CS 457/557: Assignment 3

Due: November 28, 2022, by 11:00 PM (Central)

Overview

In this assignment, you will write a program that can be used to train and evaluate a neural network for multi-class classification. Your program will allow the user to specify the structure of a multi-layer feed-forward neural network and then will train that network using backpropagation in conjunction with mini-batch gradient descent.

Note: Depending on how you structured your code for Assignment 01, you may be able to reuse some parts of it here, and it is acceptable to do so. However, you might also find it easier to rewrite things from scratch with improvements based on lessons learned from Assignment 01.

Academic Integrity Policy

All work for this assignment must be your own work and it must be completed **independently**. Using code from other students and/or online sources (e.g., Github) constitutes academic misconduct, as does sharing your code with others either directly or indirectly (e.g., by posting it online). Academic misconduct is a violation of the UWL Student Honor Code and is unacceptable. Plagiarism or cheating in any form may result in a zero on this assignment, a **negative score** on this assignment, failure of the course, and/or additional sanctions. Refer to the course syllabus for additional details on academic misconduct.

You should be able to complete the assignment using only the course notes and textbook along with relevant programming language documentation (e.g., the Java API specification). Use of additional resources is discouraged but not prohibited, provided that this is limited to high-level queries and not assignment-specific concepts. As a concrete example, searching for "how to use a HashMap in Java" is fine, but searching for "neural network in Java" is not.

Deliverables

You should submit a single compressed archive (either .zip or .tgz format) containing the following to Canvas:

- 1. The complete source code for your program. I prefer that you use Java in your implementation, but if you would like to use another language, check with me before you get started. Additional source code requirements are listed below:
 - Your name must be included in a header comment at the top of each source code file.
 - Your code should follow proper software engineering principles for the chosen language, including meaningful comments and appropriate code style.
 - Your code must not make use of any non-standard or third-party libraries.
- 2. A README text file that provides instructions for how your program can be compiled (as needed) and run from the command line. If your program is incomplete, then your README should document what parts of the program are and are not working.
- 3. (NEW) An experimentation.txt text file that describes the results of your experimentation (see page 11 for details) and includes the best performance that you were able to achieve on several of the sample data sets along with the command-line arguments that you used to achieve this.

Program Requirements

The general outline of the program is given below:

Algorithm 1 Program Flow

Process command-line arguments

Load data from the specified file

Randomly split data into training and validation sets (use 80% of data for training)

Learn min-max normalization (feature scaling) parameters from the training set

Use the "learned" scaling parameters to rescale attribute values for all data

Set up neural network architecture based on command-line arguments

Train the neural network on the training data

Evaluate the accuracy of the neural network on the validation set

The program should be runnable from the command line, and it should be able to process command-line arguments to update various program parameters as needed. The command-line arguments are listed below:

- -f <FILENAME>: Reads data from the file named <FILENAME> (specified as a String); see the File Format section for more details.
- -h <NH> <S1> <S2> ...
 - Specifies the number of hidden layers <NH> followed by <NH> additional integers corresponding to the sizes of these hidden layers. You can assume that <NH> is a non-negative integer no greater than 10. The following integer(s) <S1>, <S2>, etc. represent the sizes of hidden layer 1, hidden layer 2, and so on. There will be <NH> size values, and you can assume that each of these values will be a positive integer no greater than 500. For example, -h 2 10 5 specifies a neural network with two hidden layers, the first containing 10 neurons and the second containing 5. Note that <NH> may be 0, in which case there are no hidden layers and no additional integers following. (Using zero hidden layers is the default.)
- -a <DOUBLE>: Specifies the learning rate α in mini-batch gradient descent; default is 0.01.
- -e <INTEGER>: Specifies the epoch limit in mini-batch gradient descent; default is 1000.
- -m <INTEGER>: Specifies the batch size in mini-batch gradient descent; default is 1 for stochastic gradient descent (using -m 0 should be interpreted as full batch gradient descent).
- -1 <DOUBLE>: Specifies the regularization hyperparameter λ ; default is 0.0 (no regularization).
- -r: If specified, this flag (which has no arguments) enables randomization of data for the train/validation split **and** for batch construction at the start of each epoch; if this flag is not specified, then data should **not be randomized** (which is the default behavior; this is to make testing and debugging easier).
- -w <DOUBLE>: Specifies the value ϵ for weight initialization; default is 0.1.
- -v <INTEGER>: Specifies a verbosity level, indicating how much output the program should produce; default is 1 (See the **Output** section for details)

The -f <FILENAME> option is required; all others are optional. Filenames may include path information, so do not assume that the files are located in the same directory as your source code. You can assume that your program will only be run with valid arguments (so you do not need to include error checking, though it may be helpful for your own testing). Your program must be able to handle command-line arguments in **any** order (e.g., do **not** assume that the first argument will be -f). Several example runs of the program are shown at the end of this document.

