Should I Include Leveraged ETFs In My Portfolio?

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1 Introduction

In finance, leveraging means obtaining an exposition to an asset that surpasses one's stake. For instance, with a x2 (or "2:1") leveraged ETF (LETF), an investment of 1 euro grants 2-euro worth of exposition to the underlying asset of the LETF.

The Lifecycle Investing study showed that adopting a leveraged position on stocks may be interesting for retirement planning in a first section of one's career. The goal of such leveraging is to increase the expected returns given that, at that stage of life, one's total portfolio is overwhelmingly dominated by bond-like assets (futures savings from wages) thus causing one's

exposition to risky assets to be far below what one's level of risk aversion (or utility function) recommends.

Fundamentally, several methods make this possible, of which borrowing (e.g., mortgage loans, margin loans) is the most obvious one. But those methods also include more sophisticated schemes involving stock options (namely box spreads on future contracts).

In this study, we wil explore the intricacies of one LETFs – Amundi ETF Leveraged MSCI USA Daily UCITS ETF - EUR, whose ticker is "CL2" – which is designed to provide, at the scale of each trading day, a x2, long exposition to the performance of the MSCI USA index (Net Return).

- This LETF uses short-term, interbank borrowing to turn an investor's 1 euro stake into 2 euros of exposition. This gymnastic is solely managed by the fund.
- The fund is eligible to the Plan Epargne en Action (PEA) even though the index it tracks is entirely focused on the US. That is because it uses a *total return swap* between (i) a set of eligible assets (assets based in the European Union) it owns and (ii) the actual set of stocks in the MSCI USA Index owned by another company.
- And CL2 also happens to be capitalizing which grants the investor full control on their fiscal events.

These characteristics make CL2 and similar LETFs the easiest solution to gain leverage on stocks in France.

Nonetheless, this form of leverage implies certain additional risk factors compared to the equivalent, but unleveraged, scenario (namely a classic long, unleveraged, buy-and-hold strategy on ESE – a popular ETF tracking the S&P 500 index which is similar to the MSCI USA index):

- the cost of the borrowing carried out by the fund evolves unpredictably over time and has a direct, negative impact on the performance of the LETF;
- the daily rebalancing (daily reset of the leverage) increases the negative impact of the underlying index's volatility on the performance of the LETF this negative impact is called beta slippage. LETFs with a daily rebalancing are only marketed for detention periods of 1 trading day at most because funds want to discourage investors from exposing themselves to the daily rebalancings.

Those weaknesses can make LETFs greatly underperform equivalent unleveraged ETFs (e.g., CL2 vs. ESE) if borrowing costs and/or volatility are high.

The choice of an invest essentially rests on its expected risk-adjusted return or, in other words, on the amount of return it will provide for each unit of volatility (risk). Compared to unleveraged ETFs like ESE, the risk-adjusted return of LETFs like CL2 are more vulnerable to the underlying index's volatility and require borrowing costs not being too high (while unleveraged ETFs are not directly affected by interest rates). Hence, while LETFs are easy to use, the choice to invest in them is much more complex. That is what we will explore herein.

2 Materials

The time series used in this study are listed in Table 1.

Table 1: Metarials of the study

Time series	Source
MSCI USA index (Net, USD)	https://www.msci.com/indexes/index/984000
Euro Short-Term Rate (ESTER)	https://www.boursorama.com/bourse/taux/cours/1xESTER/
USD/EUR CL2	https://finance.yahoo.com/quote/USDEUR=X/https://finance.yahoo.com/quote/CL2.PA/

3 Understanding beta slippage

Let's first have a look at a putative 2x leveraged investment without rebalancing. That corresponds to a situation where one invested \$100 and got \$200 worth of the asset (an index fund) thanks to borrowing, for instance. For the sake of this example, we will consider a constant daily return of 2% on the index fund and ignore borrowing costs and fees. Figure 1 shows that the cumulative return of the x2 leveraged investment is constantly equal to the cumulative return of the index fund times two.

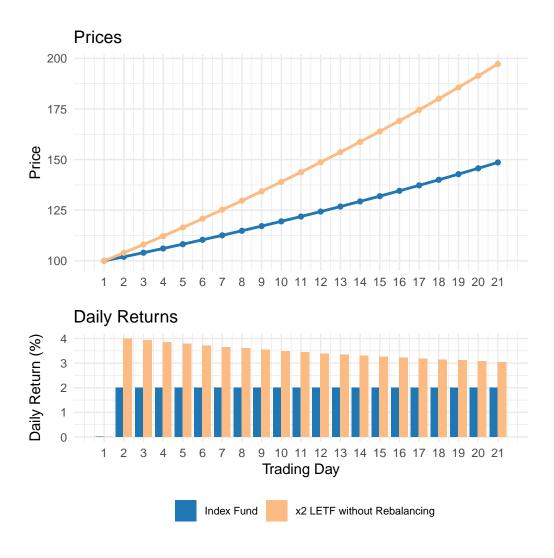


Figure 1: Leverage without rebalancing

We also notice on Figure 1 that the daily returns gradually converge: the one of the index fund was set to a constant 2%, but that translates to a daily return on the leveraged investment that starts at 4% and converges asymptotically to 2%. This is because, while the value of the initial \$200 worth of index fund shares grows by 2% daily, the value of the debt stays constant. As the total value of the position (= value of the asset) increases, the debt (= \$100) becomes negligible relative to the steadily growing equity (= position - debt). Hence, in the limit of infinitely many trading days, the leverage – which is is the position to equity ratio – approaches 1 and the daily returns asymptotically appproach 2%, like the unleveraged, underlying index fund. Equation 1 demonstrates this mathematically (with R_t = daily return).

