# a01-fnn

#### April 4, 2024

```
[1]: # Edited by: Kok Teng Ng (1936360), Minjeong Lee (1978925)
# IE 678 Deep Learning, University of Mannheim
# Author: Rainer Gemulla
```

```
[2]: %matplotlib ipympl

import math
import matplotlib.pyplot as plt
import torch
import torch.nn as nn
import torch.nn.functional as F

# import helper functions
import sys, os

sys.path.append(os.getcwd())
from a01helper import * # check out the helper functions there, if you like
```

Warning: Cannot change to a different GUI toolkit: notebook. Using ipympl instead.

# 1 Task 1: Implement an MLP

### 1.1 1a Logistic Regression

```
[3]: # nn.Module is the superclass of all PyTorch models.

class LogisticRegression(nn.Module):
    """A logistic regression model.

Parameters
    _____

D number of inputs
    C number of classes
    """

# the definition of all parameters the model uses happens here, i.e., during
    # initialization
    def __init__(self, D, C):
```

```
super(LogisticRegression, self).__init__()
             # Create and initialize model parameters. For (multinomial) logistic
      ⇔regression,
             \# we have a DxC-dimensional weight matrix W and a C-dimensional bias b.
             self.W = torch.randn(D, C) / math.sqrt(D)
             self.b = torch.randn(C) / math.sqrt(C)
             # Model parameters must be registered to PyTorch as follows. Here we_{f L}
      \hookrightarrowprovide
             # a useful name that helps to access/analyze the model later on.
             self.register_parameter("0_weight", nn.Parameter(self.W))
             self.register_parameter("0_bias", nn.Parameter(self.b))
         # the forward function computes the model output for the provided (for this
         # assignent: single) input
         def forward(self, x):
             eta = self.W.t() @ x + self.b
             logprob = F.log_softmax(eta, dim=-1)
             return logprob
[4]: # let's test it
     logreg = LogisticRegression(3, 2)
     x = torch.rand(3) # input
     logreg(x) # output (log probabilities)
     logreg(x).exp() # output (probabilities)
[4]: tensor([0.1429, 0.8571])
[5]: # you can access individual parameters as follows
     logreg.get_parameter("0_bias")
[5]: Parameter containing:
     tensor([0.0750, 0.1680], requires_grad=True)
[6]: # or all of them at once
     list(logreg.named_parameters())
[6]: [('0_weight',
      Parameter containing:
      tensor([[-1.1634, 0.1442],
               [0.9870, -0.0718],
               [-0.7443, 0.9194]], requires_grad=True)),
      ('0_bias',
      Parameter containing:
       tensor([0.0750, 0.1680], requires_grad=True))]
```

#### 1.2 1b MLP

```
[8]: class MLP(nn.Module):
          """A fully-connected MLP.
         Parameters
         sizes Contains the layer sizes. The first entry is the number of inputs, \Box
      \hookrightarrow the last
          entry the number of outputs. All entries in between correspond to the ⊔
      \hookrightarrow number of
          units in the respective hidden layer. E.q., [2,5,7,1] means: 2 inputs -> 5D_{\sqcup}
          layer -> 7D hidden layer -> 1 output.
         phi Activation function used in every hidden layer (the output layer is \Box
      \hookrightarrow linear).
          11 11 11
         def __init__(self, sizes: list[int], phi=F.sigmoid):
              super().__init__()
              # let's remember the specification in this model
              self.sizes = sizes
              self.phi = phi
              # Initialize and register the parameters. Follow the naming scheme used
       \hookrightarrow for
              # logistic regression above, i.e., the layer-i weights should be named_{f U}
       \rightarrow "i_weight" and
              # "i bias".
              for i in range(1, len(sizes)):
                   self.register_parameter(f'{i - 1}_weight', torch.nn.Parameter(torch.
       →randn(sizes[i - 1], sizes[i]) / math.sqrt(sizes[i - 1])))
                  self.register_parameter(f'{i - 1}_bias', torch.nn.Parameter(torch.
       →randn(sizes[i]) / math.sqrt(sizes[i])))
```

```
def num_layers(self):
              """Number of layers (excluding input layer)"""
              return len(self.sizes) - 1
          def forward(self, x):
              for i in range(0, self.num_layers() - 1):
                  weight = getattr(self, f"{i}_weight")
                  bias = getattr(self, f"{i} bias")
                  x = weight.t() @ x + bias
                  x = self.phi(x)
              weight = getattr(self, f"{self.num_layers() - 1}_weight")
              bias = getattr(self, f"{self.num_layers() - 1}_bias")
              x = weight.t() @ x + bias
              return x
 [9]: # here you should see the correct parameter sizes
      mlp = MLP([2, 3, 4, 2], torch.relu)
      list(mlp.named_parameters())
 [9]: [('0_weight',
       Parameter containing:
       tensor([[-0.5704, 0.5691, 1.5064],
                [-0.9854, -0.7690, -0.2701]], requires_grad=True)),
       ('0_bias',
       Parameter containing:
       tensor([ 0.6671, 0.0168, -0.4676], requires_grad=True)),
       ('1_weight',
       Parameter containing:
       tensor([[-0.8372, -0.3348, -0.9992, 0.2811],
                [0.1674, 0.1962, -0.2086, 0.0852],
                [ 0.1544, -0.7625, 0.0525, -0.5802]], requires_grad=True)),
       ('1_bias',
       Parameter containing:
       tensor([ 0.4051, -0.3382, 0.0240, 0.4486], requires_grad=True)),
       ('2_weight',
       Parameter containing:
       tensor([[-1.0556, 0.0663],
                [-0.4395, -0.8077],
                [-0.0792, 0.0922],
                [ 0.2066, 1.0688]], requires_grad=True)),
       ('2_bias',
       Parameter containing:
       tensor([-0.2358, -0.5284], requires_grad=True))]
[10]: # Test your code; we fix the parameters and check the result
      with torch.no_grad():
```

```
torch.manual_seed(0)
for l in range(mlp.num_layers()):
    W, b = mlp.get_parameter(f"{l}_weight"), mlp.get_parameter(f"{l}_bias")
    W[:] = torch.randn(W.shape)
    b[:] = torch.randn(b.shape)

mlp(torch.tensor([-1.0, 2.0])) # must give: [ 0.8315, -3.6792]
```

[10]: tensor([ 0.8315, -3.6792], grad\_fn=<AddBackward0>)

```
[11]: # You can also evaluate your model on multiple inputs at once. Here "torch.func.

ovmap"

# produces a function that applies the provided function (mlp#forward) to each

orow of

# its argument (torch.tensor...).

#

# [[ 0.8315, -3.6792],

# [ 4.8448, -6.8813]]

torch.func.vmap(mlp)(torch.tensor([[-1.0, 2.0], [1.0, -2.0]]))
```