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File Format

The data for your program will be specified in files with lines corresponding to individual examples or data points. Each line will contain the example's attribute (feature) value(s) (all of which are quantitative, or continuous-valued) and an output (target) vector with length corresponding to the number of classes. The output vector will have exactly one 1, and all remaining entries will be 0. Lines that are empty or lines that start with a # character should be skipped. Example data with two features and three classes is shown below:

```
# This is a comment line.
(0.665 0.790) (0 1 0)
(0.272 0.412) (1 0 0)
(0.936 0.872) (0 0 1)
(0.896 0.081) (1 0 0)
(0.418 0.741) (0 1 0)
```

Several example input files are provided in the a03-data.zip archive on Canvas. In particular:

- The files prefixed with iris-contain a slightly modified version of the Iris dataset.
- The mnist.dat file is a slightly modified version of the MNIST database which contains handwritten images of the digits 0 through 9.
- The image-05.dat, image-10.dat, image-15.dat, and image-20.dat files contain image data of various letters and digits (specifically, the letters 'C', 'A', 'M', and 'F', and the digits '0' through '9') at several different resolutions (with 05 being the lowest and 20 being the highest).

Training and Validation Sets

After reading the data, your program will need to construct a training set and a validation set from the data. You should split the data into these two sets, using the **first** 80% for training and the rest for validation. If the -r command-line flag is specified, then the ordering of records in the full data set should be randomized prior to the split.

Feature Scaling

After constructing the training and validation sets, your program will need to scale the feature values so that they are in the range [-1,1] (or close to it) using min-max normalization. Let L_j and U_j denote the minimum and maximum values observed for feature j in the **training** data. Then min-max normalization scales the feature values \mathbf{x}_i for example i to \mathbf{x}'_i by using

$$x'_{ij} = -1 + 2\left(\frac{x_{ij} - L_j}{U_j - L_j}\right)$$

for each feature j. If example i is in the training set, then it is guaranteed that $x'_{ij} \in [-1, 1]$ for each feature j. We cannot make this guarantee if example i is in the validation set, but it is usually close to this interval. Note that if $U_j = L_j$, then you can simply scale each feature to -1 to avoid dividing by zero.

(The reason we "learn" the feature scaling parameters from the training data is to avoid data leakage from the validation set in the form of minimum and maximum attribute values.)

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Network Architecture

Next, your program should build a fully-connected feed-forward neural network. The number of input neurons in the network should match the number of features in the training data (plus the bias neuron), and the number of output neurons in the network should match the number of classes (which is the length of the output vectors).

The number of hidden layers and the size of each hidden layer should match the values provided through the command-line arguments (if the -h flag was not specified or was specified with -h 0, then no hidden layers should be included).

How you handle the bias neuron (i.e., neuron 0 from the lectures, with a constant output of $a_0 = 1$) is up to you. You can implement it as a single neuron in the input layer with connections to every other neuron in the subsequent layers, or you may wish to have a separate bias neuron in each layer that connects to just the neurons in the subsequent layer (which may make it easier to manage the weights, depending on how you store them). You could also use another configuration, as well.

Each processing neuron (i.e., those that are neither input neurons nor bias neurons) should use the standard logistic activation function given by $g(t) = \frac{1}{1+e^{-t}}$ for all $t \in \mathbb{R}$. Recall that the derivative of the standard logistic function is given by g'(t) = g(t)(1-g(t)) for all $t \in \mathbb{R}$.

Optimization Components

All of the weights in the network should be initialized to a random value in the range $(-\epsilon, \epsilon)$, where ϵ is a small positive constant. The default value of ϵ should be 0.01, but this can be overridden by using the -w command-line argument.

