

**Задача №12.** Разложить данную функцию  $y = f(x)$  с периодом  $2\pi$ , заданную на интервале  $]-\pi, \pi[$ , в тригонометрический ряд Фурье.

**Задача №13.** Разложить функцию  $y = f(x)$ , заданную на интервале  $]0, l[$ , в тригонометрический ряд Фурье по косинусам.

**Задача №14.** Разложить функцию  $y = f(x)$ , заданную на интервале  $]0, l[$ , в тригонометрический ряд Фурье по синусам.

| Вариант | Задача 12  | Задача 13  | Задача 14   |
|---------|--|--|---|
| 1.      | $y = \begin{cases} 2, & -\pi < x < 0, \\ -x, & 0 \leq x < \pi. \end{cases}$          | $y = \begin{cases} 0, & 0 < x < 1, \\ x + 8, & 1 \leq x < 2. \end{cases}$    | $y = \begin{cases} 2, & 0 < x < 1, \\ x - 3, & 1 \leq x < 3. \end{cases}$     |
| 2.      | $y = \begin{cases} x, & -\pi < x < 0, \\ 0, & 0 \leq x < \pi. \end{cases}$           | $y = \begin{cases} 1+x, & 0 < x < 2, \\ 6, & 2 \leq x < 3. \end{cases}$      | $y = \begin{cases} 1, & 0 < x < 1, \\ x + 4, & 1 \leq x < 5. \end{cases}$     |
| 3.      | $y = \begin{cases} 2x, & -\pi < x < 0, \\ -x, & 0 \leq x < \pi. \end{cases}$         | $y = \begin{cases} 4, & 0 < x < 5, \\ 4x - 7, & 5 \leq x < 6. \end{cases}$   | $y = \begin{cases} 9, & 0 < x < 4, \\ 9 - x, & 4 \leq x < 8. \end{cases}$     |
| 4.      | $y = \begin{cases} x - 1, & -\pi < x < 0, \\ -5, & 0 \leq x < \pi. \end{cases}$      | $y = \begin{cases} 7, & 0 < x < 1, \\ 1 - x, & 1 \leq x < 3. \end{cases}$    | $y = 2x - 9, \quad l = 5$   |
| 5.      | $y = \begin{cases} \pi, & -\pi < x < 0, \\ \pi - x, & 0 \leq x < \pi. \end{cases}$   | $y = \begin{cases} 25, & 0 < x < 2, \\ \pi - 5, & 2 \leq x < 3. \end{cases}$ | $y = \begin{cases} 6 - 5x, & 0 < x < 1, \\ 0, & 1 \leq x < 3. \end{cases}$    |
| 6.      | $y = \left  \frac{\pi - x}{4 - 2} \right $   | $y = \begin{cases} 2, & 0 < x < 10, \\ -x, & 10 \leq x < 12. \end{cases}$    | $y = \begin{cases} 9, & 0 < x < 4, \\ 3x, & 4 \leq x < 8. \end{cases}$        |
| 7.      | $y = \begin{cases} -x, & -\pi \leq x < 0, \\ 3, & 0 \leq x < \pi. \end{cases}$       | $y = \begin{cases} 2 + x, & 0 < x < 1, \\ 0, & 1 \leq x < 3. \end{cases}$    | $y = \begin{cases} 0, & 0 < x < \pi, \\ 2x, & \pi \leq x < 2\pi. \end{cases}$ |
| 8.      | $y = \begin{cases} x - 9, & -\pi < x < 0, \\ -1, & 0 \leq x < \pi. \end{cases}$      | $y = \begin{cases} 1, & 0 < x < 3, \\ x - 8, & 3 \leq x < 5. \end{cases}$    | $y = \begin{cases} 0, & 0 < x < 2, \\ 1 - x, & 2 \leq x < 3. \end{cases}$     |
| 9.      | $y = \begin{cases} x + 3, & -\pi < x < 0, \\ -4, & 0 \leq x < \pi. \end{cases}$      | $y = \begin{cases} -6, & 0 < x < 3, \\ 6 - x, & 3 \leq x < 7. \end{cases}$   | $y = \begin{cases} 2, & 0 < x < 4, \\ x + 8, & 4 \leq x < 5. \end{cases}$     |
| 10.     | $y = \begin{cases} 0, & -\pi < x < 0, \\ 2 - x, & 0 \leq x < \pi. \end{cases}$       | $y = \begin{cases} x + 2, & 0 < x < 2, \\ -3, & 2 \leq x < 9. \end{cases}$   | $y = \begin{cases} 1, & 0 < x < 1, \\ 2x + 4, & 1 \leq x < 3. \end{cases}$    |
| 11.     | $y = \begin{cases} 2x + 3, & -\pi < x < 0, \\ -2, & 0 \leq x \leq \pi. \end{cases}$  | $y = \begin{cases} 2, & 0 < x < 5, \\ x - 5, & 5 \leq x < 9. \end{cases}$    | $y = \begin{cases} 0, & 0 < x < 1, \\ x + 8, & 1 \leq x < 2. \end{cases}$     |
| 12.     | $y = \begin{cases} 7 + x, & -\pi < x < 0, \\ -1, & 0 \leq x < \pi. \end{cases}$      | $y = \begin{cases} 1, & 0 < x < 4, \\ x - 3, & 4 \leq x < 9. \end{cases}$    | $y = 5x - 1, \quad l = \pi$   |
| 13.     | $y = \begin{cases} 4, & -\pi \leq x < 0, \\ x - 1, & 0 \leq x < \pi. \end{cases}$    | $y = \begin{cases} 4, & 0 < x < 3, \\ 3 - x, & 3 \leq x < 9. \end{cases}$    | $y = \begin{cases} 7, & 0 < x < 1, \\ 1 - x, & 1 \leq x < 3. \end{cases}$     |
| 14.     | $y = \begin{cases} 2x + 5, & -\pi < x < 0, \\ -3, & 0 \leq x < \pi. \end{cases}$     | $y = \begin{cases} 5, & 0 < x \leq 4, \\ 2x - 9, & 4 < x < 9. \end{cases}$   | $y = 2x - 3, \quad l = 2$   |
| 15.     | $y = \begin{cases} 0, & -\pi < x < 0, \\ x - 1, & 0 \leq x < \pi. \end{cases}$       | $y = \begin{cases} 2, & 0 < x < 1, \\ x - 3, & 1 \leq x < 3. \end{cases}$    | $y = 3x - 4, \quad l = 1$   |
| 16.     | $y = \begin{cases} x + 2\pi, & -\pi < x < 0, \\ -\pi, & 0 \leq x < \pi. \end{cases}$ | $y = \begin{cases} 1, & 0 < x < 1, \\ x + 4, & 1 \leq x < 5. \end{cases}$    | $y = 2x - 9, \quad l = 5$   |
| 17.     | $y =  2 - \pi x $  | $y = 4x - 3, \quad l = 2$  | $y = 2\pi x - 3\pi, \quad l = 2$  |

