

Ownership Structure and Economic Growth

Koki Okumura

UCLA

Ownership Structure \Rightarrow Economic Growth?

- Ownership structure is concentrated
 - BlackRock, Vanguard, State Street, and Fidelity control 30% of votes of S&P 500 firms
 - Top 4 chaebols account for 55% of stock market capitalization in Korea

Share

Ownership Structure \implies Economic Growth?

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 - Top 4 chaebols account for 55% of stock market capitalization in Korea
- Firms maximize shareholder values \implies
Partially internalize externalities for commonly owned firm
- Ownership structure (common ownership, cross ownership, M&A, FDI, ...) \implies
Economic growth?
 - Business stealing effect
 - Technology spillover effect

Quantitative Schumpeterian Growth Model with Ownership Structure

- Existing Schumpeterian growth models:
 - Monopolistic competition (no strategic interaction)
 - Very few firms in Markov perfect equilibrium
- This paper: Many oligopolists + Ownership structure

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 - Ownership structure
 - Product market rivalry
 - Technology spillover

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 - Ownership structure
 - Product market rivalry
 - Technology spillover
- Common ownership in the US:
 - Internalization of business stealing $\Rightarrow g \downarrow \downarrow$
 - Internalization of technology spillover $\Rightarrow g \uparrow$

Literature

- Competition & Innovation:

d'Aspremont and Jacquemin (1988); Kamien et al. (1992); Aghion et al. (2001, 2005); Acemoglu and Akcigit (2012); Aghion et al. (2013); Bloom et al. (2013); Lopez and Vives (2019); Peters (2020); Akcigit and Ates (2021, 2023); Liu et al. (2022); Cavenaile et al. (2023); Anton et al. (2023, 2024); Kini et al. (2024); Hopenhayn and Okumura (2024)

[Quantitative Schumpeterian growth model with ownership structure](#)

- Hedonic Demand / Empirical IO:

Lancaster (1966); Rosen (1974); Berry et al. (1995); Nevo (2001); Pellegrino (2024); Ederer and Pellegrino (2024)

[Dynamic general equilibrium / R&D](#)

- Oligopoly / Common Ownership / Market Power:

Rubinstein and Yaari (1983); Rotemberg (1984); Neary (2003); Atkeson and Burstein (2008); Gutierrez and Philippon (2017); He and Huang (2017); Azar et al. (2018, 2022); Autor et al. (2020); Baqaee and Farhi (2020); De Loecker et al. (2020); Azar and Vives (2021); Edmond et al. (2023)

Model

- Firm $i \in \{1, \dots, n\}$

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- Final good linear quadratic aggregator (Pellegrino, 2024; Ederer and Pellegrino, 2024):

$$Y_t = \mathbf{q}_t^T \mathbf{b}_t - \frac{1}{2} \mathbf{q}_t^T \mathbf{\Sigma} \mathbf{q}_t$$

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- CRS intermediate good production technology:

$$q_{i,t} = a_{i,t} l_{i,t}$$

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- CRS intermediate good production technology:

$$q_{i,t} = a_{i,t} l_{i,t}$$

- Each firm has knowledge capital (state variable): $z_{i,t}$
- Each firm allocates knowledge capital to improve labor productivity and product quality:

$$\zeta a_{i,t} + b_{i,t} = z_{i,t}$$

Law of Motion of Knowledge Capital

$$dz_t = \left(\underbrace{\Omega z_t}_{\text{tech spillover}} + \underbrace{\mu x_t}_{\text{R\&D}} \right) dt + \underbrace{\gamma z_t \circ dW_t}_{\text{shocks}}$$

- $\Omega = [\omega_{ij}]$: technology spillover matrix
- $x_{i,t} = \sqrt{d_{i,t}}$
 - $d_{i,t}$: R&D input in terms of final good
 - Innovation elasticity is 0.5
- μ, γ : positive scalars

Market Clearing and Preference

- Inelastic labor supply:

$$L = \sum_i l_{i,t}$$

- Final good market clearing:

$$C_t + \underbrace{\sum_i d_{i,t}}_{\text{R\&D input}} = Y_t$$

- Risk neutral representative household:

$$\max E_t \left[\int_t^\infty \exp(-\rho s) C_s ds \right]$$

Common Ownership Weights

- $K = [\kappa_{ij}]$: common ownership weights that firm i places on the value of firm j ($\kappa_{ii} = 1$)
- More overlapping ownership b/w firm i and $j \implies$ Higher κ_{ij}
- $K = I$: dispersed ownership (each firm maximizes its own value)
- $K = \mathbf{1}_{n \times n}$: monopoly (maximizes total producer surplus)

Proportional Influence

Cournot-Nash Equilibrium

- Firm i 's gross profit before subtracting dynamic R&D cost: [Diagram](#)

$$\pi_{i,t} = p_{i,t}q_{i,t} - w_t l_{i,t} = \left(b_{i,t} - \sum_j \sigma_{ij} q_{j,t} - \frac{w_t}{a_{i,t}} \right) q_{i,t} \quad \text{where} \quad \zeta a_{i,t} + b_{i,t} = z_{i,t}$$

- Given w_t , $z_{i,t}$, and $\{q_{j,t}\}_{j \neq i}$, firm i chooses $a_{i,t}$, $b_{i,t}$, and $q_{i,t}$ to maximize $\sum_j \kappa_{ij} \pi_{j,t}$

Cournot-Nash Equilibrium

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- Given w_t , $z_{i,t}$, and $\{q_{j,t}\}_{j \neq i}$, firm i chooses $a_{i,t}$, $b_{i,t}$, and $q_{i,t}$ to maximize $\sum_j \kappa_{ij} \pi_{j,t}$
- Quantity is a linear function of knowledge capital:

$$q(z_t) = \left\{ \underbrace{2 \frac{\zeta}{L} \mathbf{1}_{n \times n}}_{\text{labor cost}} + \underbrace{\Sigma}_{\text{substitutability}} + \underbrace{K \circ \Sigma}_{\text{ownership} \times \text{substitutability}} \right\}^{-1} z_t$$

