

Network Analysis (INFOMNWA-2021)

# Lecture 5: Social network and its measures

Jiamin Ou

# Introducing myself

- **Interdisciplinary researcher** in energy, environment and human systems
- **Current project: ENgaging Residents in Green energy Investments** through **S**ocial networks, **complExity**, and **D**esign. (<http://enrgised.nl/>, funded by NWO)

- **Previously:**

International Development (PhD), University of East Anglia, UK

International Institute for Applied Systems Analysis (IIASA), Austria

University of Texas at Austin, US

- **Awards:**

Mikahlevich Award, by IIASA, 2018

Green Talent, by the German Federal Ministry of Education and Research (BMBF), 2020

# Also in this course

## **Kevin Wittenberg**

PhD candidate Sociology

Project on sustainable cooperation: citizen collectives for health care (Dutch: zorgcoöperaties)

Research interests

- Social networks, cooperative relations, statistics, opinion dynamics, philosophy of science.

## **Thom Volker**

Second-year MSc. Methods and Statistics

First-year MSc. Sociology and Social Research

Research interests (theses) are focused on

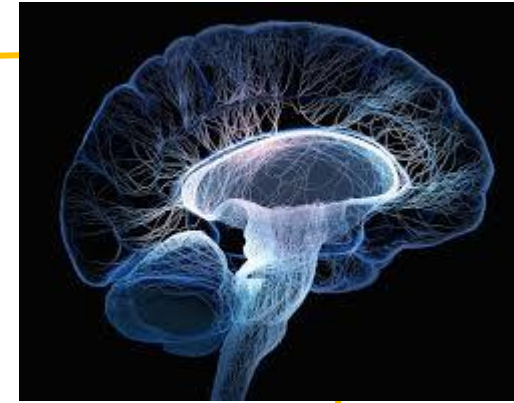
- Aggregating results from studies with divergent designs
- Cooperation in social dilemmas (e.g., Prisoner's Dilemma)
- Creation of synthetic data where privacy and confidentiality constraints prohibit sharing the observed research data

Lecture 1: Principles of deep learning in artificial networks

Lecture 2: Deep learning in biological neurons and networks

Lecture 3: Early and feedforward visual processing

Lecture 4: Higher and recurrent visual processing



Neural Networks  
Unit: neurons

Lecture 5: Social network and its measures

Lecture 6: Network formation

Lecture 7: Simple and complex contagion

Lecture 8: Influence manipulation



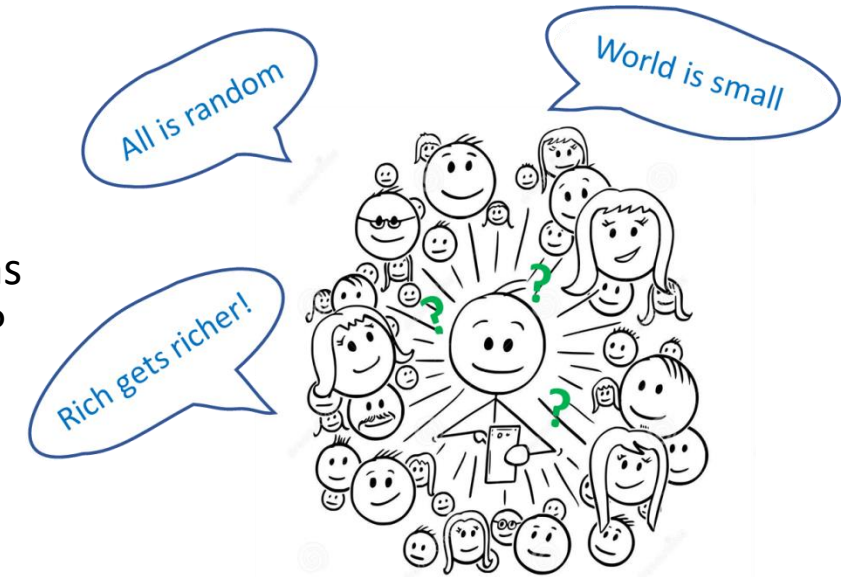
Social Networks  
Unit: people, organization

## Lecture 5: Social network and its measures

What is social network and how to measure it?

## Lecture 6: Network formation

How are individuals or complex systems wired together?



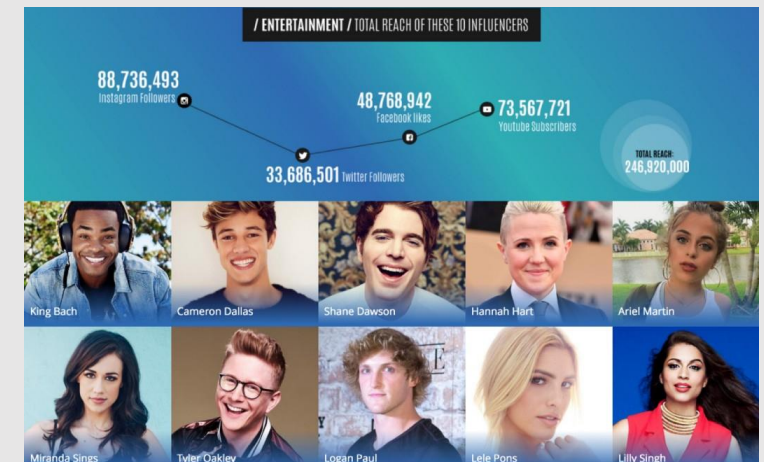
## Lecture 7: Simple and complex contagion

How does influence transmit through the network?



## Lecture 8: Influence manipulation

How can we model and control the spread of influence?



# Course goals

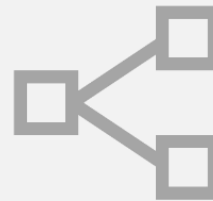
- What to look for in a social network: the perspectives and metrics
- Social contagion theory and empirical models (Independent Cascade, Threshold model...)
- Apply the knowledge, theory and models in social networks as a descriptive and predictive tool for real-world problems

# Program for today



## **Introduction of social network**

- Why we need network thinking
- Definition of social network
- Development of social network analysis



## **Measuring social network**

- Directed and undirected graph
- Node-level metrics
- Group-level metrics
- Example of Facebook user network





**WE ALL  
CONNECT,  
LIKE A NET  
WE CANNOT  
SEE**

—— *Mickenberg and Dugan, Taxi Driver Wisdom, 1995*



**Imagine:** To study companies' possibilities to support an NGO

**Standard approaches:**

- Define your potential targets
- By interview and survey to measure their variety (e.g., size, industry, profitability, their history to support NGO...)

**Anything missing?**



**Imagine:** To study companies' possibilities to support an NGO



**Standard approaches:**

- Define your potential targets
- By interview and survey to measure their variety (e.g., size, industry, profitability, , their history to support NGO ...)



**+ A network perspective**

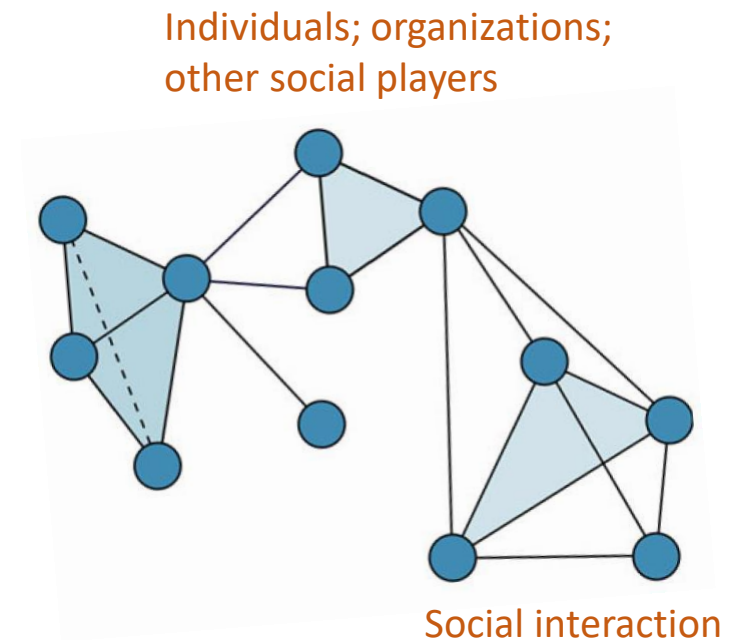


**Within/between companies relations** (e.g., memberships on each others' boards of directors, acquaintanceships of corporate officers, joint business dealings)

# Manifestation of the social relations: **A social network**

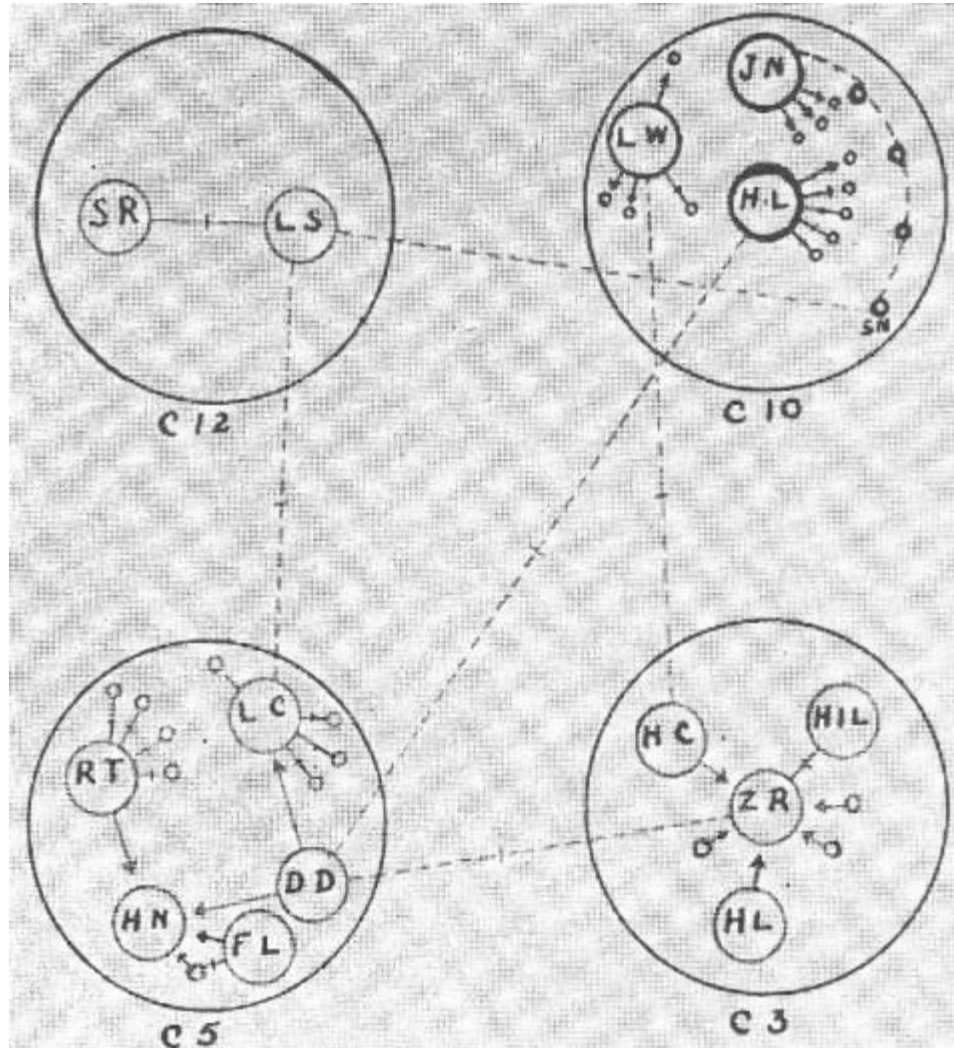
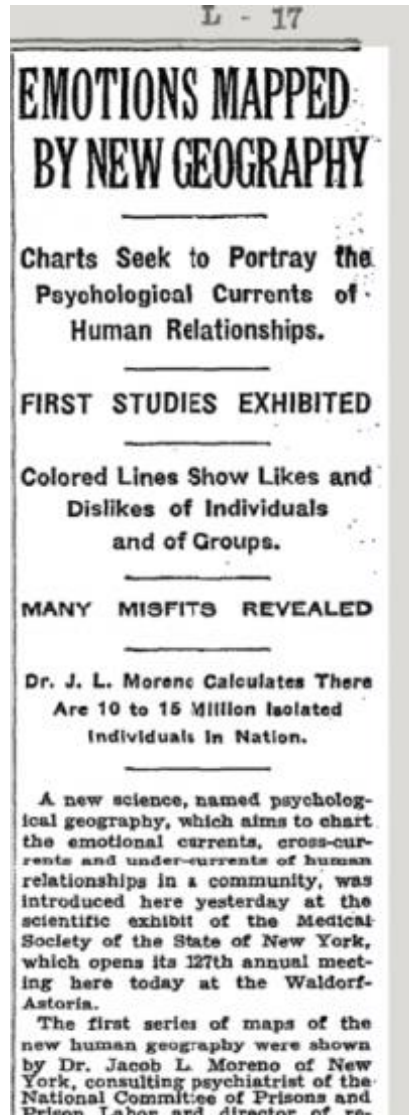
Definition of a social network: “a **graph** made up of a set of **social actors** (such as individuals or organizations), and other social **interactions between actors**”

Significance of social network analysis: provides a mathematical statements of some social concepts, and make theory more testable





# Sociogram, Moreno, 1953: Precursor to SNA



*An epidemic of runaways among the girls at the Hudson school: 14 girls runaway;*

*less to do with individual factors than with the positions of the runaways in an underlying social network*

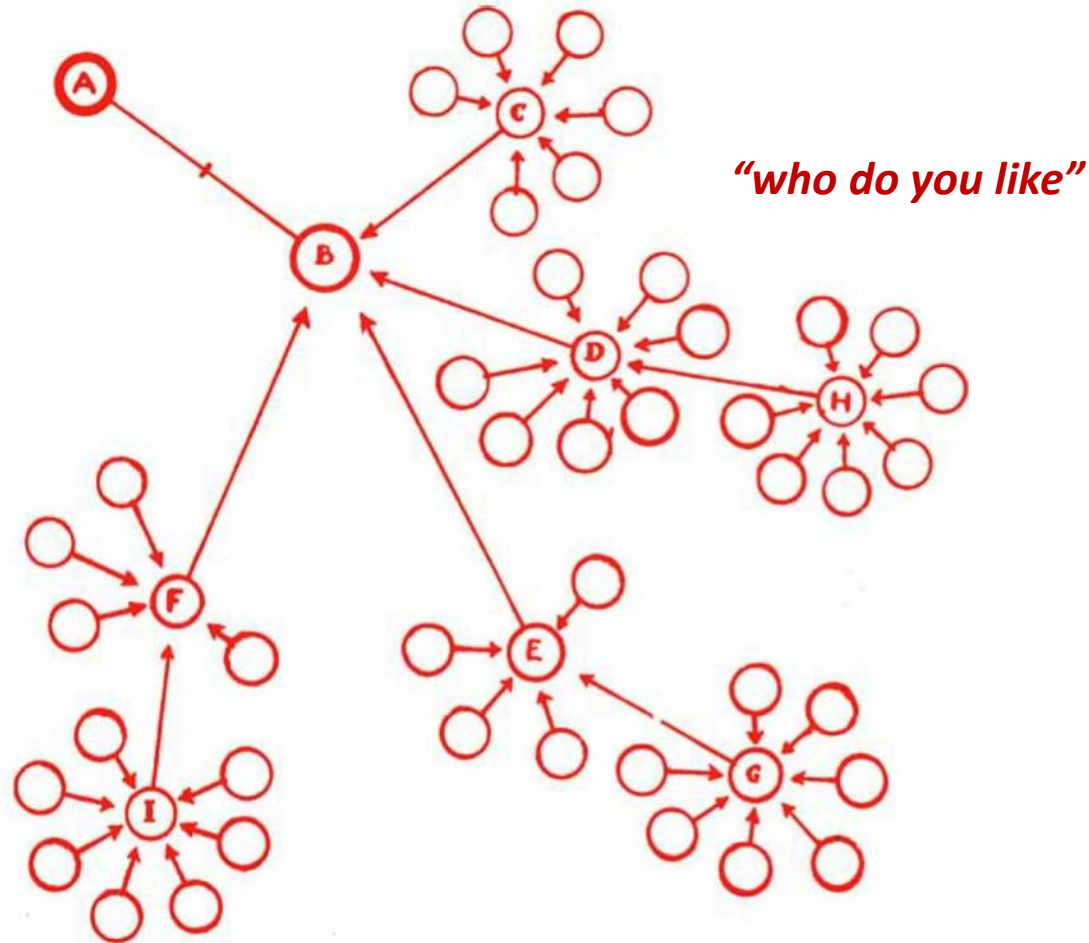
*Emotional channels between girls run away*

**It was their location in the social network that determined whether and when they ran away**

April 3, 1933  
The New York Times

Who Shall Survive? Foundations of Sociometry, Group Psychotherapy and Sociodrama.

