

TMA4205 Numerical Linear Algebra Fall 2017

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Exercise set 6

Perform two steps of the Rayleigh quotient iteration with starting vector  $v^{(0)} = (1,0,0)^T$  for approximating an eigenvalue and eigenvector of the matrix

$$A = \begin{pmatrix} 2 & 1 & 1 \\ 1 & 1 & -2 \\ 0 & 0 & 1 \end{pmatrix}.$$

2 Perform one step of the QR-iteration with shift  $\mu=2$  in order to find the eigenvalues of the matrix

$$A = \begin{pmatrix} 6 & 3 \\ 3 & 2 \end{pmatrix}.$$

3 Assume that you apply one step of the QR-iteration with shift  $\mu$  in order to find the eigenvalues of a matrix A, and that this shift is actually equal to one of the eigenvalues of A. How can you easily detect this situation based on the QR-decomposition of the shifted matrix?