Assignment 7

Responsible TA: Claudi Lleyda Moltó

Delivery instructions

To deliver an assignment you have to make sure you deliver both parts. You can deliver as many times as you want before the deadline on Blackboard. Delivery should be done in two separate files according to the following specifications.

The theoretical question answers must be uploaded as PDF, how you answer the questions (handwritten scans, Word, LaTeX, etc.) doesn't matter, as long as they are delivered as a single PDF file and the answers are readable. The filename should contain your NTNU username and the assignment number, for instance: `karinor-07.pdf`.

The notebook should be delivered in full (as `.ipynb`). That way the TAs can easily run your code and verify the output. The filename should contain your NTNU username and the assignment number, for instance: `karinor-07.ipynb`.

Theory

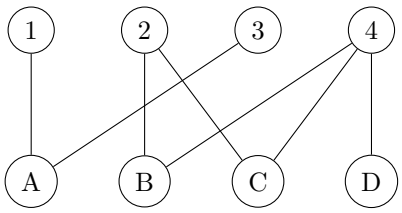
Task 1 - Maximum flow and minimum capacity cut

Prove or disprove the following statements.

1. Each maximum flow defines a unique minimum capacity cut.
2. Each minimum capacity cut defines a unique maximum flow.

Task 2 - Bipartite graph matching

Consider the following bipartite graph.



1. Use Hall's Theorem to determine whether a perfect matching exists.
2. Use the Ford–Fulkerson algorithm to find a maximal matching.

Task 3 - Antenna connections

Suppose we have n devices that want to connect to k cell towers. A device can only connect to a cell tower if it is close enough, and each cell tower can handle a maximum of N simultaneous connections.

Find a network flow algorithm that determines whether it is possible that every device connects to a cell tower with the given constraints.

Programming

This part should be solved in the corresponding Jupyter Notebook. Refer to the notebook for further details and instructions regarding the programming tasks.

Assignment submission

The assignments will be given out on Blackboard where each assignment has a written theoretical part and a programming part in Python using Jupyter Notebook. The notebook task can be solved locally (for instance in VSCode), or you can uploaded the notebook to JupyterHub and run the code there.

The notebooks will guide you though a, more or less, specific solution to a problem. You are however encouraged to attempt to implement your own/other solutions, as long as

- you don't use any additional libraries or packages,
- you don't alter the input values or structures, and
- your solution solves the problem described in the assignment.