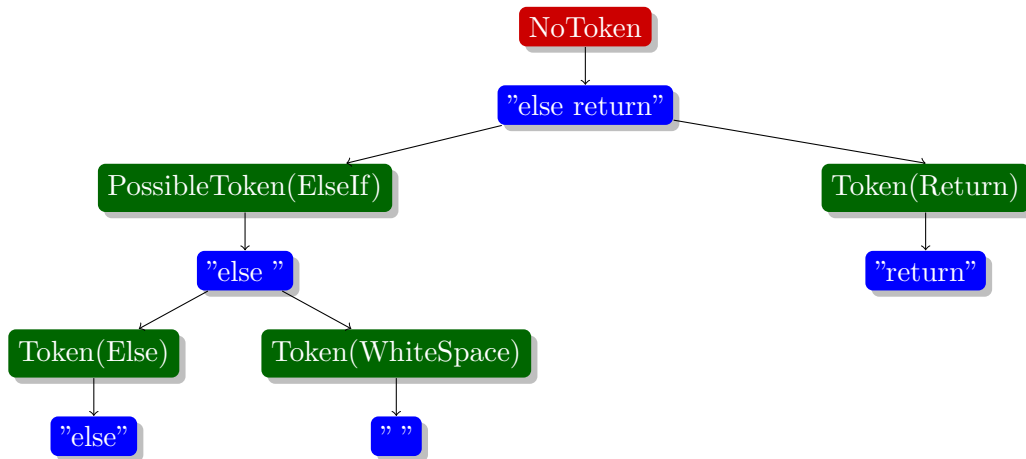
- If two tokens can be combined, combine the result with the next token.
- All tokens must start in the starting state (exception are single character tokens).
- If two tokens can’t be completely combined, combine the first token with as much as possible of the second token and check that the combination ends in an accepting state.

**Example 3.3.6** (Devide and Append). The lexer will always try to build as lage tokens as possible. When it realizes that this cant be done it has to backup and try to combine the parts in a different way. This example will show how this is done in theory.

The code segment for this example is:

"else return".

The tree in fig. 3.2 shows the first step of the token combine rutine. Clearly this returns a nonexsisting token. From here when the lexer has found that there are no tokens for

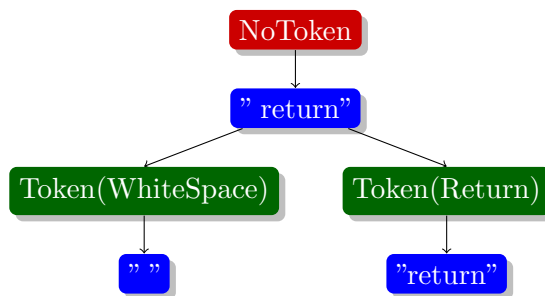


**Figure 3.2:** Lexer thinks "else " is an "else if" pattern.

this lexeme it will try to split the left child token.

`split("else ") => ["else", " "]`

Now the lexer has a pair of two lexems that represent valid tokens. The lexer knows that combining these two lexems in the pair returns in a NoToken result. So The only thing to do is to try to combine the right token in the pair with the right child token and let the token to the left in the pair stand alone. This also return a NoToken. So the



**Figure 3.3:** Lexer tries to combine an white space with a return statement

same thing will be done again. The lexer tries to split the left child before NoToken was given. In this case the whitespace.

```
split(" ") => []
```

But because the whitespace is of the lowest form and is not build up by smaller tokens the resulting list from the split function will be empty. Now the lexer knows that this token must be by it self. The "return" is the last lexeme in this example code so the lexer can't combine it futher. Thus the lexer has found the resulting sequence of tokens:

```
[(Token(Else), "else"), (Token(WhiteSpace), " "), (Token(Return), "return")]
```

### 3.4 Lexical Errors

Since the lexer has to be able to handle any kind of possible not completetokens, error handling can be done in different ways. One approach is to simply return as many tokens as possible from the code and where there might be lexical errors the lexer returns the error in as small parts as possible.

**Example 3.4.1** (A lexer that only lexes letters). When the lexer encounters the string what @ dayit would return:

String	Type
What	<i>Word</i>
' '	<i>Space</i>
'@'	<i>No-Token</i>
' '	<i>Space</i>
day	<i>Word</i>

### 3.5 Considered Data-Structures

# We should here also talk about some datastrucrters that is needed for a incremental lexer to work.

#### 3.5.1 Code Sturcture

# We should talk about how to represent the code and result as a tree structure to easy know where changes has been added in the code. and only update the result for the code affected by the changes.

#### 3.5.2 Transistion Structures

#How should our DFA or more exactly our transistions be represented to get maximum awesomeness in our program.