The cost function is the average loss over the training set plus a regularization term:

$$J(\mathbf{w}) = \frac{1}{n} \sum_{i=1}^{n} \ell\left(\mathbf{y}_{i}, h_{\mathbf{w}}(\mathbf{x}_{i})\right) + \lambda \sum_{(i,j) \in A} w_{ij}^{2}.$$

To keep things straightforward, you should use squared error as the loss function. In a multi-class classification context with K distinct classes, this loss function is

$$\ell(\mathbf{y}, h_{\mathbf{w}}(\mathbf{x})) = \sum_{k=1}^{K} (y_k - a_k)^2,$$

where a_k is the output value of the output neuron k that corresponds to class k given training example \mathbf{x} . With the above cost function and loss function, the partial derivatives of $J(\mathbf{w})$ with respect to any weight w_{ij} can be estimated using a mini-batch of training data B as

$$\frac{\partial}{\partial w_{ij}} J(\mathbf{w}) \approx \frac{1}{|B|} \left(\sum_{e \in B} \Delta_j^{(e)} a_i^{(e)} \right) + 2\lambda w_{ij}$$

where $\Delta_j^{(e)}$ and $a_i^{(e)}$ are the values for Δ_j and a_i computed by passing the values $(\mathbf{x}_e, \mathbf{y}_e)$ corresponding to training example index $e \in B$ into the backpropagation algorithm (see Lectures 07-3 and 07-4 for details).

Fitting the Training Data

Pseudocode for the mini-batch gradient descent algorithm, tailored for training a neural network via backpropagation, is shown in Algorithm 2. The stopping conditions that you should use are:

- The number of epochs reaches the specified epoch limit (which defaults to 1000).
- The absolute error at each output neuron k is at most 0.01 across an entire epoch. For a training example (\mathbf{x}, \mathbf{y}) , the error at output neuron k is given by $y_k a_k$ and the absolute error is $|y_k a_k|$. Put another way, the training process should keep going if **any** training example produces an absolute error above 0.01 at **any** output neuron; i.e., we're making a big enough mistake on some training example.

You can adjust the epoch limit with a command-line argument. You may also wish to adjust hyperparameters like the mini-batch size m, the learning rate α , the regularization penalty λ , and/or the weight initialization value ϵ to alter how quickly or slowly the network trains.

During training, you will periodically need to compute the current cost as well as average loss and accuracy on the training set in order to display the progress (see next page for details on accuracy). This should be done only when needed, however, as otherwise it will slow down the training process. In general, your implementation should be reasonably efficient and avoid unnecessary work, though it may be helpful to deal with efficiency considerations only after you have a working implementation. Note also that weight updates in neural networks generally require more work than in multiple linear regression, so your code will probably run slower than it did for Assignment 01.

```
Algorithm 2 Mini-Batch Gradient Descent for Training a Neural Network
```

```
procedure NeuralNetworkTrain( \{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^n; \mathcal{N} = (V, A); m, \alpha, \lambda, \epsilon)
    for each edge (i, j) \in A do
         w_{ij}^{(0)} \leftarrow \text{RAND}(-\epsilon, \epsilon)
                                                                                       ▶ Random initialization of weights
    t \leftarrow 0
                                                       \triangleright t is the iteration counter for number of weight updates
    e \leftarrow 0
                   \triangleright e counts number of epochs; an epoch is one full pass through the training data
    while stopping conditions not met do
         Divide \{1, 2, \ldots, n\} into mini-batches of m data points (see note below for details)
          for each mini-batch B do
              for each example index e \in B do
                   Run Backpropagate((\mathbf{x}_e, \mathbf{y}_e), \mathcal{N}, \mathbf{w}^{(t)}) to obtain \Delta_i^{(e)}, a_i^{(e)} values
              for each edge (i,j) \in A do
                  w_{ij}^{(t+1)} \leftarrow w_{ij}^{(t)} - \alpha \left( \frac{1}{|B|} \sum_{c \in B} \Delta_j^{(e)} a_i^{(e)} \right) - 2\alpha \lambda w_{ij}^{(t)}
              t \leftarrow t + 1
          e \leftarrow e + 1
                                                                  ▶ an epoch ends once we process all mini-batches
    return \mathbf{w}^{(t)}
```

For mini-batch construction, if m does not evenly divide n, then the last mini-batch should have size $n \mod m$. Additionally, if the $-\mathbf{r}$ command-line flag is given, these mini-batches should be randomized; otherwise, the first m data points should be assigned to batch 1, the next m data points to batch 2, and so on (this is to make debugging easier).

Evaluation using the Validation Data

After the network is trained, your program should compute its accuracy on the validation set. To do this, you will need to:

- 1. Run each example in the validation set through the network using forward propagation to compute the output values at all output neurons.
- 2. Predict the class for the example as the class corresponding to the output neuron with the largest output value.
- 3. Check correctness by comparing the predicted class to the actual class for this example (where the actual class is the class with the sole 1 in the example's output vector).
- 4. Compute accuracy as the proportion of correct predictions on the validation set.