# Sociogram, Moreno, 1953: Precursor to SNA



*Among a population of 435 persons, 204, or 46.5%, remained unchosen after the 1st choice; 139, or 30%, after the 2d choice; 87, or 20%, after the 3rd choice; 74, or 17%, after the 4th choice; and 66, or 15%, after the 5th choice. (Moreno 1934, p. 249)*

*15% of people being left behind.*

*Who Shall Survive? Foundations of Sociometry, Group Psychotherapy and Sociodrama.*

# How SNA evolves over time...

1940's and 1950's, **experimental structure** to study group process, using points to depict actors and lines to depict channels of communications

1950's, used **matrices** to study social network

1950's 1960's, introduced **the formal concepts** of social network analysis (e.g., density, span, connectedness, clusterability...)

SNA: “developed out of a propitious meeting of social theory and application, with formal mathematical, statistical and computing methodology” (*Inherently interdisciplinary*)

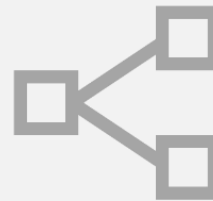


# Program for today



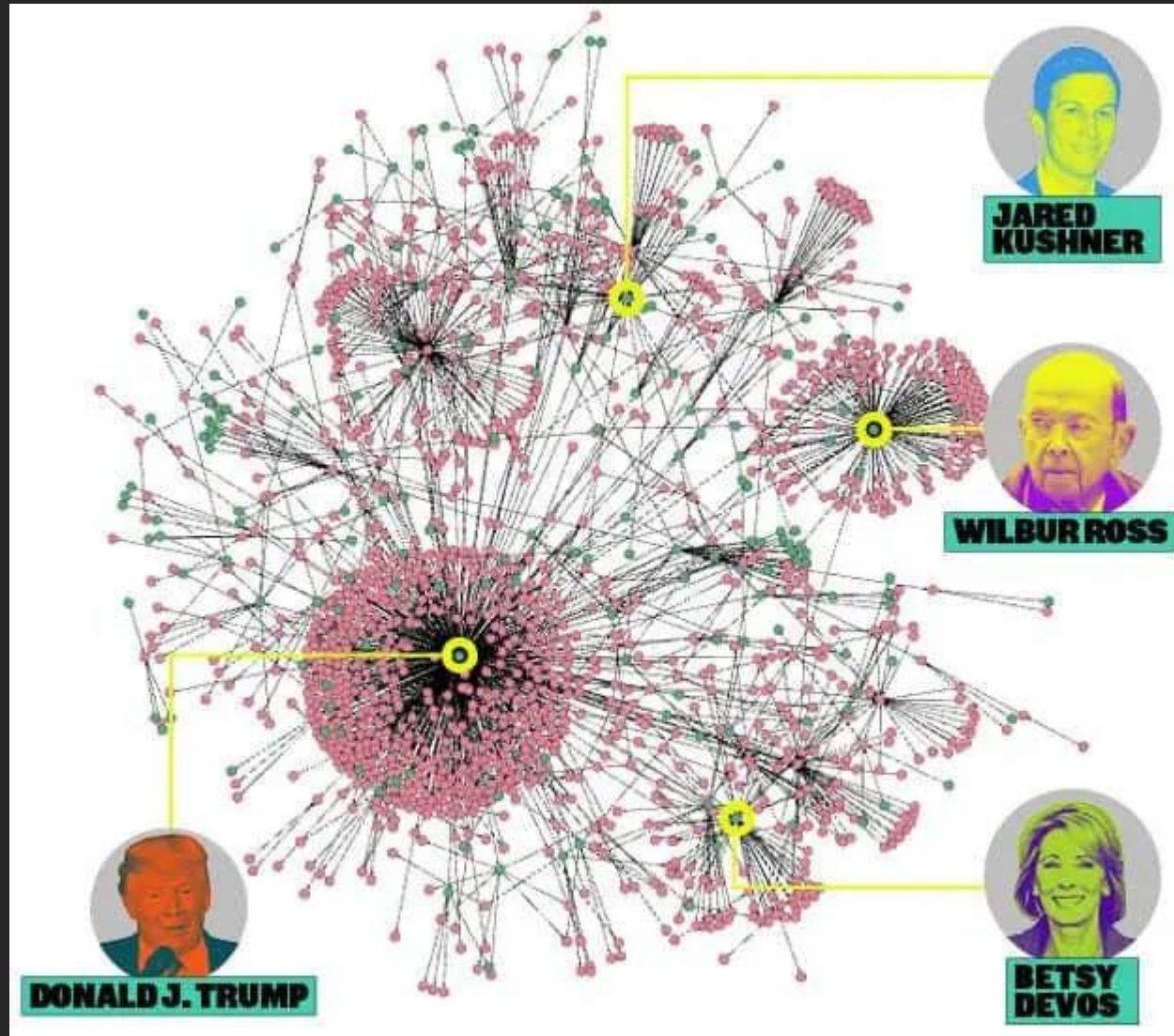
## **Introduction of social network**

- Why we need network thinking
- Definition of social network
- Development of social network analysis



## **Measuring social network**

- Directed and undirected graph
- Node-level metrics
- Group-level metrics
- Example of Facebook user network



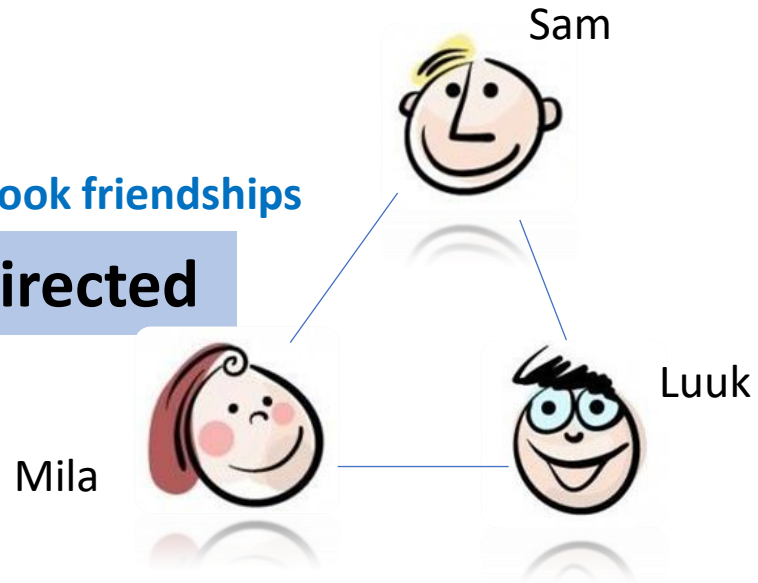
When social network data is booming now...

- *What are the things you want to know in a network?*
- *How can you measure them?*

# Directed and undirected graph

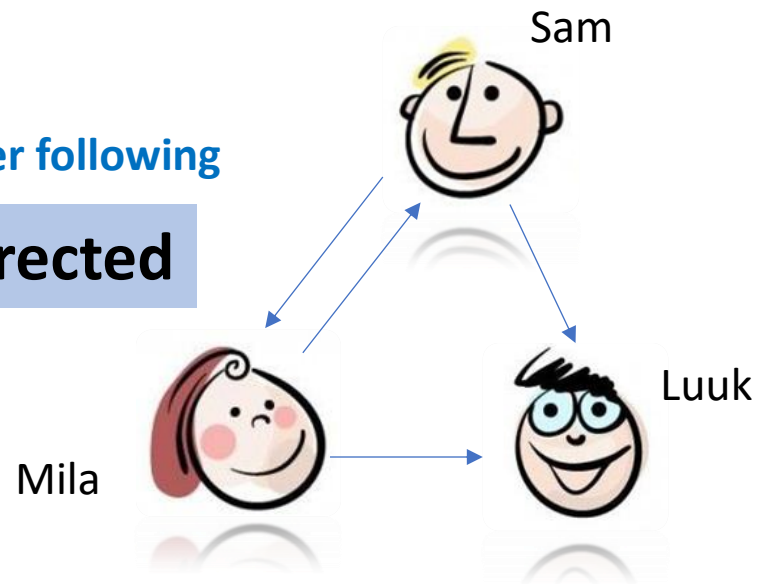
Facebook friendships

**Undirected**



Twitter following

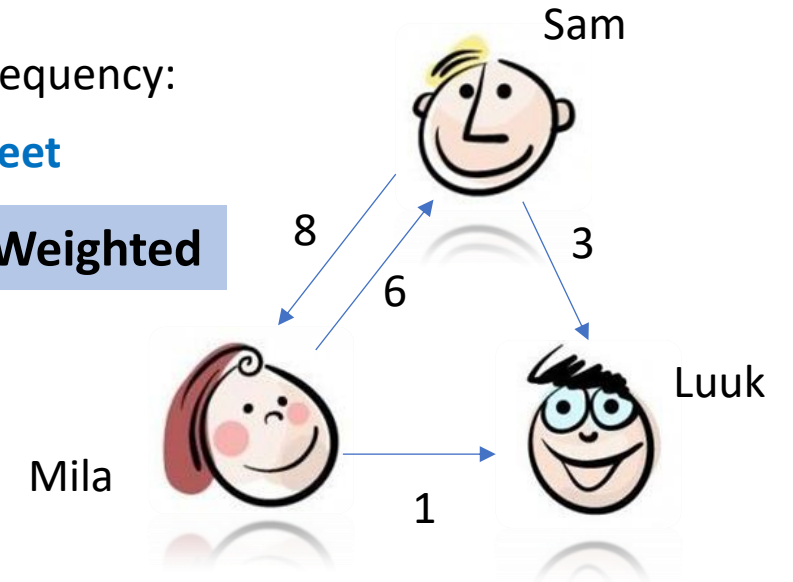
**Directed**

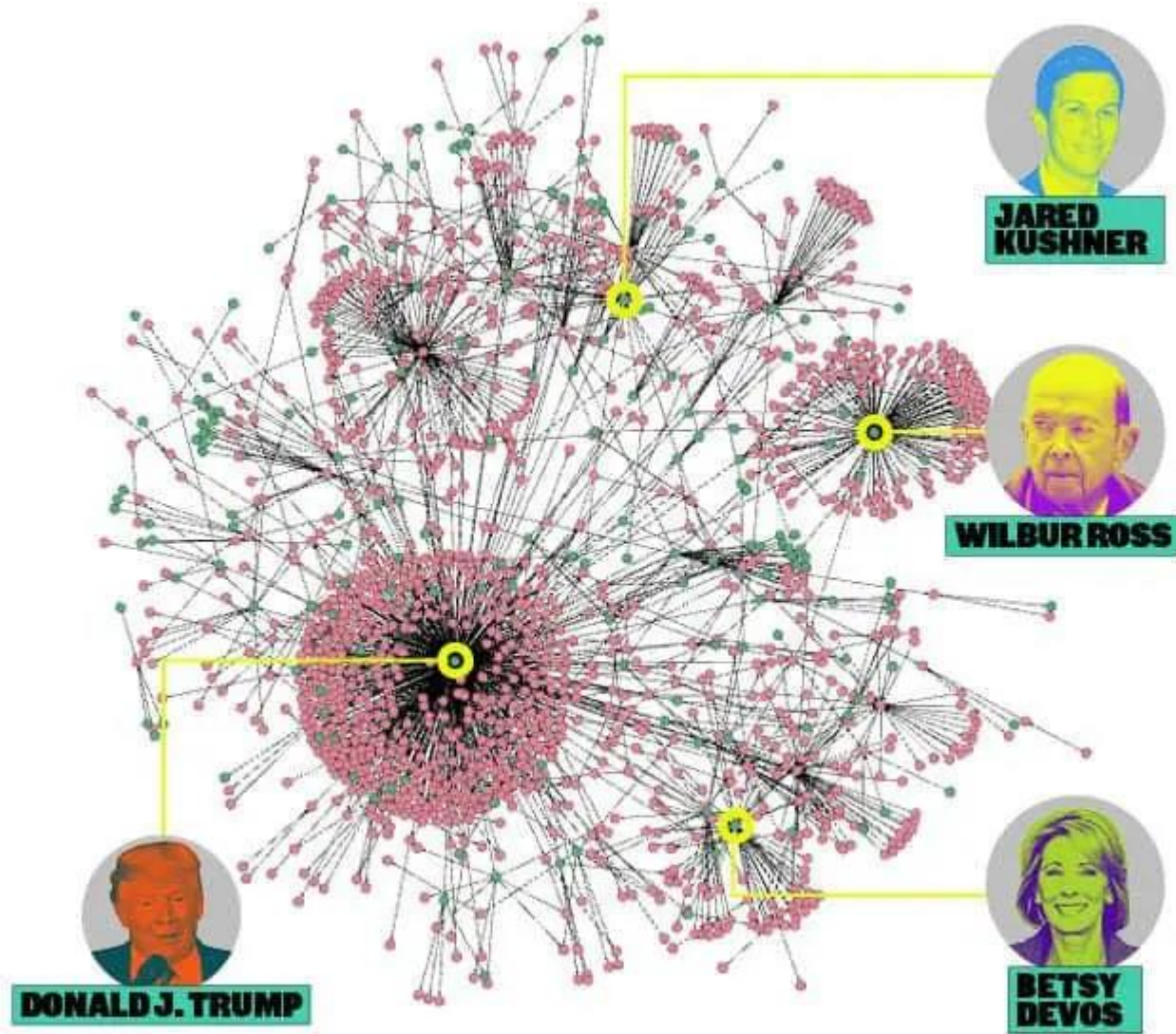


Consider the frequency:

Retweet

**Directed and Weighted**





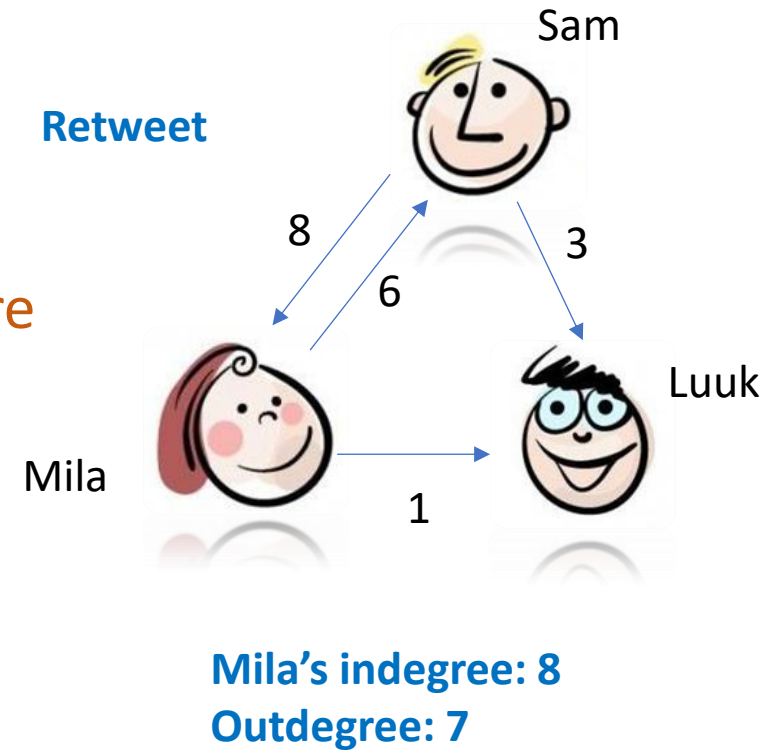
Who is the most central one in this network?



