Ownership Structure and Economic Growth

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Ownership Structure ⇒ Economic Growth?

Onwership structure is concentrated



- BlackRock, Vanguard, State Street, and Fidelity control 30% of votes of S&P 500 firms
- Top 10 chaebols account for half of stock market capitalization and exports in Korea

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- Ownership structure (common ownership, cross ownership, M&A, FDI, ...) =>
 Economic growth?
 - Business stealing effect
 - Technology spillover effect

Quantitative Schumpeterian Growth Model with Ownership Structure

- Existing Schumpeterian growth models:
 - Lack of strategic interaction (e.g., monopolistic competition)
 - Very few firms in Markov perfect equilibrium
- This paper: Many oligopolists + Ownership structure

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 - Ownership structure
 - Product market rivalry
 - Technology spillover

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- ullet Quantify three inter-firm networks for publicly listed patenting firms in the US (\simeq 1000 firms)
 - Ownership structure
 - Product market rivalry
 - Technology spillover
- Common ownership in the US:
 - Internalization of business stealing $\Longrightarrow g \downarrow \downarrow$
 - Internalization of technology spillover $\Longrightarrow g \uparrow$

Literature

- Competition & Innovation:
 - d'Aspremont and Jacquemin (1988); Aghion et al. (2001, 2005); Acemoglu and Akcigit (2012); Aghion et al. (2013); Bloom et al. (2013); Lopez and Vives (2019); Peters (2020); Akcigit and Ates (2021, 2023); Liu et al. (2022); Cavenaile et al. (2023); Anton et al. (2023, 2024); Kini et al. (2024); Hopenhayn and Okumura (2024) Quantitative Schumpeterian growth model with ownership structure
- Hedonic Demand / Empirical IO:
 Lancaster (1966); Rosen (1974); Berry et al. (1995); Nevo (2001); Pellegrino (2024); Ederer and Pellegrino (2024)
 Dynamic general equilibrium / R&D
- Oligopoly / Common Ownership / Market Power:
 Rubinstein and Yaari (1983); Rotemberg (1984); Neary (2003); Atkeson and Burstein (2008); Gutierrez and
 Philippon (2017); He and Huang (2017); Azar et al. (2018, 2022); Autor et al. (2020); Baqaee and Farhi (2020);
 De Loecker et al. (2020); Azar and Vives (2021); Edmond et al. (2023)

Simple Static Partial Equilibrium Model

- $\bullet \; \mbox{Firm} \; i \in \{1, \dots, n\}$ chooses quantity q_i and R&D effort x_i
- ullet Linear inverse demand: $\mathbf{p}(\mathbf{q}) = \mathbf{b} oldsymbol{\Sigma} \mathbf{q}$
- \bullet CRS production technology with marginal cost: $\mathbf{m}(\mathbf{x}) = \mathbf{a} \Omega \mathbf{x}$
- Quadratic cost of R&D: $c(x_i) = \frac{1}{2}x_i^2$

Common Ownership Weights

- ullet $\mathbf{K}=\left[\kappa_{ij}
 ight]$: common ownership weights that firm i places on the value of firm j
- More overlapping ownership b/w firm i and j \Longrightarrow Higher κ_{ij}

Proportional Influece

- Diagonal elements κ_{ii} are normalized to 1 for all firm i
- ullet $\mathbf{K} = \mathbf{I}$: dispersed ownership (each firm maximizes its own value)
- ullet ${f K}=[1]$: monopoly (maximizes total producer surplus)

Cournot & R&D Game

• Firm *i*'s profit:

$$\begin{split} \pi_i(\mathbf{q},\mathbf{x}) &= [p_i - m_i]q_i - c(x_i) \\ &= \left[b_i - \sum_{j=1}^n \sigma_{ij}q_j - a_i + \sum_{j=1}^n \omega_{ij}x_j\right]q_i - \frac{1}{2}x_i^2 \end{split}$$

• Given $\left\{q_j,x_j\right\}_{j\neq i}$, firm i chooses q_i and x_i to maximize $\sum_j \kappa_{ij}\pi_j(\mathbf{q},\mathbf{x})$

Impact of Common Ownership on R&D

 \bullet Comparative statics where $\left\{q_k,x_k\right\}_{k \neq i}$ are held constant:

$$\frac{\partial x_i}{\partial \kappa_{ij}} = \frac{q_j}{2 - \omega_{ii}^2} (2\omega_{ij} - \omega_{ii}\sigma_{ij}) \qquad \forall \ j \neq i$$

- SOC: $2 > \omega_{ii}^2$
- Internalize business stealing effect: $\partial^2 x_i/\partial \kappa_{ij}\partial \sigma_{ij} < 0$
- Internalize technology spillover effect: $\partial^2 x_i/\partial \kappa_{ij}\partial \omega_{ij}>0$

Overview of Identification Strategy

| Networks | Measurement |
|---------------------------------|--|
| Common ownership ${f K}$ | Institutional investor holdings in 13f filings (Backus et al., 2021) |
| Product market rivalry Σ | Product proximity (Hoberg and Phillips, 2016): Text analysis of business description in 10k filings |
| Technology spillover Ω | Technology proximity (Jaffe, 1986; Bloom et al., 2013): Patent classification |

Schumpeterian Growth Model

Linear quadratic aggregator (final good):

$$Y_t = \mathbf{q}_t^T \mathbf{b}_t - \frac{1}{2} \mathbf{q}_t^T \mathbf{\Sigma} \mathbf{q}_t$$

Linear inverse demand:

$$\mathbf{p}_t = \mathbf{b}_t - \mathbf{\Sigma} \mathbf{q}_t$$

CRS production technology (intermediate good):

$$q_{i,t} = a_{i,t} l_{i,t}$$

- Each firm has knowledge capital $z_{i,t}$
- Each firm allocates knowledge capital to improve labor productivity and product quality:

$$\zeta a_{i,t} + b_{i,t} = z_{i,t}$$

Law of Motion of Knowledge Capital

$$d\mathbf{z}_t = \left(\underbrace{\Omega\mathbf{z}_t}_{\text{tech spillover}} + \underbrace{\mu\mathbf{x}_t}_{\text{R\&D}}\right)dt + \underbrace{\gamma\mathbf{z}_t \circ d\mathbf{W}_t}_{\text{shocks}}$$