- Ownership-weighted gross profits are expressed in quadratic form: $\sum_j \kappa_{ij} \pi_{j,t} = z_t^T Q^i z_t$ [Q](#)

Linear-Quadratic Differential Game

- Given other firms' R&D $\{x_{j,t}\}_{j \neq i, t \geq 0}$, firm i chooses R&D $\{x_{i,t}\}_{t \geq 0}$ to maximize

$$\max_{\{x_{i,t}\}_{t \geq 0}} V^i(z_0) \equiv E_0 \left[\int_0^\infty \exp(-\rho t) \left\{ \sum_j \kappa_{ij} (\pi_{j,t} - x_{j,t}^2) \right\} dt \right]$$

subject to $dz_t = (\Omega z_t + \mu x_t) dt + \gamma z_t \circ dW_t$

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- Firm i 's HJB equation:

$$\rho V^i(z) = \max_{x_i} \left\{ z^T Q^i z - \sum_j \kappa_{ij} x_j^2 + V_z^i(z) [\mathbf{\Omega}z + \mu x] + \frac{\gamma^2}{2} z^T V_{zz}^i(z) z \right\}$$

HJB Equations \implies Riccati Equations

- Guess and verify $V^i(z) = z^T X^i z$ (for any z)
- X^i is the solution of stacked algebraic Riccati equations Riccati
- All public patenting firms in the US in our dataset ≈ 1000 firms \implies
 $1000^3 = 1$ billion undetermined coefficients (20 seconds on my laptop)

Oligopolistic Schumpeterian	Computation time	# of firms	Productivity space
Cavenaile et al. (2023)	$O(2^n)$	4	6 grid
Our model	$O(n^4)$	≈ 1000	Continuous

Balance Growth Path

- R&D strategy: $x_{i,t} = (\mu X_i^i)^T z_t$ where X_i^i is the i th column of X^i
- The law of motion is rewritten as $dz_t = \Phi z_t dt + \gamma z_t \circ dW_t$ where

$$\Phi \equiv \underbrace{\Omega}_{\text{Tech Spillover}} + \underbrace{\mu^2 [X_1^1 \cdots X_n^n]^T}_{\text{R\&D}}$$

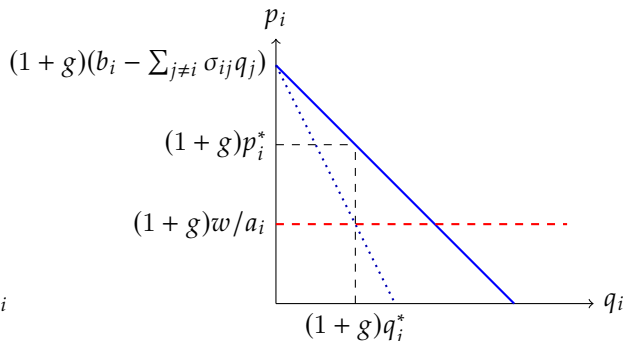
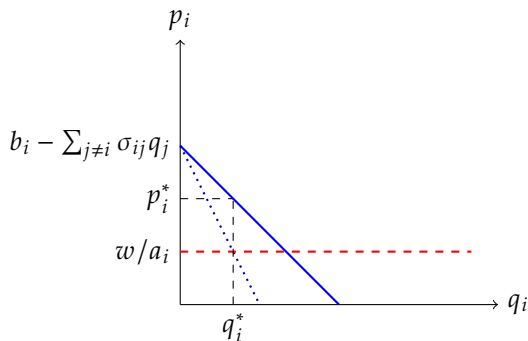
Theorem

Consider the deterministic economy ($\gamma = 0$). If Φ is irreducible, then:

- There exists largest positive eigenvalue of Φ , g , and associated positive eigenvector, z^* .
- There exists a globally stable BGP such that the knowledge capital growth rate of all firms is g , and the knowledge capital distribution is a scalar multiple of z^* .

- Proof: Perron–Frobenius Theorem
- “ Φ is irreducible” \iff “All firms are directly or indirectly connected technologically”

Partial Equilibrium Diagram and (Deterministic) BGP



- a_i , b_i , $q_i (= a_i l_i)$, p_i , and w/a_i grow at the same rate of g
- (i) (consumer surplus / producer surplus) and (ii) (cost / revenue) stay the same

Expected Growth Rate and Utility

- Apply Ito's lemma:

$$\begin{aligned} \log Y_t &= \log (z_t^T Q z_t) \\ dz_t &= \Phi z_t dt + \gamma z_t \circ dW_t \implies E_t [g_t | z_t] \end{aligned}$$

Decomposition

- Expected utility is expressed in quadratic form:

$$E_t \left[\int_t^\infty \exp(-\rho s) C_s ds \middle| z_t \right] = z_t^T X z_t$$

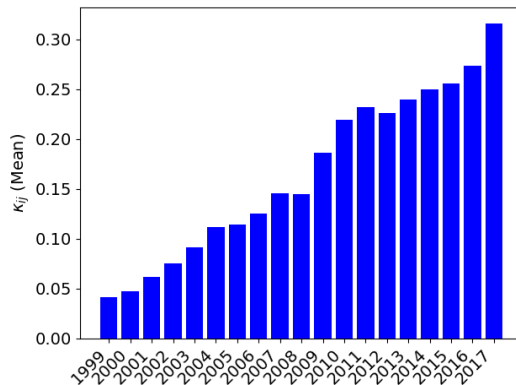
- Solve the equilibrium once \implies Can compute expected growth and utility for any z_t

x

Common Ownership K

- Backus et al. (2021) construct a dataset on investors' holdings based on Form 13F
- Baseline: Rotemberg (1984) proportional influence