# Node level network measures

- Degree (number of links)
  - Indegree
  - Outdegree
- Degree centrality
- Closeness centrality
- Betweenness centrality
- Eigenvector centrality
- Local clustering
- ....

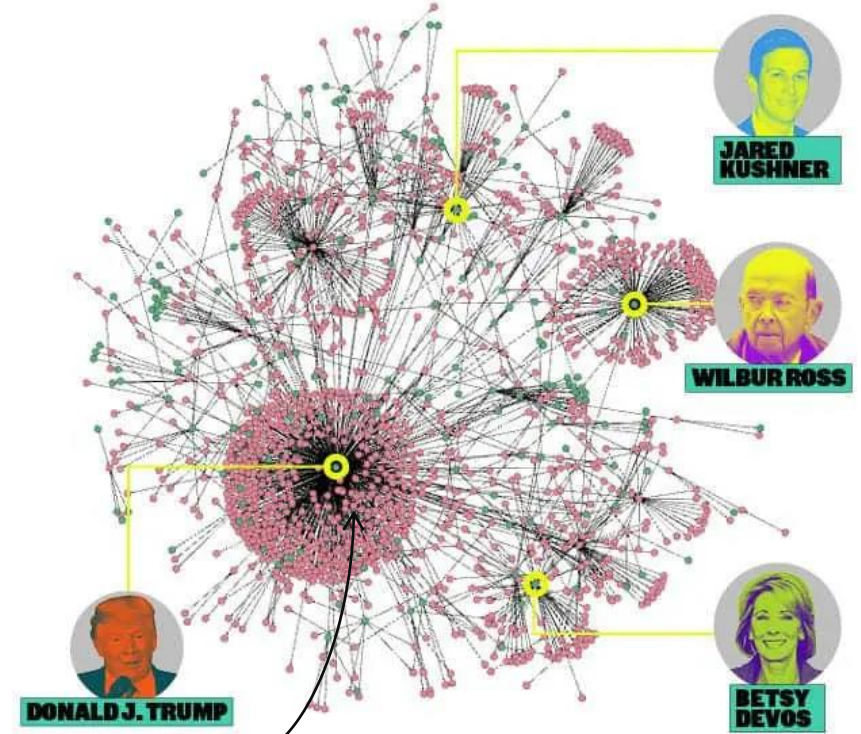
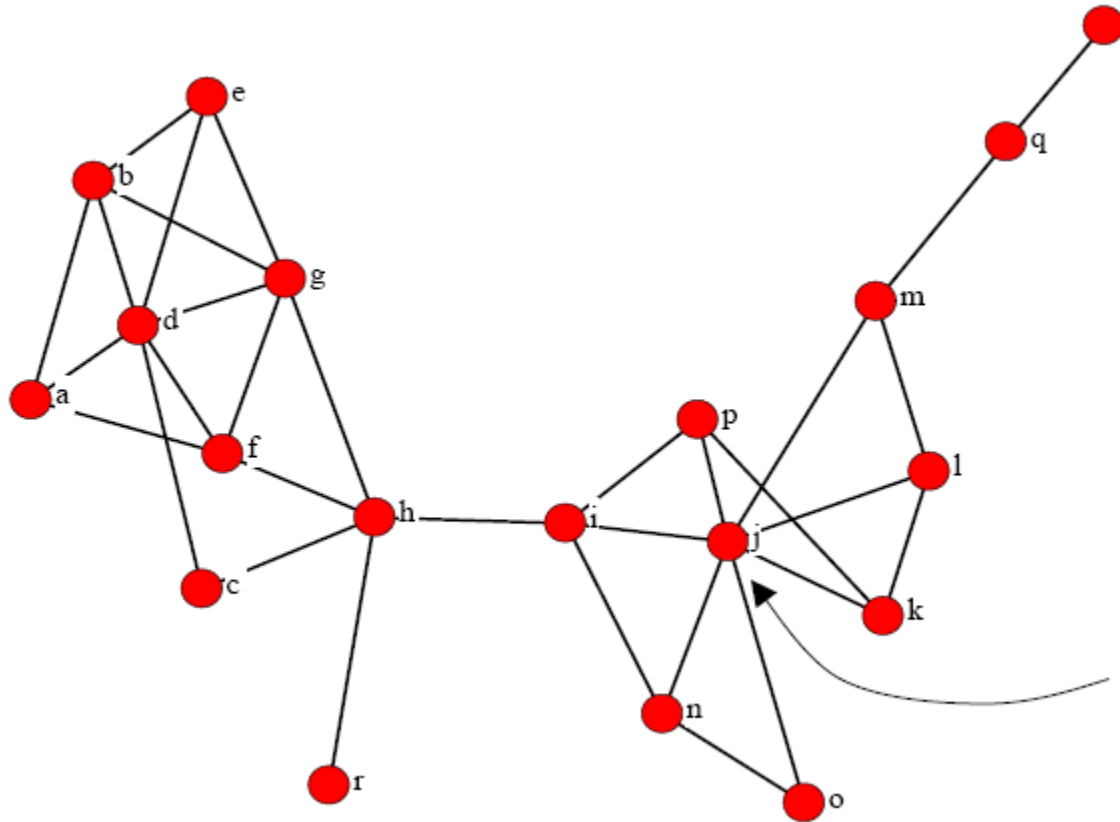
How central you are



*"It's all about location, location and location"*

## Degree Centrality

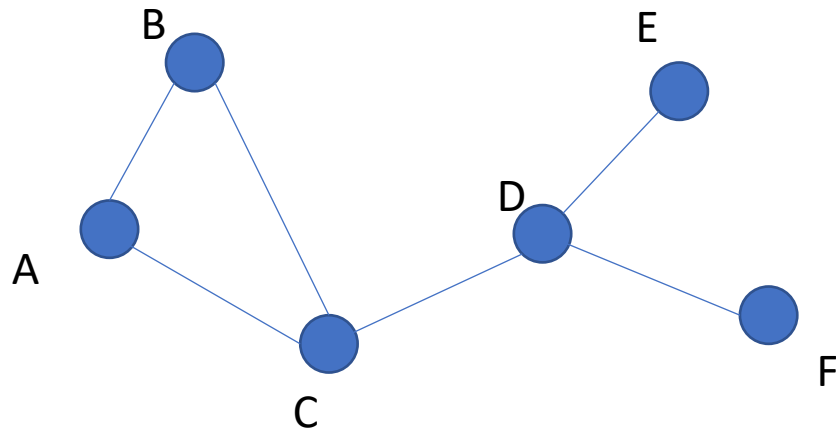
The number of nodes adjacent to a given node





## Closeness centrality: the closest one to all other nodes

Sum of geodesic distances (shortest paths) to all other nodes



Shortest paths between A and others:

A to B: A-B 1

A to C: A-C 1

A to D: A-C-D 2

A to E: A-C-D-E 3

A to F: A-C-D-F 3

Sum of the shortest path from A to others: 10

Shortest paths between C and others:

C to A: C-A 1

C to B: C-B 1

C to D: C-D 1

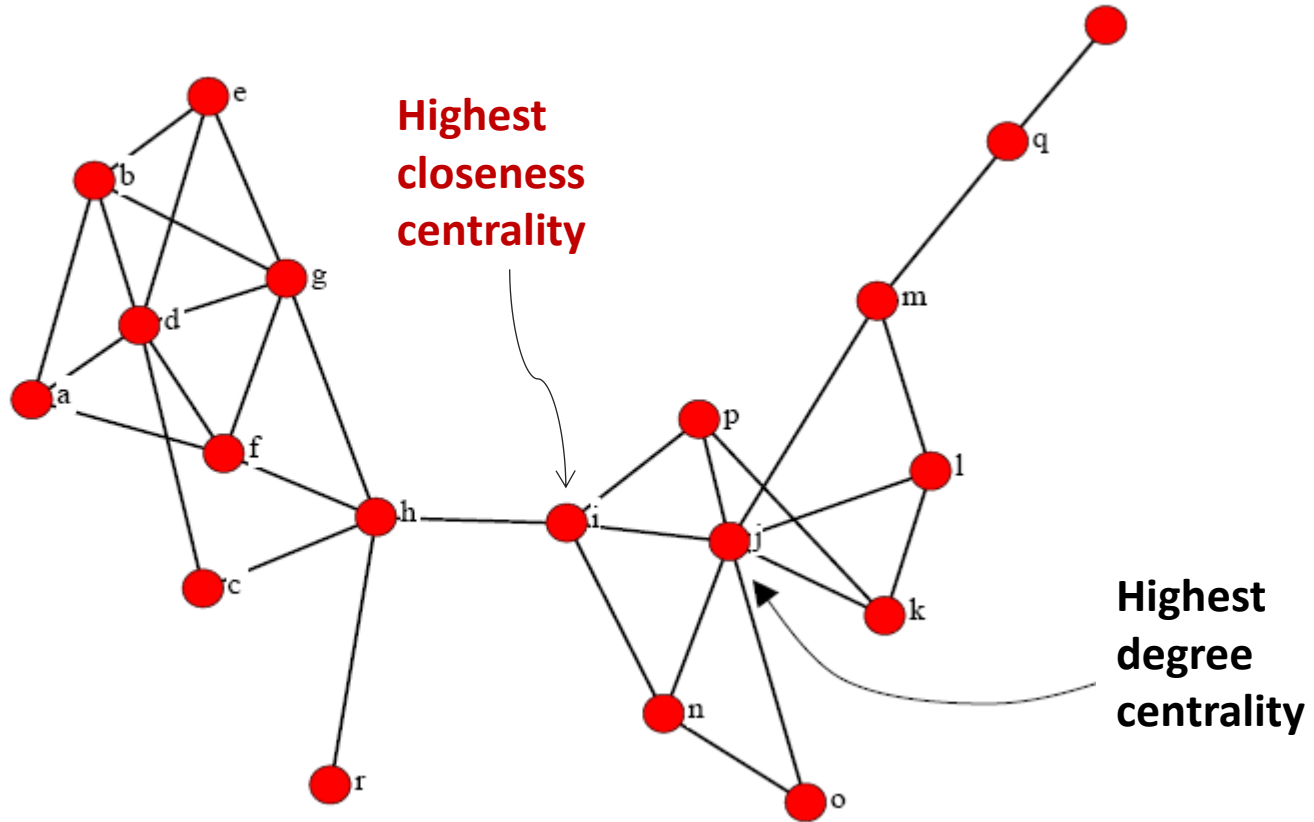
C to E: C-D-E 2

C to F: C-D-F 2

Sum of the shortest path from C to others: 7

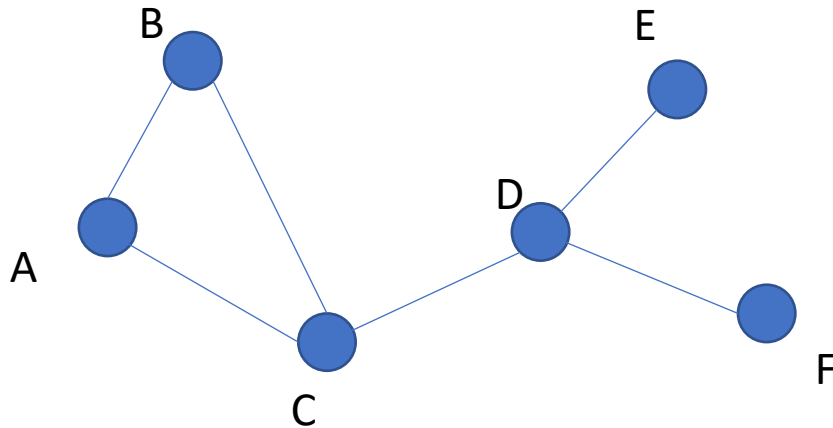
## Node level measures

It takes the fewest steps for anyone to reach node *i*



## Betweenness centrality: how often a node is a bridge between other nodes

Number of times that a node lies along the shortest path between two others



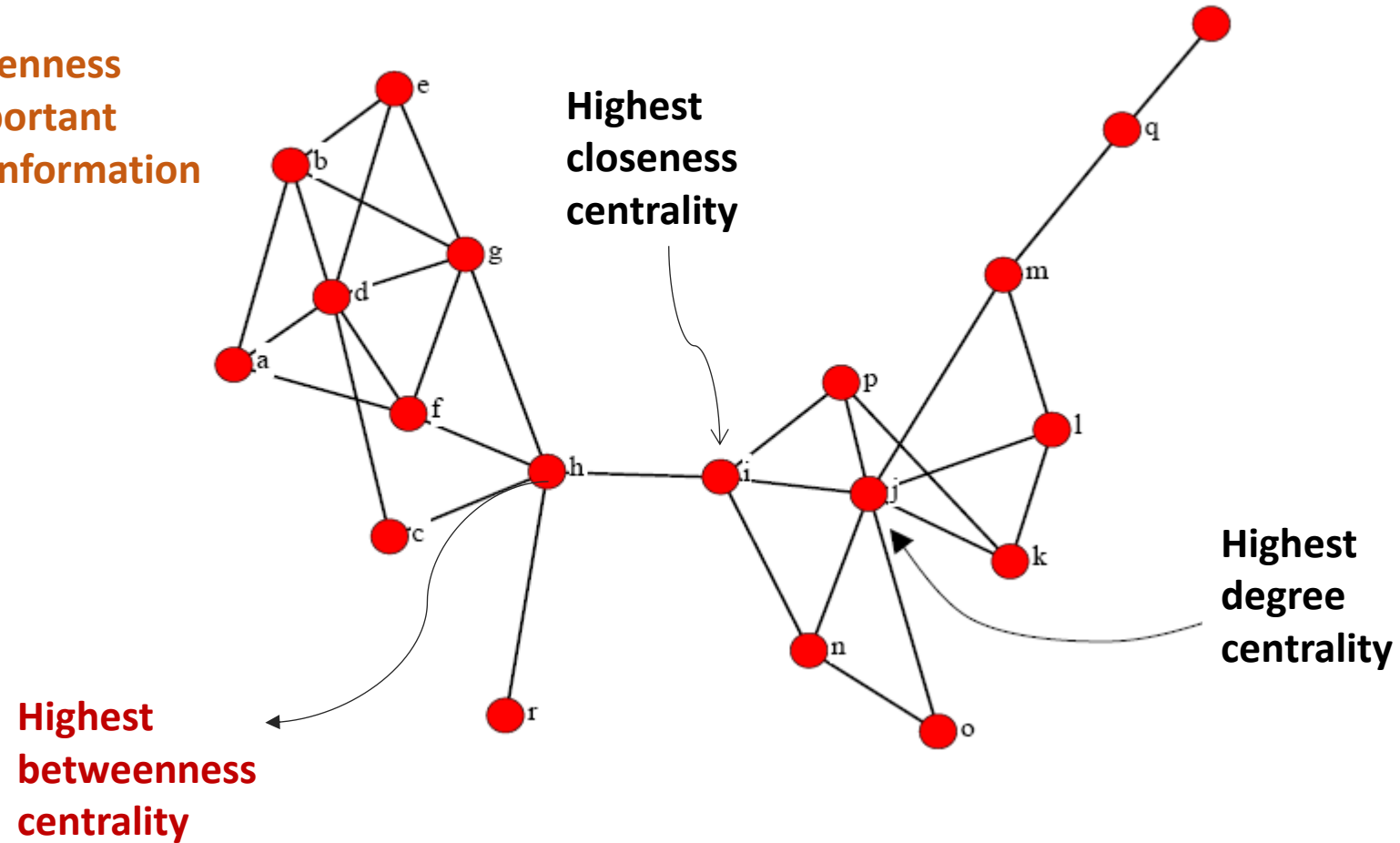
Shortest paths between every nodes:

