

### soluția

$$3) \delta_{\odot} \in [-23^{\circ} 27', +23^{\circ} 27']$$

$$p = 46^{\circ} 45' 47''$$

a)  $A_{max}$ ,  $A_{min}$  pt răsărit și apus  
de soare pe an ~~durata zilei maxime~~  
~~si minime~~.

b) durata zilei maxime și minime

$$a) \cos A = - \frac{\sin \delta}{\cos p}$$

$$I \delta = -23^{\circ} 27'$$

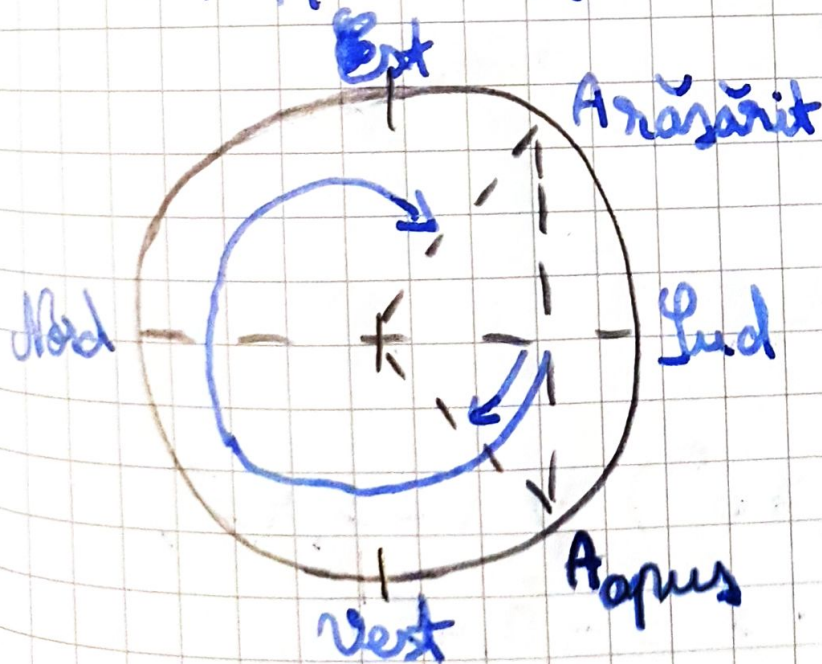
$$\cos A = \frac{-\sin(-23^{\circ} 27')}{\cos(46^{\circ} 45' 47'')}$$

$$23^{\circ} 24' = 23^{\circ} + \left(\frac{24}{60}\right)^{\circ} = 23,45^{\circ}$$

$$46^{\circ} 45' 47'' = 46^{\circ} + \left(\frac{45}{60}\right)^{\circ} + \left(\frac{47}{3600}\right)^{\circ} = 46,76^{\circ}$$

$$\cos A = \frac{\sin(23,45^{\circ})}{\cos(46,76^{\circ})} = \frac{0,39}{0,42} = 0,58$$

$$\Rightarrow A = 54,5^{\circ} = 54^{\circ} 30' \Rightarrow A_{apus} = 54^{\circ} 30'$$



$$A_{nășărit} = 360^{\circ} - 54^{\circ} 30' = 305^{\circ} 30'$$



$$a) \underline{\underline{\beta}} = 23,45^\circ$$

$$\cos A = \frac{-\sin(23,45^\circ)}{\cos(46,76^\circ)} =$$

$$= \frac{-0,39}{0,42} = -0,58$$

$$\Rightarrow A = 124,91^\circ = 124^\circ 54,6' = 124^\circ 54' 36''$$

$$\Rightarrow A_{\text{apun}} = 124^\circ 54' 36''$$

$$A_{\text{zavřít}} = 360^\circ - 124^\circ 54' 36'' =$$

$$\begin{aligned} &= 359^\circ 60' - 124^\circ 54' 36'' = \\ &= 235^\circ 5' 24'' \end{aligned}$$

$$b) \cos H = -\operatorname{tg} \varphi \operatorname{tg} \rho$$

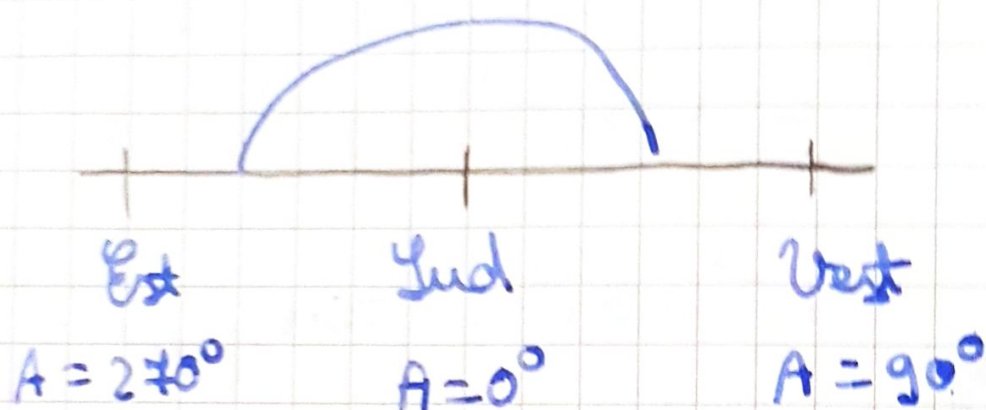
$$\cos H = -\operatorname{tg} (46,46^\circ) \operatorname{tg} (-23,45^\circ)$$

$$= -1,06 \cdot (-0,43) = 0,45$$

$$H = \arccos(0,45) = 63,03^\circ = 63^\circ 1,8' = 63^\circ 1' 48''$$

$$H_1 = 63,03 / 15 = 4,2 \text{ h punct de apus}$$

$$24 \text{ h} - 4,2 \text{ h} = 19,8 \text{ h punct de răsărit}$$



$$\cos H = -\operatorname{tg} \rho \operatorname{tg} \delta$$

$$\cos H = -\operatorname{tg}(46,76^\circ) \operatorname{tg}(23,45^\circ)$$

$$= -1,06 \cdot 0,43 = -0,45$$

$$H = \arccos(-0,45) = ~~116,31^\circ~~ 116,31^\circ = 116^\circ 18,6' = 116^\circ 18' 36''$$

$$H_2 = 116,31 / 15 = 7,75 \text{ h}$$

$$24 \text{ h} - 7,75 \text{ h} = ~~16,25 \text{ h}~~ 16,25 \text{ h}$$



$$\Delta\theta_1 = 2H_1 = 2 \cdot 4,2 = 8,4\text{h}$$

$$\Delta\theta_2 = 2H_2 = 2 \cdot 7,75 = 15,5\text{h}$$