numbers

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0.1 Adding

```
[14]: class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          def __add__(self, other):
              return Point(self.x + other.x, self.y + other.y)
          def __radd__(self, other):
              if isinstance(other, (float, int)):
                  return Point(self.x, other, self.y + other)
              else:
                  return self.__add__(other)
          def __iadd__(self, other):
              if isinstance(other, (float, int)):
                  self.x += other
                  self.y += other
              else:
                  self.x += other.x
                  self.y += other.y
              return self
      p1 = Point(0, 0)
      p2 = Point(1, 3)
      p3 = Point(-2, -4)
      p2 + p3
      print(sum([p1, p2, p2], Point(0, 0)))
     p1 += p2
```

<Point (x=2, y=6)>

0.2 Subtracting

```
[19]: class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          def __sub__(self, other):
              if not isinstance(other, (Point, int, float)):
                    raise TypeError(f"Subtraction is not supported for a Point and
       →{other}")
              if isinstance(other, (int, float)):
                  return Point(self.x - other, self.y - other)
                  return Point(self.x - other.x, self.y - other.y)
          # if you want to do reverse calculation
          def __rsub__(self, other):
              if not isinstance(other, Point):
                  raise TypeError("Try the reverse order. Be careful difference may⊔
       ⇔change")
              return self. sub (other)
          # if you want to do inplace calculation
          def __isub__(self, other):
             print('in place')
              return self.__sub__(other)
      p1 = Point(0, 0)
     p2 = Point(1, 3)
     p3 = Point(-2, -4)
     p2 - p1
     p2 -= 5
```

in place

0.3 Multiplying

• instresting behavioris when you do 5 * 'abc', you except failure but because of rsub/radd type behavior, it will try 'abc' * 5 and that is valid and would work

```
[25]: class Point:
    def __init__(self, x, y):
        self.x = x
```

```
self.y = y

def __repr__(self):
    return f"<Point (x={self.x}, y={self.y})>"

def __mul__(self, other):
    if isinstance(other, (int, float)):
        return Point(self.x * other, self.y * other)
    return Point(self.x * other.x, self.y * other.y)

def __rmul__(self, other):
    return self.__mul__(other)

def __imul__(self, other):
    return self.__mul__(other)

p1 = Point(0, 0)
p2 = Point(1, 3)
p3 = Point(-2, -4)
```

[25]: $\langle Point (x=-2, y=-12) \rangle$

0.4 Dividing

• divmod(5, 4) returns a tuple with the div and the modulus

```
[40]: class Point:
    def __init__(self, x, y):
        self.x = x
        self.y = y

    def __repr__(self):
        return f"<Point (x={self.x}, y={self.y})>"

    def __truediv__(self, other):
        if isinstance(other, (int, float)):
            return Point(self.x / other, self.y / other)
        return Point(self.x / other.x, self.y / other.y)

def __rtruediv__(self, other):
        return self.__truediv__(other)

def __itruedive__(self, other):
        return self.__truediv__(other)
```

```
def __floordiv__(self, other):
    if isinstance(other, (int, float)):
        return Point(self.x // other, self.y // other)
    return Point(self.x // other.x, self.y // other.y)

def __rfloordiv__(self, other):
    return self.__floordiv__(other)

def __ifloordiv__(self, other):
    return self.__floordiv__(other)

p1 = Point(0, 0)
    p2 = Point(1, 3)
    p3 = Point(-2, -4)

print(p2 / p3)
    p2 //= p3
    print(p2)

<Point (x=-0.5, y=-0.75)>
```

<Point (x=-0.5, y=-0.75)>

0.5 Modulo and Powers

• mod is used defined for number and string formatting

```
[6]: class Point:
         def __init__(self, x, y):
             self.x = x
             self.y = y
         def __repr__(self):
             return f"<Point (x={self.x}, y={self.y})>"
         def __mod__(self, other):
             return Point(self.x % other.x, self.y % other.y)
         def __rmod__(self, other):
             print('rmod')
         # mutate object iself or mutate something and then return that
         def __imod__(self, other):
             self.x %= other.x
             self.y %= other.y
             return self
         def __pow__(self, other):
```

```
return Point(self.x ** other.x, self.y ** other.y)

def __rpow__(self, other):
    return other ** self.x

def __ipow__(self):
    self.x **= other.x
    self.y **= other.y
    return self

p1 = Point(0, 0)
    p2 = Point(1, 3)
    p3 = Point(-2, -4)

p2 % p3
```

