

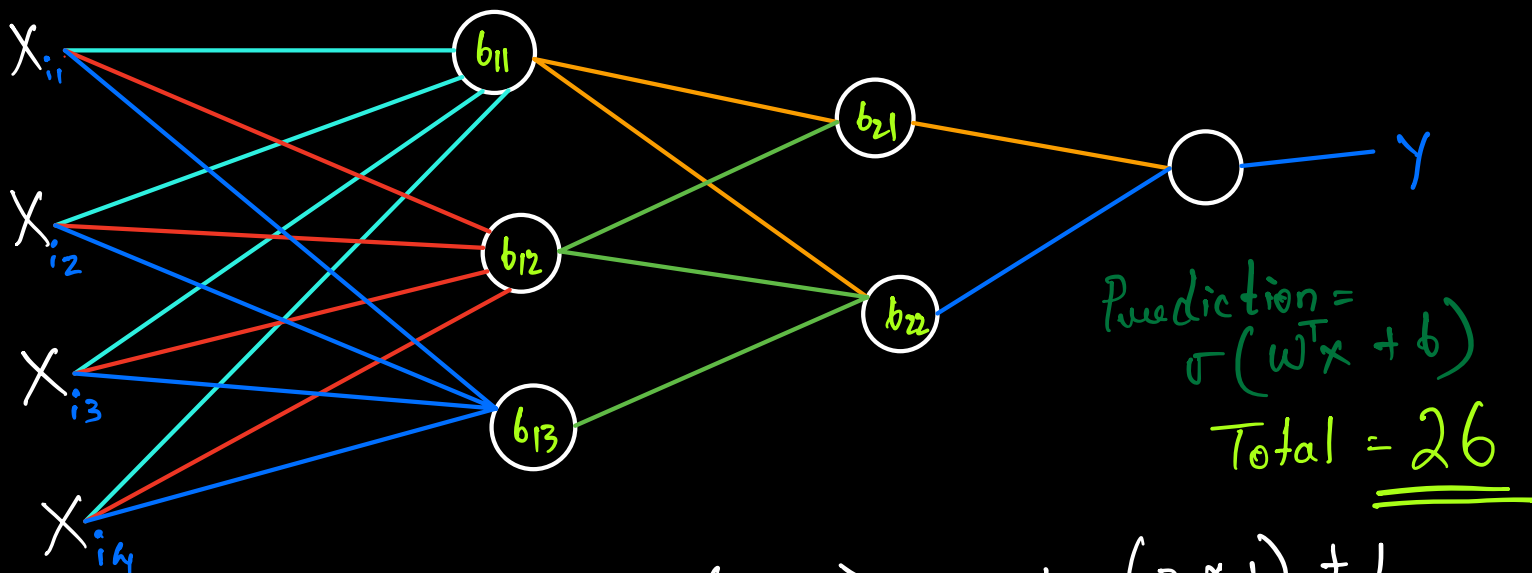
Today's Agenda

- 1) Recap of OOPs Project
- 2) MLP \rightarrow Internal Maths (Linear Algebra)
 \rightarrow Practical (MNIST) \rightarrow Classification

Multi Layer Perceptron

Non - Linear

Parameters = Weights + Bias



$$\begin{aligned} &= (4 \times 3) + 3 + (3 \times 2) + 2 + (2 \times 1) + 1 \\ &= 15 + 8 + 3 \\ &= 26 \end{aligned}$$

Layer 1

$$\begin{bmatrix} w'_{11} & w'_{12} & w'_{13} \\ w'_{21} & w'_{22} & w'_{23} \\ w'_{31} & w'_{32} & w'_{33} \\ w'_{41} & w'_{42} & w'_{43} \end{bmatrix}$$