- $oldsymbol{\Omega} = ig[\omega_{ij}ig]$: technology spillover matrix
- $x_{i,t} = \sqrt{d_{i,t}}$
 - $d_{i,t}$: R&D input in terms of final good
 - Innovation elasticity is 0.5
- μ , γ : positive scalars

Market Clearing and Preference

Inelastic labor supply:

$$L = \sum_{i} l_{i,t}$$

Final good market clearing:

$$C_t + \underbrace{\sum_i d_{i,t}}_{\text{R\&D input}} = Y_t$$

Risk neutral representative household:

$$\max \ \mathbf{E}_t \left[\int_t^\infty \exp \left(-\rho s \right) C_s ds \right]$$

Cournot-Nash Equilibrium

• Firm i's gross profit before subtracting dynamic R&D cost:

$$\pi_{i,t} = p_{i,t}q_{i,t} - w_tl_{i,t} = \left(b_{i,t} - \frac{w_t}{a_{i,t}} - \sum_i \sigma_{ij}q_{j,t}\right)q_{i,t} \quad \text{where} \quad \zeta a_{i,t} + b_{i,t} = z_{i,t}$$

• Given w_t , $z_{i,t}$, and $\left\{q_{j,t}\right\}_{i\neq i}$, firm i chooses $a_{i,t}$, $b_{i,t}$, and $q_{i,t}$ to maximize $\sum_j \kappa_{ij} \pi_{j,t}$

Cournot-Nash Equilibrium

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- Given w_t , $z_{i,t}$, and $\left\{q_{j,t}\right\}_{j \neq i}$, firm i chooses $a_{i,t}$, $b_{i,t}$, and $q_{i,t}$ to maximize $\sum_j \kappa_{ij} \pi_{j,t}$
- Quantity is a linear function of knowledge capital:

$$\mathbf{q}_t(\mathbf{z}_t) = \left\{ \underbrace{2\frac{\zeta}{L}\mathbf{J}}_{\text{labor cost}} + \underbrace{\mathbf{\Sigma}}_{\text{substitutability}} + \underbrace{\mathbf{K} \circ \mathbf{\Sigma}}_{\text{ownership} \times \text{substitutability}} \right\}^{-1} \mathbf{z}_t$$

- J = [1]
- Ownership-weighted gross profits are expressed in quadratic form: $\sum_i \kappa_{ij} \pi_{j,t} = \mathbf{z}_t^T \mathbf{Q}^i \mathbf{z}_t$ $oldsymbol{ iny}$

Linear-Quadratic Differential Game

• Given other players' strategy $\left\{x_{j,t}\right\}_{j \neq i, t > 0}$, firm i chooses R&D effort $\left\{x_{i,t}\right\}_{t > 0}$ to maximize

$$\max_{\left\{x_{i,t}\right\}_{t\geq0}}\quad V^{i}\left(\mathbf{z}_{0}\right)\equiv\mathbf{E}_{0}\left[\int_{0}^{\infty}\exp\left(-\rho t\right)\left\{\sum_{j}\kappa_{ij}\left(\pi_{j,t}-x_{j,t}^{2}\right)\right\}dt\right]$$

subject to
$$d\mathbf{z}_t = (\mathbf{\Omega}\mathbf{z}_t + \mu\mathbf{x}_t)\,dt + \gamma\mathbf{z}_t \circ d\mathbf{W}_t$$

Linear-Quadratic Differential Game

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subject to $d\mathbf{z}_t = (\mathbf{\Omega}\mathbf{z}_t + \mu\mathbf{x}_t)\,dt + \gamma\mathbf{z}_t \circ d\mathbf{W}_t$

Firm i's HJB equation:

$$\rho V^{i}\left(\mathbf{z}\right) = \max_{x_{i}} \left\{ \mathbf{z}^{T} \mathbf{Q}^{i} \mathbf{z} - \sum_{j} \kappa_{ij} x_{j}^{2} + V_{\mathbf{z}}^{i}\left(\mathbf{z}\right) \left[\mathbf{\Omega} \mathbf{z} + \mu \mathbf{x}\right] + \frac{\gamma^{2}}{2} \mathbf{z}^{T} V_{\mathbf{z}\mathbf{z}}^{i}\left(\mathbf{z}\right) \mathbf{z} \right\}$$

HJB Equations ⇒ Riccati Equations

- Guess and verify $V^i(\mathbf{z}) = \mathbf{z}^T \mathbf{X}^i \mathbf{z}$ (for any \mathbf{z})
- ullet \mathbf{X}^i is the solution of stacked algebraic Riccati equations lacktriangle
- All public patenting firms in the US in our dataset \simeq 1000 firms \Longrightarrow $1000^3=1$ billion undetermined coefficients (20 seconds on my laptop)

| Oligopolistic Schumpeterian | Computation time | # of firms | Productivity space |
|-----------------------------|------------------|------------|--------------------|
| Cavenaile et al. (2023) | $O(2^n)$ | 4 | 6 grid |
| Our model | $O(n^4)$ | ≈1000 | Continuous |

Balance Growth Path

- R&D strategy: $x_{i,t} = (\mu \mathbf{X}_i^i)^T \mathbf{z}_t$ where \mathbf{X}_i^i is the i th column of \mathbf{X}^i
- The law of motion is rewritten as $d\mathbf{z}_t = \mathbf{\Phi}\mathbf{z}_t dt + \gamma \mathbf{z}_t \circ d\mathbf{W}_t$ where

$$\mathbf{\Phi} \equiv \underbrace{\mathbf{\Omega}}_{\text{Tech Spillover}} + \underbrace{\mu^2 \left[\mathbf{X}_1^1 \, \cdots \, \mathbf{X}_n^n \right]^T}_{\text{R\&D}}$$

Theorem

Consider the deterministic economy ($\gamma = 0$). If Φ is irreducible, then:

- (i) There exists largest positive eigenvalue of Φ , g, and associated positive eigenvector, \mathbf{z}^* .
- (ii) There exists a globally stable BGP such that the knowledge capital growth rate of all firms is g, and the knowledge capital distribution is a scalar multiple of \mathbf{z}^* .
 - Proof: Perron–Frobenius Theorem
 - " Φ is irreducible" \iff "All firms are directly or indirectly connected technologically"

Intuition of Why the Model Has the BGP

• On the BGP, \mathbf{a}_t , \mathbf{b}_t , \mathbf{z}_t , and \mathbf{q}_t grow at the same rate