Proportional Influence



Product Market Rivalry Σ

- Hoberg and Phillips (2016) estimates product proximity using business descriptions in 10-K
- Pellegrino (2024) estimates α to align with the cross-price elasticity of demand micro estimates

$$\underbrace{\sigma_{ij}}_{\text{substitutability}} = \alpha \times \text{product proximity b/w } i \text{ and } j \quad (i \neq j)$$

Technological Proximity $\tilde{\Omega}$

- Technological profile of firm i
 - The vector of the share of patents held by firm i in each technology class
 - Baseline: group-level patent classifications (≈ 4000)
- Jaffe (1986) technological proximity measure $\tilde{\omega}_{ij}$:
 - Cosine similarity of the technological profiles b/w firm i and j

Distribution of Knowledge Capital z_t

Variables	Identification
$\pi_{i,t}$	Gross profit (before R&D cost) = Revenue – Cost of goods sold
\boldsymbol{q}_t	$\pi_{i,t} = \sum_j \kappa_{ij} \sigma_{ij} q_{i,t} q_{j,t}$
ζ/L	Matches sample firms' cost share (average markup)
\boldsymbol{z}_t	$\boldsymbol{z}_t = \left\{ 2 \frac{\zeta}{L} \boldsymbol{J} + \boldsymbol{\Sigma} + \boldsymbol{K} \circ \boldsymbol{\Sigma} \right\} \boldsymbol{q}_t$

Technology Spillover $\Omega = \beta \times \text{Technological Proximity } \tilde{\Omega}$ First Stage

$$z_{i,t+1} - z_{i,t} = \beta \sum_{j \neq i} \tilde{\omega}_{ij,t} z_{j,t} + \text{Year FE}_t + \epsilon_{i,t}$$

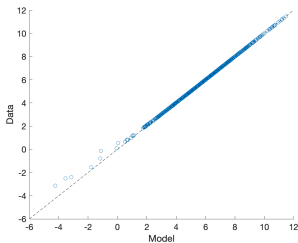
	(1)	(2)	(3)
	$z_{i,t+1} - z_{i,t}$	$z_{i,t+1} - z_{i,t}$	$z_{i,t+1} - z_{i,t}$
$\sum_{j \neq i} \tilde{\omega}_{ij,t} z_{j,t}$	0.000191** (0.000035)	0.000152*** (0.000035)	0.000140*** (0.000039)
$\sqrt{\text{R\&D Expenditure}}$		0.037** (0.021)	
Year Fixed Effects	✓	✓	✓
IV			✓
IV 1st Stage F-statistics			4176
No. observations	16,324	15,173	14,181

SEs clustered by years and 4-digit naics industries are reported in parentheses. * $p < 0.1$, ** $p < 0.05$, *** $p < 0.01$.

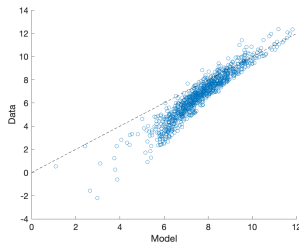
- IV: Firm-specific tax price of R&D from federal and state-specific rules (Bloom et al., 2013)

Fit b/w Model and Data

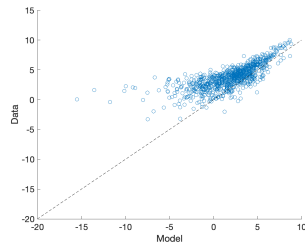
- Comparison of firm-level model-generated values (x -axis) with observed data (y -axis)



(a) Log of Profit (Targeted)



(b) Log of Sales



(c) Log of R&D Expenditure

Counterfactual Ownership Structures

Ownership Structure	Description
Baseline	Observed ownership structure in 2017
Dispersed	$K^D = I$
Mean=1999	$\kappa_{ij,2017}^{M1999} = \text{const} \times \kappa_{ij,2017}$ and $E \left[\kappa_{ij,2017}^{M1999} \right] = E \left[\kappa_{ij,1999} \right]$ for $j \neq i$
Uniform	$\kappa_{ij,2017}^U = E \left[\kappa_{ij,2017} \right]$ for $j \neq i$
Monopoly	$K^M = 1$

Total Output

Total Output in 2017 (Social Optimum: 100)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	91.30	91.02	90.78	89.08	89.17
Only Business Steal $\Omega = [0]$					
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

- Inelastic labor supply \implies Changes arise from product misallocation
- Common ownership exacerbates product misallocation

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Only Business Steal $\Omega = [0]$	91.30	91.02	90.78	89.08	89.17
Only Tech Spill $\Sigma = I, \zeta/L = 0$	75.00	75.00	75.00	75.00	75.00

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- Common ownership exacerbates product misallocation

Total R&D Expenditure

Total R&D in 2017 (Social Optimum: 100)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	27.08	26.83	26.44	23.21	18.48
Only Business Steal $\Omega = [0]$					
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- Internalization of business stealing > Internalization of technology spillover
- Network heterogeneity is important

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Only Business Steal $\Omega = [0]$	29.08	28.72	27.95	24.23	18.85
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Only Tech Spill $\Sigma = I, \zeta/L = 0$	18.27	18.34	18.75	18.86	19.84

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- Network heterogeneity is important

Expected Growth Rate

Expected Economic Growth Rate in 2017 (%)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	1.796	1.793	1.791	1.753	1.713
Only Business Steal $\Omega = [0]$					
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

- In baseline, the expected growth rate is
 - 0.043 pp (2.4%) lower compared to dispersed ownership, and
 - 0.040 pp (2.2%) lower compared to common ownership level in 1999.

