

Assignment 09

과제 정의

Build a binary classifier to classify digit 0 against all the other digits at MNIST dataset.

Let $x = (x_1, x_2, \dots, x_m)$ be a vector representing an image in the dataset.

The prediction function $f_w(x)$ is defined by the linear combination of data $(1, x)$ and the model parameter w :
 $f_w(x) = w_0 * 1 + w_1 * x_1 + w_2 * x_2 + \dots + w_m * x_m$ where $w = (w_0, w_1, \dots, w_m)$

The prediction function $f_w(x)$ should have the following values:

$$f_w(x) = +1 \text{ if } label(x) = 0$$

$$f_w(x) = -1 \text{ if } label(x) \neq 0$$

The optimal model parameter w is obtained by minimizing the following objective function: $\sum_i (f_w(x^{(i)}) - y^{(i)})^2$

1. Compute an optimal model parameter using the training dataset
2. Compute (1) True Positive, (2) False Positive, (3) True Negative, (4) False Negative based on the computed optimal model parameter using (1) training dataset and (2) testing dataset.

모듈 정의

```
In [23]: import numpy as np
import collections
```

1. Compute an optimal model parameter using the training dataset

```

In [40]: file_data    = "mnist_train.csv"
         handle_file = open(file_data, "r")
         data        = handle_file.readlines()
         handle_file.close()

         size_row     = 28      # height of the image
         size_col     = 28      # width of the image

         num_image    = len(data)
         count        = 0      # count for the number of images

         def normalize(data):
             data_normalized = (data - min(data)) / (max(data) - min(data))
             return(data_normalized)

         list_label    = np.empty(num_image, dtype=int)

         zero_data     = []
         zero_data_y   = []
         for line in data:
             line_data  = line.split(',')
             label       = line_data[0]
             im_vector  = np.asfarray(line_data[1:])
             im_vector  = normalize(im_vector)
             im_vector  = np.insert(im_vector, 0, 1)
             zero_data.append(im_vector)
             list_label[count] = label
             if label == '0':
                 zero_data_y.append(1.0);
             else:
                 zero_data_y.append(-1.0);
             count += 1

         xn = np.array(zero_data,dtype=float)
         yn = np.array(zero_data_y,dtype=float)
         X = np.dot(np.linalg.pinv(xn) , yn)
         print(X)