Technological Choice: $\zeta a_{i,t} + b_{i,t} = z_{i,t}$

 $\label{eq:qi} \mbox{Linear Production Technology:} \qquad q_{i,t} = a_{i,t} l_{i,t}$

Inelastic Labor Supply: $L = \textstyle \sum_i l_{i,t}$

ullet Linear and quadratic term in $old q_t$ of output grow at the same rate: Equilibrium Summary

$$Y_t = \mathbf{q}_t^T \mathbf{b}_t - \frac{1}{2} \mathbf{q}_t^T \mathbf{\Sigma} \mathbf{q}_t$$

Expected Growth Rate and Utility

Apply Ito's lemma:

$$\begin{array}{ll} \log Y_t &= \log \left(\mathbf{z}_t^T \mathbf{Q} \mathbf{z}_t\right) \\ d\mathbf{z}_t &= \mathbf{\Phi} \mathbf{z}_t dt + \gamma \mathbf{z}_t \circ d\mathbf{W}_t \end{array} \implies \quad \mathbf{E}_t \left[\left. g_t \right| \mathbf{z}_t \right] \end{array}$$

Expected utility is expressed in quadratic form:



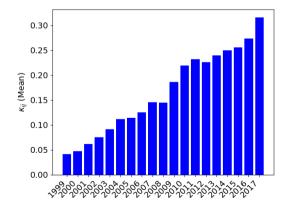
$$\mathbf{E}_t \left[\left. \int_t^\infty \exp\left(-\rho s \right) C_s ds \right| \mathbf{z}_t \right] = \mathbf{z}_t^T \! X \mathbf{z}_t$$

ullet Solve the equilibrium once \Longrightarrow Can compute expected growth and utility for any \mathbf{z}_t

Common Ownership ${f K}$

- Backus et al. (2021) construct a dataset on investors' holdings based on Form 13F.
- Baseline: Rotemberg (1984) proportional influence assumption.

Proportional Influence



Product Market Rivalry ∑

- Hoberg and Phillips (2016) estimates product similarity using business descriptions in 10-K
- ullet Pellegrino (2024) estimates lpha to align with the cross-price elasticity of demand ${}^{ ext{micro estimates}}$

$$\underbrace{\sigma_{ij}}_{\text{substitutability}} = \alpha \times \text{product similarity b/w } i \text{ and } j \quad (i \neq j)$$

Technological Proximity $\widehat{\Omega}$

- Technological profile of firm i
 - ullet The vector of the share of patents held by firm i in each technology class
 - Baseline: group-level patent classifications (≈ 4000)
- Jaffe (1986) technological proximity measure $\tilde{\omega}_{ij}$:
 - \bullet Cosine similarity of the technological profiles b/w firm i and j

Distribution of Knowledge Capital \mathbf{z}_t

| Variables | Identification |
|----------------|---|
| $\pi_{i,t}$ | ${\sf Gross\ profit\ (before\ R\&D\ cost) = Revenue-Cost\ of\ goods\ sold}$ |
| \mathbf{q}_t | $\pi_{i,t} = \sum_i \kappa_{ij} \sigma_{ij} q_{i,t} q_{j,t}$ |
| ζ/L | Matches sample firms' cost share (average markup) |
| \mathbf{z}_t | $\mathbf{q}_t = \left\{ 2 rac{\zeta}{L} \mathbf{J} + \mathbf{\Sigma} + \mathbf{K} \circ \mathbf{\Sigma} ight\}^{-1} \mathbf{z}_t$ |

Simple Model

Growth Model

Equilibrium 000000 Identification 0000●00 Exercise 00000000

Technology Spillover $oldsymbol{\Omega}=eta imes$ Technological Proximity $oldsymbol{\widetilde{\Omega}}$

$$z_{i,t+1} - z_{i,t} = \beta \sum_{j \neq i} \tilde{\omega}_{ij,t} z_{j,t} + \text{Year FE}_t + \epsilon_{i,t}$$

| | (1) | (2) | (3) |
|---|---|---|---|
| | $\boldsymbol{z}_{i,t+1} - \boldsymbol{z}_{i,t}$ | $\boldsymbol{z}_{i,t+1} - \boldsymbol{z}_{i,t}$ | $\boldsymbol{z}_{i,t+1} - \boldsymbol{z}_{i,t}$ |
| \(\sigma \) | 0.000191*** | 0.000152*** | 0.000140^{***} |
| $\sum_{j eq i} 	ilde{\omega}_{ij,t} z_{j,t}$ | (0.000035) | (0.000035) | (0.000039) |
| DOD Evenorediture | | 0.037** | |
| √R&D Expenditure | | (0.021) | |
| Year Fixed Effects | ✓ | ✓ | √ |
| IV | | | \checkmark |
| IV 1st Stage F-statistics | | | 4176 |
| No. observations | 16,324 | 15,173 | 14,181 |

SEs clustered by years and 4-digit naics industries are reported in parentheses. * p < 0.1, ** p < 0.05, *** p < 0.01.

• IV: Firm-specific tax price of R&D from federal and state-specific rules (Bloom et al., 2013)

Identification: Summary

Publicly available data + Compustat

| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
|--|---------|
| $\begin{array}{llll} \mathbf{K} & \text{Common ownership weights} & \text{Form 13F, Backus et al. (2021)} \\ \alpha & \text{Product proximity} \rightarrow \text{Substitutability} & 0.12 & \text{Pellegrino (2024)} \\ \beta & \text{Technological proximity} \rightarrow \text{Spillover} & 0.00014 & \text{Estimate the law of motion} \\ \gamma & \text{St.d. of idiosyncratic shocks} & 0.027 & \text{Estimate the law of motion} \\ \zeta/L & \text{Labor augmentation efficiency} & 0.0063 & \text{Compustat, Cost of goods sold} \\ \end{array}$ | (2016) |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| $\begin{array}{lll} \beta & & \text{Technological proximity} \rightarrow \text{Spillover} & 0.00014 & \text{Estimate the law of motion} \\ \gamma & & \text{St.d. of idiosyncratic shocks} & 0.027 & \text{Estimate the law of motion} \\ \zeta/L & \text{Labor augmentation efficiency} & 0.0063 & \text{Compustat, Cost of goods sold} \\ \end{array}$ | |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |
| ζ/L Labor augmentation efficiency 0.0063 Compustat, Cost of goods sold | |
| | |
| ρ Discount rate 0.10 > risk free rates, < private R&D | |
| r = 1.555 a.m. 1.415 | returns |
| μ R&D efficiency 0.05 1.7% economic growth rate | |