Expected Growth Rate

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	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	1.796	1.793	1.791	1.753	1.713
Only Business Steal $\Omega = [0]$	1.097	1.094	1.093	1.062	1.020
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

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Only Business Steal $\Omega = [0]$	1.097	1.094	1.093	1.062	1.020
Only Tech Spill $\Sigma = I, \zeta/L = 0$	2.051	2.054	2.068	2.072	2.107

- In baseline, the expected growth rate is
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Expected Social Welfare

Expected Social Welfare (Social Optimum: 100)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	87.72	87.42	87.16	85.25	85.18
Only Business Steal $\Omega = [0]$					
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

- In the baseline, the consumption-equivalent welfare loss is
 - 2.8% compared to dispersed ownership, and
 - 2.5% compared to the common ownership level in 1999.

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	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	87.72	87.42	87.16	85.25	85.18
Only Business Steal $\Omega = [0]$	88.83	88.53	88.30	86.44	86.41
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

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Only Business Steal $\Omega = [0]$	88.83	88.53	88.30	86.44	86.41
Only Tech Spill $\Sigma = I, \zeta/L = 0$	68.81	68.82	68.88	68.89	69.02

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 - 2.5% compared to the common ownership level in 1999.

Firm Value Share

Firm Value Share in 2017 (%)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	28.74	29.63	33.43	33.34	40.92
Only Business Steal $\Omega = [0]$					
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

- In baseline, firm value share is
 - 5.6% higher compared to dispersed ownership, and
 - 4.7% higher compared to common ownership level in 1999.

Firm Value Share

Firm Value Share in 2017 (%)	Ownership (Baseline: 2017)				
	Dispersed	Mean=1999	Uniform	Baseline	Monopoly
Baseline	28.74	29.63	33.43	33.34	40.92
Only Business Steal $\Omega = [0]$	27.91	28.80	32.60	33.51	40.14
Only Tech Spill $\Sigma = I, \zeta/L = 0$					

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Only Business Steal					
$\Omega = [0]$	27.91	28.80	32.60	33.51	40.14
Only Tech Spill					
$\Sigma = I, \zeta/L = 0$	64.82	64.81	64.76	64.74	64.63

- In baseline, firm value share is
 - 5.6% higher compared to dispersed ownership, and
 - 4.7% higher compared to common ownership level in 1999.

Conclusion

- Quantitative Schumpeterian growth model with ownership structure
 - Utilize micro data and computational capability
- Common ownership in the US:
 1. Internalization of business stealing effect $\Rightarrow g \downarrow \downarrow$
 2. Internalization of technology spillover effect $\Rightarrow g \uparrow$
- Potential applications:
 - Chaebols in Korea
 - Zaibatsu (pre-WWII) and cross-shareholding (late 20th century) in Japan
 - FDI / multinational companies and international technology diffusion

Share of Top 5 Shareholders in Largest Market Cap Firms [Back](#)

Microsoft	
Vanguard	9.20%
Blackrock	7.75%
Steven Ballmer	4.48%
State Street	3.97%
Fidelity	2.66%

Google	
Vanguard	7.36%
Blackrock	6.47%
State Street	3.39%
Fidelity	3.01%
Sergey Brin	2.99%

Nvidia	
Vanguard	8.93%
BlackRock	7.74%
Fidelity	4.12%
State Street	3.97%
Jensen Huang	3.80%

Amazon	
Jeffrey Bezos	8.58%
Vanguard	7.77%
Blackrock	6.50%
State Street	3.44%
Fidelity	3.10%

Apple	
Vanguard	9.29%
Blackrock	7.48%
State Street	3.96%
Fidelity	2.27%
Geode Capital	2.26%

Meta	
Vanguard	7.55%
Blackrock	6.50%
Fidelity	5.38%
Accel IX LP	3.88%
State Street	3.40%

Equity Investments by Big tech in AI Startups [Back](#)

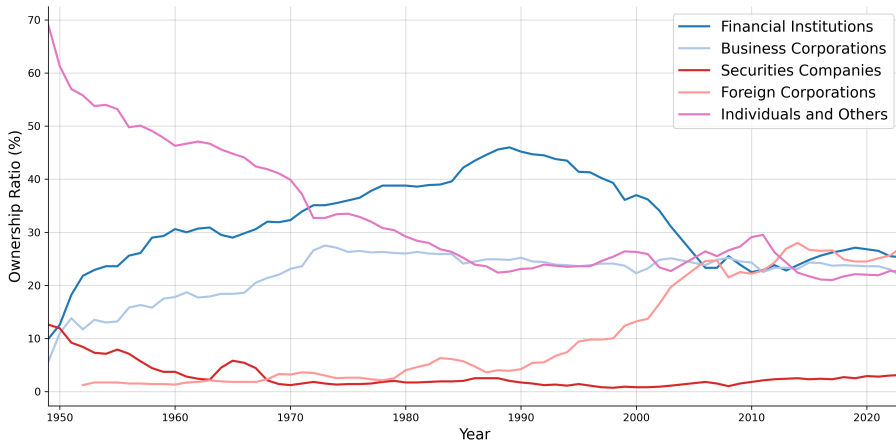
Shareholding percentage	Microsoft	Google	Amazon
OpenAI (ChatGPT)	49%	—	—
Anthropic (Claude)	—	14%	23%

Technology & Product Proximity: Example

Tesla vs. Ford	
Technology Proximity	0.11
Product Proximity	0.15

Apple vs. Intel	
Technology Proximity	0.57
Product Proximity	0.00

Ownership Ratio by Holder Types in Japan



Simple Model

- Static partial equilibrium model of oligopolistic competition in production and R&D
 - d'Aspremont and Jacquemin (1988); Kamien et al. (1992); Leahy and Neary (1997); Lopez and Vives (2019); Anton et al. (2024)
- Firm $i \in \{1, \dots, n\}$ chooses quantity q_i and R&D effort x_i
- Linear inverse demand: $p(q) = b - \Sigma q$ ($\sigma_{ii} = 1$)
- CRS production technology with marginal cost: $m(x) = \bar{m} - \Omega x$
- Quadratic cost of R&D: $c(x_i) = \frac{1}{2}x_i^2$