```

[-6.84406870e-01 1.02756547e-12 -2.53897628e-12 -1.43117440e-12
-8.09054705e-13 -1.00663532e-12 -2.86102582e-12 -1.32965371e-12
-7.89867287e-13 -1.49647371e-12 4.59362118e-13 7.43197493e-13
1.89601442e-12 1.53458664e-01 1.98220986e-01 -1.53345669e-01
-6.38940288e-03 4.47361378e-12 -1.15733488e-12 9.92574581e-13
6.00965476e-14 1.85045849e-12 1.29649017e-12 4.87411594e-15
2.31356154e-12 5.71223233e-14 -2.14432285e-12 2.01999570e-12
7.60771616e-13 -1.56596542e-13 9.99917224e-13 -2.31901119e-12
7.25859287e-15 -4.06289060e+00 1.05099744e+00 1.23101922e-01
2.11306669e-01 6.51508445e-02 2.55392530e-03 5.52498152e-02
1.15990558e-01 -7.23390275e-02 2.72683304e-01 -1.63118357e-01
6.19145739e-02 3.85382309e-05 7.70688345e-02 -6.15820985e-02
1.52778049e-02 8.53863822e-02 -1.41982541e-01 2.38270481e-01
3.58333722e-02 1.43063859e-12 -1.45557527e-12 -6.86825758e-12
2.23255856e-12 -3.05791426e-12 6.38880534e-12 -8.36059853e+00
9.77593181e+00 5.34144080e-01 -7.99936568e-01 -1.89682766e-01
1.01087544e-01 -5.27782579e-02 -8.17534204e-02 -7.48630136e-02
5.01256328e-02 -4.91614464e-02 -1.42921940e-02 -3.38311142e-02
3.52755065e-03 -1.10751292e-01 -2.59229330e-02 -4.38081127e-02
-4.70799587e-02 -9.88395498e-02 1.01588630e-01 -1.69319576e-01
1.03897289e-01 -2.46427687e-01 4.10216976e-01 -1.04092224e-12
-8.19159451e-14 -1.17258396e-12 -2.16587176e-12 3.95434813e+00
-1.79359733e+00 -8.68499683e-02 -8.20073230e-02 -6.32433515e-02
-1.82101353e-03 2.33142466e-02 -6.21453144e-02 -3.36839292e-02
5.46815877e-02 -5.94164193e-02 4.61485594e-02 -4.58733621e-02
-3.06237392e-02 -1.76278944e-02 -4.09481750e-02 -1.03436869e-01
-4.58517277e-02 -1.08105115e-01 -1.05007043e-01 -6.90997253e-02
-6.71496011e-02 1.07949793e-01 -1.11765369e-01 2.28174578e-01
2.03614652e-12 2.02997519e-13 6.18091090e-01 -2.88022934e-01
-5.60173775e-02 7.27680834e-02 -1.15032164e-02 -2.07682000e-02
-4.97472829e-02 3.72950169e-02 -4.34850573e-02 -2.24350027e-02
-2.82845323e-02 1.66644578e-03 3.06577987e-02 -3.48394437e-02
3.91208914e-02 -1.66416499e-02 3.82942676e-03 -2.43450472e-03
2.57119769e-02 -6.91423765e-03 2.78355493e-02 -2.46222020e-02
-6.62873397e-02 -6.42904228e-02 -3.59056314e-02 -2.42324348e-01
1.32591422e+00 -9.56015967e-13 1.37911216e-12 -9.18140767e-01
-7.59158102e-02 -1.37934055e-02 -4.03775682e-02 3.84716436e-02
-1.51256434e-02 -2.94318523e-02 -2.44712072e-02 -1.96691887e-02
9.80477629e-04 -2.24541051e-02 3.57542879e-02 1.15025008e-04
1.94593316e-02 9.74017026e-03 1.41481511e-02 -1.47587351e-02
1.89919848e-02 -2.54640490e-02 -1.82647686e-02 -5.10601180e-02
-6.28953006e-02 -2.35283865e-02 -2.87450168e-02 -1.11628448e-01
-8.97641357e-01 1.50028469e-12 -2.54615777e+00 1.77054232e-01
6.51639999e-03 1.89324682e-02 -2.88200629e-02 1.47532681e-02
-1.67811983e-02 1.85848674e-02 -2.69291781e-02 -2.21421420e-02
-1.06494634e-02 -1.71309113e-03 2.28669380e-02 2.94280678e-03
-5.01942060e-03 1.20090491e-02 -1.13210503e-03 1.50315298e-02
-1.38217775e-02 2.76423728e-03 1.92529974e-02 5.79218032e-03
-3.81634649e-02 -1.03944358e-01 -3.14676432e-02 -7.65759887e-02
-8.50549840e-02 -3.03249788e+01 -5.54541295e-02 -3.13129791e-01
4.15213998e-02 -1.29074041e-02 1.49939310e-02 -7.85612034e-03
4.49740552e-03 -2.59042120e-02 3.58688890e-02 -1.58589842e-02
1.42294856e-02 1.44020017e-02 1.37852173e-02 3.68645005e-02
3.21009183e-02 1.84545540e-03 3.82445587e-02 2.14842305e-02
1.88490310e-02 -2.09385855e-02 -7.04304552e-03 3.74623018e-03
-1.69926825e-02 -1.09216750e-01 -4.70023874e-02 -3.34857107e-02
1.18512098e-01 7.73735685e+00 7.99143648e-02 3.22226999e-02
-3.82070853e-02 -4.49128403e-03 -1.08295897e-02 3.77210140e-02
-1.01925718e-02 4.94795889e-03 -4.63040005e-03 1.23028027e-03
-1.29121106e-02 1.50728522e-02 4.12847137e-03 2.00257205e-02
1.81355516e-02 5.21674636e-02 1.40269931e-02 1.59614918e-02
9.93535240e-04 3.12223004e-02 -2.69868252e-02 1.21752778e-02
-7.24205297e-04 -1.22883530e-01 -1.26552514e-01 -2.67225984e-02
-7.38626850e-02 -6.27322344e-01 1.27248200e-01 -5.28187663e-02
4.45343641e-03 -1.71999311e-02 -1.74501373e-02 -2.30254058e-03