Fit b/w Model and Data

• Comparison of firm-level model-generated values (x-axis) with observed data (y-axis)



Counterfactual Ownership Structures

| Ownership Structure | Description |
|---------------------|--|
| Baseline | Observed ownership structure in 2017 |
| Dispersed | $\mathbf{K}^D = \mathbf{I}$ |
| Mean=1999 | $\kappa_{ij,2017}^{M1999} = const 	imes \kappa_{ij,2017}$ and $\mathbf{E}\left[\kappa_{ij,2017}^{M1999} ight] = \mathbf{E}\left[\kappa_{ij,1999} ight]$ for $j \neq i$ |
| Uniform | $\kappa^{U}_{ij,2017} = \mathbf{E}\left[\kappa_{ij,2017} ight]$ for $j eq i$ |
| Monopoly | $\mathbf{K}^M = [1]$ |

Total Output

| Total Output in 2017 | Ownership (Baseline: 2017) | | | | |
|---|----------------------------|-----------|---------|----------|----------|
| (Social Optimum: 100) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly |
| Baseline | 91.30 | 91.02 | 90.78 | 89.08 | 89.17 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | | | | | |
| Only Tech Spill ${f \Sigma}={f I},\zeta/L=0$ | | | | | |

- Inelastic labor supply ⇒ Changes arise from product misallocation
- Common ownership exacerbates product misallocation

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| Only Business Steal $oldsymbol{\Omega} = [0]$ | 91.30 | 91.02 | 90.78 | 89.08 | 89.17 |
| Only Tech Spill ${f \Sigma}={f I},\zeta/L=0$ | 75.00 | 75.00 | 75.00 | 75.00 | 75.00 |

- Inelastic labor supply ⇒ Changes arise from product misallocation
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Total R&D Expenditure

| Total R&D in 2017 | Ownership (Baseline: 2017) | | | | |
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| (Social Optimum: 100) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly |
| Baseline | 26.16 | 25.90 | 25.56 | 22.36 | 19.36 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | | | | | |
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- Internalization of business stealing > Internalization of technology spillover
- Network heterogeneity is important

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| Baseline | 26.16 | 25.90 | 25.56 | 22.36 | 19.36 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | 28.15 | 27.79 | 27.07 | 23.42 | 19.80 |
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| Only Business Steal $oldsymbol{\Omega} = [0]$ | 28.15 | 27.79 | 27.07 | 23.42 | 19.80 | |
| Only Tech Spill ${f \Sigma}={f I},\ \zeta/L=0$ | 18.27 | 18.34 | 18.75 | 18.86 | 19.84 | |

- Network heterogeneity is important

Expected Growth Rate

| Expected Economic | Ownership (Baseline: 2017) | | | | |
|--------------------------------------|----------------------------|-----------|---------|----------|----------|
| Growth Rate in 2017 (%) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly |
| Baseline | 1.796 | 1.793 | 1.791 | 1.753 | 1.713 |
| Only Business Steal ${f \Omega}=[0]$ | | | | | |
| Only Tech Spill | | | | | |
| $\Sigma = I, \zeta/L = 0$ | | | | | |

- In baseline, the expected growth rate is
 - 0.043 pp (2.4%) lower compared to dispersed ownership, and
 - 0.040 pp (2.2%) lower compared to common ownership level in 1999.

Expected Growth Rate

| Expected Economic | Ownership (Baseline: 2017) | | | | |
|---|----------------------------|-----------|---------|----------|----------|
| Growth Rate in 2017 (%) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly |
| Baseline | 1.796 | 1.793 | 1.791 | 1.753 | 1.713 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | 1.097 | 1.094 | 1.093 | 1.062 | 1.020 |
| Only Tech Spill ${f \Sigma}={f I},\zeta/L=0$ | | | | | |

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| Baseline | 1.796 | 1.793 | 1.791 | 1.753 | 1.713 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | 1.097 | 1.094 | 1.093 | 1.062 | 1.020 |
| Only Tech Spill ${f \Sigma}={f I},\zeta/L=0$ | 2.051 | 2.054 | 2.068 | 2.072 | 2.107 |

- In baseline, the expected growth rate is
 - 0.043 pp (2.4%) lower compared to dispersed ownership, and
 - 0.040 pp (2.2%) lower compared to common ownership level in 1999.

Expected Social Welfare

| Expected Social Welfare | Ownership (Baseline: 2017) | | | | | |
|---|----------------------------|-----------|---------|----------|----------|--|
| (Social Optimum: 100) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly | |
| Baseline | 87.72 | 87.42 | 87.16 | 85.25 | 85.18 | |
| Only Business Steal ${f \Omega}=[0]$ | | | | | | |
| Only Tech Spill $\mathbf{\Sigma} = \mathbf{I}, \ \zeta/L = 0$ | | | | | | |

- In the baseline, the consumption-equivalent welfare loss is
 - 2.8% compared to dispersed ownership, and
 - 2.5% compared to the common ownership level in 1999.

Expected Social Welfare

| Expected Social Welfare | Ownership (Baseline: 2017) | | | | |
|---|----------------------------|-----------|---------|----------|----------|
| (Social Optimum: 100) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly |
| Baseline | 87.72 | 87.42 | 87.16 | 85.25 | 85.18 |
| Only Business Steal $oldsymbol{\Omega} = [0]$ | 88.83 | 88.53 | 88.30 | 86.44 | 86.41 |
| Only Tech Spill $oldsymbol{\Sigma} = \mathbf{I}, \zeta/L = 0$ | | | | | |

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|--|----------------------------|-----------|---------|----------|----------|--|
| (Social Optimum: 100) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly | |
| Baseline | 87.72 | 87.42 | 87.16 | 85.25 | 85.18 | |
| Only Business Steal ${f \Omega}=[0]$ | 88.83 | 88.53 | 88.30 | 86.44 | 86.41 | |
| Only Tech Spill ${f \Sigma}={f I},\ \zeta/L=0$ | 68.81 | 68.82 | 68.88 | 68.89 | 69.02 | |

- In the baseline, the consumption-equivalent welfare loss is
 - 2.8% compared to dispersed ownership, and
 - 2.5% compared to the common ownership level in 1999.