#### 1.3 1c Batching

```
[12]: class MLP(nn.Module):
          def __init__(self, sizes: list[int], phi=F.sigmoid):
              super().__init__()
              self.sizes = sizes
              self.phi = phi
              for i in range(1, len(sizes)):
                  self.register_parameter(f'{i - 1}_weight', torch.nn.Parameter(torch.
       →randn(sizes[i - 1], sizes[i]) / math.sqrt(sizes[i - 1])))
                  self.register_parameter(f'{i - 1}_bias', torch.nn.Parameter(torch.
       →randn(sizes[i]) / math.sqrt(sizes[i])))
          def num_layers(self):
              return len(self.sizes) - 1
          def forward(self, x):
              if x.dim == 1:
                  x = x.unsqueeze(0)
              for i in range(0, self.num_layers() - 1):
                  weight = getattr(self, f"{i}_weight")
                  bias = getattr(self, f"{i}_bias")
```

```
x = x @ weight + bias.unsqueeze(0)
                  x = self.phi(x)
              weight = getattr(self, f"{self.num_layers() - 1}_weight")
              bias = getattr(self, f"{self.num_layers() - 1}_bias")
              x = x @ weight + bias.unsqueeze(0)
              return x
[13]: # here you should see the correct parameter sizes
      mlp = MLP([2, 3, 4, 2], torch.relu)
[14]: # Test your code; we fix the parameters and check the result
      with torch.no_grad():
          torch.manual_seed(0)
          for 1 in range(mlp.num_layers()):
              W, b = mlp.get_parameter(f"{1}_weight"), mlp.get_parameter(f"{1}_bias")
              W[:] = torch.randn(W.shape)
              b[:] = torch.randn(b.shape)
[15]: # After you adapted the MLP class, you should get the same results as above.
      mlp(torch.tensor([-1.0, 2.0])) # must give: [ 0.8315, -3.6792]
[15]: tensor([[ 0.8315, -3.6792]], grad_fn=<AddBackward0>)
[16]: # Now without umap. Only proceed to task 2 once this works correctly.
      # [[ 0.8315, -3.6792],
      # [ 4.8448, -6.8813]]
      mlp(torch.tensor([[-1.0, 2.0], [1.0, -2.0]]))
[16]: tensor([[ 0.8315, -3.6792],
```

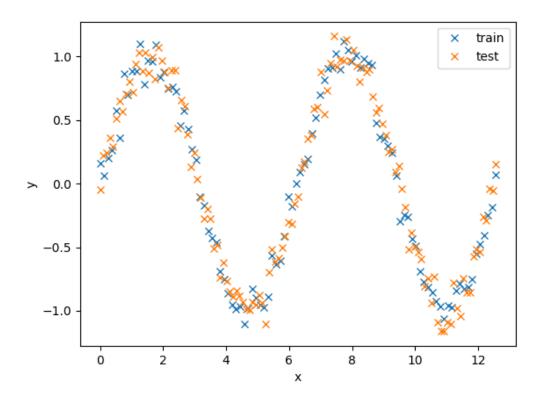
# 2 Multi-Layer Feed-Forward Neural Networks

[ 4.8448, -6.8813]], grad\_fn=<AddBackward0>)

### 2.1 2a Conjecture how an FNN fit will look like

```
[17]: # here is the one-dimensional dataset that we will use
nextplot()
plot1(X1, y1, label="train")
plot1(X1test, y1test, label="test")
plt.legend()
```

[17]: <matplotlib.legend.Legend at 0x17ec1a2e0>



#### 2.2 2b Train with 2 hidden units

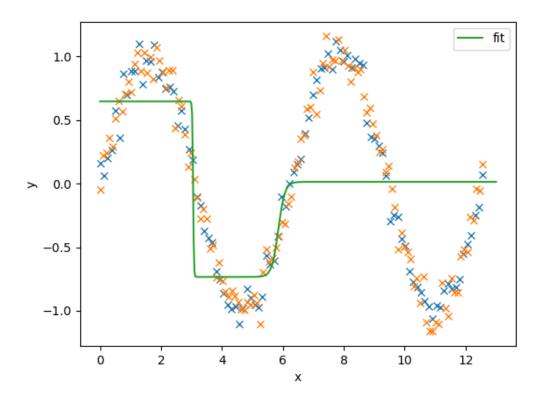
```
[18]: # Training code. You do not need to modify this code.
    train_bfgs = lambda model, **kwargs: train_scipy(X1, y1, model, **kwargs)

def train1(hidden_sizes, nreps=10, phi=F.sigmoid, train=train_bfgs, **kwargs):
    """Train an FNN.

    hidden_sizes is a (possibly empty) list containing the sizes of the hidden_dayer(s).
    nreps refers to the number of repetitions.
    """

    best_model = None
    best_cost = math.inf
    for rep in range(nreps):
        model = MLP([1] + hidden_sizes + [1], phi) # that's your model!
        print(f"X1 shape: {X1.shape}")
```

```
print(f"Repetition {rep: 2d}: ", end="")
              model = train(model, **kwargs)
              mse = F.mse_loss(y1, model(X1)).item()
              if mse < best_cost:</pre>
                  best_model = model
                  best_cost = mse
              print(f"best_cost={best_cost:.3f}")
          return best_model
[19]: # Let's fit the model with one hidden layer consisting of 2 units.
      model = train1([2], nreps=1)
      print("Training error:", F.mse_loss(y1, model(X1)).item())
      print("Test error :", F.mse_loss(y1test, model(X1test)).item())
     X1 shape: torch.Size([100, 1])
     Repetition 0: Optimization terminated successfully.
              Current function value: 0.293673
              Iterations: 120
              Function evaluations: 240
              Gradient evaluations: 233
     best_cost=0.294
     Training error: 0.29367321729660034
     Test error : 0.30551230907440186
[20]: # plot the data and the fit
     nextplot()
      plot1(X1, y1, label="train")
      plot1(X1test, y1test, label="test")
      plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model)
```



```
[21]: # The weight matrices and bias vectors can be read out as follows. If you want,
       use
      # these parameters to compute the output of the network (on X1) directly and
      ⇔compare to
      # vmap(model)(X1).
      for par, value in model.state_dict().items():
          print(f"{par:<15}= {value}")</pre>
     0_{weight}
                    = tensor([[75.7091, 9.2566]])
                    = tensor([-231.3285, -54.1847])
     0_bias
                    = tensor([[-1.3810],
     1_weight
             [ 0.7480]])
                    = tensor([0.6471])
     1_bias
[22]: # now repeat this multiple times
      for i in range (0, 5):
          model = train1([2], nreps=1)
          print("Training error:", F.mse_loss(y1, model(X1)).item())
          print("Test error :", F.mse_loss(y1test, model(X1test)).item())
          nextplot()
          plot1(X1, y1, label="train")
```

```
plot1(X1test, y1test, label="test")
    plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model)
X1 shape: torch.Size([100, 1])
Repetition 0:
                        Current function value: 0.079572
         Iterations: 387
         Function evaluations: 521
         Gradient evaluations: 511
best_cost=0.080
Training error: 0.07957355678081512
Test error
              : 0.08671201020479202
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
X1 shape: torch.Size([100, 1])
Repetition 0: Optimization terminated successfully.
         Current function value: 0.303902
         Iterations: 143
         Function evaluations: 155
         Gradient evaluations: 155
best cost=0.304
Training error: 0.30390220880508423
Test error
             : 0.3037970960140228
X1 shape: torch.Size([100, 1])
Repetition 0:
                        Current function value: 0.079573
         Iterations: 400
         Function evaluations: 562
         Gradient evaluations: 551
best_cost=0.080
Training error: 0.07957581430673599
Test error
              : 0.0867120772600174
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
X1 shape: torch.Size([100, 1])
                        Current function value: 0.286909
Repetition 0:
         Iterations: 302
         Function evaluations: 458
         Gradient evaluations: 445
best_cost=0.287
```

Training error: 0.28690817952156067 Test error : 0.29484879970550537

X1 shape: torch.Size([100, 1])