[6]: <Point (x=-1, y=-1)>

0.6 Bit Shifting Operations

```
[15]: class Binary:
          def __init__(self, number):
              self.number = number
              self._binnumber = bin(number)
          def repr (self):
              return f'<Binary number={self.number} binnumber={self._binnumber}>'
          def __lshift__(self, other):
              return Binary(self.number << other.number)</pre>
          def __rshift__(self, other):
              return Binary(self.number >> other.number)
          def __rlshift__(self, other):
              return Binary(self .number << other.number)</pre>
          def __rrshift__(self, other):
              if isinstance(other, int):
                  return Binary(self.number >> other)
              return Binary(self.number >> other.number)
          def __irshift__(self, other):
              self.number >>= other.number
              self._binnumber = bin(self.number)
              return self
```

```
def __ilshift__(self, other):
    self.number <<= other.number
    self._binnumber = bin(self.number)
    return self

b1 = Binary(2)
b2 = Binary(32)

b1 << b2

1 >> b1
```

[15]: <Binary number=1 binnumber=0b1>

0.7 Bitwise Logical Operations

- you can use bitwise operators to get bitwise or-ing/and-ing
- bin(5 & 7)

```
[19]: class Binary:
          def __init__(self, number):
              self.number = number
              self._binnumber = bin(number)
          def __repr__(self):
              return f'<Binary number={self.number} binnumber={self._binnumber}>'
          def __and__(self, other):
              return Binary(self.number & other.number)
          def __or__(self, other):
              return Binary(self.number | other.number)
          def __xor__(self, other):
              return Binary(self.number ^ other.number)
          def __rand__(self, other):
              if isinstance(other, int):
                  return Binary(self.number & other)
              return Binary(self.number & other.number)
          def __ror__(self, other):
              if isinstance(other, int):
                  return Binary(self.number | other)
              return Binary(self.number | other.number)
```

```
def __rxor__(self, other):
        if isinstance(other, int):
            return Binary(self.number ^ other)
        return Binary(self.number ^ other.number)
    def __iand__(self, other):
        temp = self.__and__(other)
        self.number = temp.number
        self._binnumber = temp._binnumber
        return self
    def __ior__(self, other):
        temp = self.__or__(other)
        self.number = temp.number
        self._binnumber = temp._binnumber
        return self
    def __ixor__(self, other):
        temp = self.__xor__(other)
        self.number = temp.number
        self._binnumber = temp._binnumber
        return self
b1 = Binary(5)
b2 = Binary(7)
b1 & b2
```

[19]: <Binary number=5 binnumber=0b101>

0.8 Negative and Postive

- we are going to be trying to deal with things like these --1/+4/+-1
- we can do fraction addition or subtractions

```
[25]: from fractions import Fraction

x = Fraction(1, 4)
x.numerator

print('x')
print(x)
print("")
print("")
print("+x")
print(+x)
print("")
```

```
print("-x")
     print(-x)
     X
     1/4
     +x
     1/4
     -1/4
[30]: from datetime import datetime
      class Date(datetime):
          def __pos__(self):
              return self.timestamp()
          def __neg__(self):
              return -self.timestamp()
      class JString(str):
          def __pos__(self):
              return float(self)
      class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          def __pos__(self):
              return self
          def __neg__(self):
              return Point(-self.x, -self.y)
      dt = Date.now()
      +dt
      -dt
      js = JString('1.234')
      +js
```

[30]: 1.234

0.9 Absolute Values and Inverse

- ~ is also called inverse
- used in loops to acces other end
- \sim means bounce to the other side -1
- whats happening is its taking binary and then flips it

```
[45]: class Fraction:
          def __init__(self, num, denom):
              self.num = num
              self.denom = denom
          def __repr__(self):
              return f'<Fraction ({self.num}/{self.denom})'</pre>
          def __mul__(self, other):
              return Fraction(self.num * other.num, self.denom * other.denom)
          def __invert__(self):
              return Fraction(self.denom, self.num)
      class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          # you can use this to return a number an not just point object
          def __abs__(self):
              return Point(abs(self.x), abs(self.y))
          def __invert__(self):
              return Point(self.y, self.x)
      p1 = Point(1, 2)
      p2 = Point(3, 2)
      p3 = Point(-5, -4)
      abs(p1)
      ~p1
      f = Fraction(1, 2)
```

```
~f
f * ~f
```

[45]: <Fraction (2/2)