Firm Value Share

| Firm Value | Ownership (Baseline: 2017) | | | | | |
|--|----------------------------|-----------|---------|----------|----------|--|
| Share in 2017 (%) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly | |
| Baseline | 28.74 | 29.63 | 33.43 | 33.34 | 40.92 | |
| Only Business Steal ${f \Omega}=[0]$ | | | | | | |
| Only Tech Spill ${f \Sigma}={f I},\zeta/L=0$ | | | | | | |

- In baseline, firm value share is
 - 5.6% lower compared to dispersed ownership, and
 - 4.7% lower compared to common ownership level in 1999.

Firm Value Share

| Ownership (Baseline: 2017) | | | | | |
|----------------------------|-----------|---------------------------------|---|--|--|
| Dispersed | Mean=1999 | Uniform | Baseline | Monopoly | |
| 28.74 | 29.63 | 33.43 | 33.34 | 40.92 | |
| 27.91 | 28.80 | 32.60 | 33.51 | 40.14 | |
| | | | | | |
| | 28.74 | Dispersed Mean=1999 28.74 29.63 | Dispersed Mean=1999 Uniform 28.74 29.63 33.43 | Dispersed Mean=1999 Uniform Baseline 28.74 29.63 33.43 33.34 | |

- In baseline, firm value share is
 - 5.6% lower compared to dispersed ownership, and
 - 4.7% lower compared to common ownership level in 1999.

Firm Value Share

| Firm Value | Ownership (Baseline: 2017) | | | | | |
|---------------------------|----------------------------|-----------|---------|----------|----------|--|
| Share in 2017 (%) | Dispersed | Mean=1999 | Uniform | Baseline | Monopoly | |
| Baseline | 28.74 | 29.63 | 33.43 | 33.34 | 40.92 | |
| Only Business Steal | | | | | | |
| $\mathbf{\Omega} = [0]$ | 27.91 | 28.80 | 32.60 | 33.51 | 40.14 | |
| Only Tech Spill | | | | | | |
| $\Sigma = I, \zeta/L = 0$ | 64.82 | 64.81 | 64.76 | 64.74 | 64.63 | |

- In baseline, firm value share is
 - 5.6% lower compared to dispersed ownership, and
 - 4.7% lower compared to common ownership level in 1999.

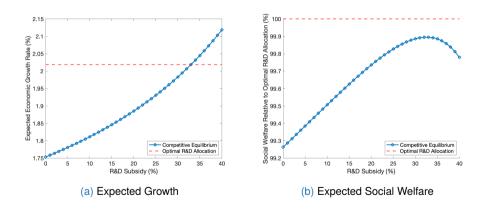
When Common Ownership Affects only R&D Decisions

Common ownership only influence R&D decisions (d'Aspremont and Jacquemin, 1988)

| | Ownership Structure | | | |
|---|---------------------|------------|----------|--|
| | Dispersed | Common R&D | Baseline | |
| Output (Social Optimum: 100) | 91.30 | 91.30 | 89.08 | |
| R&D Expenditure (Social Optimum: 100) | 26.17 | 19.76 | 22.36 | |
| Expected Growth Rate (%) | 1.796 | 1.726 | 1.753 | |
| Expected Social Welfare (Social Optimum: 100) | 87.72 | 87.49 | 85.25 | |
| Firm Value Share (%) | 28.74 | 29.04 | 34.34 | |

- Lowest R&D expenditure and expected growth rate
- Intermediate social welfare and firm value share

Uniform R&D Subsidy Social Optimum



- Optimal rate is s = 33%, which increases g by 0.25 pp (14%)
- CE Welfare loss relative to optimal R&D allocation is reduced to 0.1% (Initially 0.7%)

Conclusion

- Quantitative Schumpeterian growth model with ownership structure
 - Utilize micro data and computational capability
- Common ownership in the US:
 - 1. Internalization of business stealing effect $\Longrightarrow g \downarrow \downarrow$
 - 2. Internalization of technology spillover effect $\Longrightarrow g \uparrow$
- Potential application:
 - Chaebols in Korea
 - Zaibatsu (pre-WWII) and cross-shareholding (late 20th century) in Japan
 - FDI / multinational companies and international technology diffusion

Share of Top 5 Shareholders in Largest Market Cap Firms (Back)

A 1 . 11

| Microsoft | |
|----------------|-------|
| Vanguard | 9.20% |
| Blackrock | 7.75% |
| Steven Ballmer | 4.48% |
| State Street | 3.97% |
| Fidelity | 2.66% |

| Nvidia | |
|----------------|-------|
| Vanguard 8 | 3.93% |
| BlackRock 7 | '.74% |
| Fidelity 4 | .12% |
| State Street 3 | 3.97% |
| Jensen Huang 3 | 3.80% |

| Apple | |
|---------------|-------|
| Vanguard | 9.29% |
| Blackrock | 7.48% |
| State Street | 3.96% |
| Fidelity | 2.27% |
| Geode Capital | 2.26% |

| Google | |
|--------------|-------|
| Vanguard | 7.36% |
| Blackrock | 6.47% |
| State Street | 3.39% |
| Fidelity | 3.01% |
| Sergey Brin | 2.99% |

| Amazon | |
|---------------|-------|
| Jeffrey Bezos | 8.58% |
| Vanguard | 7.77% |
| Blackrock | 6.50% |
| State Street | 3.44% |
| Fidelity | 3.10% |
| | |

| Meta | |
|--------------|-------|
| Vanguard | 7.55% |
| Blackrock | 6.50% |
| Fidelity | 5.38% |
| Accel IX LP | 3.88% |
| State Street | 3.40% |



Equity Investments by Big tech in Al Startups (Back)

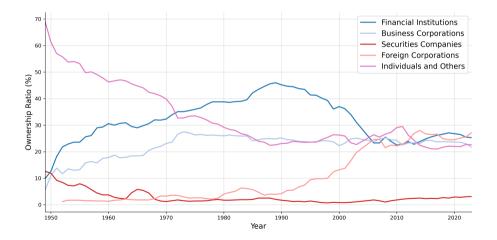
| Shareholding percentage | Microsoft | Google | Amazon |
|-------------------------|-----------|--------|---------|
| OpenAl (ChatGPT) | 49% | | |
| Anthropic (Claude) | | 14% | 23% |