A to B: A-B  
A to C: A-C  
A to D: A-C-D  
A to E: A-C-D-E  
A to F: A-C-D-F  
B to C: B-C  
B to D: B-C-D  
B to E: B-C-D-E  
B to F: B-C-D-F  
C to D: C-D  
C to E: C-D-E  
C to F: C-D-F  
D to E: D-E  
D to F: D-F

C appears 6 times  
D appears 2 times  
C has the highest betweenness

## Node level measures

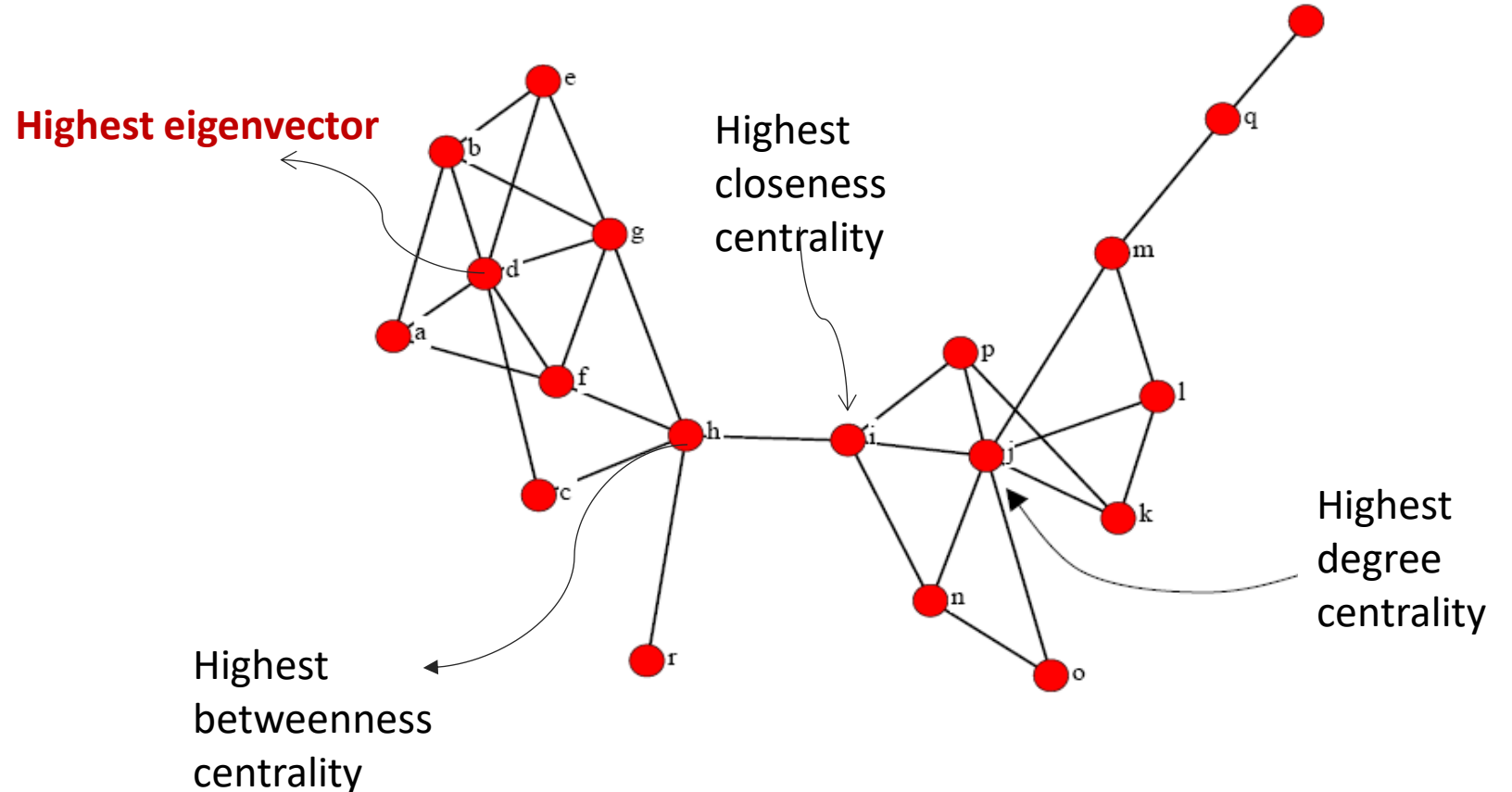
Nodes with high betweenness centrality are often important controller of power or information (check point)



## Eigenvector centrality

How central you are depends on how central your neighbors are (**The sum of the centrality of your neighbours**) (Triumph of Quality Over Quantity!)

A node with 30 unpopular (e.g., low degree) friends  
< A node with 10 very popular friends (like Barack Obama)



The PageRank algorithm used by Google's search engine is a variant of Eigenvector Centrality.



Google Search

I'm Feeling Lucky

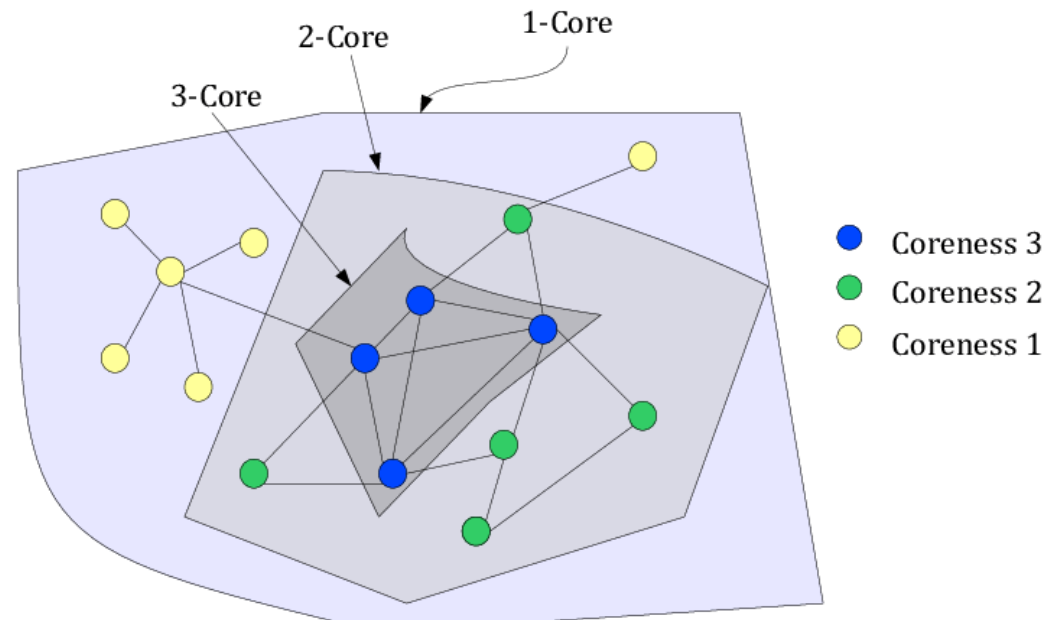
Google offered in: [Nederlands](#) [Frysk](#)

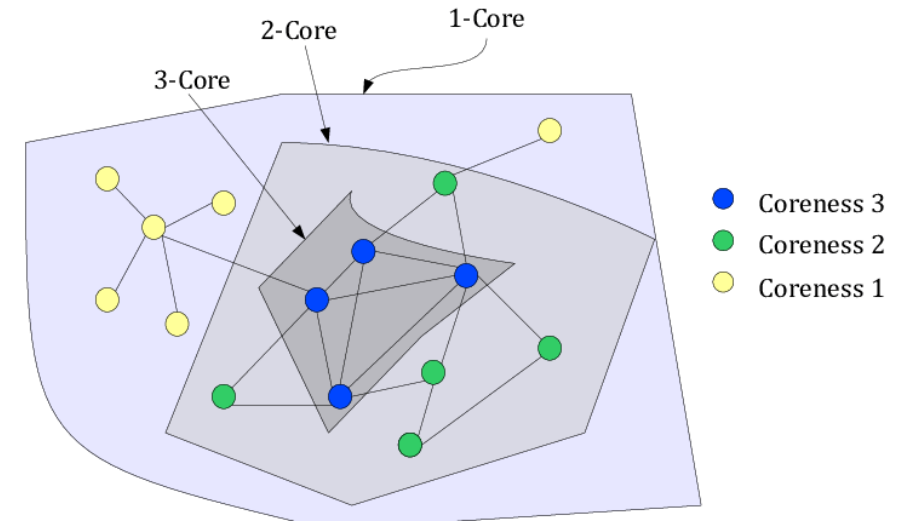
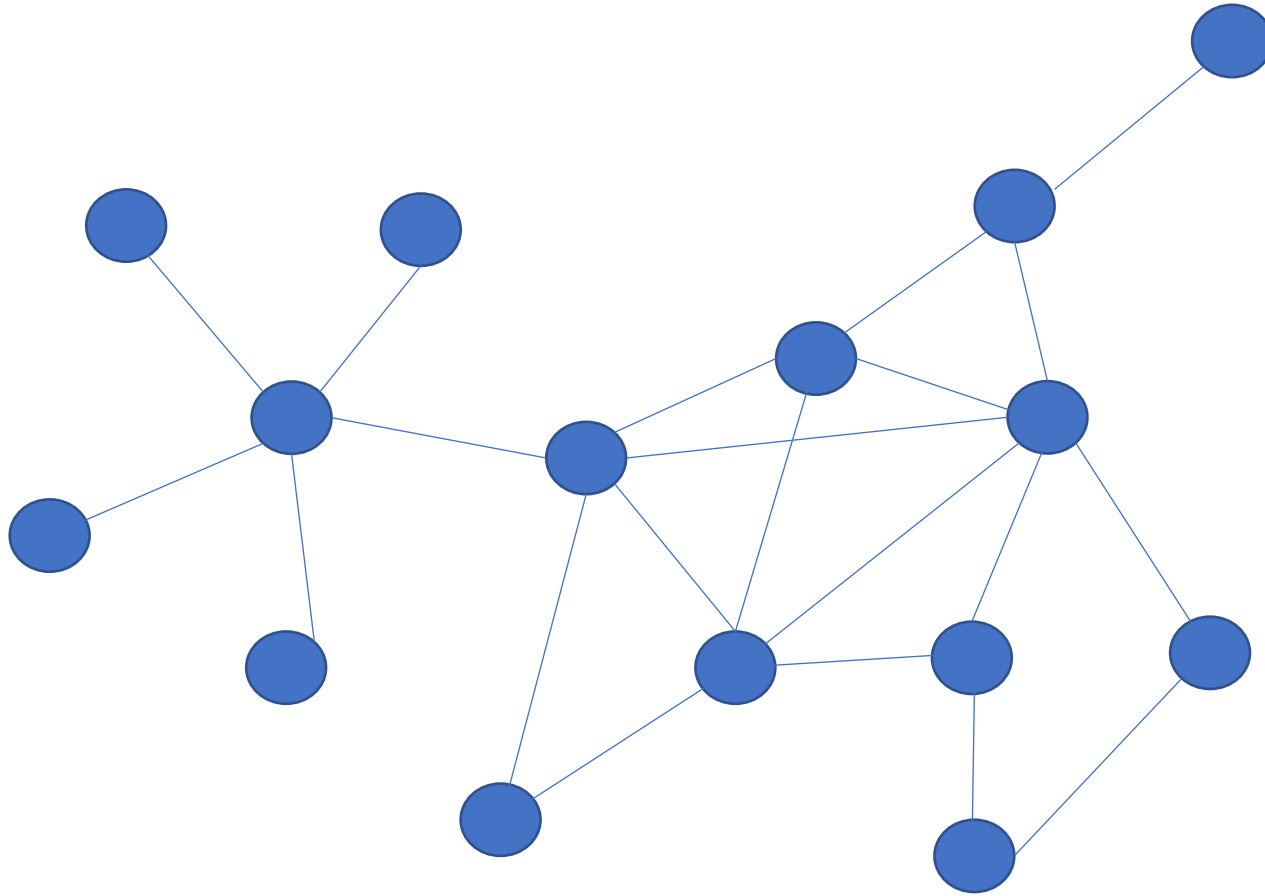
“PageRank works by ***counting the number and quality*** of links to a page to determine a rough estimate of how important the website is. The underlying assumption is that more important websites are likely to receive more links from other websites”



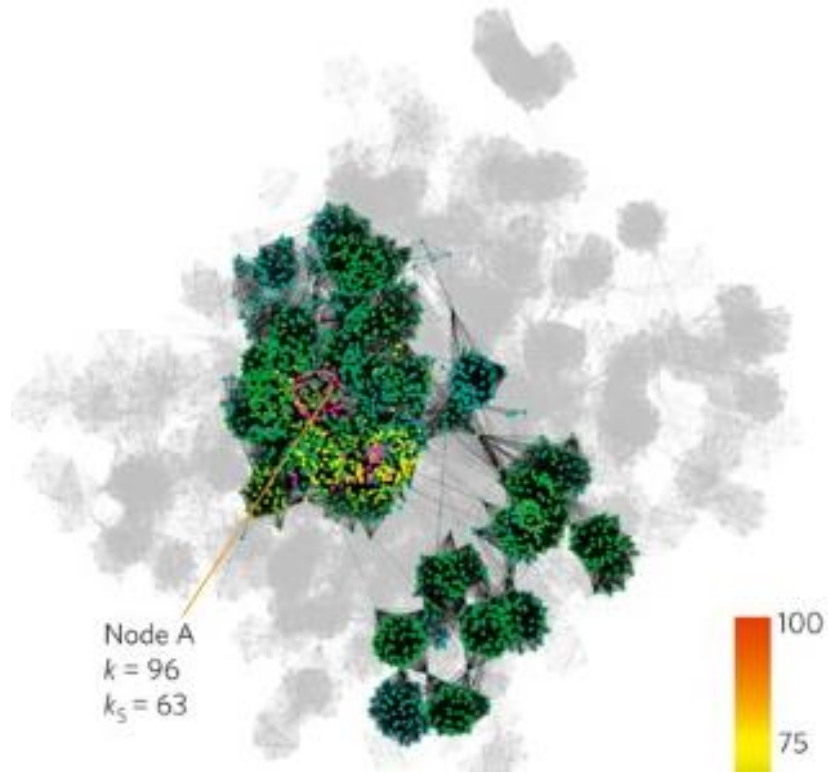
## k-cores

- Obtained by **recursively removing** all nodes of degree smaller or equal to  $k$ , **until** the degree of all remaining vertices is larger than  $k$ .