Output

The level of output produced by the program is controlled by the $\neg v$ flag (for verbosity). The levels range from 1 to 4, with 4 containing the most output; the output produced is additive, meaning that the output for level i should also be produced for any level j with $j \ge i$. The desired output for each level is discussed in more detail below.

The output produced by your program does not have to match what is shown **exactly**, but it should be well-formatted and reasonably easy to read. Additional requirements for displaying numeric quantities include:

- Final training and validation accuracy should be displayed with 6 decimal places
- Time per iteration should be displayed with 4 decimal places
- In gradient descent, costs and losses should be displayed with 6 decimal places and accuracy should be displayed with 4 places

Additionally, don't use tabs (\t) in your output! (See here for a discussion of why.)

Output Level 1

Level 1 prints a brief summary of the program flow followed by the results.

```
shell$ java Driver -f data/iris-shuf.dat

* Reading data/iris-shuf.dat

* Doing train/validation split

* Scaling features

* Building network

* Training network (using 120 examples)

* Evaluating accuracy
    TrainAcc: 0.941667
    ValidAcc: 0.933333
```

Output Level 2

Level 2 includes a few more details during each part of the program flow, such as the minimum and maximum values for each feature within the training set, the network layer sizes, and the gradient descent parameters, training time, and stopping condition:

```
shell$ java Driver -f data/iris-shuf.dat -v 2
* Reading data/iris-shuf.dat
* Doing train/validation split
* Scaling features
```

```
* min/max values on training set:
   Feature 1: 4.400, 7.900
   Feature 2: 2.000, 4.200
   Feature 3: 1.000, 6.900
   Feature 4: 0.100, 2.500
* Building network
 * Layer sizes (excluding bias neuron(s)):
   Layer 1 (input) :
   Layer 2 (output):
* Training network (using 120 examples)
 * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=1000, learningRate=0.0100, lambda=0.0000)
  * Done with fitting!
    Training took 180ms, 1000 epochs, 120000 iterations (0.0015ms / iteration)
    GD Stop condition: Epoch Limit
* Evaluating accuracy
 TrainAcc: 0.941667
  ValidAcc: 0.933333
```

Output Level 3

Level 3 prints additional details about the model's performance on the training data (cost, loss, and accuracy) before, during, and after the training process:

```
shell$ java Driver -f data/iris-shuf.dat -v 3 -h 1 2
* Reading data/iris-shuf.dat
* Doing train/validation split
* Scaling features
 * min/max values on training set:
   Feature 1: 4.400, 7.900
   Feature 2: 2.000, 4.200
   Feature 3: 1.000, 6.900
   Feature 4: 0.100, 2.500
* Building network
 * Layer sizes (excluding bias neuron(s)):
   Layer 1 (input) :
                        4
   Layer 2 (hidden):
   Layer 3 (output):
                        3
* Training network (using 120 examples)
 * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=1000, learningRate=0.0100, lambda=0.0000)
    Initial model with random weights: Cost = 0.757058; Loss = 0.757058; Acc = 0.3083
   After
            100 epochs ( 12000 iter.): Cost = 0.365432; Loss = 0.365432; Acc = 0.7000
            200 epochs ( 24000 iter.): Cost = 0.289164; Loss = 0.289164; Acc = 0.8750
   After
   After
            300 epochs ( 36000 iter.): Cost = 0.198624; Loss = 0.198624; Acc = 0.9583
   After
            400 epochs ( 48000 iter.): Cost = 0.125109; Loss = 0.125109; Acc = 0.9667
   After
            500 epochs ( 60000 iter.): Cost = 0.087541; Loss = 0.087541; Acc = 0.9667
            600 epochs ( 72000 iter.): Cost = 0.067797; Loss = 0.067797; Acc = 0.9750
   After
            700 epochs ( 84000 iter.): Cost = 0.056384; Loss = 0.056384; Acc = 0.9750
   After
   After
            800 epochs ( 96000 iter.): Cost = 0.049125; Loss = 0.049125; Acc = 0.9750
            900 epochs (108000 iter.): Cost = 0.044119; Loss = 0.044119; Acc = 0.9750
   After
   After
            1000 epochs (120000 iter.): Cost = 0.040448; Loss = 0.040448; Acc = 0.9833
  * Done with fitting!
   Training took 262ms, 1000 epochs, 120000 iterations (0.0022ms / iteration)
```

```
GD Stop condition: Epoch Limit
* Evaluating accuracy
TrainAcc: 0.983333
ValidAcc: 0.966667
```

Note: Unlike Assignment 01, where model performance was printed after every 1000 epochs, here the printing should occur after every epochLimit/10 epochs. So with a default epochLimit of 1000, this means printing should occur after every 100 epochs; however, with an epochLimit of 10000, printing should occur after every 1000 epochs, while an epochLimit of 100 should result in printing after every 10 epochs. For epochLimit values less than 10, printing should be done after every epoch.