Technology & Product Proximity: Example

| Tesla vs. Ford | |
|----------------------|------|
| Technology Proximity | 0.11 |
| Product Proximity | 0.15 |

| Apple vs. Intel | |
|----------------------|------|
| Technology Proximity | 0.57 |
| Product Proximity | 0.00 |

Ownership Ratio by Holder Types in Japan



Rotemberg (1984) Proportional Influence

- $o \in \{1, 2, ..., n_o\}$: owners
- s_{io} : the proportion of shares in firm i owned by owner o where $\sum_o s_{io} = 1$
- $\hat{V}_{i,t}$: value of firm i
- $\tilde{V}_{o,t} \equiv \sum_i s_{io} \hat{V}_{i,t}$: value of owner o
- Firms' objective:

$$\sum_{o} s_{io} \tilde{V}_{o,t} \propto \sum_{j} \kappa_{ij} \hat{V}_{j,t}$$

where

$$\kappa_{ij} \equiv \mathbf{s}_i^T \mathbf{s}_j / \mathbf{s}_i^T \mathbf{s}_i \quad \text{where} \quad \mathbf{s}_i \equiv \left[s_{i1},...,s_{io},...,s_{in_o}\right]^T$$

Total Surplus

Total surplus for product i:

$$ts_i(\mathbf{q},\mathbf{x}) = \pi_i(\mathbf{q},\mathbf{x}) + cs_i(\mathbf{q}) = q_i \left[b_i - \frac{1}{2} \sum_{i=1}^n \sigma_{ij} q_j - a_i + \sum_{i=1}^n \omega_{ij} x_j \right] - \frac{1}{2} x_i^2$$

R&D Externalities

- 1. Business stealing effect
 - Innovators steel the business (profits) of other firms
- 2. Technology spillover effect
 - Innovation improves the productivity of other firms
- 3. Appropriability effect (market power)
 - Innovators cannot appropriate the entire consumer surplus

R&D Allocation and Externalities

Firms maximize common owner weighted profits:

$$\mathbf{x}^* = (\mathbf{K} \circ \mathbf{\Omega})[\mathbf{\Sigma} + \mathbf{K} \circ \mathbf{\Sigma} - \mathbf{\Omega}(\mathbf{K} \circ \mathbf{\Omega})]^{-1}(\mathbf{b} - \mathbf{a})$$

Firms maximize common owner weighted total surplus (*):

$$\mathbf{x}_{TS}^* = (\mathbf{K} \circ \mathbf{\Omega}) \left[\frac{1}{2} (\mathbf{\Sigma} + \mathbf{K} \circ \mathbf{\Sigma}) - \mathbf{\Omega} (\mathbf{K} \circ \mathbf{\Omega}) \right]^{-1} (\mathbf{b} - \mathbf{a})$$

- $\mathbf{K} = [1]$ in $(\star) \Longrightarrow$ Social Optimum
- Externalities: (i) Appropriability, (ii) Business stealing, (iii) Technology spillover

Generalized Hedonic-Linear Demand (Pellegrino, 2024)

- $i \in \{1, 2, ..., n\}$: firms / products
- 1 unit of product i provides
 - 1 unit of idiosyncratic characteristic $k \in \{1, 2, ..., n\}$
 - $\psi_{k,i}$ unit of shared characteristic $k \in \{n+1, n+2, ..., n+n_k\}$ where $\sum_k \psi_{k,i}^2 = 1$
- Aggregate each characteristic:

$$y_{k,t} = \begin{cases} q_{k,t} & k = 1, 2, ..., n \\ \sum_{i} \psi_{k,i} q_{i,t} & k = n + 1, n + 2, ..., n + n_k \end{cases}$$

Linear quadratic aggregator over characteristics:

$$Y_t = (1-\alpha)\sum_{k=1}^n \left(\underbrace{\hat{b}_{k,t} y_{k,t} - \frac{1}{2} y_{k,t}^2}_{\text{idiosyncratic characteristic}} \right) + \alpha \sum_{k=n+1}^{n+n_k} \left(\underbrace{\hat{b}_{k,t} y_{k,t} - \frac{1}{2} y_{k,t}^2}_{\text{shared characteristic}} \right)$$

Generalized Hedonic-Linear Demand (Pellegrino, 2024)

Quality:

$$b_i = (1 - \alpha)\,\hat{b}_i + \alpha \sum_{k=n+1}^{n+n_k} \psi_k \hat{b}_k$$

Inverse demand:

$$\frac{\mathbf{p}}{P} = \mathbf{b} - \mathbf{\Sigma}\mathbf{q}$$

Inverse cross price elasticity of demand:

$$\frac{\partial \log p_i}{\partial \log q_j} = -\frac{q_j}{p_i} \cdot \sigma_{ij}$$

Cross price elasticity of demand:

$$\frac{\partial \log q_i}{\partial \log p_j} = -\frac{p_j}{q_i} (\mathbf{\Sigma}^{-1})_{ij}$$

Static Profits

- Gross profit: $rac{\pi_{i,t}}{P_t} = \sum_j \kappa_{ij} \sigma_{ij} q_{i,t} q_{j,t}$
- Firms choose labor productivity and product quality: $\zeta a_{i,t} = \sqrt{\zeta \frac{w_t}{P_t}}$, $b_{i,t} = z_{i,t} \sqrt{\zeta \frac{w_t}{P_t}}$
- Labor market clearing: $L=\sum_i rac{q_{i,t}}{a_{i,t}} \Longrightarrow \sqrt{\zeta rac{w_t}{P_t}} = rac{\zeta}{L} \sum_i q_{i,t}$
- $\bullet \ \, \mathbf{q}_t = \mathbf{N}\mathbf{z}_t \ \, \text{where} \ \, N \equiv \left\{ 2\frac{\zeta}{L}\mathbf{J} + \mathbf{\Sigma} + \mathbf{K} \circ \mathbf{\Sigma} \right\}^{-1}$
- N_i : the i th row of N
- Ownership weighted profit:

$$\sum_{j} \kappa_{ij} \frac{\pi_{j,t}}{P_t} = \sum_{j} \kappa_{ij} \sum_{h} \kappa_{jh} \sigma_{jh} q_{j,t} q_{h,t} = \mathbf{z}_t^T \mathbf{Q}^i \mathbf{z}_t$$

where

$$\mathbf{Q}^{i} = \frac{1}{2} \sum_{j} \kappa_{ij} \sum_{h} \kappa_{jh} \sigma_{jh} \left(N_{j}^{T} N_{h} + N_{h}^{T} N_{j} \right)$$