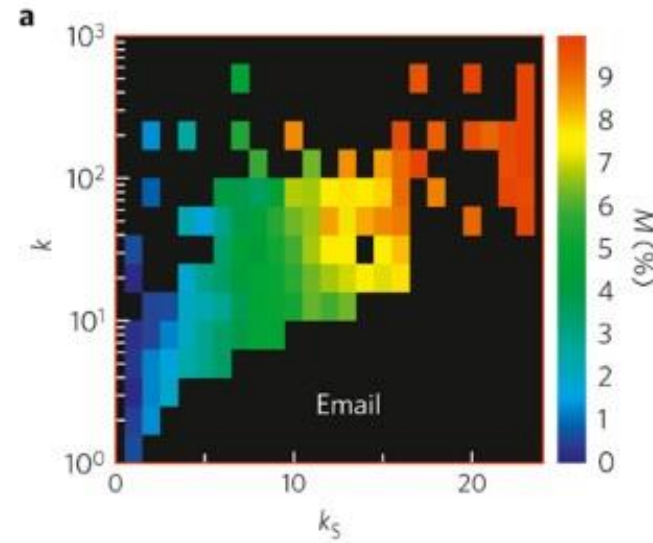




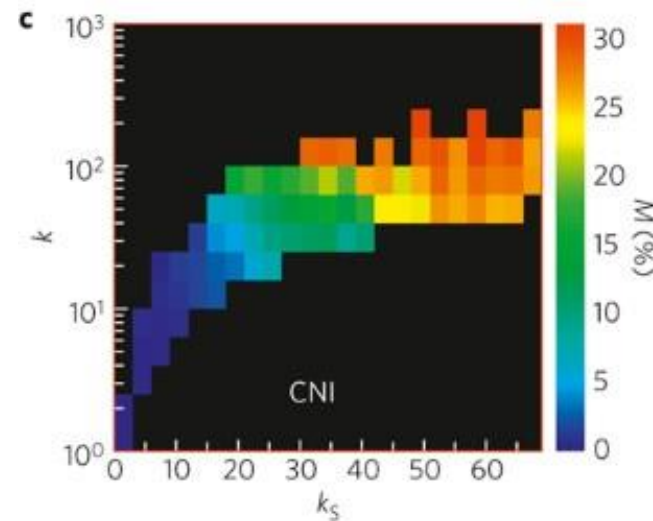
- High  $k_s$ : at the centre of network
- Low  $k_s$ : at the outer ring of network



The contact network of hospital patients (CNI)



The network of email contacts in the Computer Science Department of University College London



The contact network of hospital patients (CNI)

**Degree is the most obvious metrics of centrality, but it shouldn't be the only one**

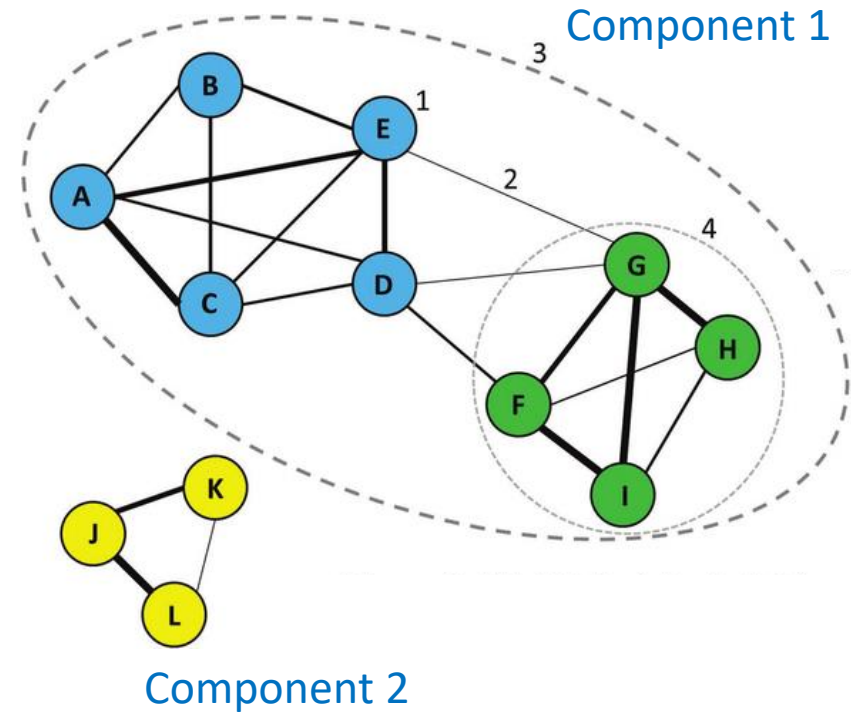
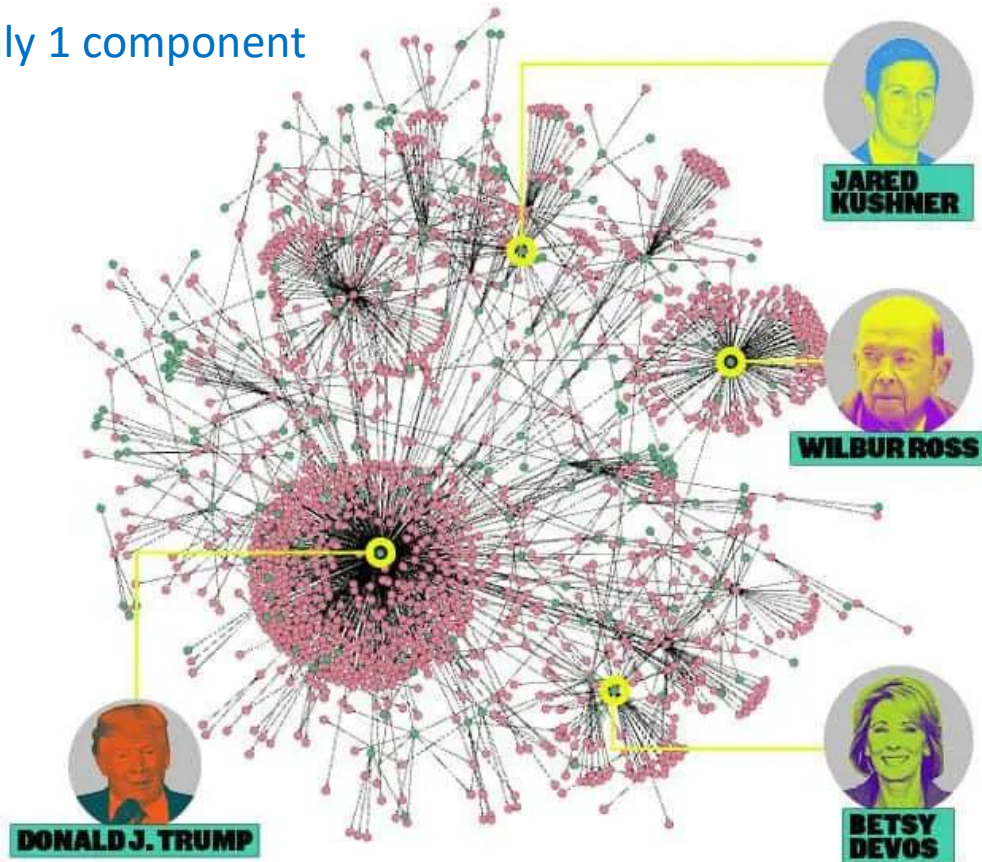
## Network-level measures

- Component
- Community
- Degree distribution
- Density
- Global clustering
- Centralization

# Component

No path between the nodes in different subsets

Only 1 component

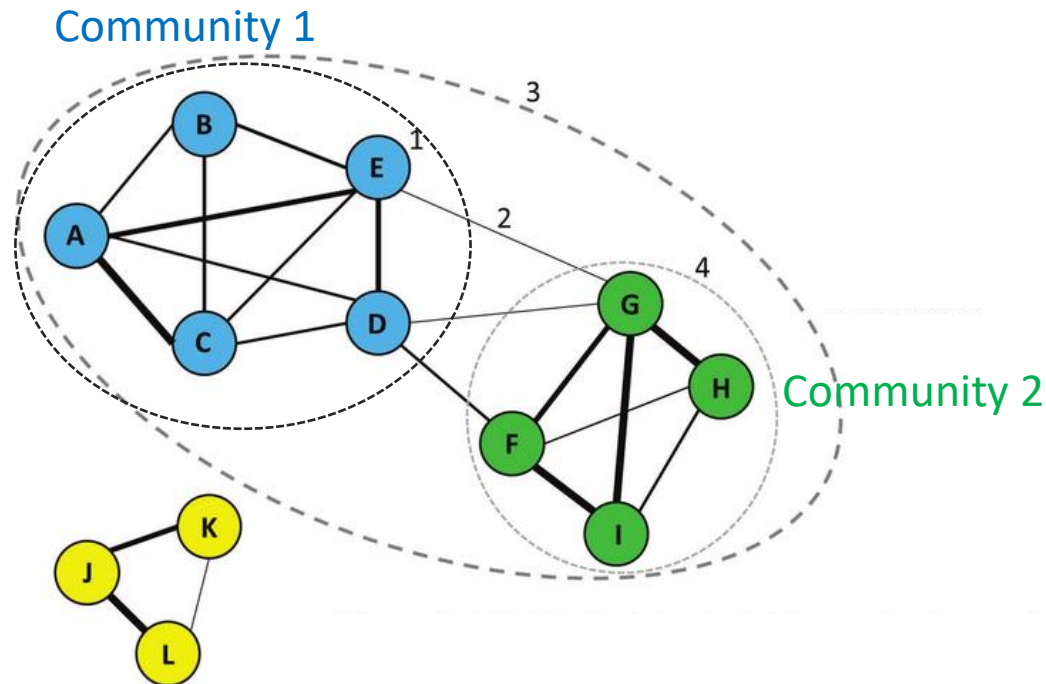


# Community

Most real networks contain parts in which the nodes are **more connected to each other than to the rest of the network**: clusters, communities, cohesive groups or modules (no widely accepted, unique definition)

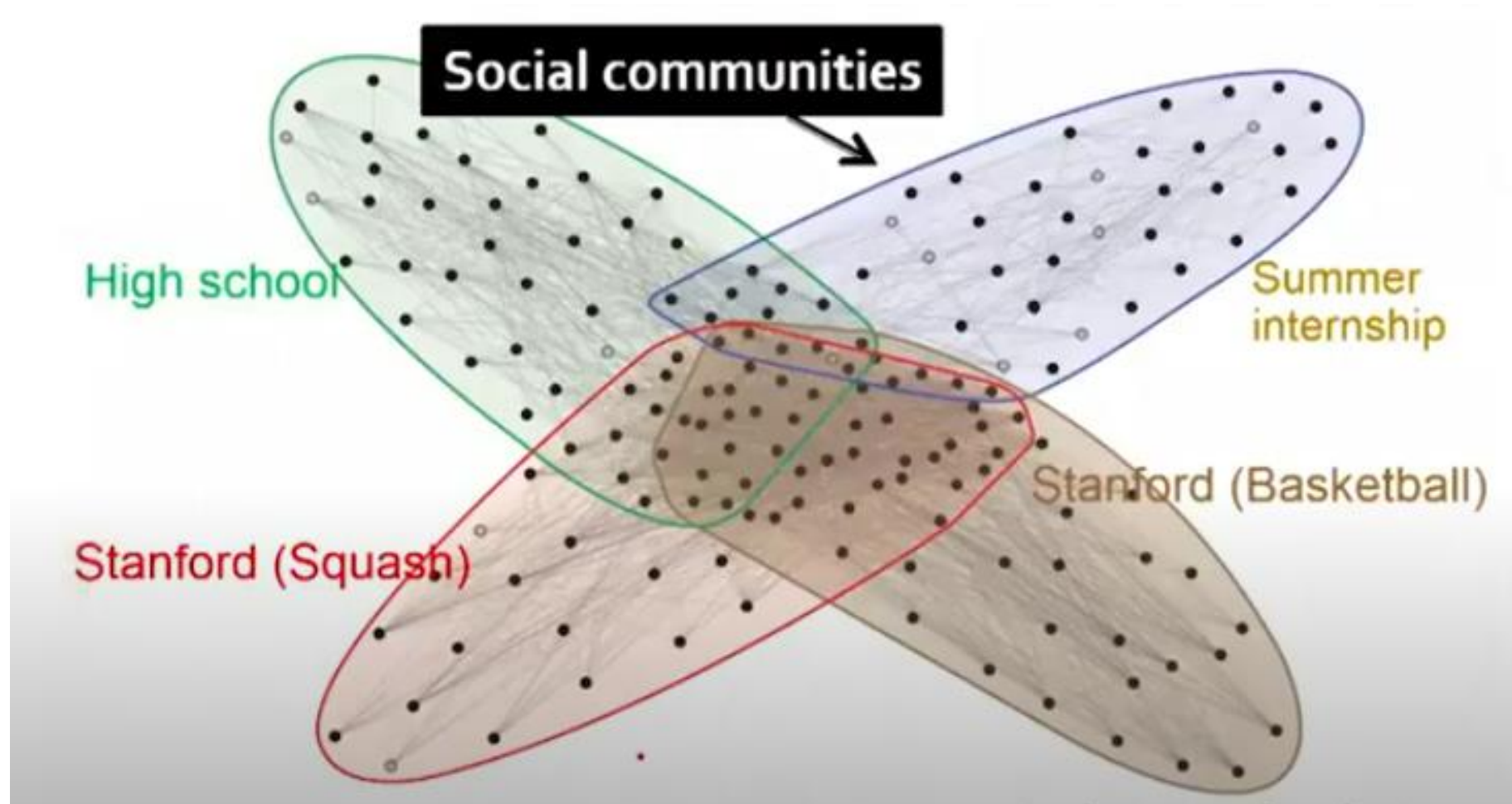
Why important: a signature of the hierarchical nature of complex systems