0.10 Integers and Floats

- integers are whole numbers
- floats are anything with decimals
- what if you want an interger representation of a string

```
[2]: s = '1.23'
     print(float(s))
     f = 1.23
    print(int(f))
    1.23
    1
[9]: class Point:
         def __init__(self, x, y):
             self.x = x
             self.y = y
         def __repr__(self):
             return f"<Point (x={self.x}, y={self.y})>"
         def __int__(self):
             distance = (self.x **2 + self.y **2) ** 0.5
             return int(distance)
         def __float__(self):
             distance = (self.x **2 + self.y **2) ** 0.5
             return float(distance)
     # Bad do not do
     class Bacteria:
         def __init__(self, size, color):
             self.size = size
             self.color = color
         def __float__(self):
             return float(self.size)
     p1 = Point(3, 5)
     int(p1)
```

```
float(p1)
bacteria = Bacteria(10.5, "red")
float(bacteria)
```

[9]: 10.5

0.11 Rounding

- be careful about rounding when you have whole numbers verus when you have decimals
- \bullet so 3.5 rounding is different than 3.15
- round can take negative numbers and it basically goes and rounds to the right

```
[15]: i = 3
      f = 3.214
      print('round(i)')
      print(round(i))
      print("")
      print('round(f, 2)')
      print(round(f, 2))
     round(i)
     3
     round(f, 2)
     3.21
[14]: class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          def __round__(self, n=0):
              distance = (self.x **2 + self.y **2) ** 0.5
              return round(distance, n)
      p1 = Point(3, 5)
      print(round(p1))
```

6.0

0.12 Floor and Ceiling

- celing gives us the next highest number
- floor gives us the next lowest number

- basically celing is rounding up and floor is rounding down
- truncate gives us the whole number
- floor and truncate closely related but behave a bit differently depending on situation
- if you define float, you can get floor and ceil for free

```
[25]: from math import floor, ceil, trunc
      class Point:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __repr__(self):
              return f"<Point (x={self.x}, y={self.y})>"
          def __floor__(self):
              s = self.x + self.y
              return floor(s)
          def __ceil__(self):
              s = self.x + self.y
              return ceil(s)
          def __trunc__(self):
              return Point(trunc(self.x), trunc(self.y))
      p = Point(3.6, 2.7)
      print('floor(p)')
      print(floor(p))
      print("")
      print('ceil(p)')
      print(ceil(p))
      print("")
      print("trunc(p)")
      print(trunc(p))
     floor(p)
     ceil(p)
     trunc(p)
     <Point (x=3, y=2)>
```

0.13 Indexing

- we can use a custom object with indexing
- it would be intersting if we could index chars: letters['a':'c']
- __index__ has to return an index
- documentation says that you need to define int along with index

```
[28]: class Character:
    first = 'A'

    def __init__(self, char):
        self.char = char

def __repr__(self):
        return f'<Character ("{self.char}")>'

def __index__(self):
        return ord(self.char) - ord(self.__class__.first)

def __int__(self):
        return ord(self.char) - ord(self.__class__.first)

a = Character('A')
b = Character('B')
p = Character('P')

letters = 'ABCDEFGHIJKLMNOPQRSTUVWXYZ'
```

[28]: 'A'

0.14 Complex Numbers

- complex is a class
- complex(1) gives us (1+0j)

```
[29]: print(complex)
    print('')
    print('complex(1)')
    print(complex(1))
    print('')
    print('complex(1, 1)')
    print(complex(1, 1))
    print('')
    print('')
    print('complex(1) + complex(2, 3)')
```

```
print(complex(1) + complex(2, 3))
     <class 'complex'>
     complex(1)
     (1+0j)
     complex(1, 1)
     (1+1j)
     complex(1) + complex(2, 3)
     (3+3j)
[41]: from pprint import pprint
      from math import pi, cos, sin
      class Vector2D:
          def __init__(self, x, y):
              self.x = x
              self.y = y
          def __complex__(self):
              return complex(self.x, self.y)
      class Voltage:
          def __init__(self, base_voltage, frequency):
              self.base_voltage = base_voltage
              self.afrequency = 2 * pi * frequency
          def __complex__(self):
              \# assumption is time = 1
              real = cos(self.afrequency) * self.base_voltage
              imag = sin(self.afrequency) * self.base_voltage
              return complex(real, imag)
          def at(self, t=0):
              real = cos(self.afrequency * t) * self.base_voltage
              imag = sin(self.afrequency * t) * self.base_voltage
              return complex(real, imag)
      v = Voltage(120, 60)
      print('complex(v)')
      print(complex(v))
```

```
print('')
seconds = [s/len(seconds) for s in seconds]
results = [v.at(s) for s in seconds]
pprint(results)

complex(v)
(120-5.1740965224206694e-12j)

[(120+0j),
    (120-3.526982781544377e-13j),
    (120-7.053965563088754e-13j),
    (120-4.468699966111794e-12j),
    (120-1.4107931126177507e-12j)]
```