Back

Riccati Equations

ullet $V^{i}\left(\mathbf{z}
ight)=\mathbf{z}^{T}\mathbf{X}^{i}\mathbf{z}$ where \mathbf{X}^{i} is the solution of the stacked Riccati equation

$$0 = \mathbf{Q}^{i} - \mu^{2} \sum_{i} \kappa_{ij} \mathbf{X}_{j}^{j} \left(\mathbf{X}_{j}^{j} \right)^{T} + \left(\mathbf{\Phi} - \frac{1}{2} \left(\rho - \gamma^{2} \right) \mathbf{I} \right)^{T} \mathbf{X}^{i} + \mathbf{X}^{i} \left(\mathbf{\Phi} - \frac{1}{2} \left(\rho - \gamma^{2} \right) \mathbf{I} \right)$$

- $\mathbf{X}_{i}^{i} \equiv \text{the } i \text{ th column of } \mathbf{X}^{i}$
- $\mathbf{\Phi} \equiv \mathbf{\Omega} + \mu^2 \begin{bmatrix} \mathbf{X}_1^1 & \cdots & \mathbf{X}_n^n \end{bmatrix}^T$
- Algorithm: Given $\left[egin{array}{ccc} \mathbf{X}_{ au}^1 & \cdots & \mathbf{X}_{ au}^n \end{array}
 ight]$, update $\left[egin{array}{ccc} \mathbf{X}_{ au-\Delta}^1 & \cdots & \mathbf{X}_{ au-\Delta}^n \end{array}
 ight]$ by

$$-\frac{\mathbf{X}_{\tau}^{i}-\mathbf{X}_{\tau-\Delta}^{i}}{\Delta}=\mathbf{Q}^{i}-\mu^{2}\sum_{j}\kappa_{ij}\mathbf{X}_{j,\tau}^{j}\left(\mathbf{X}_{j,\tau}^{j}\right)^{T}+\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\mathbf{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}\right)\boldsymbol{I}\right)^{T}\mathbf{X}_{\tau}^{i}+\mathbf{X}_{\tau}^{i}\left(\boldsymbol{\Phi}_{\tau}-\frac{1}{2}\left(\rho-\gamma^{2}$$

Summary of Equilibrium

| Description | Expression |
|---------------------------------|--|
| Production strategy | $\mathbf{q}_t = N\mathbf{z}_t$ |
| R&D strategy | $\mathbf{x}_t = \mu 	ilde{X} \mathbf{z}_t$ |
| Law of motion | $d\mathbf{z}_t = (\Omega \mathbf{z}_t + \mu \mathbf{x}_t) dt + \gamma \mathbf{z}_t dW_t$ |
| Profit of final producers | $\Pi_t^F/P_t = \mathbf{q}_t^T\left(rac{1}{2}\Sigma ight)\mathbf{q}_t$ |
| Total operating profit of firms | $\Pi_t/P_t = \mathbf{q}_t^T \left(\frac{1}{2} \Sigma \circ (K + K^T) \right) \mathbf{q}_t$ |
| Labor income | $w_t L/P_t = \mathbf{q}_t^T \left(rac{\zeta}{L} J ight) \mathbf{q}_t$ |
| Output | $Y_t = \mathbf{q}_t^T \left(\frac{\zeta}{L} J + \frac{1}{2} \Sigma + \frac{1}{2} \Sigma \circ (K + K^T) \right) \mathbf{q}_t$ |
| Consumption | $C_t = Y_t - \mathbf{x}_t^T \mathbf{x}_t$ |

Output and Expected Utility

• Output: $Y_t = \mathbf{q}_t^T Q \mathbf{q}_t$ where

$$Q = \frac{\zeta}{L}J + \frac{1}{2}\Sigma + \frac{1}{2}\Sigma \circ \left(K + K^T\right)$$

Expected utility:

$$V(\mathbf{z}_t) \equiv \mathbf{E}_t \left[\left. \int_t^\infty \exp\left(-\rho s\right) C_s ds \right| \mathbf{z}_t \right] = \mathbf{z}_t^T X \mathbf{z}_t$$

where X is the solution of the Lyapunov equation (obtained from households' HJB equation):

$$0 = Q - \mu^2 \tilde{X}^T \tilde{X} + X \left(\Phi - \frac{1}{2} \left(\rho - \gamma^2\right) I\right) + \left(\Phi - \frac{1}{2} \left(\rho - \gamma^2\right) I\right)^T X$$



Social Optimum

- Static optimal allocation: $\mathbf{q}_t^* = N^*\mathbf{z}_t$ where $N^* \equiv \left\{2\frac{\zeta}{L}J + \Sigma\right\}^{-1}$
- \bullet Optimal output: $Y_t^* = \mathbf{z}_t^T Q^* \mathbf{z}_t$ where $Q^* = \frac{1}{2} N^*$
- Optimal expected utility:

$$V^*\left(\mathbf{z}_t\right) \equiv \mathbf{E}_t \left[\left. \int_t^\infty \exp\left(-\rho s\right) C_s ds \right| \mathbf{z}_t \right] = \mathbf{z}_t^T X^* \mathbf{z}_t,$$

where X^* is the solution of the Riccati equation (obtained from planner's HJB equation):

$$0 = Q^* - \mu^2 \left(X^*\right)^2 + X^* \left(\Phi^* - \frac{1}{2} \left(\rho - \gamma^2\right) I\right) + \left(\Phi^* - \frac{1}{2} \left(\rho - \gamma^2\right) I\right) X^*$$

- Optimal R&D: $\mathbf{x}_t^* = \mu X^* \mathbf{z}_t$
- Optimal technology transition matrix: $\Phi^* = \Omega + \mu^2 X^*$

Stochastic Process of Output

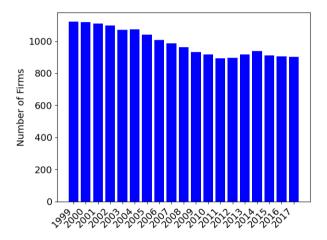
Applying It's lemma,

$$d\log Y_t = \left[\frac{\mathbf{z}_t^T \left(Q\Phi + \Phi^T Q\right)\mathbf{z}_t}{Y_t} + \gamma^2 \left\{\frac{\sum_i z_{i,t}^2 Q_{ii}}{Y_t} - \frac{2\mathbf{z}_t^T Q \operatorname{diag}\left(\mathbf{z}_t^2\right)Q\mathbf{z}_t}{Y_t^2}\right\}\right] dt + \frac{2\gamma \mathbf{z}_t^T Q \operatorname{diag}\left(\mathbf{z}_t\right)}{Y_t} dW_t$$