## Non-overlapping communities



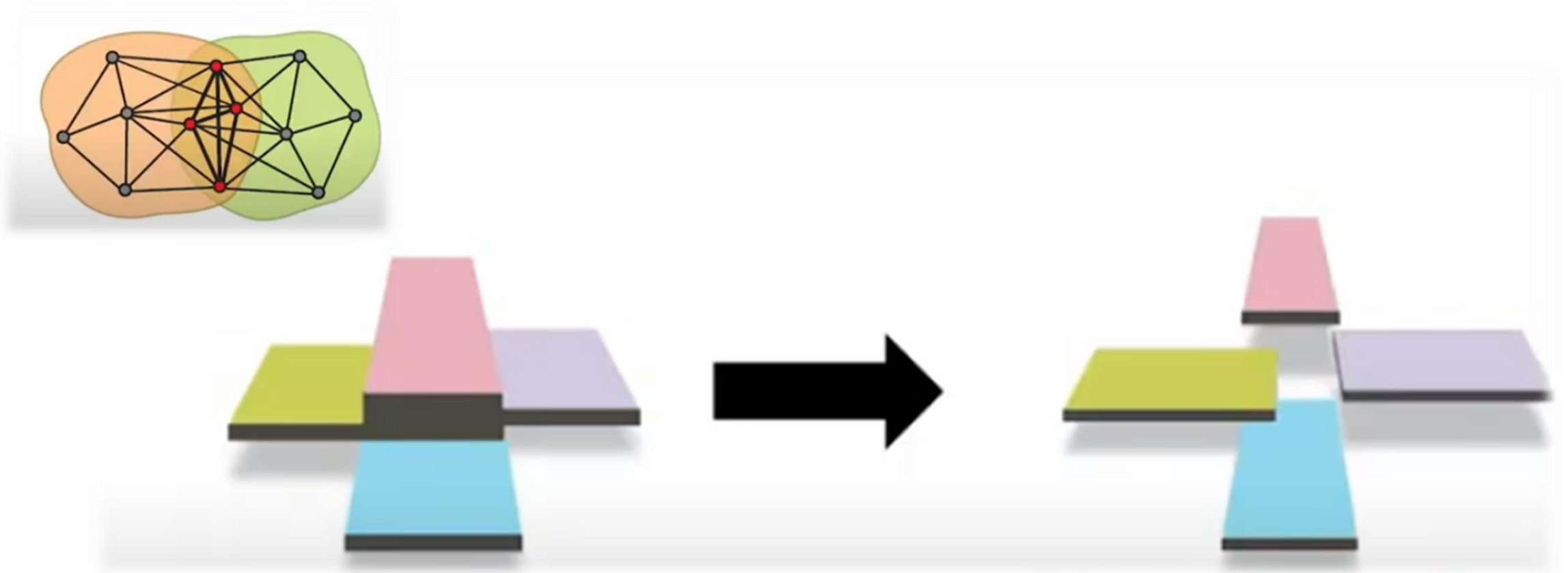


# Overlapping communities



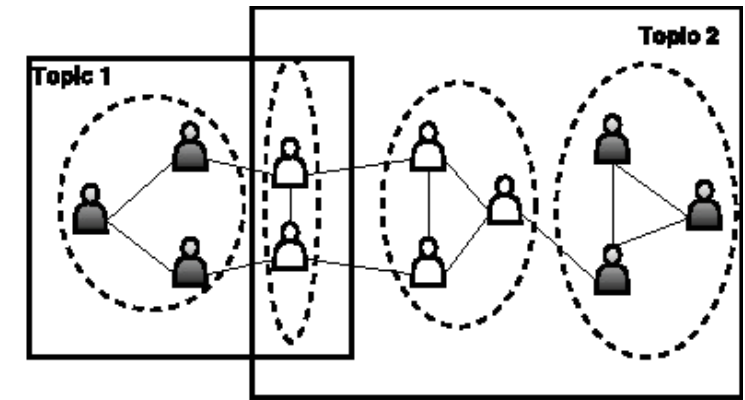
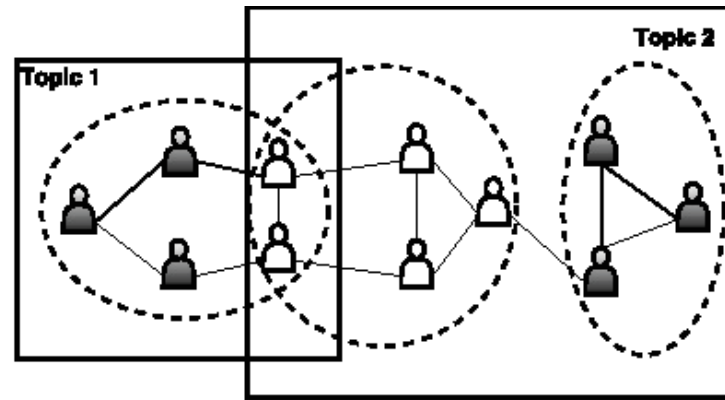
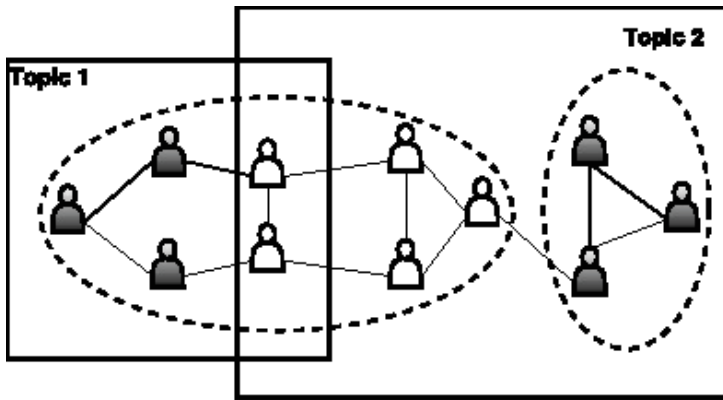
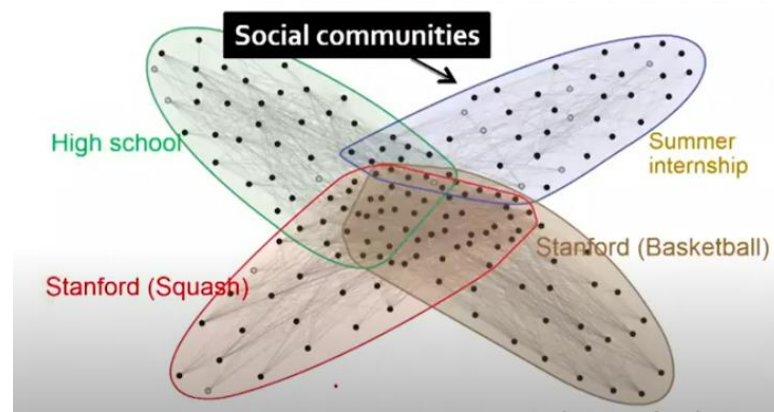
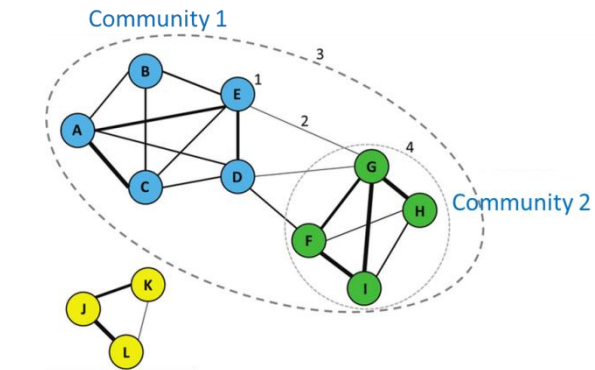
From Leskovec, Rajaraman and Ullman, Stanford University

# Community detection algorithms



“community over community”  
“tiles on top of tiles”

# You can use many criteria to design community detection algorithms



Only based on network structure

Network structure+ Topic

Network structure+ Topic+ Opinion



Negative opinion holder



Positive opinion holder

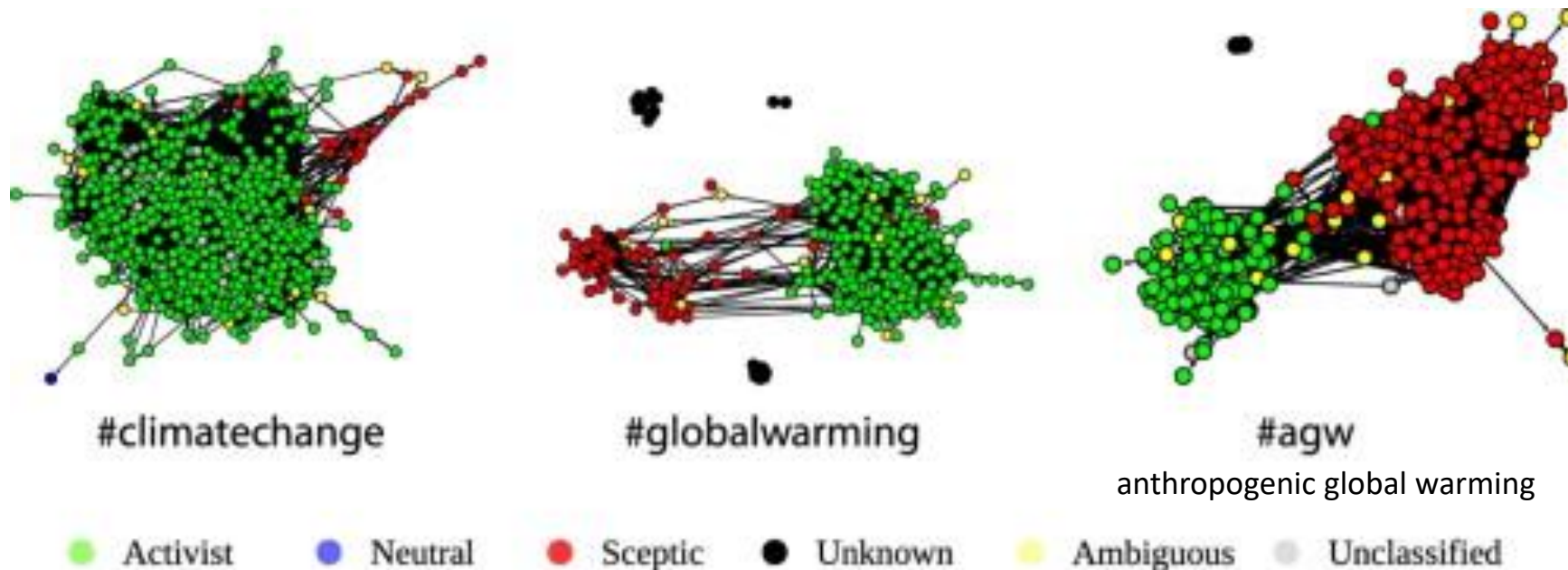
Common topics

Social communities

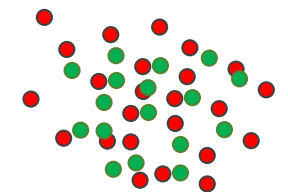
More: Behavior base community....

## Opinion-based communities: Echo chambers

Echo chamber: "an environment where a person only encounters information or opinions that reflect and reinforce their own." (you hear the same voice again and again...)



When there is no echo chamber effect:

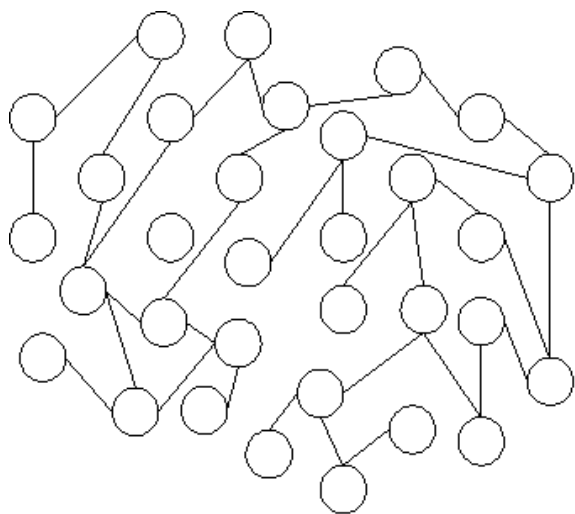


Others: polarization of opinion (pro-vaccination and anti-vaccination)

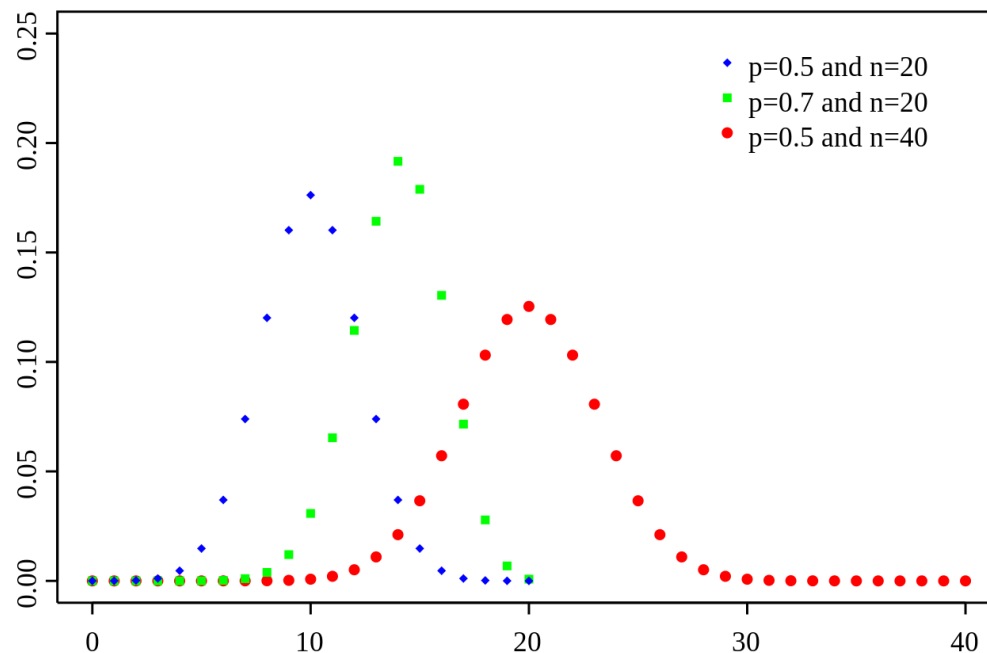
# Degree distribution

## How to summarize the degree of **all nodes of a network**--Degree distribution

The degree by nodes ( $d_i$ ) follow a distribution of  $\{(p_{k(i)}, d_i), i \in N\}$



Each of  $n$  nodes is independently connected (or not) with probability  $p$  (or  $1 - p$ ) (the Erdős-Rényi random graph)

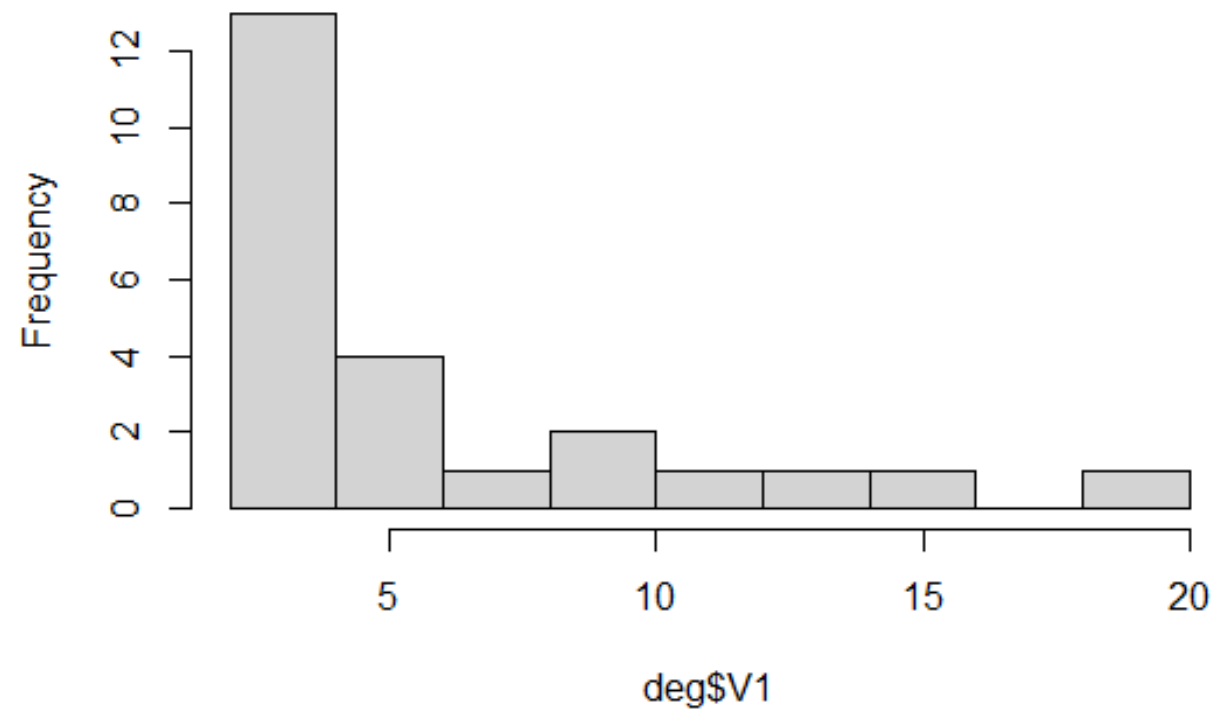


A binomial distribution

Does degree distribution of real-world social networks look like this?

# Degree distribution of class network of INFOMNWA-2021

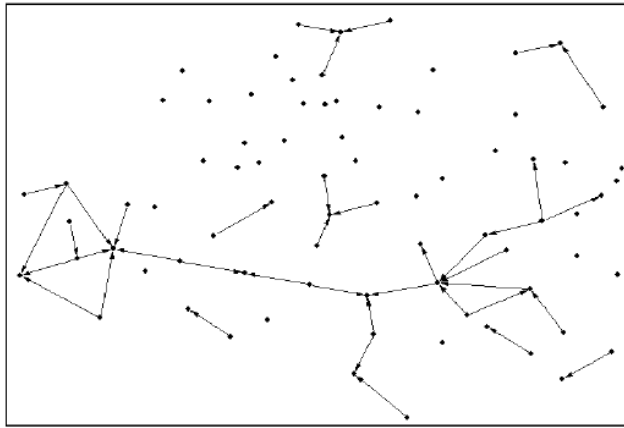
3. Name the people that you know in this class.