$$R_{t} = \frac{200(1.02)^{t} - 200(1.02)^{t-1}}{200(1.02)^{t-1} - 100}$$

$$= \frac{200(1.02)^{t-1} \cdot (1.02 - 1)}{200(1.02)^{t-1} - 100}$$

$$= \frac{200(1.02)^{t-1} \cdot 0.02}{200(1.02)^{t-1} - 100}$$

$$= \frac{(1.02)^{t-1} \cdot 0.02}{(1.02)^{t-1} - 0.5}$$

$$\lim_{t \to \infty} R_{t} = \lim_{t \to \infty} \frac{(1.02)^{t-1} \cdot 0.02}{(1.02)^{t-1} - 0.5}$$

$$= \frac{0.02 \cdot \infty}{\infty} = 0.02$$
(1)

?@fig-lev-sce-up-sta steady, 2% daily growth of the index. Constant returns which simply correspond to the index growth times 2 or 3. In such a case with low volatility, the performance of LETFs strictly equals the performance of the index times the amount of leverage. When that trend goes upward, long LETFs (i.e., LETFs whose leverage is positive) are very efficient in terms risk-adjusted yield.

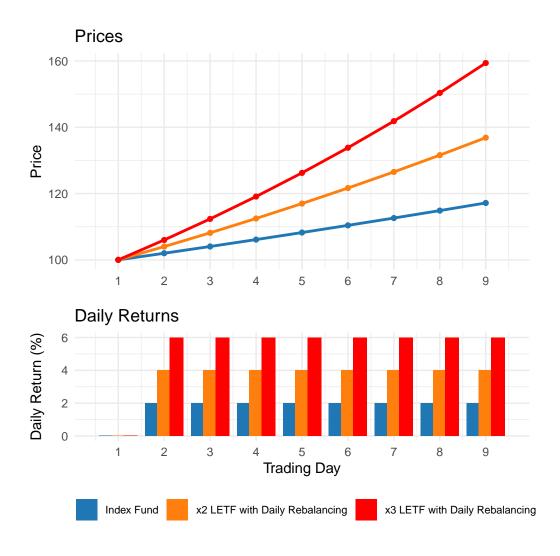


Figure 2: To name



Figure 3: To name

But when volatility is introduced, a new phenomenon appears. Let's take an example.

- index, market agrees on \$100 but with some fluctuations around that valuation.
- 10% drop means \$100 down to \$90
- to go back to the initial \$100, we need a 11.1% increase

with leverage:

- 100 20% gives 80%
- 80 + 22.2% gives \$97.78

I.e. the multiplicative factor that was enough to bring the index back to \$100 (1.111), when multiplied by two (1.222), is not enough to bring back the 2x LETF back to \$100. That's because the LETF lost more worth and, after the 10%/20% drop, one percent of the index is worth .9 cents while 1% of the 2x LETF is worth only .8 cents.

Figure 4, index value goes sideways but with volatility above and below its 100 center point. Don't stay centered on 100, though. This drift is beta slippage.

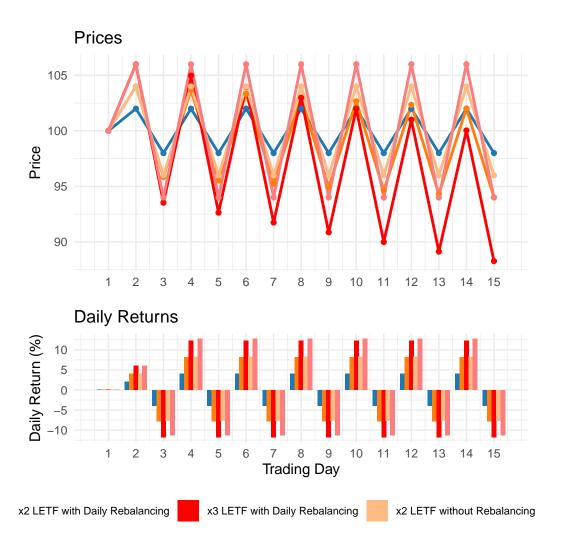


Figure 4: To name

4 Borrowing cost

- 5 Reconstructing the past price action of CL2
- 6 Forward simulations of CL2

7 Conclusions

Maybe.

8 Appendix

This qmd took 0 minutes to render. It was rendered in the following environment:

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R version 4.5.1 (2025-06-13)
Platform: x86_64-pc-linux-gnu
Running under: Ubuntu 24.04.2 LTS
Matrix products: default
BLAS: /usr/lib/x86_64-linux-gnu/openblas-pthread/libblas.so.3
LAPACK:
/usr/lib/x86_64-linux-gnu/openblas-pthread/libopenblasp-r0.3.26.so;
LAPACK version 3.12.0
attached base packages:
[1] stats graphics grDevices datasets utils methods base
other attached packages:
[1] patchwork_1.3.1 lubridate_1.9.4 readxl_1.4.5 plotly_4.11.0
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[9] zoo_1.8-14 data.table_1.17.6
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