Repetition 0: Current function value: 0.079573

Iterations: 336

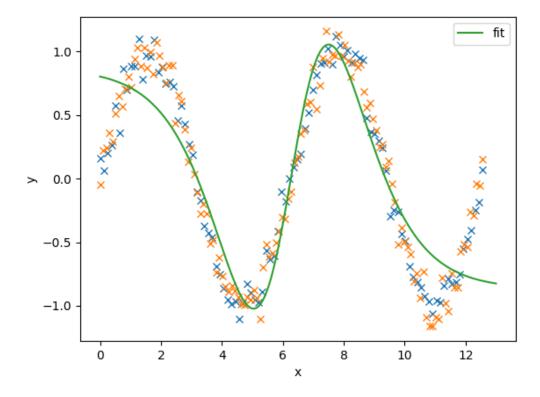
Function evaluations: 470 Gradient evaluations: 458

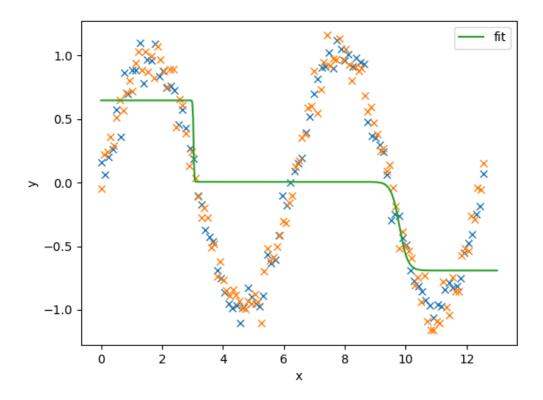
best\_cost=0.080

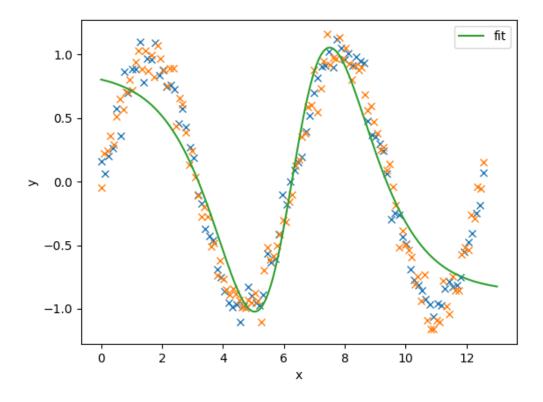
Training error: 0.07956987619400024 Test error : 0.0867103710770607

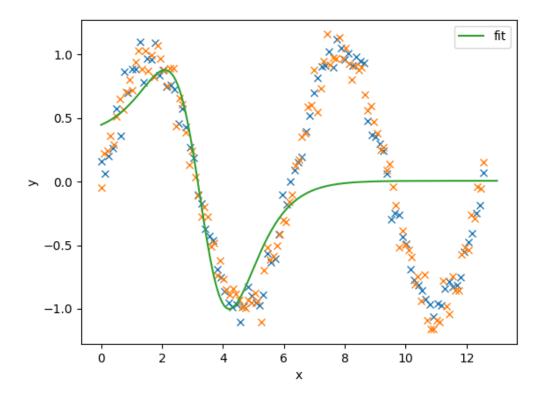
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

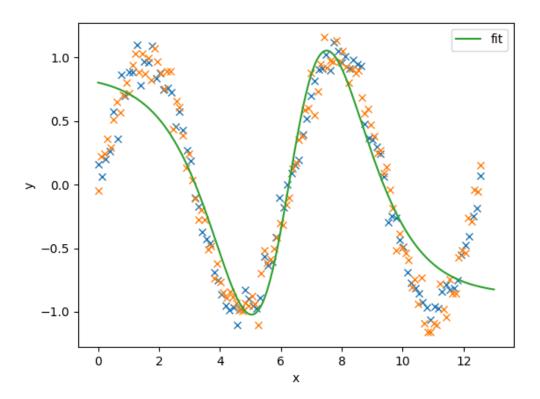
res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)











```
[23]: # From now on, always train multiple times (nreps=10 by default) and report
       \hookrightarrow best model.
      model = train1([2], nreps=10)
      print("Training error:", F.mse_loss(y1, model(X1)).item())
                            :", F.mse_loss(y1test, model(X1test)).item())
      print("Test error
     X1 shape: torch.Size([100, 1])
     Repetition 0: Optimization terminated successfully.
              Current function value: 0.357250
              Iterations: 66
              Function evaluations: 76
              Gradient evaluations: 76
     best_cost=0.357
     X1 shape: torch.Size([100, 1])
     Repetition 1:
                              Current function value: 0.438546
              Iterations: 278
              Function evaluations: 398
              Gradient evaluations: 386
     best_cost=0.357
     X1 shape: torch.Size([100, 1])
```

#### Repetition 2:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.286909

Iterations: 448

Function evaluations: 577 Gradient evaluations: 565

best\_cost=0.287

X1 shape: torch.Size([100, 1])

Repetition 3: Current function value: 0.079573

Iterations: 310

Function evaluations: 459
Gradient evaluations: 449

best cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 4:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.286909

Iterations: 307

Function evaluations: 413 Gradient evaluations: 401

best cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 5: Current function value: 0.286909

Iterations: 534

Function evaluations: 690 Gradient evaluations: 681

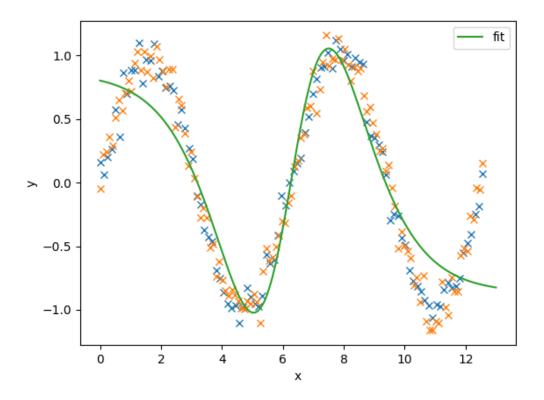
best\_cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 6:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not

```
necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
              Current function value: 0.079573
              Iterations: 330
              Function evaluations: 470
              Gradient evaluations: 458
     best_cost=0.080
     X1 shape: torch.Size([100, 1])
                             Current function value: 0.079573
     Repetition 7:
              Iterations: 381
              Function evaluations: 537
              Gradient evaluations: 524
     best_cost=0.080
     X1 shape: torch.Size([100, 1])
     Repetition 8: Optimization terminated successfully.
              Current function value: 0.357250
              Iterations: 78
              Function evaluations: 80
              Gradient evaluations: 80
     best cost=0.080
     X1 shape: torch.Size([100, 1])
                             Current function value: 0.286909
     Repetition 9:
              Iterations: 324
              Function evaluations: 546
              Gradient evaluations: 533
     best_cost=0.080
     Training error: 0.07957330346107483
     Test error
                   : 0.0867152065038681
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
[24]: # plot the data and the fit
      nextplot()
      plot1(X1, y1, label="train")
      plot1(X1test, y1test, label="test")
      plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model)
```



### 2.3 2c Width

```
[25]: # Experiment with different hidden layer sizes. To avoid recomputing
    # models, you may want to save your models using torch.save(model, filename) and
    # load them again using torch.load(filename).

for i in [1, 2, 3, 10, 50, 100]:
    model = train1([i], nreps = 1)
    print("Training error:", F.mse_loss(y1, model(X1)).item())
    print("Test error :", F.mse_loss(y1test, model(X1test)).item())
    torch.save(model, f"model_{i}.pth")
```

X1 shape: torch.Size([100, 1])

Repetition 0: Optimization terminated successfully.