Cournot & R&D Game

- Firm i 's profit:

$$\begin{aligned}\pi_i(\mathbf{q}, \mathbf{x}) &= [p_i(\mathbf{q}) - m_i(\mathbf{x})]q_i - c(x_i) \\ &= \left[b_i - \sum_{j=1}^n \sigma_{ij}q_j - \bar{m}_i + \sum_{j=1}^n \omega_{ij}x_j \right] q_i - \frac{1}{2}x_i^2\end{aligned}$$

- Given $\{q_j, x_j\}_{j \neq i}$, firm i chooses q_i and x_i to maximize $\sum_j \kappa_{ij} \pi_j(q, x)$

- Comparative statics where $\{q_k, x_k\}_{k \neq i}$ are held constant:

Rotemberg (1984) Proportional Influence

- $o \in \{1, 2, \dots, n_o\}$: owners
- s_{io} : the proportion of shares in firm i owned by owner o where $\sum_o s_{io} = 1$
- \widehat{V}_i : value of firm i
- $\widetilde{V}_o \equiv \sum_i s_{io} \widehat{V}_i$: value of owner o
- Firms' objective:

$$\sum_o s_{io} \widetilde{V}_o \propto \sum_j \kappa_{ij} \widehat{V}_j$$

where

$$\kappa_{ij} \equiv \frac{\mathbf{s}_i^T \mathbf{s}_j}{\sqrt{\mathbf{s}_i^T \mathbf{s}_i \mathbf{s}_j^T \mathbf{s}_j}} = \cos(\mathbf{s}_i, \mathbf{s}_j) \quad \text{where} \quad \mathbf{s}_i \equiv [s_{i1}, \dots, s_{i0}, \dots, s_{in_0}]^T$$

Total Surplus

- Total surplus for product i :

$$ts_i(\mathbf{q}, \mathbf{x}) = \pi_i(\mathbf{q}, \mathbf{x}) + cs_i(\mathbf{q}) = q_i \left[b_i - \frac{1}{2} \sum_{j=1}^n \sigma_{ij} q_j - \bar{m}_i + \sum_{j=1}^n \omega_{ij} x_j \right] - \frac{1}{2} x_i^2$$

1. Business stealing effect
 - Innovators steal the business (profits) of other firms
2. Technology spillover effect
 - Innovation improves the productivity of other firms
3. Appropriability effect (market power)
 - Innovators cannot appropriate the entire consumer surplus

R&D Allocation and Externalities

- Firms maximize common owner weighted profits:

$$x^* = (K \circ \Omega)[\Sigma + K \circ \Sigma - \Omega(K \circ \Omega)]^{-1}(b - \bar{m})$$

- Firms maximize common owner weighted total surplus (★):

$$x_{TS}^* = (K \circ \Omega) \left[\frac{1}{2}(\Sigma + K \circ \Sigma) - \Omega(K \circ \Omega) \right]^{-1} (b - \bar{m})$$

- $K = [1]$ in (★) \implies Social Optimum
- Externalities: (i) Appropriability, (ii) Business stealing, (iii) Technology spillover

Generalized Hedonic-Linear Demand (Pellegrino, 2024)

- $i \in \{1, 2, \dots, n\}$: firms / products
- 1 unit of product i provides
 - 1 unit of idiosyncratic characteristic $k \in \{1, 2, \dots, n\}$
 - $\psi_{k,i}$ unit of shared characteristic $k \in \{n+1, n+2, \dots, n+n_k\}$ where $\sum_k \psi_{k,i}^2 = 1$
- Aggregate each characteristic:

$$y_{k,t} = \begin{cases} q_{k,t} & k = 1, 2, \dots, n \\ \sum_i \psi_{k,i} q_{i,t} & k = n+1, n+2, \dots, n+n_k \end{cases}$$

- Linear quadratic aggregator over characteristics:

$$Y_t = (1 - \alpha) \sum_{k=1}^n \left(\underbrace{\hat{b}_{k,t} y_{k,t} - \frac{1}{2} y_{k,t}^2}_{\text{idiosyncratic characteristic}} \right) + \alpha \sum_{k=n+1}^{n+n_k} \left(\underbrace{\hat{b}_{k,t} y_{k,t} - \frac{1}{2} y_{k,t}^2}_{\text{shared characteristic}} \right)$$

Preview of Identification Strategy

Networks	Measurement
Common ownership K	Institutional investor holdings (Backus et al., 2021)
Product market rivalry Σ	Product proximity (Hoberg and Phillips, 2016): Text analysis of business description
Technology spillover Ω	Technology proximity (Jaffe, 1986; Bloom et al., 2013): Patent classification

Generalized Hedonic-Linear Demand (Pellegrino, 2024)

- Quality:

$$b_i = (1 - \alpha) \hat{b}_i + \alpha \sum_{k=n+1}^{n+n_k} \psi_k \hat{b}_k$$

- Inverse demand:

$$\frac{p}{P} = b - \Sigma q$$

- Inverse cross price elasticity of demand:

$$\frac{\partial \log p_i}{\partial \log q_j} = -\frac{q_j}{p_i} \cdot \sigma_{ij}$$

- Cross price elasticity of demand:

$$\frac{\partial \log q_i}{\partial \log p_j} = -\frac{p_j}{q_i} (\Sigma^{-1})_{ij}$$