The below example uses an epoch limit of 5000, two hidden layers with sizes 3 and 2, and a regularization parameter of $\lambda = 0.0001$ (which is why the cost and the loss are not always the same):

```
shell$ java Driver -f data/iris-shuf.dat -v 3 -e 5000 -h 2 3 2 -l 0.0001
* Reading data/iris-shuf.dat
* Doing train/validation split
* Scaling features
 * min/max values on training set:
   Feature 1: 4.400, 7.900
   Feature 2: 2.000, 4.200
   Feature 3: 1.000, 6.900
   Feature 4: 0.100, 2.500
* Building network
  * Layer sizes (excluding bias neuron(s)):
   Layer 1 (input) :
   Layer 2 (hidden):
   Layer 3 (hidden):
                         2
   Layer 4 (output):
                        3
* Training network (using 120 examples)
  * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=5000, learningRate=0.0100, lambda=0.0001)
    Initial model with random weights: Cost = 0.735975; Loss = 0.735964; Acc = 0.3250
   After
            500 epochs ( 60000 iter.): Cost = 0.664997; Loss = 0.664892; Acc = 0.3667
   After
           1000 epochs (120000 iter.): Cost = 0.664995; Loss = 0.664888; Acc = 0.3667
           1500 epochs (180000 iter.): Cost = 0.664991; Loss = 0.664882; Acc = 0.3667
   After
           2000 epochs (240000 iter.): Cost = 0.664846; Loss = 0.664722; Acc = 0.3667
   After
           2500 epochs (300000 iter.): Cost = 0.304122; Loss = 0.293052; Acc = 0.8750
   After
           3000 epochs (360000 iter.): Cost = 0.138447; Loss = 0.109819; Acc = 0.9667
   After
   After
           3500 epochs (420000 iter.): Cost = 0.086505; Loss = 0.044383; Acc = 0.9833
   After
           4000 epochs (480000 iter.): Cost = 0.081379; Loss = 0.035461; Acc = 0.9917
   After
            4500 epochs (540000 iter.): Cost = 0.079597; Loss = 0.032547; Acc = 0.9917
            5000 epochs (600000 iter.): Cost = 0.078498; Loss = 0.031244; Acc = 0.9917
   After
  * Done with fitting!
    Training took 1472ms, 5000 epochs, 600000 iterations (0.0025ms / iteration)
    GD Stop condition: Epoch Limit
* Evaluating accuracy
 TrainAcc: 0.991667
  ValidAcc: 0.966667
```

Output Level 4

Level 4 provides additional details about the forward and backward propagation passes used during training. Specifically, whenever a training example is run through the BACKPROPUPDATE procedure, the in_j and a_j values computed during forward propagation and the Δ_j values computed during backward propagation should be printed for the neurons in each layer.