Current function value: 0.372919

Iterations: 42

Function evaluations: 47 Gradient evaluations: 47

best\_cost=0.373

Training error: 0.3729189336299896 Test error : 0.3743167221546173 X1 shape: torch.Size([100, 1]) Current function value: 0.079573 Repetition 0: Iterations: 390 Function evaluations: 593 Gradient evaluations: 583 best\_cost=0.080 Training error: 0.07957376539707184 Test error : 0.08670931309461594 X1 shape: torch.Size([100, 1]) Repetition 0: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.049892 Iterations: 289 Function evaluations: 469 Gradient evaluations: 456 best\_cost=0.050 Training error: 0.04989229515194893 Test error : 0.0598050132393837 X1 shape: torch.Size([100, 1]) Repetition 0: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.005721 Iterations: 1026 Function evaluations: 1250 Gradient evaluations: 1234 best\_cost=0.006 Training error: 0.0057213036343455315 Test error : 0.0150537034496665 X1 shape: torch.Size([100, 1]) Repetition 0: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.003007

Iterations: 5655

Function evaluations: 6282 Gradient evaluations: 6268

best\_cost=0.003

Training error: 0.0030068017076700926 Test error : 2.0873610973358154 X1 shape: torch.Size([100, 1])

Repetition 0: Current function value: 0.001826

Iterations: 8126

Function evaluations: 8804 Gradient evaluations: 8792

best\_cost=0.002

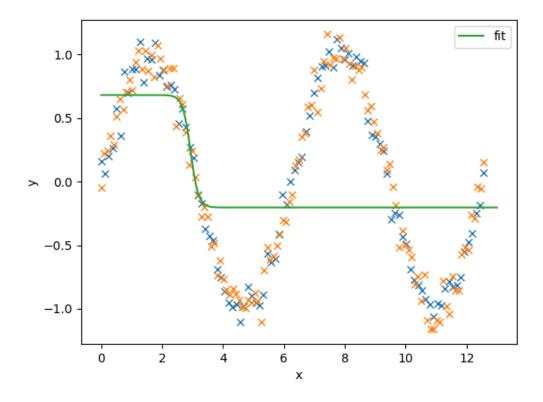
Training error: 0.001825749408453703 Test error : 4.303783893585205

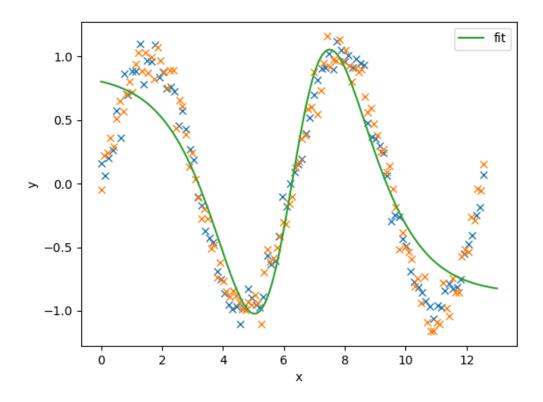
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

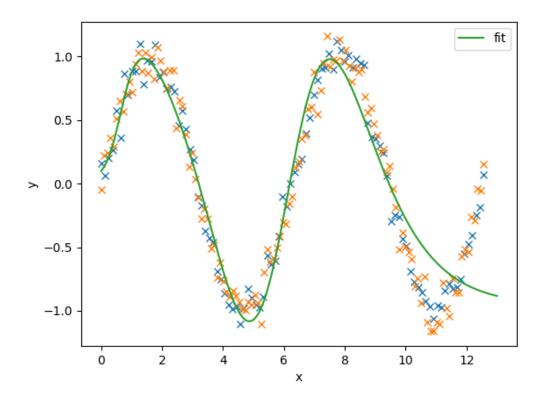
res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

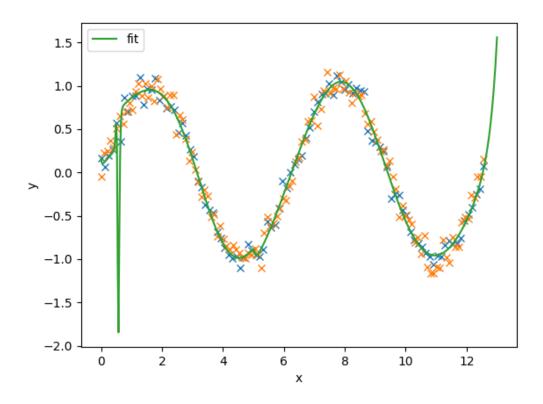
```
[26]: # torch.load(filename)

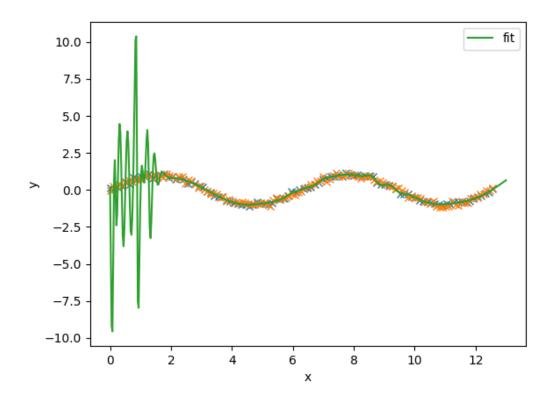
for i in [1, 2, 3, 10, 50, 100]:
    model = torch.load(f"model_{i}.pth")
    nextplot()
    plot1(X1, y1, label="train")
    plot1(X1test, y1test, label="test")
    plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model)
```

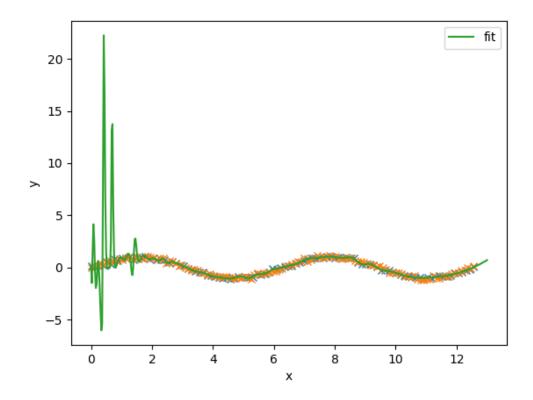












## 2.4 2d Distributed representations

```
[27]: # train a model to analyze
     model = train1([2])
     X1 shape: torch.Size([100, 1])
     Repetition 0:
                             Current function value: 0.079573
              Iterations: 399
              Function evaluations: 542
              Gradient evaluations: 533
     best_cost=0.080
     X1 shape: torch.Size([100, 1])
     Repetition 1: Optimization terminated successfully.
              Current function value: 0.301865
              Iterations: 131
              Function evaluations: 161
              Gradient evaluations: 161
     best_cost=0.080
     X1 shape: torch.Size([100, 1])
     Repetition 2:
```

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.079573

Iterations: 384

Function evaluations: 538 Gradient evaluations: 526

best cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 3: Current function value: 0.079573

Iterations: 379

Function evaluations: 534 Gradient evaluations: 523

best\_cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 4: Optimization terminated successfully.