### 3.6 Transition map

To be able to make a divide-and-conquer lexer work you can use a transition map for the subexpression that has currently been lexed. That is you store for each subexpression a list of tuples which are built up of an in state, a list of tokens and an out state. This could in haskell look something like this.

```
type Transition = (State, Tokens, State)
type Transitions = [Transition]
```

The *tokens* type helps to think of as being a suffix, that is the first part of the substring, this has to end in an accepting state; a list of tokens which all are complete tokens, they start in the starting state and end in an accepting state; and a prefix, the last part of the lexed substring, this part has to begin in the starting state; or just a single partial token that can be anywhere in a token.

```
data Tokens = Single String
            | Multiple String [Token] String
```

Now lets see how these data types work in order to create list of tokens for a String.

#### 3.6.1 The Base Case

When the lexer tries to lex one character it will create the above transition table using the DFA for the language. It will for each state in the DFA lookup what out state the character would yield and create a Tokens type of Single. For the character '/' part of a transition map might look like the following.

$$\begin{bmatrix} 10 & \text{Single}'/' & 10 \\ 11 & \text{Single}'/' & \text{NoState} \\ 12 & \text{Single}'/' & 10 \end{bmatrix}$$

The reason we keep track of *NoState* will be evident once we show how the conquer step work.

#### 3.6.2 Conquer Step

The most general case is a naive lexer that takes the first accepting state it can find. When two lists of tokens are combined it will create two tokens if the out state of the first list is accepting then the second list will be appended to the first list. The other case us when the first list of tokens does not end in an accepting state. In this case the lexer will try to find an in state in the second list that is the same as the out state of the first transition.



$$\begin{bmatrix} 0 & \text{Single}'/' & 1 \\ 1 & \text{Single}'/' & \text{Accepting5} \end{bmatrix} \text{'combineTokens'} \begin{bmatrix} 0 & \text{Single}'/' & 1 \\ 1 & \text{Single}'/' & \text{Accepting5} \end{bmatrix} = \\ \begin{bmatrix} 0 & \text{Single}'/' & \text{Accepting5} \\ 1 & \text{Multiple}'/'\text{'/'}' & \text{Accepting1} \end{bmatrix}$$

This won't work as a lexer for most languages since it will lex a variable to variables where the length is a single character, for example "os" will be lexed as two tokens, "o" and "s". To solve this some more work is needed to be done.

### 3.6.3 Longest Match

Instead of taking the naive approach where a token is created if you find an accepting state, the rule for creating a new token will instead be when the combination of two transitions yields *NoState* the lists will be appended. That is, when there is an out state from the first transition that corresponds to an in state of the second transition and the out state of the second transition isn't *NoState*, the last token of the first transition and the first token of the second transition will become one token, otherwise append the second list to the first list.

$$\begin{bmatrix} 0 & \text{Single}'/' & \text{Accepting5} \\ 1 & \text{Multiple}'/'\text{'/'}' & 1 \end{bmatrix} \text{'combineTokens'} \begin{bmatrix} 0 & \text{Single}'\backslash n' & \text{Accepting6} \\ 1 & \text{Single}'\backslash n' & 1 \\ 5 & \text{Single}'\backslash n' & \text{NoState} \end{bmatrix} = \\ \begin{bmatrix} 0 & \text{Multiple}'/'\text{'/'}'\backslash n' & \text{Accepting6} \\ 1 & \text{Multiple}'/'\text{'/'}'\backslash n' & 1 \end{bmatrix}$$

The second case is when the out state for the right token list is *NoState*. This means that the two lists of tokens can't be combined. In this case the first token in the second list will be viewed as the start of a token and the last token in the first list will be viewed as the end of a token.

# 4

## Parallelism

# Our solution should be able to run on several cores. This chapter should be about why how and so on.

# 5

## Used Structures

#Unertain of the name of this chapter. But here we should talk about bnfc and alex. What we use from the differnet programs. How this is usefull is it becouse of lazynes or are the existing solutions good??

# 6

## Testing

#How is the testing of this project preform!?

# 7

## Result

#What have been the result?

# Just some bench data:

Hugos Home-Computer: AMD X2 3.1 GHz, 4 Gb Ram, 32 bit OS Windows 8 Func:  
Alex - 12.38 ms IncLex - 55.02 ms Update - 35.29 ms Array: Alex - 14.22 ms IncLex -  
331.75 ms Update - 9.92 ms

Hugos Laptop: Intel Celeron M 1.6 GHz, 1 Gb Ram, 32 bit OS Unix Fick inte Bench  
att fungera Func: Array:

# 8

## Performance Analysis

#How fast is the lexer. How have we come to this conclusion?

# 9

## Discussion

#Discuss discuss!!

# 10

## Conclusion and Futher Work

#what will our Minions do???