Static Profits

- Gross profit: $\pi_{i,t} = \sum_j \kappa_{ij} \sigma_{ij} q_{i,t} q_{j,t}$
- Firms choose labor productivity and product quality: $\zeta a_{i,t} = \sqrt{\zeta w_t}$, $b_{i,t} = z_{i,t} - \sqrt{\zeta w_t}$
- Labor market clearing: $L = \sum_i \frac{q_{i,t}}{a_{i,t}} \implies \sqrt{\zeta w_t} = \frac{\zeta}{L} \sum_i q_{i,t}$
- $q_t = N z_t$ where $N \equiv \left\{ 2 \frac{\zeta}{L} J + \Sigma + K \circ \Sigma \right\}^{-1}$
- N_i : the i th row of N
- Ownership weighted profit:

$$\sum_j \kappa_{ij} \frac{\pi_{j,t}}{P_t} = \sum_j \kappa_{ij} \sum_h \kappa_{jh} \sigma_{jh} q_{j,t} q_{h,t} = z_t^T Q^i z_t$$

where

$$Q^i = \frac{1}{2} \sum_j \kappa_{ij} \sum_h \kappa_{jh} \sigma_{jh} \left(N_j^T N_h + N_h^T N_j \right)$$

Riccati Equations

- $V^i(z) = z^T X^i z$ where X^i is the solution of the stacked Riccati equation

$$0 = Q^i - \mu^2 \sum_j \kappa_{ij} X_j^j (X_j^j)^T + \left(\Phi - \frac{1}{2} (\rho - \gamma^2) I \right)^T X^i + X^i \left(\Phi - \frac{1}{2} (\rho - \gamma^2) I \right)$$

- $X_i^i \equiv$ the i th column of X^i
- $\Phi \equiv \Omega + \mu^2 \begin{bmatrix} X_1^1 & \cdots & X_n^n \end{bmatrix}^T$
- Algorithm: Given $\begin{bmatrix} X_\tau^1 & \cdots & X_\tau^n \end{bmatrix}$, update $\begin{bmatrix} X_{\tau-\Delta}^1 & \cdots & X_{\tau-\Delta}^n \end{bmatrix}$ by

$$-\frac{X_\tau^i - X_{\tau-\Delta}^i}{\Delta} = Q^i - \mu^2 \sum_j \kappa_{ij} X_{j,\tau}^j (X_{j,\tau}^j)^T + \left(\Phi_\tau - \frac{1}{2} (\rho - \gamma^2) I \right)^T X_\tau^i + X_\tau^i \left(\Phi_\tau - \frac{1}{2} (\rho - \gamma^2) I \right)$$

Summary of Equilibrium

Description	Expression
Production strategy	$\mathbf{q}_t = N \mathbf{z}_t$
R&D strategy	$\mathbf{x}_t = \mu \tilde{X} \mathbf{z}_t$
Law of motion	$d\mathbf{z}_t = (\Omega \mathbf{z}_t + \mu \mathbf{x}_t) dt + \gamma \mathbf{z}_t dW_t$
Profit of final producers	$\Pi_t^F / P_t = \mathbf{q}_t^T \left(\frac{1}{2} \Sigma \right) \mathbf{q}_t$
Total operating profit of firms	$\Pi_t / P_t = \mathbf{q}_t^T \left(\frac{1}{2} \Sigma \circ (K + K^T) \right) \mathbf{q}_t$
Labor income	$w_t L / P_t = \mathbf{q}_t^T \left(\frac{\zeta}{L} J \right) \mathbf{q}_t$
Output	$Y_t = \mathbf{q}_t^T \left(\frac{\zeta}{L} J + \frac{1}{2} \Sigma + \frac{1}{2} \Sigma \circ (K + K^T) \right) \mathbf{q}_t$
Consumption	$C_t = Y_t - \mathbf{x}_t^T \mathbf{x}_t$

Intuition of Why the Model Has the BGP

- On the BGP, a_t , b_t , z_t , and q_t grow at the same rate

Technological Choice: $\zeta a_{i,t} + b_{i,t} = z_{i,t}$

Linear Production Technology: $q_{i,t} = a_{i,t} l_{i,t}$

Inelastic Labor Supply: $L = \sum_i l_{i,t}$

- Linear and quadratic term in q_t of output grow at the same rate: [Equilibrium Summary](#)

$$Y_t = q_t^T b_t - \frac{1}{2} q_t^T \Sigma q_t$$

Output and Expected Utility

- Output: $Y_t = q_t^T Q q_t$ where

$$Q = \frac{\zeta}{L} J + \frac{1}{2} \Sigma + \frac{1}{2} \Sigma \circ (K + K^T)$$

- Expected utility:

$$V(z_t) \equiv E_t \left[\int_t^\infty \exp(-\rho s) C_s ds \middle| z_t \right] = z_t^T X z_t$$

where X is the solution of the Lyapunov equation (obtained from households' HJB equation):

$$0 = Q - \mu^2 \tilde{X}^T \tilde{X} + X \left(\Phi - \frac{1}{2} (\rho - \gamma^2) I \right) + \left(\Phi - \frac{1}{2} (\rho - \gamma^2) I \right)^T X$$

Social Optimum

- Static optimal allocation: $q_t^* = N^* z_t$ where $N^* \equiv \{2\frac{\zeta}{L}J + \Sigma\}^{-1}$
- Optimal output: $Y_t^* = z_t^T Q^* z_t$ where $Q^* = \frac{1}{2}N^*$
- Optimal expected utility:

$$V^*(z_t) \equiv E_t \left[\int_t^\infty \exp(-\rho s) C_s ds \middle| z_t \right] = z_t^T X^* z_t,$$

where X^* is the solution of the Riccati equation (obtained from planner's HJB equation):

$$0 = Q^* - \mu^2 (X^*)^2 + X^* \left(\Phi^* - \frac{1}{2} (\rho - \gamma^2) I \right) + \left(\Phi^* - \frac{1}{2} (\rho - \gamma^2) I \right) X^*$$