Current function value: 0.372457

Iterations: 131

Function evaluations: 137 Gradient evaluations: 137

best\_cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 5:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.079573

Iterations: 402

Function evaluations: 536 Gradient evaluations: 525

best\_cost=0.080

X1 shape: torch.Size([100, 1])

Repetition 6: Optimization terminated successfully.

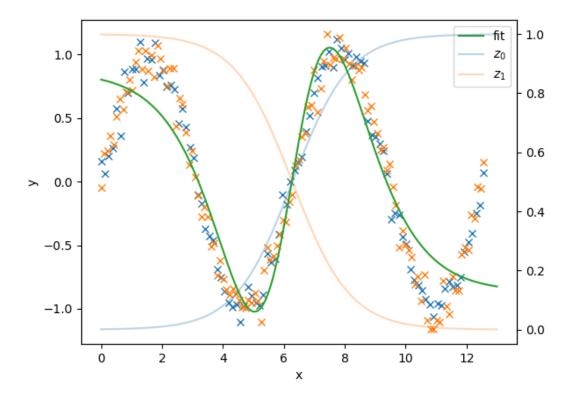
Current function value: 0.277769

Iterations: 86

Function evaluations: 97

```
best_cost=0.080
     X1 shape: torch.Size([100, 1])
     Repetition 7: Optimization terminated successfully.
              Current function value: 0.357250
              Iterations: 85
              Function evaluations: 90
              Gradient evaluations: 90
     best cost=0.080
     X1 shape: torch.Size([100, 1])
                             Current function value: 0.079572
     Repetition 8:
              Iterations: 392
              Function evaluations: 619
              Gradient evaluations: 605
     best_cost=0.080
     X1 shape: torch.Size([100, 1])
     Repetition 9:
                             Current function value: 0.079573
              Iterations: 403
              Function evaluations: 646
              Gradient evaluations: 633
     best cost=0.080
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
[28]: # plot the fit as well as the outputs of each neuron in the hidden
      # layer (scale for the latter is shown on right y-axis)
      nextplot()
      plot1(X1, y1, label="train")
      plot1(X1test, y1test, label="test")
      plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model, hidden=True,
       ⇔scale=False)
```

Gradient evaluations: 97



# [29]: # train a model to analyze model = train1([3])

X1 shape: torch.Size([100, 1])

Repetition 0: Current function value: 0.007324

Iterations: 422

Function evaluations: 535 Gradient evaluations: 523

best\_cost=0.007

X1 shape: torch.Size([100, 1])

Repetition 1:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.079572

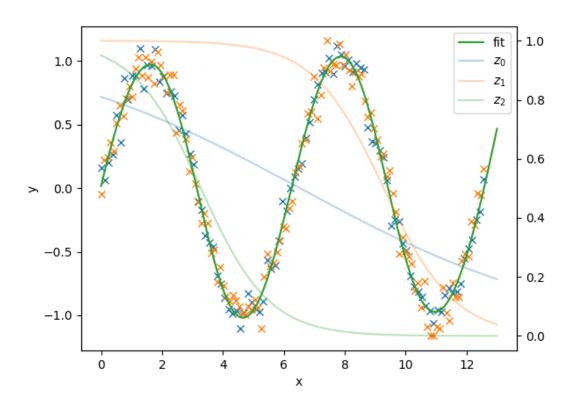
Iterations: 397 Function evaluations: 577 Gradient evaluations: 565 best cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 2: Current function value: 0.007324 Iterations: 543 Function evaluations: 689 Gradient evaluations: 677 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 3: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.049886 Iterations: 317 Function evaluations: 514 Gradient evaluations: 503 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 4: Optimization terminated successfully. Current function value: 0.042560 Iterations: 155 Function evaluations: 172 Gradient evaluations: 172 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 5: Current function value: 0.079573 Iterations: 364 Function evaluations: 561 Gradient evaluations: 548 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 6: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not

```
necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
              Current function value: 0.079573
              Iterations: 343
              Function evaluations: 561
              Gradient evaluations: 548
     best cost=0.007
     X1 shape: torch.Size([100, 1])
     Repetition 7:
                             Current function value: 0.049901
              Iterations: 221
              Function evaluations: 320
              Gradient evaluations: 308
     best cost=0.007
     X1 shape: torch.Size([100, 1])
     Repetition 8:
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
              Current function value: 0.049877
              Iterations: 563
              Function evaluations: 811
              Gradient evaluations: 799
     best_cost=0.007
     X1 shape: torch.Size([100, 1])
     Repetition 9:
                             Current function value: 0.053823
              Iterations: 540
              Function evaluations: 743
              Gradient evaluations: 728
     best_cost=0.007
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
     /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
     packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
     necessarily achieved due to precision loss.
       res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
[30]: # plot the fit as well as the outputs of each neuron in the hidden
      # layer (scale for the latter is shown on right y-axis)
      nextplot()
      plot1(X1, y1, label="train")
      plot1(X1test, y1test, label="test")
```

plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model, hidden=True, ⊔
⇒scale=False)



```
[31]: # train a model to analyze
model = train1([10])
```

X1 shape: torch.Size([100, 1])
Repetition 0:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.006069

Iterations: 2361

Function evaluations: 2702 Gradient evaluations: 2683

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Repetition 1:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.006260

Iterations: 2624

Function evaluations: 3005 Gradient evaluations: 2995

best cost=0.006

X1 shape: torch.Size([100, 1])

Repetition 2: Current function value: 0.006688

Iterations: 587

Function evaluations: 696 Gradient evaluations: 686

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Repetition 3:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.006667

Iterations: 1257

Function evaluations: 1487 Gradient evaluations: 1475

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Repetition 4:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

Current function value: 0.006232

Iterations: 1648

Function evaluations: 1908 Gradient evaluations: 1897

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Repetition 5:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/minimize.py:708: OptimizeWarning: Desired error not

```
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.006114
         Iterations: 1489
         Function evaluations: 1719
         Gradient evaluations: 1707
best cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 6:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.006576
         Iterations: 2629
         Function evaluations: 2955
         Gradient evaluations: 2945
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 7:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.006076
         Iterations: 1852
         Function evaluations: 2128
         Gradient evaluations: 2116
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 8:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.006614
         Iterations: 2289
         Function evaluations: 2825
         Gradient evaluations: 2807
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 9:
                        Current function value: 0.006805
         Iterations: 1034
         Function evaluations: 1288
```

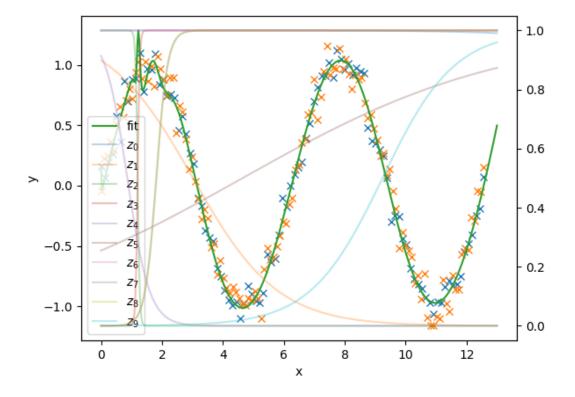
Gradient evaluations: 1275
best\_cost=0.006