2.25724809e-02	1.17416898e-02	5.02298624e-03	1.09617011e-02
-1.80156042e-02	-6.30583859e-03	2.91698268e-02	2.58267363e-02
3.28687784e-02	4.22587482e-03	1.17818029e-02	8.77213799e-03
4.14944303e-02	1.05755469e-02	2.09568952e-02	-3.49942692e-02
2.64943604e-02	-3.32182580e-02	-2.19752946e-01	3.58305269e-03
-7.48816740e-02	4.18957867e-01	-2.18045061e-01	-6.24291898e-03
-2.11050407e-02	4.25264894e-03	2.24552106e-02	-1.20506272e-03
-1.36266811e-02	-1.63404825e-02	2.85703697e-02	-3.93904658e-03
1.09725370e-02	1.73111813e-02	9.11564016e-03	8.90299627e-03
3.04191955e-02	1.91257431e-02	3.60257052e-02	3.42702070e-02
7.87979252e-03	6.67227735e-02	3.30600147e-02	4.33365216e-02
7.53291073e-02	-7.62440689e-02	-2.23405116e-01	-1.68173775e-01
3.89237123e-01	-3.80811748e-01	2.97387609e-01	-5.61442283e-02
-3.43231122e-02	2.94597817e-03	-6.96512694e-02	8.98677407e-04
1.92926765e-02	1.03144421e-02	-1.29220519e-02	2.35269623e-02
1.45621788e-02	-2.05347095e-02	-1.51127791e-03	-4.22912417e-02
-2.55523189e-02	-2.08643574e-02	7.58496119e-04	9.88128237e-03
4.17800111e-02	2.00277180e-02	6.42581226e-02	1.47980509e-02
7.06556316e-02	1.07036530e-01	-3.40858900e-01	1.45597629e-02
-6.71918956e-01	1.33406797e-01	-2.36439043e-01	-7.46582387e-02
2.28924283e-02	-7.51003437e-02	-9.99749446e-03	1.87249191e-02
-1.54045077e-02	1.97633852e-02	9.56839230e-03	1.75595175e-02
-2.31656086e-02	1.47696624e-02	-1.09907080e-02	-7.64654750e-02
-2.89851250e-02	-4.27671985e-02	-3.35512445e-02	-3.72411965e-02
-2.87444652e-02	2.67571439e-02	1.62979898e-02	2.82561441e-02
1.28250228e-01	8.37250697e-02	-3.81218645e-02	-3.28052397e-01
7.05674148e-01	3.63110341e-01	7.10313597e-01	2.41499138e-02
-2.05539209e-03	-1.29324611e-02	-1.07866613e-02	-2.09651390e-02
1.95231675e-02	-2.23026408e-02	1.53915500e-02	1.00517438e-02
7.87008735e-03	-2.81797455e-02	-4.15333942e-02	-5.19998437e-02
-2.62643585e-02	-2.30192098e-02	-4.85780741e-02	-4.99575948e-02
-2.31449969e-02	-4.54315280e-02	1.83590882e-02	8.82262779e-02
7.19746907e-02	-9.63454256e-02	4.64711972e-04	1.18632499e-01
-4.11982927e-01	-3.35332957e-01	-4.34764244e-01	-6.17469782e-02
-6.03415505e-02	-1.38495558e-01	2.08704780e-02	3.93140973e-02
2.41313134e-02	1.45085147e-02	2.05524243e-02	5.01242979e-02
1.01364241e-04	-4.30134977e-02	5.17781332e-03	-6.97470077e-02
5.63711764e-03	-4.00069758e-02	-4.28528257e-02	-2.95278733e-02
-3.82561159e-02	1.85397753e-02	8.03620483e-02	3.46008304e-04
2.37996144e-02	2.94729437e-02	-5.23216875e-02	-5.90680735e-02
6.62195895e-01	-4.29210243e-01	2.52607443e-01	1.73402328e-02
-3.14452026e-02	4.84402580e-02	5.70984466e-02	-3.66184434e-02
3.51417996e-02	3.31553407e-02	3.73607626e-02	3.17000887e-02
-1.43734465e-02	-3.23869638e-02	-2.20822703e-02	-5.77931322e-02
-8.11349417e-03	-4.95793602e-02	-4.01245350e-02	-2.96377915e-02
-1.42454933e-02	3.16969883e-02	-5.00143928e-03	-1.38310361e-03
2.56643222e-02	-2.54677540e-02	-5.12622825e-02	-3.16903947e-02
1.48476771e-01	-1.82520546e+00	5.17803502e-02	3.00535671e-01
-2.36293327e-01	7.56630711e-03	1.00367779e-02	2.92923949e-02
6.97245018e-03	2.72067325e-02	9.55875478e-03	2.10924880e-02
-1.01636105e-02	-5.61730362e-02	-3.69367142e-02	-3.53812007e-02
-2.99457580e-02	-4.09076093e-02	-4.48277347e-02	-5.58197081e-03
1.54182004e-02	1.39168119e-02	1.06910131e-02	-5.47042901e-02
2.46556418e-02	2.35494096e-02	-1.27004520e-02	-6.38621386e-02
-4.25018506e-01	-1.88131377e-14	-1.29223160e-01	-1.87415458e-01
-2.74218442e-02	1.67616152e-02	2.42206933e-02	2.83859045e-02
2.48848750e-02	-4.18491369e-03	1.52699735e-02	1.68604462e-02
-1.50302662e-02	-1.44521357e-02	-4.43427204e-02	-5.59167160e-02
-4.79870056e-02	-1.81934611e-02	1.09120628e-02	9.09260197e-04
2.17567215e-02	-1.44962744e-02	-1.60245832e-02	5.41224889e-02
-2.42767738e-02	5.00929933e-03	-1.80489732e-02	1.65186943e-01
1.64785941e+00	-2.19509739e-01	-1.31617157e-01	2.54456139e-01
-2.36282055e-01	-4.86076891e-03	3.42595156e-02	-8.52251158e-03
4.06953455e-02	3.33248092e-02	3.99209311e-03	-7.80583438e-03
8.52431406e-03	-2.65320802e-02	-1.83140904e-02	-3.06411374e-02