- Optimal R&D: $x_t^* = \mu X^* z_t$
- Optimal technology transition matrix: $\Phi^* = \Omega + \mu^2 X^*$

Stochastic Process of Output

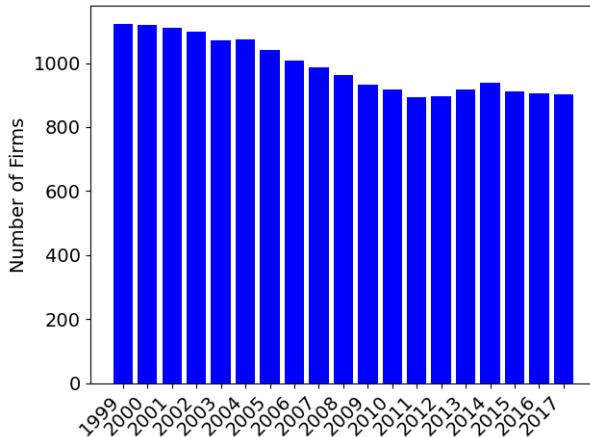
- Applying Itô's lemma,

$$d \log Y_t = \left[\frac{\mathbf{z}_t^T (Q\Phi + \Phi^T Q) \mathbf{z}_t}{Y_t} + \gamma^2 \left\{ \frac{\sum_i z_{i,t}^2 Q_{ii}}{Y_t} - \frac{2\mathbf{z}_t^T Q \text{diag}(\mathbf{z}_t^2) Q \mathbf{z}_t}{Y_t^2} \right\} \right] dt + \frac{2\gamma \mathbf{z}_t^T Q \text{diag}(\mathbf{z}_t)}{Y_t} dW_t$$

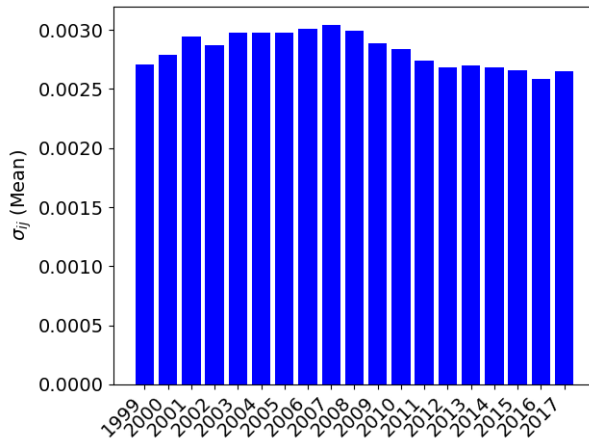
where $Y_t = \mathbf{z}_t^T Q \mathbf{z}_t$ and $\Phi = \Omega + \mu^2 \tilde{X}$

Tech Spillover	$\frac{\mathbf{z}_t^T (Q\Omega + \Omega Q) \mathbf{z}_t}{Y_t}$
R&D Contribution	$\frac{\mu^2 \mathbf{z}_t^T (Q\tilde{X} + \tilde{X}^T Q) \mathbf{z}_t}{Y_t}$
Itô Correction	$\gamma^2 \left\{ \frac{\sum_i z_{i,t}^2 Q_{ii}}{Y_t} - \frac{2\mathbf{z}_t^T Q \text{diag}(\mathbf{z}_t^2) Q \mathbf{z}_t}{Y_t^2} \right\}$
Total	$E[d \log Y_t]$

Number of Sample Firms

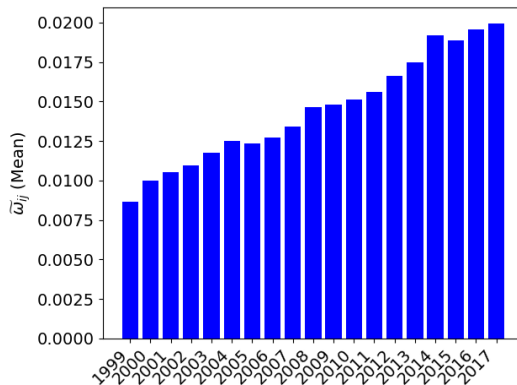


Trend of Product Substitutability



Technological Proximity

- Merge USPTO data with Compustat firms using DISCERN 2 dataset (Arora et al., 2024)
- Jaffe measure, Group-level patent classification, Stack for 5 years

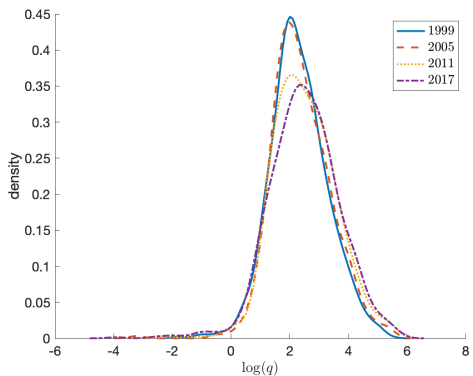


Identification: Summary

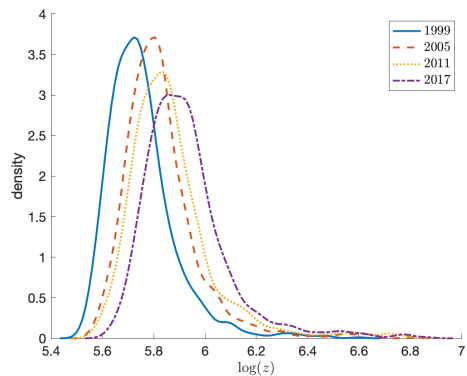
- Publicly available data + Compustat

Notation	Description	Value	Source
Σ	Product proximity		Form 10-K, Hoberg and Phillips (2016)
$\tilde{\Omega}$	Technological proximity		USPTO, Patent classification
K	Common ownership weights		Form 13-F, Backus et al. (2021)
α	Product proximity \rightarrow Substitutability	0.12	Pellegrino (2024)
β	Technological proximity \rightarrow Spillover	0.00014	Estimate the law of motion
γ	St.d. of idiosyncratic shocks	0.027	Estimate the law of motion
ζ/L	Labor augmentation efficiency	0.0063	Compustat, Cost of goods sold
ρ	Discount rate	0.10	$>$ risk free rates, $<$ private R&D returns
μ	R&D efficiency	0.05	1.7% economic growth rate