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)

```
[32]: # plot the fit as well as the outputs of each neuron in the hidden
# layer (scale for the latter is shown on right y-axis)
nextplot()
plot1(X1, y1, label="train")
plot1(X1test, y1test, label="test")
plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model, hidden=True,

→scale=False)
```

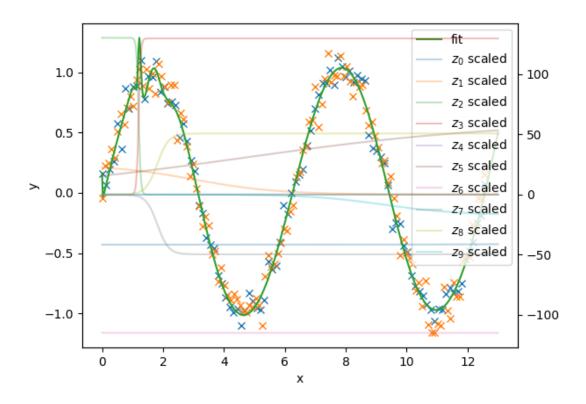


```
[33]: # plot the fit as well as the outputs of each neuron in the hidden layer, scaled # by its weight for the output neuron (scale for the latter is shown on right # y-axis)

nextplot()
```

```
plot1(X1, y1, label="train")
plot1(X1test, y1test, label="test")
plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model, hidden=True,

⇔scale=True)
```



## 2.5 2e Experiment with different optimizers (optional)

0: cost=

0.547

0.508

Repetition 0: Epoch

1: cost=

2: cost=

Epoch

Epoch

0.561

Epoch	3:	cost=	0.491
Epoch	4:	cost=	0.482
Epoch	5:	cost=	0.464
Epoch	6:	cost=	0.450
Epoch	7:	cost=	0.447
Epoch	8:	cost=	0.445
Epoch	9:	cost=	0.439
Epoch	10:	cost=	0.437
Epoch	11:	cost=	0.440
Epoch	12:	cost=	0.443
Epoch	13:	cost=	0.443
Epoch	14:	cost=	0.443
Epoch	15:	cost=	0.445
Epoch	16:	cost=	0.446
Epoch	17:	cost=	0.445
Epoch	18:	cost=	0.443
Epoch	19:	cost=	0.441
Epoch	20:	cost=	0.441
Epoch	21:	cost=	0.438
Epoch	22:	cost=	0.436
Epoch	23:	cost=	0.434
Epoch	24:	cost=	0.433
Epoch	25:	cost=	0.431
Epoch	26:	cost=	0.430
Epoch	27:	cost=	0.429
Epoch	28:	cost=	0.428
Epoch	29:	cost=	0.428
Epoch	30:	cost=	0.428
Epoch	31:	cost=	0.427
Epoch	32:	cost=	0.427
Epoch	33:	cost=	0.427
Epoch	34:	cost=	0.426
Epoch	35:	cost=	0.426
Epoch	36:	cost=	0.425
Epoch	37:	cost=	0.425
Epoch	38:	cost=	0.424
Epoch	39:	cost=	0.423
Epoch	40:	cost=	0.422
Epoch	41:	cost=	0.421
Epoch	42:	cost=	0.421
Epoch	43:	cost=	0.420
Epoch	44:	cost=	0.419
Epoch	45:	cost=	0.419
Epoch	46:	cost=	0.418
Epoch	47:	cost=	0.418
Epoch	48:	cost=	0.417
Epoch	49:	cost=	0.417
Epoch	50:	cost=	0.416

Epoch	51:	cost=	0.416
Epoch	52:	cost=	0.415
Epoch	53:	cost=	0.415
Epoch	54:	cost=	0.414
Epoch	55:	cost=	0.414
Epoch	56:	cost=	0.413
Epoch	57:	cost=	0.412
Epoch	58:	cost=	0.412
Epoch	59:	cost=	0.411
Epoch	60:	cost=	0.411
Epoch	61:	cost=	0.410
Epoch	62:	cost=	0.410
Epoch	63:	cost=	0.409
Epoch	64:	cost=	0.409
Epoch	65:	cost=	0.408
Epoch	66:	cost=	0.408
Epoch	67:	cost=	0.407
Epoch	68:	cost=	0.407
Epoch	69:	cost=	0.406
Epoch	70:	cost=	0.406
Epoch	71:	cost=	0.405
Epoch	72:	cost=	0.405
Epoch	73:	cost=	0.404
Epoch	74:	cost=	0.403
Epoch	75:	cost=	0.403
Epoch	76:	cost=	0.402
Epoch	77:	cost=	0.402
Epoch	78:	cost=	0.401
Epoch	79:	cost=	0.401
Epoch	80:	cost=	0.400
Epoch	81:	cost=	0.400
Epoch	82:	cost=	0.399
Epoch	83:	cost=	0.399
Epoch	84:	cost=	0.398
Epoch	85:	cost=	0.398
Epoch	86:	cost=	0.397
Epoch	87:	cost=	0.397
Epoch	88:	cost=	0.396
Epoch	89:	cost=	0.396
Epoch	90:	cost=	0.395
Epoch	91:	cost=	0.395
Epoch	92:	cost=	0.394
Epoch	93:	cost=	0.394
Epoch	94:	cost=	0.393
Epoch	95:	cost=	0.393
Epoch	96:	cost=	0.393
Epoch	97:	cost=	0.392
Epoch	98:	cost=	0.392

Epoch	99:	cost=	0.391
Epoch	100:	cost=	0.391
Epoch	101:	cost=	0.390
Epoch	102:	cost=	0.390
Epoch	103:	cost=	0.389
Epoch	104:	cost=	0.389
Epoch	105:	cost=	0.388
Epoch	106:	cost=	0.388
Epoch	107:	cost=	0.387
Epoch	108:	cost=	0.387
Epoch	109:	cost=	0.386
Epoch	110:	cost=	0.386
Epoch	111:	cost=	0.386
Epoch	112:	cost=	0.385
Epoch	113:	cost=	0.385
Epoch	114:	cost=	0.384
Epoch	115:	cost=	0.384
Epoch	116:	cost=	0.383
Epoch	117:	cost=	0.383
Epoch	118:	cost=	0.382
Epoch	119:	cost=	0.382
Epoch	120:	cost=	0.382
Epoch	121:	cost=	0.381
Epoch	122:	cost=	0.381
Epoch	123:	cost=	0.380
Epoch	124:	cost=	0.380
Epoch	125:	cost=	0.379
Epoch	126:	cost=	0.379
Epoch	127:	cost=	0.379
Epoch	128:	cost=	0.378
Epoch	129:	cost=	0.378
Epoch	130:	cost=	0.377
Epoch	131:	cost=	0.377
Epoch	132:	cost=	0.377
Epoch	133:	cost=	0.376
Epoch	134:	cost=	0.376
Epoch	135:	cost=	0.375
Epoch	136:	cost=	0.375
Epoch	137:	cost=	0.374
Epoch	138:	cost=	0.374
Epoch	139:	cost=	0.374
Epoch	140:	cost=	0.373
Epoch	141:	cost=	0.373
Epoch	142:	cost=	0.372
Epoch	143:	cost=	0.372
Epoch	144:	cost=	0.371
Epoch	145:	cost=	0.371
Epoch	146:	cost=	0.371