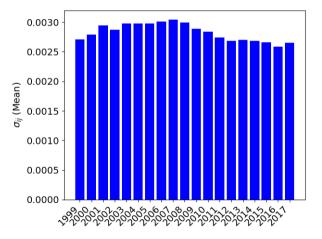
where
$$Y_t = \mathbf{z}_t^T Q \mathbf{z}_t$$
 and $\Phi = \Omega + \mu^2 \widetilde{X}$

| Description | Expression |
|----------------|--|
| Tech Spillover | $\mathbf{z}_t^T (Q\Omega + \Omega Q) \mathbf{z}_t / Y_t$ |
| R&D | $\mu^2 \mathbf{z}_t^T ig(Q \widetilde{X} + \widetilde{X}^T Q ig) \mathbf{z}_t / Y_t$ |
| Ito | $\gamma^2 \left\{ \sum_i z_{i,t}^2 Q_{ii}/Y_t - 2 \mathbf{z}_t^T Q \mathrm{diag}\left(\mathbf{z}_t^2 ight) Q \mathbf{z}_t/Y_t^2 ight\}$ |
| Total | $\mathbf{E}\left[d\log Y_{t} ight]$ |

Number of Sample Firms

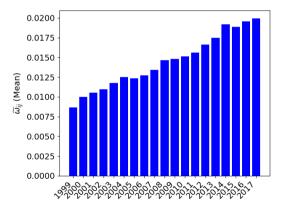


Trend of Product Substitutability

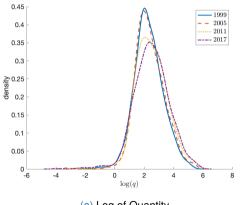


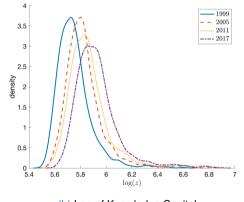
Technological Proximity

- Merge USPTO data with Compustat firms using DISCERN 2 dataset (Arora et al., 2024)
- Jaffe measure, Group-level patent classification, Stack for 5 years



Distributions of Estimated Knowledge Capital and Quantity





(a) Log of Quantity

(b) Log of Knowledge Capital

Microeconometric Estimates vs. GHL (Pellegrino, 2024) (1/2)

| Market | Firm i | Firm j | Micro Estimate | GHL |
|--------|----------------|---------------------------------------|----------------|--------|
| Auto | Ford | Ford | -4.320 | -5.197 |
| Auto | Ford | General Motors | 0.034 | 0.056 |
| Auto | Ford | Toyota | 0.007 | 0.017 |
| Auto | General Motors | Ford | 0.065 | 0.052 |
| Auto | General Motors | General Motors | -6.433 | -4.685 |
| Auto | General Motors | Toyota | 0.008 | 0.005 |
| Auto | Toyota | Ford | 0.018 | 0.025 |
| Auto | Toyota | General Motors | 0.008 | 0.008 |
| Auto | Toyota | Toyota | -3.085 | -4.851 |
| · | · | · · · · · · · · · · · · · · · · · · · | · | · |

Microeconometric Estimates vs. GHL (Pellegrino, 2024) (2/2)

| Market | $Firm\ i$ | $Firm\; j$ | Micro Estimate | GHL |
|-----------|-------------|-------------|----------------|--------|
| Cereals | Kellogg's | Kellogg's | -3.231 | -1.770 |
| Cereals | Kellogg's | Quaker Oats | 0.033 | 0.023 |
| Cereals | Quaker Oats | Kellogg's | 0.046 | 0.031 |
| Cereals | Quaker Oats | Quaker Oats | -3.031 | -1.941 |
| Computers | Apple | Apple | -11.979 | -8.945 |
| Computers | Apple | Dell | 0.018 | 0.025 |
| Computers | Dell | Apple | 0.027 | 0.047 |
| Computers | Dell | Dell | -5.570 | -5.110 |
| | - | | | |



First Stage Back

| | (1) |
|---------------------|-----------------|
| Dependent Variable: | $z_{i,t}$ |
| User cost of R&D | -39.495^{***} |
| Osei cosi di nad | (4.7044) |
| Year Fixed Effects | ✓ |
| No. observations | 12,947 |

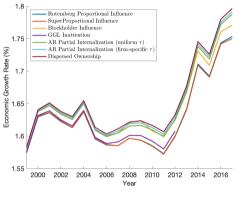
SEs clustered by years and 4-digit naics industries are reported in parentheses.

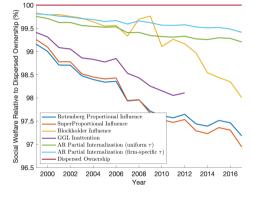
• IV: User cost of R&D, driven by state-level tax variations (Wilson, 2009; Bloom et al., 2013)

Alternative Corporate Governance Models: Ederer and Pellegrino (2024)

- 1. Super-proportional influence: $\tilde{\kappa}_{ij}=\frac{\sum_{z=1}^Z s_{iz}\gamma_{iz}s_{jz}}{\sum_{z=1}^Z s_{iz}\gamma_{iz}s_{iz}}$ where $\gamma_{iz}=\sqrt{s_{iz}}$
- 2. Blockholder influence: $\tilde{\kappa}_{ij}=\frac{\sum_{z=1}^{Z}s_{iz}b_{iz}s_{jz}}{\sum_{z=1}^{Z}s_{iz}s_{jz}}$ $(i\neq j),$ where $b_{iz}=1$ if $s_{iz}>5\%$
- 3. Rational investor inattention
 - Gilje et al. (2020) (GGL) estimate the probability that an investor votes against Institutional Shareholders Service recommendations
 - Utilize the estimate to capture the investor's level of attention
- 4. Governance frictions and entrenchment
 - Azar and Ribeiro (2021) (AR) estimate an objective function where the manager of firm i discounts other firms' profit by τ_i

Alternative Corporate Governance Models





(a) Expected Growth

(b) Expected Social Welfare

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