$$\begin{bmatrix} x_{i1} \\ x_{i2} \\ x_{i3} \\ x_{i4} \end{bmatrix}$$

+

$$\begin{bmatrix} b_{11} \\ b_{12} \\ b_{13} \end{bmatrix}$$

$$4 \times 3 \xrightarrow{T} 3 \times 4$$

$$4 \times 1$$

$$3 \times 1$$

$$= (m \times n) (n \times k)$$

$$= 3 \times 1$$

$$+ 3 \times 1$$

$$= (m \times k)$$

$$= 3 \times 1$$

$$= \begin{bmatrix} w'_{11} \cdot x_{i1} + w'_{21} \cdot x_{i2} + w'_{31} \cdot x_{i3} + w'_{41} \cdot x_{i4} \\ w'_{12} \cdot x_{i1} + \\ w'_{13} \cdot x_{i1} \end{bmatrix}$$

$$= \begin{bmatrix} \\ \\ \end{bmatrix} + \begin{bmatrix} b_{11} \\ b_{12} \\ b_{13} \end{bmatrix}$$

\Downarrow
 $a^{[1]}$

$$= \begin{bmatrix} w_{11} \cdot x_{i1} + w_{21} \cdot x_{i2} + w_{31} \cdot x_{i3} + w_{41} \cdot x_{i4} + b_{11} \\ + b_{22} \\ + b_{33} \end{bmatrix}$$

$$= \sigma \left(\begin{bmatrix} 0_{11} \\ 0_{12} \\ 0_{13} \end{bmatrix} \right)$$

Layer 2

$$= \begin{bmatrix} w_{11}^2 & w_{12}^2 \\ w_{21}^2 & w_{22}^2 \\ w_{31}^2 & w_{32}^2 \end{bmatrix} \cdot \begin{bmatrix} 0_{11} \\ 0_{12} \\ 0_{13} \end{bmatrix} + \begin{bmatrix} b_{21} \\ b_{22} \end{bmatrix}$$

$3 \times 2 \rightarrow 2 \times 3 \quad 3 \times 1 \quad 2 \times 1$

$$= \begin{bmatrix} w_{11}^2 \cdot 0_{11} + w_{21}^2 \cdot 0_{12} + w_{31}^2 \cdot 0_{13} + b_{21} \end{bmatrix}$$

$$= \sigma \left(\begin{bmatrix} 0_{21} \\ 0_{22} \end{bmatrix} \right) = a^{[2]}$$

Layer 3

$$\begin{bmatrix} w_{11} \\ w_{21} \end{bmatrix}^T \begin{bmatrix} 0_{21} \\ 0_{22} \end{bmatrix} + b_{31}$$

$$= \begin{bmatrix} w_{11} 0_{21} + w_{21} 0_{22} + b_{31} \end{bmatrix}$$

$$= \sigma \left(\begin{bmatrix} 0_{31} \end{bmatrix} \right) \Downarrow a^{[3]}$$

$$a^{[1]} = \sigma \left(a^{[0]} \cdot w^{[1]} + b^{[1]} \right)$$

$$a^{[2]} = \sigma \left(a^{[1]} \cdot w^{[2]} + b^{[2]} \right)$$

$$a^{[3]} = \sigma \left(a^{[2]} \cdot w^{[3]} + b^{[3]} \right)$$

$$= \sigma \left(\sigma \left(\left(\sigma \left(a^{[0]} \cdot w^{[1]} + b^{[1]} \right) \right) \cdot w^{[2]} + b^{[2]} \right) \cdot w^{[3]} + b^{[3]} \right)$$

$$= a^{[3]}$$

Forward Propagation

$$1 \text{ pass} = \text{F.P} + \text{B.P}$$

1 F.P

Input \rightarrow B.B \rightarrow Output

<u>Layer</u>	<u>Understanding</u>
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- 1) Dense \rightarrow Linear, Hidden, Fully Connected
- 2) Flatten layer
 \rightarrow Reshape to 1D

Input \rightarrow image \rightarrow $\overset{2D}{28 \times 28}$ \rightarrow 784
 $\overset{1D}{(784, 1)} \leftarrow$

<u>Network</u>	
<u>Input</u>	<u>hidden layer</u>
0	0
1	1
2	2
3	3
4	...
...	...
784	128

Node Selection Number

Hyperparameter

Thumb Rule :- 2^n

Software + Hardware (GPU)

2^n

SIMD

GPU Memory allocation
optimal

Nodes, Batches, kernels

2^n

128

64

32

91

256

127



130

128