Epoch	147:	cost=	0.370
Epoch	148:	cost=	0.370
Epoch	149:	cost=	0.369
Epoch	150:	cost=	0.369
Epoch	151:	cost=	0.368
Epoch	152:	cost=	0.368
Epoch	153:	cost=	0.368
Epoch	154:	cost=	0.367
Epoch	155:	cost=	0.367
Epoch	156:	cost=	0.366
Epoch	157:	cost=	0.366
Epoch	158:	cost=	0.365
Epoch	159:	cost=	0.365
Epoch	160:	cost=	0.364
Epoch	161:	cost=	0.364
Epoch	162:	cost=	0.363
Epoch	163:	cost=	0.363
Epoch	164:	cost=	0.363
Epoch	165:	cost=	0.362
Epoch	166:	cost=	0.362
Epoch	167:	cost=	0.361
Epoch	168:	cost=	0.361
Epoch	169:	cost=	0.360
Epoch	170:	cost=	0.360
Epoch	171:	cost=	0.359
Epoch	172:	cost=	0.359
Epoch	173:	cost=	0.358
Epoch	174:	cost=	0.357
Epoch	175:	cost=	0.357
Epoch	176:	cost=	0.356
Epoch	177:	cost=	0.356
Epoch	178:	cost=	0.355
Epoch	179:	cost=	0.355
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Epoch	3320:	cost=	0.009
Epoch	3321:	cost=	0.010
Epoch	3322:	cost=	0.011
Epoch	3323:	cost=	0.012
Epoch	3324:	cost=	0.012
Epoch	3325:	cost=	0.011
Epoch	3326:	cost=	0.009
Epoch	3327:	cost=	0.007
Epoch	3328:	cost=	0.007
Epoch	3329:	cost=	0.008
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Epoch 3364: cost=
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     Epoch 3365: cost=
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            3366: cost=
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            3368: cost=
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     Epoch 3398: cost=
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     Epoch 3399: cost=
                          0.007
     Epoch 3400: cost=
                          0.007
     best_cost=0.007
[35]: # Experiment with different number of layers and activation functions. Here is
      # an example with three hidden layers (of sizes 4, 5, and 6) and ReLU _{\!\!\!\! \sqcup}
       ⇔activations.
      #
      # You can also plot the outputs of the hidden neurons in the first layer (using
      # the same code above).
      model = train1([4, 5, 6], nreps=50, phi=F.relu)
```

Epoch 3363: cost=

0.007

```
nextplot()
plot1(X1, y1, label="train")
plot1(X1test, y1test, label="test")
plot1fit(torch.linspace(0, 13, 500).unsqueeze(1), model)
print("Training error:", F.mse_loss(y1, model(X1)).item())
                     :", F.mse_loss(y1test, model(X1test)).item())
print("Test error
X1 shape: torch.Size([100, 1])
Repetition 0:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.027642
         Iterations: 106
         Function evaluations: 226
         Gradient evaluations: 221
best_cost=0.028
X1 shape: torch.Size([100, 1])
                        Current function value: 0.372736
Repetition 1:
         Iterations: 20
         Function evaluations: 93
         Gradient evaluations: 89
best_cost=0.028
X1 shape: torch.Size([100, 1])
                        Current function value: 0.082316
Repetition 2:
         Iterations: 77
         Function evaluations: 175
         Gradient evaluations: 169
best_cost=0.028
X1 shape: torch.Size([100, 1])
Repetition 3:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
```

necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.372829 Iterations: 54 Function evaluations: 224 Gradient evaluations: 219 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 4: Current function value: 0.356289 Iterations: 62 Function evaluations: 159 Gradient evaluations: 151 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Current function value: 0.436769 Repetition 5: Iterations: 19 Function evaluations: 107 Gradient evaluations: 98 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 6: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.082545 Iterations: 87 Function evaluations: 201 Gradient evaluations: 196 best cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 7: Current function value: 0.355800 Iterations: 47 Function evaluations: 226 Gradient evaluations: 220 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 8:

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.098439 Iterations: 131 Function evaluations: 239 Gradient evaluations: 227 best cost=0.028 X1 shape: torch.Size([100, 1]) Current function value: 0.355687 Repetition 9: Iterations: 139 Function evaluations: 261 Gradient evaluations: 257 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 10: Optimization terminated successfully. Current function value: 0.101445 Iterations: 53 Function evaluations: 66 Gradient evaluations: 66 best\_cost=0.028 X1 shape: torch.Size([100, 1]) Repetition 11: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = minimize bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.356116 Iterations: 52 Function evaluations: 161

Gradient evaluations: 155

X1 shape: torch.Size([100, 1])

best\_cost=0.028

```
Repetition 12:
                         Current function value: 0.435001
         Iterations: 46
         Function evaluations: 123
         Gradient evaluations: 119
best cost=0.028
X1 shape: torch.Size([100, 1])
Repetition 13:
                         Current function value: 0.435068
         Iterations: 41
         Function evaluations: 131
         Gradient evaluations: 125
best_cost=0.028
X1 shape: torch.Size([100, 1])
Repetition 14:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = minimize bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.007341
         Iterations: 212
         Function evaluations: 447
         Gradient evaluations: 433
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 15:
                         Current function value: 0.355830
         Iterations: 46
         Function evaluations: 140
         Gradient evaluations: 135
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 16:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.353423
         Iterations: 154
         Function evaluations: 435
         Gradient evaluations: 415
```

best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 17: Current function value: 0.405736 Iterations: 15 Function evaluations: 95 Gradient evaluations: 90 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 18: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = minimize bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.085500 Iterations: 113 Function evaluations: 241 Gradient evaluations: 234 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Current function value: 0.082287 Repetition 19: Iterations: 96 Function evaluations: 187 Gradient evaluations: 183 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Current function value: 0.434775 Repetition 20: Iterations: 18 Function evaluations: 113 Gradient evaluations: 102 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 21: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-

packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not

```
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.356477
         Iterations: 34
         Function evaluations: 122
         Gradient evaluations: 118
best_cost=0.007
X1 shape: torch.Size([100, 1])
                         Current function value: 0.355919
Repetition 22:
         Iterations: 54
         Function evaluations: 154
         Gradient evaluations: 149
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 23:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.008464
         Iterations: 251
         Function evaluations: 460
         Gradient evaluations: 451
best_cost=0.007
X1 shape: torch.Size([100, 1])
                         Current function value: 0.008703
Repetition 24:
         Iterations: 185
         Function evaluations: 276
         Gradient evaluations: 270
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 25:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
```

```
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.355581
         Iterations: 138
         Function evaluations: 261
         Gradient evaluations: 255
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 26:
                         Current function value: 0.085421
         Iterations: 55
         Function evaluations: 161
         Gradient evaluations: 155
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 27:
                         Current function value: 0.357612
         Iterations: 46
         Function evaluations: 123
         Gradient evaluations: 116
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 28:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.434378
         Iterations: 34
         Function evaluations: 122
         Gradient evaluations: 116
best_cost=0.007
X1 shape: torch.Size([100, 1])
                        Current function value: 0.083644
Repetition 29:
         Iterations: 205
         Function evaluations: 328
         Gradient evaluations: 323
best_cost=0.007
X1 shape: torch.Size([100, 1])
Repetition 30:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
```

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.434433 Iterations: 28 Function evaluations: 111 Gradient evaluations: 107 best cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 31: Current function value: 0.356297 Iterations: 72 Function evaluations: 166 Gradient evaluations: 161 best\_cost=0.007 X1 shape: torch.Size([100, 1]) Repetition 32: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.005862 Iterations: 382 Function evaluations: 528 Gradient evaluations: 523

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Current function value: 0.308671 Repetition 33:

Iterations: 68

Function evaluations: 180 Gradient evaluations: 175

best\_cost=0.006

X1 shape: torch.Size([100, 1])

Current function value: 0.436922 Repetition 34:

Iterations: 60

Function evaluations: 163 Gradient evaluations: 155

best\_cost=0.006