This level of output is **extremely verbose**, and so is intended primarily for debugging purposes when training on small data sets with a very small epoch limit. The example below illustrates this on a small data set with a learning rate of $\alpha = 0.5$ and a weight initialization value of $\epsilon = 0$ (which means that all the weights start at 0; this is good for debugging but bad for training!):

```
shell$ java Driver -f data/iris-small.dat -v 4 -h 1 2 -e 1 -w 0 -a 0.5
* Reading data/iris-small.dat
* Doing train/validation split
* Scaling features
 * min/max values on training set:
    Feature 1: 4.800, 7.600
    Feature 2: 2.300, 3.400
    Feature 3: 1.600, 6.600
    Feature 4: 0.200, 2.500
* Building network
  * Layer sizes (excluding bias neuron(s)):
    Layer 1 (input) :
   Layer 2 (hidden):
                         2
    Layer 3 (output):
                         3
* Training network (using 8 examples)
  * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=1, learningRate=0.5000, lambda=0.0000)
    Initial model with random weights: Cost = 0.750000; Loss = 0.750000; Acc = 0.2500
    * Forward Propagation on example 1
     Layer 1 (input) :
                                               0.273 0.440 0.565
                           a_j: 1.000
                                        0.214
                          in_j: 0.000
     Layer 2 (hidden):
                                        0.000
                           a_j: 0.500
                                        0.500
     Layer 3 (output):
                           in_j: 0.000
                                        0.000
                                               0.000
                           a_j: 0.500
                                        0.500
                                               0.500
             example's actual y: 0.000
                                        0.000
                                               1.000
    * Backward Propagation on example 1
     Layer 3 (output): Delta_j: 0.250
                                        0.250 - 0.250
     Layer 2 (hidden): Delta_j: 0.000
                                        0.000
    * Forward Propagation on example 2
      (OUTPUT OMITTED FOR BREVITY)
    * Forward Propagation on example 8
     Layer 1 (input) :
                           a_j: 1.000 0.071 -1.000 0.120 -0.043
     Layer 2 (hidden):
                          in_j: -0.005 -0.005
                           a_j: 0.499 0.499
     Layer 3 (output):
                           in_j: -0.507 -0.338 -0.171
                           a_j: 0.376
                                        0.416
                                               0.457
             example's actual y: 0.000
                                        1.000
                                               0.000
    * Backward Propagation on example 8
     Layer 3 (output): Delta_j: 0.176 -0.284
     Layer 2 (hidden): Delta_j: -0.003 -0.003
```

```
After 1 epochs ( 8 iter.): Cost = 0.675760; Loss = 0.675760; Acc = 0.3750

* Done with fitting!
Training took 36ms, 1 epochs, 8 iterations (4.5000ms / iteration)
GD Stop condition: Epoch Limit

* Evaluating accuracy
TrainAcc: 0.375000
ValidAcc: 0.500000
```

Experimentation

Once you have finished your implementation (and debugged it!), you should experiment with different network architectures and hyperparameter values to see what yields good performance on the image-NN.dat and mnist.dat sample data sets. (Note: These are large files with a high number of features, so expect the training process to be slow!) Try to find options that lead to high accuracy on the validation data. Make notes of any observations you might have regarding the influence of various hyperparameters on performance. Provide, in a text file, a list of the best training and validation set accuracy values that you were able to achieve on these data sets, along with the command-line flags that you used to generate those results.

Extra Credit Options (Added on 2022-11-15)

Additional Activation Functions

For a small amount of extra credit (about 3–5% of the overall assignment), you can implement support for additional activation functions via another command-line argument:

- -g <NAME>: Specifies the name of the activation function to be used at neurons in the **hidden** layers, where <NAME> is a String that matches one of the following (case-insensitive):
 - logistic: The standard logistic function, with

$$g(t) = \frac{1}{1 + e^{-t}}$$
 $g'(t) = g(t)(1 - g(t))$

- relu: The rectified linear unit function, with

$$g(t) = \max\{0, t\}$$
 $g'(t) = \begin{cases} 1 & \text{if } t > 0 \\ 0 & \text{if } t < 0 \end{cases}$

(Technically, g' is undefined at 0 for ReLU, but we can use g'(0) = 0 in code.)

- softplus: The softplus function, with

$$g(t) = \ln(1 + e^t)$$
 $g'(t) = \sigma(t) = \frac{1}{1 + e^{-t}}$

- tanh: The hyperbolic tangent function, with

$$g(t) = \frac{e^t - e^{-t}}{e^t + e^{-t}}$$

$$g'(t) = 1 - g(t)^2$$

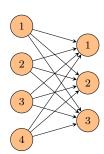
Note that neurons in the output layer should always use the logistic activation function in order to ensure that outputs are in the range [0,1].

Deterministic Weight Initialization

For a small amount of extra credit (about 3–5% of the overall assignment), you can implement support for **deterministic** weight initialization, which should be activated by passing a negative value to the -w command-line argument. In deterministic weight initialization, the edge weights should be initialized as follows:

- The weights on the edges leaving the bias neuron(s) should be initialized to 0.1.
- For the edges between non-bias neurons in layers l and l + 1:
 - Temporarily relabel the neurons in layer l from 1 to m
 - Temporarily relabel the neurons in layer l+1 from 1 to n
 - Initialize the weight on the edge from neuron i in layer l to neuron j in layer l+1 as $1/(i \cdot 2^{j-1})$. (I.e., the first edge out of neuron i has weight 1/i, the second edge out of neuron i has weight (1/i)/2, the third edge out of neuron i has weight (1/i)/2/2, etc.)
 - Restore neuron labels as needed

(Note: This initialization should be used even if layer l is the input layer; i.e., l = 1.)



