General Physics Midterm Review

Kongsak Tipakornrojanakit

- 1. A poorly designed electric device has two bolts attached to different parts of the device that almost touch each other in its interior, as shown. When they touch, a short circuit will develop and damage the device. If the initial gap between the ends of the bolts is $5.0\,\mu m$ at $27\,^{\circ}C$, at what temperature will the bolts touch?
 - (a) Steel $_{\rm length}=0.01\,\mathrm{m}=1\times10^{-2}\mathrm{m}$
 - (b) $Brass_{length} = 0.03 \, m = 3 \times 10^{-2} m$
 - (c) $Gap_{length} = 0.05 \, \mu m = 5 \times 10^{-6} m$
 - (d) $\alpha_{\text{Steel}} = 11 \times 10^{-6} \, ^{\circ}\text{C}^{-1}$
 - (e) $\alpha_{\text{Brass}} = 19 \times 10^{-6} \, ^{\circ}\text{C}^{-1}$
 - (f) $\triangle L = \alpha L_0 \triangle T$
 - (g) $\triangle L = \text{Gap}_{\text{length}} = 5 \times 10^{-6} \text{m}$

$$\begin{split} \triangle T &= \frac{\triangle L}{\alpha L_0} \\ &= \frac{\text{Gap}_{\text{length}}}{\alpha_{\text{Steel}} \text{Steel}_{\text{length}} + \alpha_{\text{Brass}} \text{Brass}_{\text{length}}} \, ^{\circ} \text{C} \\ &= \frac{5 \times 10^{-6}}{(11 \times 10^{-6} \times 1 \times 10^{-2}) + (19 \times 10^{-6} \times 3 \times 10^{-2})} \, ^{\circ} \text{C} \\ &= \frac{5 \times 10^{-6}}{(11 \times 10^{-8}) + (57 \times 10^{-8})} \, ^{\circ} \text{C} \\ &= \frac{5 \times 10^{-6} \text{m}}{(68 \times 10^{-8})} \, ^{\circ} \text{C} \\ &= \frac{5}{(68 \times 10^{-2})} \, ^{\circ} \text{C} \\ &= \frac{5}{(68 \times 10^{-2})} \, ^{\circ} \text{C} \\ &= 7.3529 \, ^{\circ} \text{C} \end{split}$$

$$T_1 = T_0 + \triangle T ^{\circ} C$$

= 27 + 7.3529 $^{\circ} C$
= 34.3529 $^{\circ} C$

- 2. 500 g of ice is added to an insulated cup that contains 200 g of water at 50.0 °C. What is the final temperature.
 - (a) $Ice_{mass} = 500 g = 5 \times 10^{-1} kg$
 - (b) $Water_{mass} = 200 g = 2 \times 10^{-1} kg$
 - (c) $Ice_{temp} = 0$ °C
 - (d) $Water_{temp} = 50 \, ^{\circ}C$
 - (e) $c_{water} = 4.186 \times 10^3 \frac{J}{kg} ^{\circ}C$
 - $(f)~L_{\rm \scriptscriptstyle ice} = 3.33 \times 10^5 \, \frac{J}{kg}$
 - (g) $Q_{water} = -Q_{ice}$
 - (h) $Q = mc \triangle T$
 - (i) Q = mL
 - (j) False Assumption: All the ice is melted

How much Ice_{mass} would it take for $Water_{temp}$ to bring to $0^{\circ}C$?

$$\begin{split} Q_{\rm water} &= -Q_{\rm ice} \\ Water_{\rm mass} \times c_{\rm water} \times (0\,^{\circ}\mathrm{C} - \mathrm{Water}_{\rm temp_0}) = -L_{\rm ice} \times \mathrm{Ice}_{\rm mass} \\ 2 \times 10^{-1} \times 4.186 \times 10^{3} \times (0-50) = -3.33 \times 10^{5} \times \mathrm{Ice}_{\rm mass} \\ \frac{2 \times 10^{-1} \times 4.186 \times 10^{3} \times -50}{-3.33 \times 10^{5}} &= \mathrm{Ice}_{\rm mass} \\ \frac{2 \times 4.186 \times 5}{3.33 \times 10^{2}} &= \mathrm{Ice}_{\rm mass} \\ \frac{4.186}{3.33 \times 10^{1}} &= \mathrm{Ice}_{\rm mass} \\ 1.257 \times 10^{-1} &= \mathrm{Ice}_{\rm mass} \\ 125.7\,\mathrm{g} &= \mathrm{Ice}_{\rm mass} \end{split}$$

- \therefore It takes 125.7 g of Ice to bring Water_{temp} to 0 °C
- ∴ The final temperature is 0°C with 325.7 g of Water and 374.3 g of Ice