Distributions of Estimated Knowledge Capital and Quantity



(a) Log of Quantity



(b) Log of Knowledge Capital

Microeconomic Estimates vs. GHL (Pellegrino, 2024) (1/2)

Market	Firm i	Firm j	Micro Estimate	GHL
Auto	Ford	Ford	-4.320	-5.197
Auto	Ford	General Motors	0.034	0.056
Auto	Ford	Toyota	0.007	0.017
Auto	General Motors	Ford	0.065	0.052
Auto	General Motors	General Motors	-6.433	-4.685
Auto	General Motors	Toyota	0.008	0.005
Auto	Toyota	Ford	0.018	0.025
Auto	Toyota	General Motors	0.008	0.008
Auto	Toyota	Toyota	-3.085	-4.851

Microeconomic Estimates vs. GHL (Pellegrino, 2024) (2/2)

Market	Firm i	Firm j	Micro Estimate	GHL
Cereals	Kellogg's	Kellogg's	-3.231	-1.770
Cereals	Kellogg's	Quaker Oats	0.033	0.023
Cereals	Quaker Oats	Kellogg's	0.046	0.031
Cereals	Quaker Oats	Quaker Oats	-3.031	-1.941
Computers	Apple	Apple	-11.979	-8.945
Computers	Apple	Dell	0.018	0.025
Computers	Dell	Apple	0.027	0.047
Computers	Dell	Dell	-5.570	-5.110

First Stage

[Back](#)

	(1)
Dependent Variable:	$z_{i,t}$
User cost of R&D	-39.495^{***} (4.7044)
Year Fixed Effects	✓
No. observations	12,947

SEs clustered by years and 4-digit naics industries are reported in parentheses.

- IV: User cost of R&D, driven by state-level tax variations (Wilson, 2009; Bloom et al., 2013)

When Common Ownership Affects only R&D Decisions

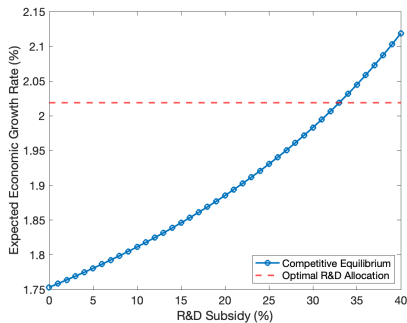
- Common ownership only influences R&D decisions (cf. d'Aspremont and Jacquemin (1988))

	Ownership Structure		
	Dispersed	Common R&D	Baseline
Output (Social Optimum: 100)	91.30	91.30	89.08
R&D Expenditure (Social Optimum: 100)	26.17	19.76	22.36
Expected Growth Rate (%)	1.796	1.726	1.753
Expected Social Welfare (Social Optimum: 100)	87.72	87.49	85.25
Firm Value Share (%)	28.74	29.04	34.34

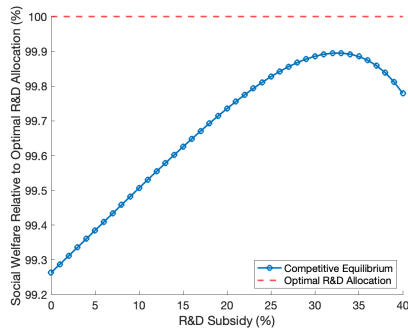
- Lowest R&D expenditure and expected growth rate
- Intermediate social welfare and firm value share

Optimal Uniform R&D Subsidy

Social Optimum



(a) Expected Growth

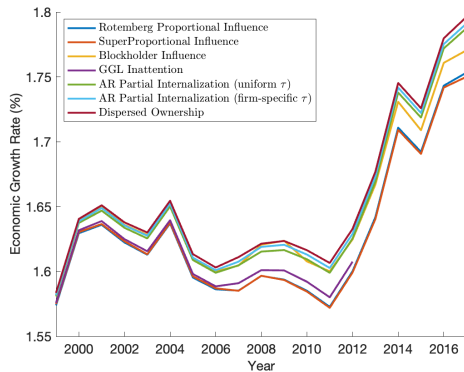


(b) Expected Social Welfare

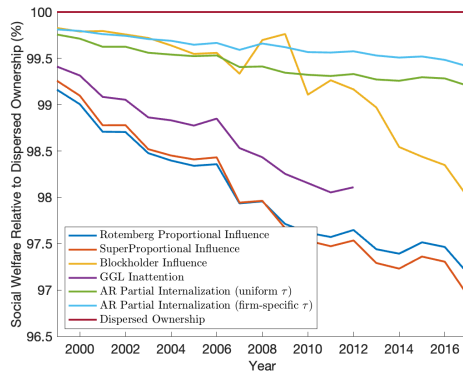
- Optimal rate is $s = 33\%$, which increases g by 0.25 pp (14%)

- Azar and Ribeiro (2021) (AR) estimate an objective function where the manager of firm i discounts other firms' profit by τ_i

Alternative Corporate Governance Models



(a) Expected Growth



(b) Expected Social Welfare

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