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|---------|---|--|---|
| 18.     | $y = \begin{cases} -5, & -\pi < x < 0, \\ \pi x - 1, & 0 \leq x < \pi. \end{cases}$ | $y = \begin{cases} 0, & 0 < x < 7, \\ 4x + 1, & 7 \leq x < 8. \end{cases}$     | $y = \begin{cases} 2, & 0 < x < 1, \\ x - 3, & 1 \leq x < 3. \end{cases}$       |
| 19.     | $y = \left  \frac{\pi}{2} - x \right $  | $y = 2x - 3, \quad l = 2$  | $y = \frac{2x - 3}{4}, \quad l = 4$   |
| 20.     | $y = \left  2\pi - \frac{x}{2} \right $   | $y = 3x - 4, \quad l = 1$  | $y = x - \pi, \quad l = 4$  |
| 21.     | $y = \begin{cases} 2x + \pi, & -\pi < x < 0, \\ -1, & 0 \leq x < \pi. \end{cases}$  | $y = \begin{cases} 9, & 0 < x < 4, \\ 9 - x, & 4 \leq x < 8. \end{cases}$      | $y = \begin{cases} 1, & 0 < x < 4, \\ x - 3, & 4 \leq x < 9. \end{cases}$       |
| 22.     | $y =  \pi + x $   | $y = 2x - 9, \quad l = 5$  | $y = \begin{cases} 0, & 0 < x < 7, \\ 4x + 1, & 7 \leq x < 8. \end{cases}$      |
| 23.     | $y = \left  \frac{\pi - x}{3} \right $  | $y = x - 1, \quad l = 2$   | $y = \begin{cases} 4 - x, & 0 \leq x < 1, \\ -1, & 1 \leq x < \pi. \end{cases}$ |
| 24.     | $y =  2(\pi - x) $  | $y = 3 - x, \quad l = 2$   | $y = \begin{cases} 4, & 0 < x < 5, \\ 4x + 7, & 5 \leq x < 6. \end{cases}$      |
| 25.     | $y = \begin{cases} 4 - x, & -\pi \leq x < 0, \\ -1, & 0 \leq x < \pi. \end{cases}$  | $y = 2\pi x - 3\pi, \quad l = 2$   | $y = 6 - x, \quad l = 4$  |
| 26.     | $y =  x - 1 $   | $y = x - \pi, \quad l = 4$   | $y = \begin{cases} \pi, & 0 < x < 2, \\ x - e, & 2 \leq x < 3. \end{cases}$     |
| 27.     | $y = \left  \frac{3\pi + x}{5} \right $   | $y = \frac{2x - 3}{4}, \quad l = 4$  | $y = \begin{cases} 2, & 0 < x < 5, \\ x - 5, & 5 \leq x < 9. \end{cases}$       |
| 28.     | $y =  2\pi - x $  | $y = \begin{cases} 4, & 0 \leq x < 2, \\ x - 1, & 2 \leq x < \pi. \end{cases}$ | $y = 2x, \quad l = 1$   |
| 29.     | $y =  0,3(\pi + x) $  | $y = \frac{x}{2}, \quad l = 6$   | $y = \begin{cases} -6, & 0 < x < 3, \\ 6 - x, & 3 \leq x < 7. \end{cases}$      |
| 30.     | $y =  0,2(3\pi - x) $   | $y = \begin{cases} 2, & 0 < x < 5, \\ 3x - 7, & 5 \leq x < 6. \end{cases}$     | $y = \begin{cases} 2, & 0 < x < 10, \\ -x, & 10 \leq x < 12. \end{cases}$       |