```
X1 shape: torch.Size([100, 1])
Repetition 35:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.435347
         Iterations: 37
        Function evaluations: 109
        Gradient evaluations: 101
best cost=0.006
X1 shape: torch.Size([100, 1])
                         Current function value: 0.371726
Repetition 36:
         Iterations: 35
        Function evaluations: 118
        Gradient evaluations: 113
best_cost=0.006
X1 shape: torch.Size([100, 1])
                         Current function value: 0.008174
Repetition 37:
         Iterations: 108
        Function evaluations: 221
         Gradient evaluations: 217
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 38:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
  res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.355790
```

Iterations: 129 Function evaluations: 232 Gradient evaluations: 227 best\_cost=0.006 X1 shape: torch.Size([100, 1]) Repetition 39: Optimization terminated successfully. Current function value: 0.435275 Iterations: 35 Function evaluations: 52 Gradient evaluations: 52 best\_cost=0.006 X1 shape: torch.Size([100, 1]) Current function value: 0.435287 Repetition 40: Iterations: 18 Function evaluations: 99 Gradient evaluations: 94 best\_cost=0.006 X1 shape: torch.Size([100, 1]) Repetition 41: Current function value: 0.372387 Iterations: 57 Function evaluations: 177 Gradient evaluations: 173 best\_cost=0.006 X1 shape: torch.Size([100, 1]) Repetition 42: /Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/sitepackages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss. res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options) Current function value: 0.356134 Iterations: 110 Function evaluations: 214 Gradient evaluations: 209 best cost=0.006 X1 shape: torch.Size([100, 1]) Repetition 43: Optimization terminated successfully. Current function value: 0.098100 Iterations: 147 Function evaluations: 169 Gradient evaluations: 169 best\_cost=0.006

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

X1 shape: torch.Size([100, 1])

Repetition 44:

```
res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/ minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.356624
         Iterations: 28
         Function evaluations: 115
         Gradient evaluations: 103
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 45: Optimization terminated successfully.
         Current function value: 0.506238
         Iterations: 14
         Function evaluations: 16
         Gradient evaluations: 16
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 46:
                         Current function value: 0.092225
         Iterations: 89
         Function evaluations: 209
         Gradient evaluations: 204
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 47:
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-
packages/scipy/optimize/_minimize.py:708: OptimizeWarning: Desired error not
necessarily achieved due to precision loss.
 res = _minimize_bfgs(fun, x0, args, jac, callback, **options)
         Current function value: 0.355652
         Iterations: 168
         Function evaluations: 310
         Gradient evaluations: 306
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 48:
                         Current function value: 0.008766
         Iterations: 145
         Function evaluations: 251
         Gradient evaluations: 243
best_cost=0.006
X1 shape: torch.Size([100, 1])
Repetition 49:
                        Current function value: 0.007130
```

Iterations: 196

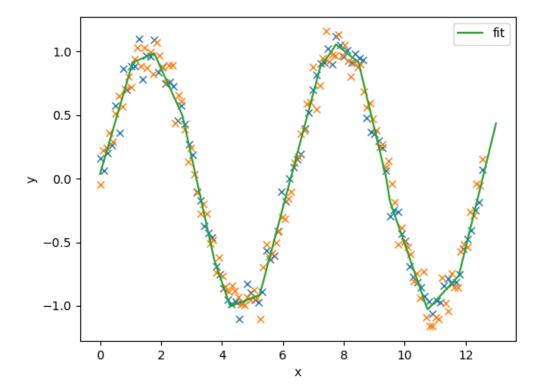
Function evaluations: 295 Gradient evaluations: 288

best\_cost=0.006

Training error: 0.005861788988113403 Test error : 0.010837704874575138

/Users/ngkokteng/PycharmProjects/Deep Learning/.venv/lib/python3.9/site-packages/scipy/optimize/\_minimize.py:708: OptimizeWarning: Desired error not necessarily achieved due to precision loss.

res = \_minimize\_bfgs(fun, x0, args, jac, callback, \*\*options)



## 3 Backpropagation

```
[]: # Let's fit the model with one hidden layer consisting of 50 units.
model = train1([50], nreps=1)
print("Training error:", F.mse_loss(y1, model(X1)).item())
print("Test error :", F.mse_loss(y1test, model(X1test)).item())
# Extract parameters
```

```
pars = dict(model.named_parameters())
W1 = pars["0_weight"].data # 1x50
b1 = pars["0_bias"].data # 50
W2 = pars["1_weight"].data # 50x1
b2 = pars["1_bias"].data # 1
```

X1 shape: torch.Size([100, 1])
Repetition 0:

## 3.1 3a Forward pass

## 3.2 3b Backward pass

```
[]: # Compute results of backward pass on example output (i.e., delta_x, delta_W1, odelta_z1,
    # delta_b1, delta_z2, delta_z3, delta_W2, delta_z4, delta_b2, delta_yhat, odelta_l, delta_y)

delta_l = 1
    delta_y = (2 * (y - y_hat)).squeeze(1)
    delta_yhat = -2 * (y - y_hat)
    delta_b2 = (delta_yhat * 1).squeeze(1)
    delta_z4 = delta_yhat * 1
    delta_W2 = delta_z4 * z3
    delta_z3 = delta_z4 * W2
    delta_z2 = delta_z3 * z3 * (1 - z3)
    delta_b1 = delta_z2.squeeze(1)
```

```
delta_z1 = delta_z2
     delta_x = torch.zeros(1, 1)
     for i in range(W1.shape[0]):
         delta_x += delta_z1[i] * W1[0][i]
     delta_x = delta_x.squeeze(1)
     delta_W1 = (delta_z1 * x).t()
[]: # Use PyTorch's backprop
     x.requires grad = True
     y.requires_grad = True
     if x.grad is not None:
         x.grad.zero_()
     if y.grad is not None:
         y.grad.zero_()
     model.zero_grad()
     t_yhat = model(x)
     t_yhat.retain_grad()
     t_1 = torch.nn.MSELoss()(t_yhat, y)
     t_l.backward()
     t delta l = 1
     t_delta_y = y.grad
     t_delta_yhat = t_yhat.grad
     t_delta_b2 = model.get_parameter("1_bias").grad
     t delta W2 = model.get parameter("1 weight").grad
     t_delta_b1 = model.get_parameter("0_bias").grad
     t_delta_W1 = model.get_parameter("0_weight").grad
     t_delta_x = x.grad
[]: # Check if equal (show squared error)
     for v in ["y", "yhat", "b2", "W2", "b1", "W1", "x"]:
         print(f'{v}, squared error={torch.

sum((eval("t_delta_"+v)-eval("delta_"+v))**2)}')
[]: # Check if equal (show actual values)
     for v in ["1", "y", "yhat", "b2", "W2", "b1", "W1", "x"]:
         print(f'{v}, pytorch={eval("t_delta_"+v)}, you={eval("delta_"+v)}')
```