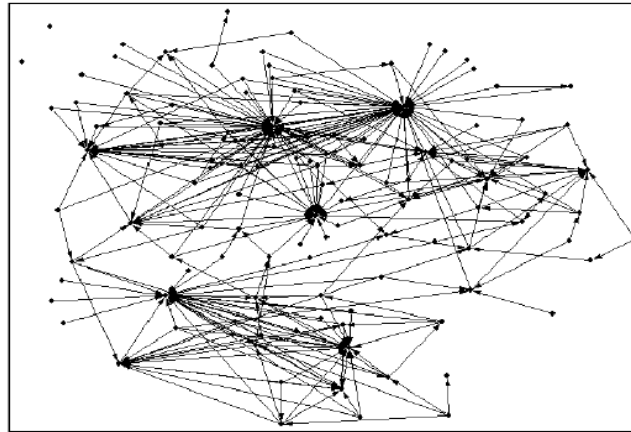
# Density of network: how well connected

The number of connections a network has, divided by the total possible connections a network could have  $\binom{n}{2} = n(n-1)/2$  possible unordered pairs of nodes

## Help With the Rice Harvest



Village 1



Village 2

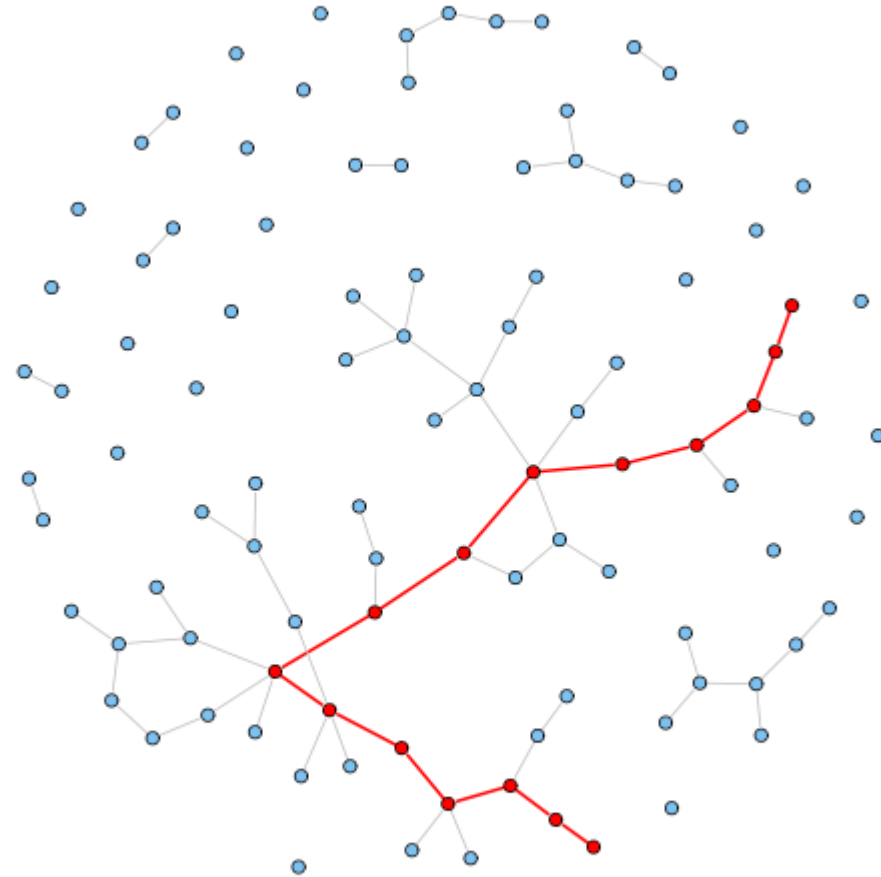
Which village has a higher density?

**The redundancy of connection is important.**

If there are many efficient paths connecting two actors, the odds are improved that a signal will get from one to the other.

# Diameter of network: how big it is

The longest of the shortest path  
between two nodes



14 or what? (~60)



# Clustering: The probability that your friends know each other

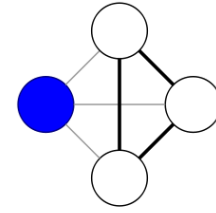
## (Transitivity)

**Local clustering coefficient** of a node in a graph quantifies how close its neighbours are to being a clique (complete graph)

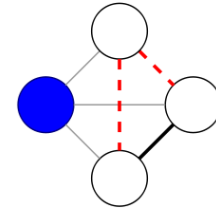
**Global clustering coefficient** counts the percentage of close triangles in the whole network.

### How connected are your friends?

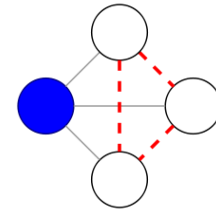
- If your “friends” all know each other, you have a high clustering coefficient. If your “friends” don’t know each other, then you have a low clustering coefficient and you need to introduce them to each other!



$$c = 1$$



$$c = 1/3$$

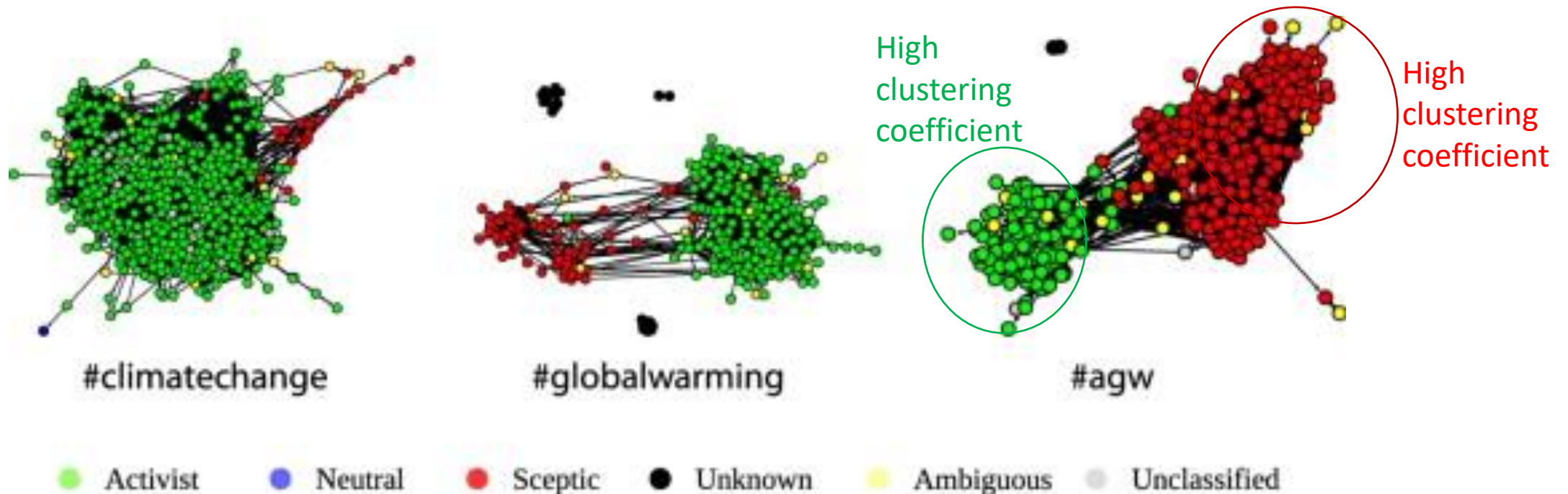


$$c = 0$$

## Echo chambers & clustering coefficient

People tend to know each other very well in a liked-mined communities

But which one is the cause ??

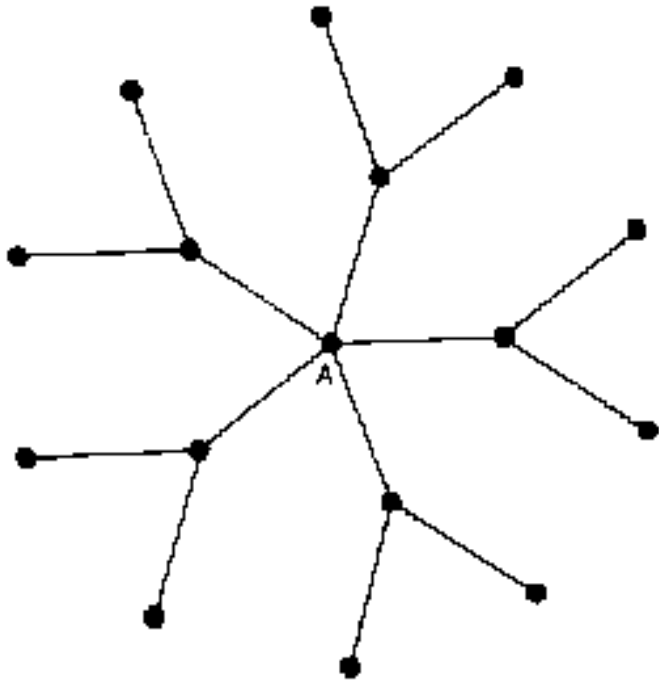


Hywel T.P. Williams et al., 2015. Network analysis reveals open forums and echo chambers in social media discussions of climate change. *Global Environmental Change*, 32, :126-138.

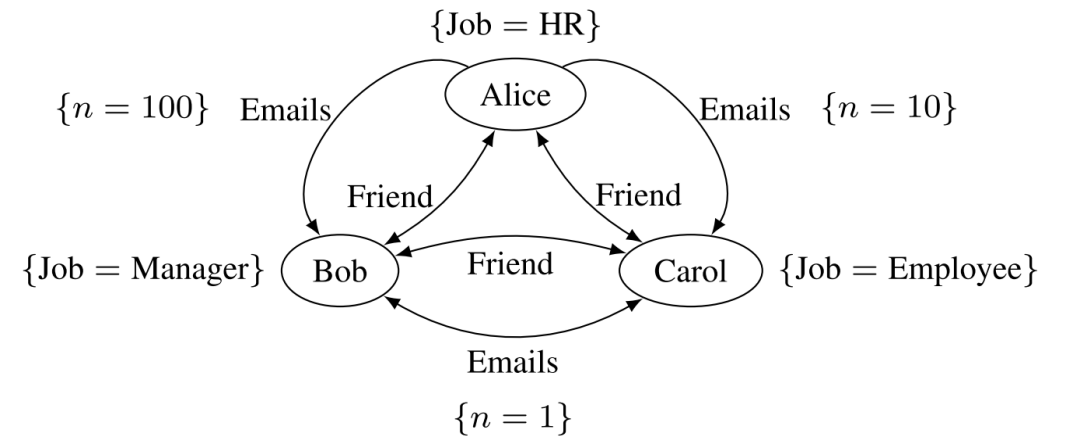
# Centralization: to which degree a network revolves around a single node

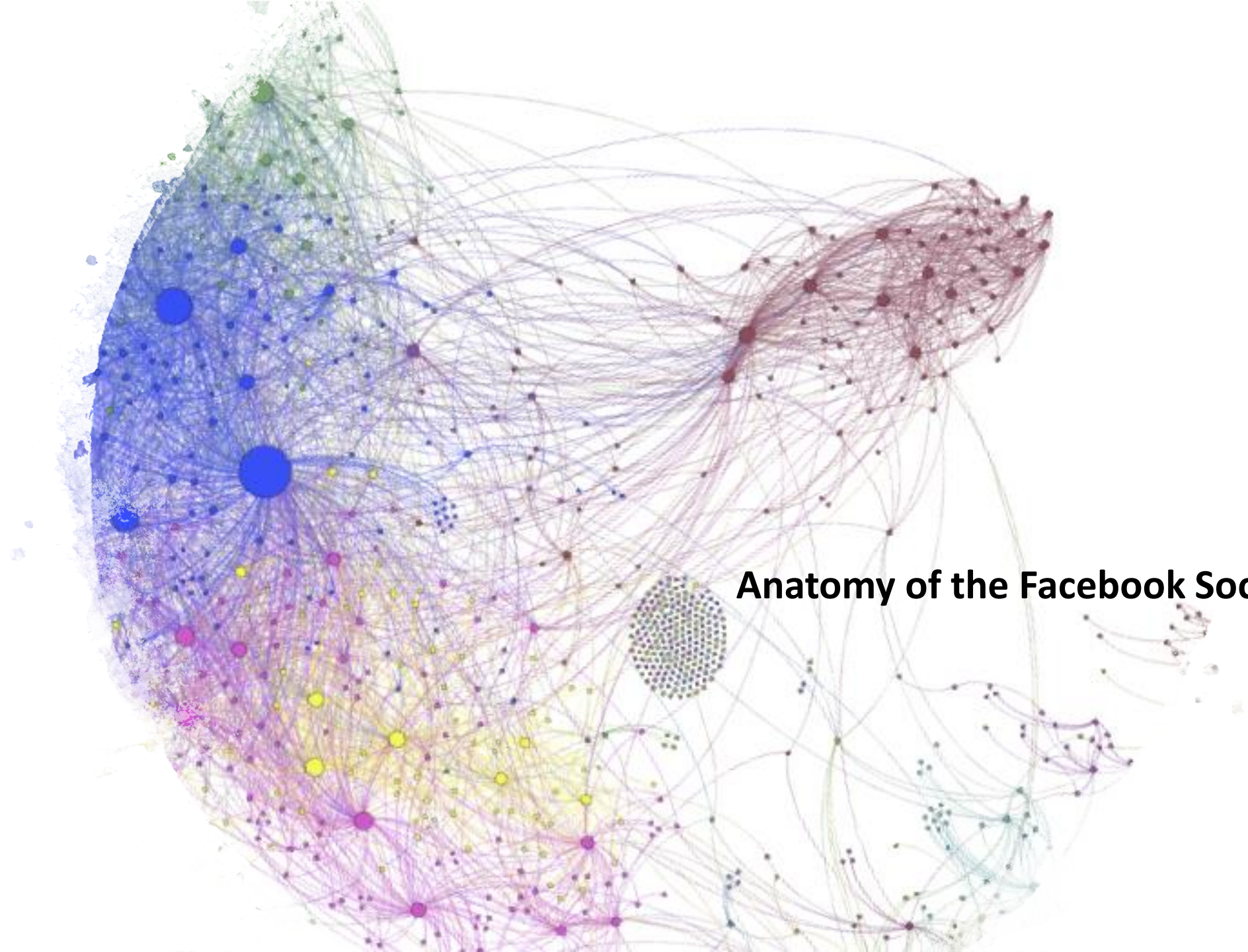
*Opinion leader; information controller*

*Which network is more centralized?*



*Think about nowadays news media...*



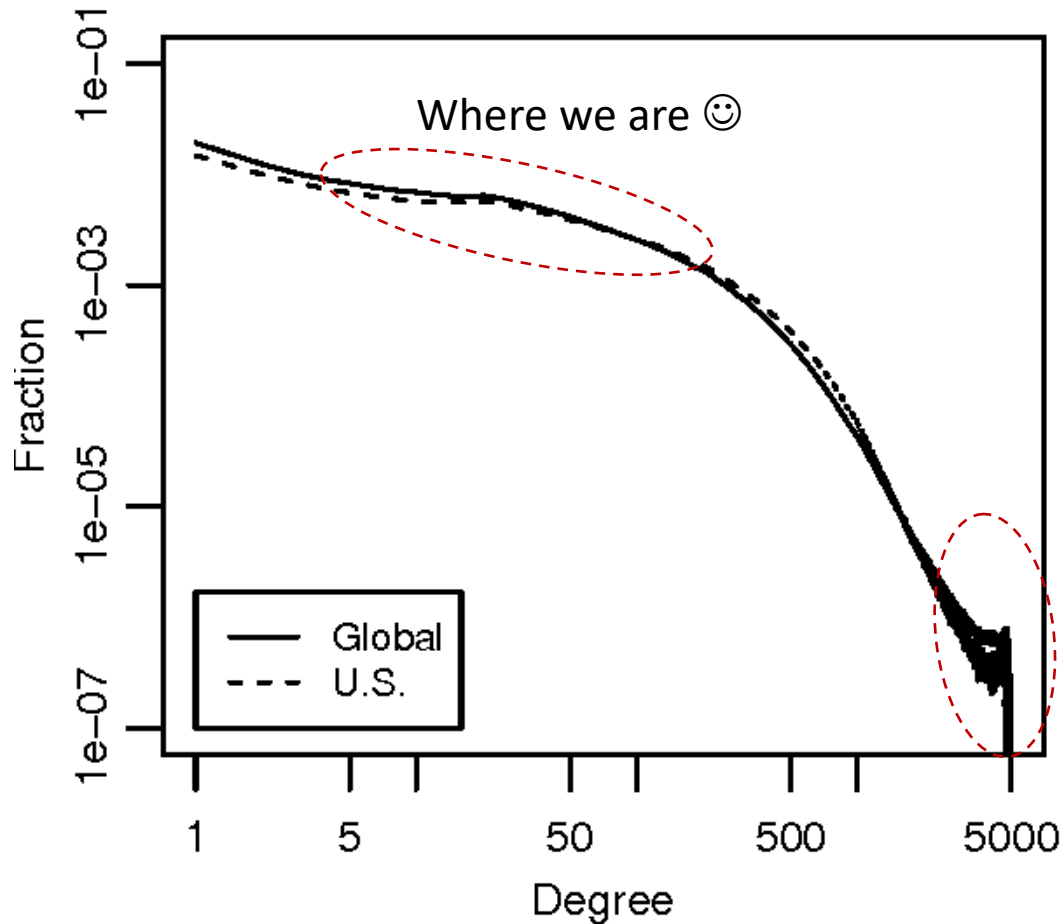


**Anatomy of the Facebook Social Network**

- $n = 721$  million active users in May 2011
- 68.7 billion friendship edges

World's population in 2011: 6.9 billion

### (1) degree distribution $p_k$



- Right-skewed with a high variance, but doesn't fit strict power-law distribution
- Nearly monotonically decreasing, except for a small anomaly near 20 friends. (Facebook encourage low friend count individuals to gain more friends until they reach 20 friends.)
- Most individuals have a moderate number of friends on Facebook, less than 200. (media=99)
- Small population of users with abnormally high degrees: *hubs*

