

Pokemon Collector

First Generation

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Road to Pokemon Master

How many PokeBall do we need ?

What if we want 2 of each, or 3 or 4 even ?

Questions ?

There are 151 different Pokemon



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