

Înălțate 5

Determinați durata intervalului cuprins între apusul Soarelui și fârșitul crepusculului astronomic la Cluj Napoca (latitudine geografică $\varphi = 46^{\circ}46'N$), când declinația Soarelui este $\pm 23^{\circ}27'$, respectiv 0° . Exprimați intervalul de timp în timp solar mediu.

$$\varphi = 46^{\circ}46'N = 46,76^{\circ}N$$

$$I \varphi = 23^{\circ}27' = 23,45^{\circ}$$

$$h=0 \Rightarrow \cos H = \frac{\sin 0 - \sin(23,45^{\circ}) \sin(46,76^{\circ})}{\cos(23,45^{\circ}) \cos(46,76^{\circ})} =$$

$$= \frac{0 - 0,39 \cdot 0,72}{0,91 \cdot 0,68} = \frac{-0,28}{0,61} = -0,45$$

$$\Rightarrow H = ~~120^{\circ}~~ 2,03 \text{ rad} = 116,3^{\circ}$$

$$h = -18^{\circ} \Rightarrow \cos H = \frac{\sin(-18^{\circ}) - 0,28}{0,61} = \frac{-0,30 - 0,28}{0,61} =$$

$$= \frac{-0,58}{0,61} = -0,95 \Rightarrow H = 2,82 \text{ rad} = ~~161,5^{\circ}~~ 161,5^{\circ}$$

$$161,58^\circ - 116,31^\circ = 45,27^\circ = 3,018 \text{ rad} =$$

~~$$= 3,018 \text{ rad} = 1,728 \text{ rad} = 1,728 \text{ rad} =$$~~

~~$$= 1,728$$~~

$$= 3^{\text{h}} 1' = 10800 \Delta + 60 \Delta = 10860 \Delta \text{ (zecimală medie)}$$

$$= 10824 \Delta = 3,0045 \text{ rad} = 3^{\text{h}} 0,45' = 3^{\text{h}} 24''$$

$$\vec{p} = -23,45^\circ$$

$$R=0 \Rightarrow \cos H = \frac{\sin 0 - \sin(-23,45^\circ) \cdot \sin(46,46^\circ)}{\cos(-23,45^\circ) \cos(46,46^\circ)}$$

$$= \frac{0 + 0,39 \cdot 0,72}{0,91 \cdot 0,68} = \overset{\Rightarrow H}{0,45 \text{ rad}} = 1,10 \text{ rad} =$$

$$= 63,03^\circ$$

$$R = -18^\circ \Rightarrow \cos H = \frac{\sin(-18^\circ) + 0,39 \cdot 0,72}{0,91 \cdot 0,68} =$$

$$= \frac{-0,30 + 0,28}{0,61} = \frac{-0,02}{0,61} = -0,03$$

$$\Rightarrow H = 1,6 \text{ rad} = 91,68^\circ$$

$$31,68^\circ - 63,03^\circ = 28,65^\circ = 1,91 \text{ h} =$$

$$= 1^{\text{h}} 54,6' = 1^{\text{h}} 54' 36'' =$$

$$= 3600 + 3240 + 36 = 6876 \text{ s (seconde}$$

$$\text{sidérale}) = 6854 \text{ s (seconde moyen)} =$$

$$= 1,90 \text{ h} = 1^{\text{h}} 54'$$

$$\text{III } \varphi = 0^\circ$$

$$A = 0 \Rightarrow \cos H = \frac{\sin 0^\circ - \sin 0^\circ \cdot \sin(46,76^\circ)}{\cos 0^\circ \cdot \cos(46,76^\circ)}$$

$$= 0 \Rightarrow H = 1,54 \text{ rad} = 89,96^\circ$$

$$A = -18^\circ \Rightarrow \text{~~sin 0^\circ - sin 0^\circ \cdot sin(46,76^\circ)~~}$$

$$\Rightarrow \cos H = \frac{\sin(-18^\circ) - \sin 0^\circ \cdot \sin(46,76^\circ)}{\cos 0^\circ \cdot \cos(46,76^\circ)}$$

$$= \frac{-0,30 - 0}{1 \cdot 0,68} = -0,44 \Rightarrow H = 2,02 \text{ rad} =$$

$$= 115,74^\circ$$

$$115,74^\circ - 89,96^\circ = 25,78^\circ = 1,71 \text{ h} =$$

$$= 1^h 42,6^m = 1^h 42' 36'' = 3600s + 2520s = 6120s$$

$$= 6156s (\text{sidereal}) = 6139s \text{ solar time}$$

$$= 1,70h = 1^h 42'$$