

Figure 1: Mallard and its thruster configuration. Arrows show forward force direction produced by each thruster (T_1, T_2, T_3 and T_4).

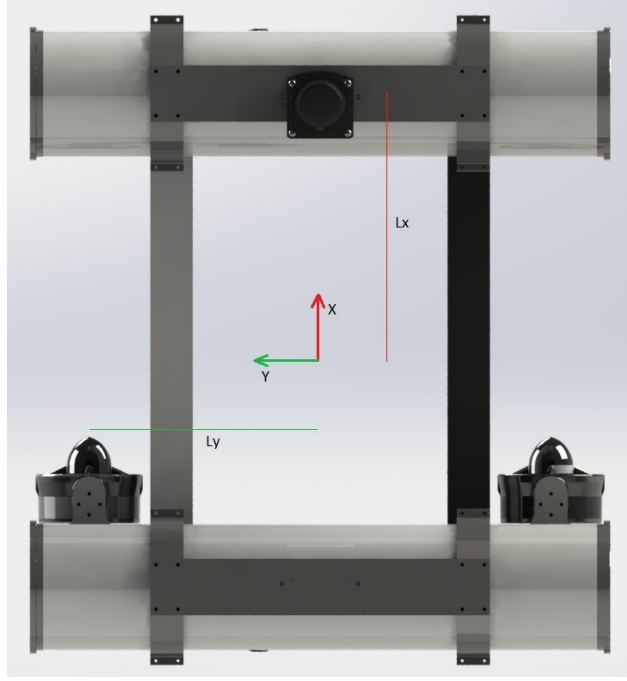


Figure 2: Top view. Moment arms L_x and L_y that are measured from the centre of Mallard, i.e. half the distance between thrusters.

$\boldsymbol{\tau} = [U \ V \ R]^T$ - velocity vector in body (Mallard's) reference frame

$\mathbf{u} = [T_1 \ T_2 \ T_3 \ T_4]^T$ - forces to be allocated for each thruster

L_x, L_y - moment arms

$$\begin{bmatrix} U \\ V \\ R \end{bmatrix} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ L_y & -L_y & L_x & -L_x \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \end{bmatrix} \quad (1)$$

$$\boldsymbol{\tau} = \mathbf{B} * \mathbf{u} \quad (2)$$

$$\mathbf{u} = \mathbf{B}^+ * \boldsymbol{\tau} \quad (3)$$

$$\begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \end{bmatrix} = \begin{bmatrix} 0.5 & 0 & a \\ 0.5 & 0 & -a \\ 0 & 0.5 & b \\ 0 & 0.5 & -b \end{bmatrix} \begin{bmatrix} U \\ V \\ R \end{bmatrix} \quad (4)$$