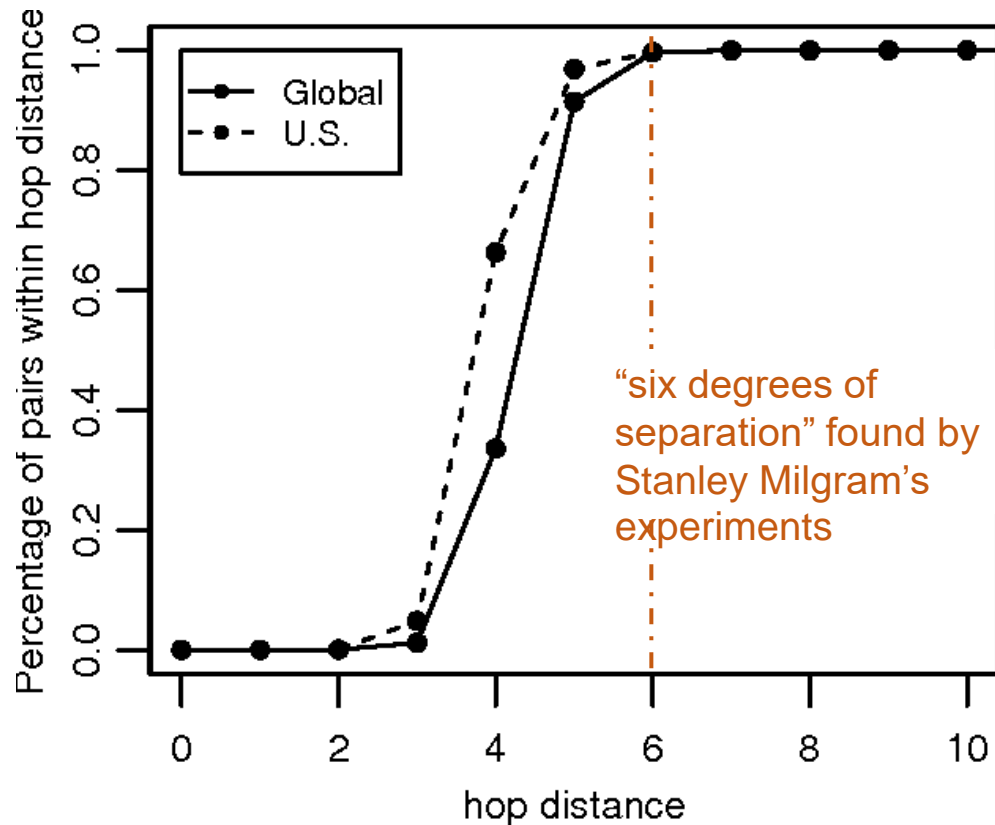


## (2) Path lengths

an extremal measure easily distorted by a single ill-connected path in some peripheral regions of the graph

**Diameter:** the maximum distance between any pair of vertices in the graph.

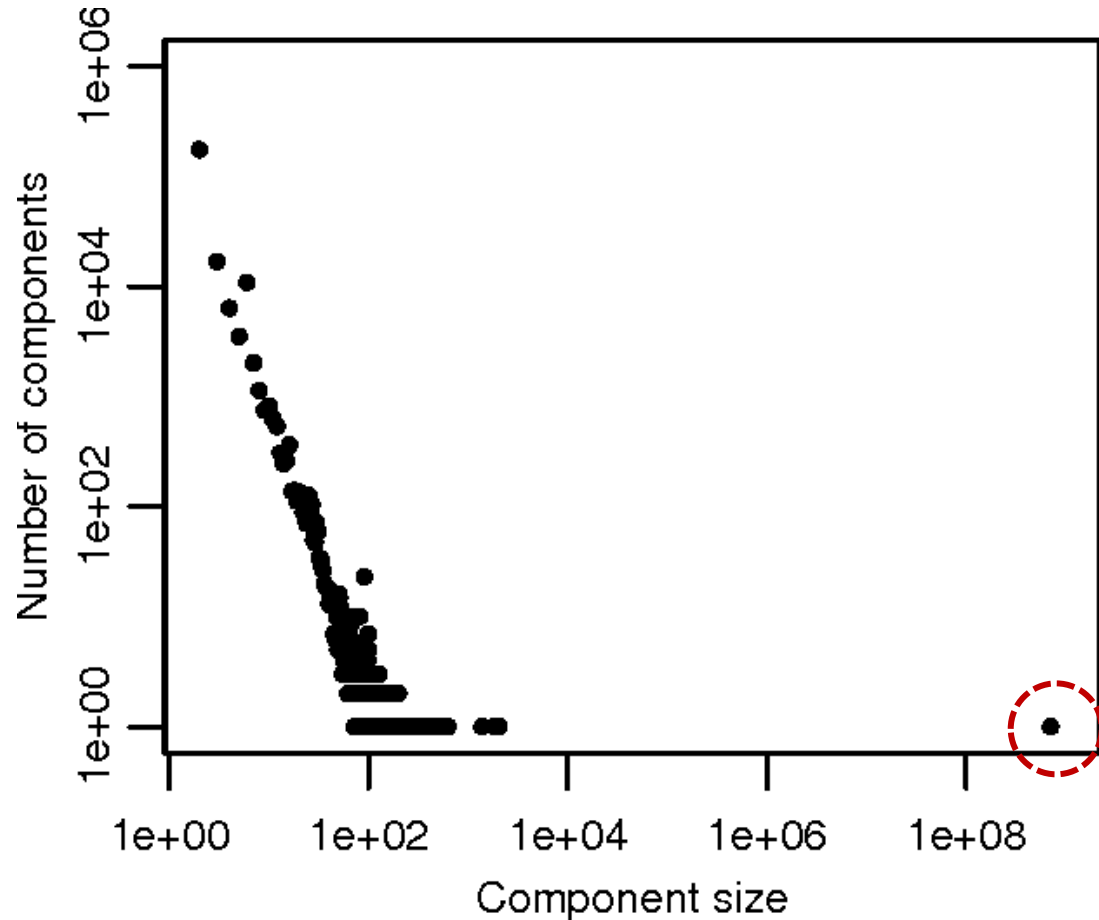
**Hop distance:** for a pair of vertices  $(u, v)$ ,  $u$  is reachable from  $v$  along a path in the network with  $h$  edges or less. (from the neighborhood function  $N(h)$ )



- The average distance between pairs of users was 4.7 for global users and 4.3 for U.S. users.
- 92% of all pairs of Facebook users were within five degrees of separation, and 99.6% were within six degrees.
- For only U.S. users, 96% were within five degrees and 99.7% were within six degrees.



### (3) Component size

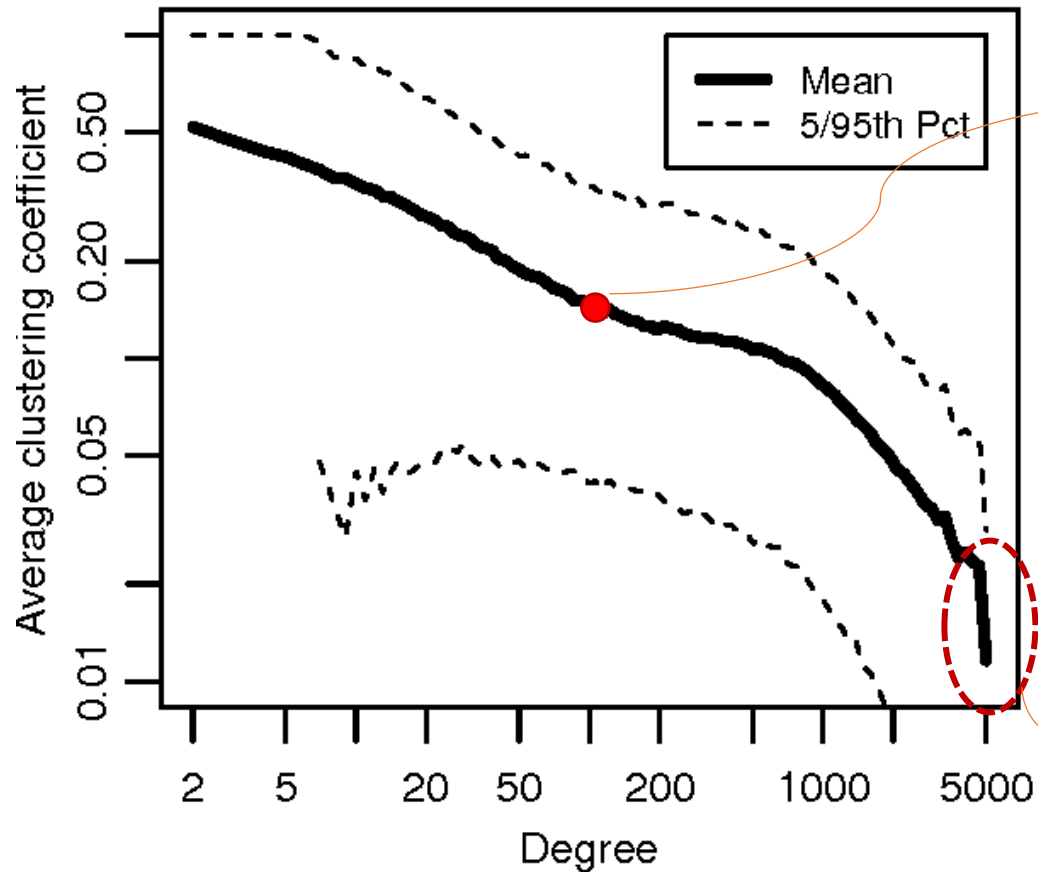


- There are many connected components, most of these components are extremely small.
- The second-largest connected component only has just over 2000 individuals
- The largest connected component, the outlier all the way on the right-hand side of the figure, consists of 99.91% percent of users.

*99.91% of individuals belonging to a single large connected component*

## (4) Local clustering coefficient

Average local clustering coefficient for users as a function of degree:

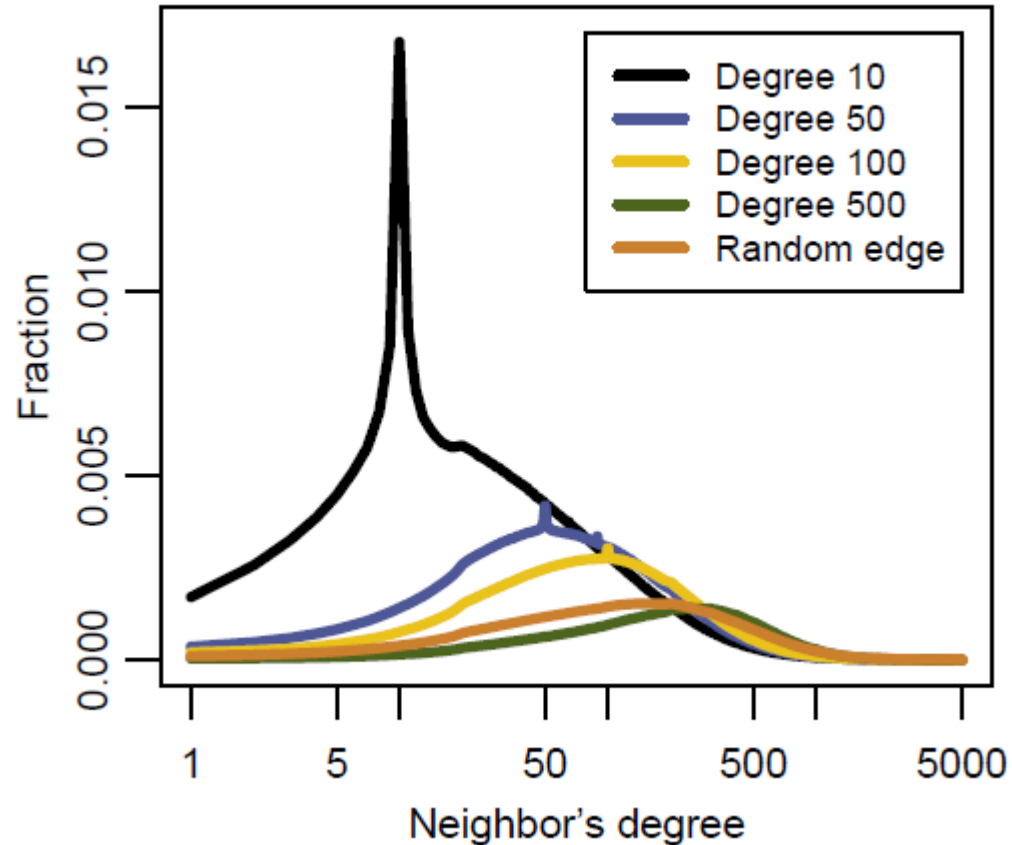


For users with 100 friends, the average local clustering coefficient is 0.14, indicating that for a median user, 14% of all their friend know each other.

The clustering coefficient drops rapidly for users with close to 5000 friends, indicating that these users are likely using Facebook for less coherently social purposes and friending users more indiscriminately.

>5 times the clustering coefficient for the graph of MSN messenger correspondences in the same neighborhood size

## (5) Friendship paradox in Facebook



The **friendship paradox**: a phenomenon first observed by the sociologist Scott L. Feld in 1991 that **most people have fewer friends than their friends have, on average.**

Facebook: 83.6% of users have less friends than the median friend count of their friends

What might be the application for marketing strategy?

Questions?

# Practicalities of the courses

- Group assignments/ Computer labs
- Individual assignments
- Exam

<div> <div>Day</div> <div>Week</div> <div>Month</div> <div>List</div> </div> <div> <div>April 2021</div> <div> <div>&lt;</div> <div>Today</div> <div>&gt;</div> </div> </div>				
week 13	Mon 29	Tue 30	Wed 31	Thu 1
			11:00 Network analysis - Lecture 01	
			Lecture 8	
week 14	5	6	7	8
			11:00 Network analysis - Lecture 01	11:00 Network analysis - Seminar 01
			15:15 Network analysis - Seminar 01	11:00 Network analysis - Seminar 02
			15:15 Network analysis - Seminar 02	11:00 Network analysis - Seminar 03
			15:15 Network analysis - Seminar 03	11:00 Network analysis - Seminar 04
			15:15 Network analysis - Seminar 04	
week 15	12	13	14	15
				15:15 Network analysis - Final result
				15:15 Network analysis - Final result
				15:15 Network analysis - Final result



Lecture 5: Social network and its measures



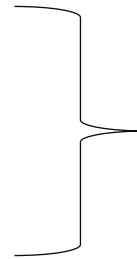
Ex1 in group assignment

Lecture 6: Network formation



Ex2 and bonus question in group assignment

Lecture 7: Simple and complex contagion



Ex3 in group assignment

Lecture 8: Influence manipulation