Example — Observer Design

- Given a system characterized by $A = \begin{bmatrix} 1 & 3 \\ 3 & 1 \end{bmatrix}$, $C = \begin{bmatrix} 0.5 & 1 \end{bmatrix}$
- Find linear state-observer gain $L = \begin{bmatrix} l_1 & l_2 \end{bmatrix}^{\top}$ such that the poles of the estimation error are -5 and -3
- Characteristic polynomial:

$$\lambda^2 + (-2 + I_2 + 0.5I_1)\lambda + (-8 + 0.5I_2 + 2.5I_1) = 0$$

- Solution: $L = \begin{bmatrix} 8 \\ 6 \end{bmatrix}$
- MATLAB command: L = place(A',C',eig_desired)