With a deterministic weight initialization, it should be possible for your program's behavior to exactly match that of a reference implementation (e.g., mine). This is useful for double-checking the overall training process as well as forward and backward propagation calculations with verbosity level 4 on small examples.

Some caveats:

- I make no claims or guarantees regarding this particular weight initialization scheme; in my limited testing, it seems to prevent any two edges from always having the same weight, thus allowing the training process to take full advantage of all the weight parameters available for tuning. However, I don't (yet) have a formal proof that this will always work as intended. For production purposes, using random initial weights is recommended.
- I am fairly confident that the output below from my reference implementation is correct, but if you spot any differences between my output and yours, let me know and I can take a closer look (I've been known to make the occasional mistake!).

```
shell$ java Driver -f data/iris-shuf.dat -h 2 3 2 -w -1 -v 3 -a 0.5 -e 10
* Reading data/iris-shuf.dat
* Doing train/validation split
* Scaling features
 * min/max values on training set:
    Feature 1: 4.400, 7.900
    Feature 2: 2.000, 4.200
    Feature 3: 1.000, 6.900
    Feature 4: 0.100, 2.500
* Building network
  * Layer sizes (excluding bias neuron(s)):
   Layer 1 (input):
                         4
   Layer 2 (hidden):
                         3
   Layer 3 (hidden):
                         2
   Layer 4 (output):
```

```
* Training network (using 120 examples)
  * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=10, learningRate=0.5000, lambda=0.0000)
    Initial model with determ. weights: Cost = 1.028471; Loss = 1.028471; Acc = 0.3083
              1 epochs ( 120 iter.): Cost = 0.697988; Loss = 0.697988; Acc = 0.3667
    After
   After
              2 epochs (
                           240 iter.): Cost = 0.690464; Loss = 0.690464; Acc = 0.3667
   After
              3 epochs (
                           360 iter.): Cost = 0.670832; Loss = 0.670832; Acc = 0.3667
              4 epochs ( 480 iter.): Cost = 0.577479; Loss = 0.577479; Acc = 0.6750
   After
                           600 iter.): Cost = 0.464022; Loss = 0.464022; Acc = 0.6750
   After
              5 epochs (
              6 epochs ( 720 iter.): Cost = 0.414322; Loss = 0.414322; Acc = 0.6750
   After
   After
              7 epochs ( 840 iter.): Cost = 0.383633; Loss = 0.383633; Acc = 0.6750
   After
              8 epochs ( 960 iter.): Cost = 0.356763; Loss = 0.356763; Acc = 0.6750
              9 epochs ( 1080 iter.): Cost = 0.334091; Loss = 0.334091; Acc = 0.6750
   After
   After
             10 epochs ( 1200 iter.): Cost = 0.318682; Loss = 0.318682; Acc = 0.6750
  * Done with fitting!
    Training took 13ms, 10 epochs, 1200 iterations (0.0108ms / iteration)
    GD Stop condition: Epoch Limit
* Evaluating accuracy
 TrainAcc: 0.675000
 ValidAcc: 0.633333
shell$ java Driver -f data/iris-small.dat -v 4 -h 1 2 -e 1 -w -1 -a 0.5
* Reading data/iris-small.dat
* Doing train/validation split
* Scaling features
 * min/max values on training set:
    Feature 1: 4.800, 7.600
   Feature 2: 2.300, 3.400
   Feature 3: 1.600, 6.600
    Feature 4: 0.200, 2.500
* Building network
 * Layer sizes (excluding bias neuron(s)):
   Layer 1 (input): 4
   Layer 2 (hidden):
   Layer 3 (output):
                        3
* Training network (using 8 examples)
 * Beginning mini-batch gradient descent
    (batchSize=1, epochLimit=1, learningRate=0.5000, lambda=0.0000)
    Initial model with determ. weights: Cost = 1.006318; Loss = 1.006318; Acc = 0.2500
    * Forward Propagation on example 1
      Layer 1 (input) :
                            a_j: 1.000 0.214 0.273 0.440 0.565
      Layer 2 (hidden):
                           in_j: 0.739 0.419
                            a_j: 0.677 0.603
      Layer 3 (output):
                           in_j: 1.078 0.589 0.345
                            a_j: 0.746 0.643 0.585
             example's actual y: 0.000 0.000 1.000
    * Backward Propagation on example 1
      Layer 3 (output): Delta_j: 0.283 0.295 -0.201
      Layer 2 (hidden): Delta_j: 0.083 0.045
    * Forward Propagation on example 2
```

a_j: 1.000 -1.000 1.000 -1.000 -1.000

in_j: -0.986 -0.443 a_j: 0.272 0.391

Layer 1 (input) :

Layer 2 (hidden):

```
Layer 3 (output):
                     in_j: 0.367 0.124 0.360
                      a_j: 0.591 0.531 0.589
        example's actual y: 1.000 0.000 0.000
* Backward Propagation on example 2
 Layer 3 (output): Delta_j: -0.198  0.264  0.285
 Layer 2 (hidden): Delta_j: 0.003 0.003
* Forward Propagation on example 3
 Layer 1 (input) :
                      a_j: 1.000 -0.571 1.000 -0.960 -1.000
 Layer 2 (hidden):
                      in_j: -0.556 -0.232
                      a_j: 0.364 0.442
 Layer 3 (output):
                      in_j: 0.598 0.001 0.217
                      a_j: 0.645 0.500 0.554
        example's actual y: 1.000 0.000 0.000
* Backward Propagation on example 3
 Layer 3 (output): Delta_j: -0.162 0.250 0.274
 Layer 2 (hidden): Delta_j: 0.004 -0.003
* Forward Propagation on example 4
                      a_j: 1.000 0.357 0.818 0.640 1.000
 Layer 1 (input) :
 Layer 2 (hidden):
                      in_j: 1.241 0.666
                      a_j: 0.776 0.661
 Layer 3 (output):
                      in_j: 1.208 -0.022 0.145
                      a_j: 0.770 0.494 0.536
        example's actual y: 0.000 0.000 1.000
* Backward Propagation on example 4
 Layer 3 (output): Delta_j: 0.273 0.247 -0.231
 Layer 2 (hidden): Delta_j: 0.050 0.029
* Forward Propagation on example 5
 Layer 1 (input) :
                      a_j: 1.000 -0.357 0.273 0.040 -0.130
 Layer 2 (hidden):
                     in_j: -0.210 -0.057
                      a_j: 0.448 0.486
 Layer 3 (output):
                      in_j: 0.579 -0.342 0.250
                      a_j: 0.641 0.415 0.562
        example's actual y: 0.000 1.000 0.000
* Backward Propagation on example 5
 Layer 3 (output): Delta_j: 0.295 -0.284 0.277
 Layer 2 (hidden): Delta_j: 0.069 0.041
* Forward Propagation on example 6
 Layer 1 (input) :
                      a_j: 1.000 1.000 0.273 1.000 0.652
 Layer 2 (hidden):
                     in_j: 1.555 0.814
                      a_j: 0.826 0.693
                      in_j: 0.733 -0.022 0.165
 Layer 3 (output):
                      a_j: 0.676 0.495 0.541
        example's actual y: 0.000 0.000 1.000
* Backward Propagation on example 6
 Layer 3 (output): Delta_j: 0.296 0.247 -0.228
 Layer 2 (hidden): Delta_j: 0.035 0.019
* Forward Propagation on example 7
 Layer 1 (input) :
                     a_j: 1.000 0.357 0.455 0.120 0.043
 Layer 2 (hidden):
                     in_j: 0.575 0.329
```

```
a_j: 0.640 0.581
      Layer 3 (output):
                           in_j: 0.264 -0.318 0.328
                           a_j: 0.566 0.421 0.581
             example's actual y: 0.000 1.000 0.000
    * Backward Propagation on example 7
      Layer 3 (output): Delta_j: 0.278 -0.282 0.283
      Layer 2 (hidden): Delta_j: 0.054 0.029
    * Forward Propagation on example 8
      Layer 1 (input) :
                           a_j: 1.000 0.071 -1.000 0.120 -0.043
      Layer 2 (hidden):
                          in_j: -0.393 -0.152
                           a_j: 0.403 0.462
      Layer 3 (output):
                          in_j: -0.133 -0.141 0.010
                           a_j: 0.467 0.465 0.503
             example's actual y: 0.000 1.000 0.000
    * Backward Propagation on example 8
      Layer 3 (output): Delta_j: 0.232 -0.266 0.251
      Layer 2 (hidden): Delta_j: 0.030 0.011
              1 epochs (
                            8 iter.): Cost = 0.736744; Loss = 0.736744; Acc = 0.3750
 * Done with fitting!
   Training took 24ms, 1 epochs, 8 iterations (3.0000ms / iteration)
   GD Stop condition: Epoch Limit
* Evaluating accuracy
 TrainAcc: 0.375000
  ValidAcc: 0.500000
```