2.91128260e-03	-1.30926158e-02	-1.13170294e-02	-1.43181116e-02
-1.24840887e-03	-2.74338544e-02	-5.38618589e-03	-6.68669799e-03
-7.08162299e-02	6.47336340e-02	-3.47759836e-02	-1.91659491e-01
-1.23578611e+00	-1.12312577e+00	2.42183248e-01	-9.17405306e-02
1.25022287e-02	-6.37620262e-03	-2.72170606e-02	1.56103307e-02
2.49191492e-02	1.22834419e-02	3.45549891e-02	-5.27491250e-03
1.81049784e-02	1.31972083e-02	1.15739178e-02	2.38121837e-03
-1.19633821e-02	-3.66833657e-03	2.28370791e-03	1.65742660e-05
-1.33416002e-02	7.12521178e-03	-8.66952595e-03	8.03540302e-04
1.28174931e-02	-1.80418601e-02	-5.29804019e-02	4.08863923e-02
8.58968333e-01	1.85006006e-13	9.90390513e-01	1.01516547e-01
-1.02853460e-01	-2.74799620e-02	1.71246672e-02	-1.59466059e-02
-4.41256562e-04	1.11776718e-02	1.64047290e-03	2.09760583e-02
5.39196690e-04	2.18820131e-02	1.26726631e-02	9.80587122e-05
6.68817542e-03	-2.57719503e-02	8.27967543e-03	-1.95479269e-02
1.78533707e-03	-1.86333285e-02	3.21933245e-02	-1.98862439e-02
-5.78130510e-02	8.28494936e-03	9.78974481e-02	-1.08752359e-01
-3.06954502e-01	3.58949236e-01	-1.03849184e+00	-3.07864377e-02
-6.31754505e-03	5.62501274e-02	-2.56597721e-02	-7.91721714e-03
-9.75980198e-03	-9.24629337e-03	2.74498536e-02	1.69854320e-02
2.12478202e-02	-7.89461426e-04	-1.25203659e-02	3.22711764e-03
2.68066041e-02	5.74733337e-03	-2.35661763e-02	6.23550517e-03
-8.57166899e-03	-3.89784316e-03	-1.61280583e-02	1.18028401e-02
-4.36724031e-02	2.19057467e-02	-1.08059735e-02	2.61187616e-01
5.74405642e-01	3.47732072e-01	-1.02562345e+00	-1.76792965e-02
9.90417699e-03	-1.16172693e-01	2.55762439e-02	3.26737750e-02
1.00548008e-02	5.54314170e-03	1.70297693e-02	2.79392902e-03
1.93708086e-02	1.47361004e-02	4.21844802e-02	1.08704349e-02
-1.52939597e-02	-6.02194830e-03	-5.77472198e-03	-3.49974095e-02
1.63384816e-02	-4.85612262e-02	2.03114851e-02	1.32151781e-02
-1.49572657e-02	1.82686709e-02	1.04598116e-02	3.54365368e-01
1.06044118e+00	-4.33731458e-14	-2.83209956e-14	1.25388339e-01
-2.30958457e-02	-5.88113771e-02	-1.84364883e-03	-6.04406353e-02
2.54449826e-02	-1.90813667e-02	1.31559119e-02	3.17327666e-03
2.14089830e-02	2.56670589e-02	3.40819846e-03	3.02783250e-02
3.78463391e-02	2.17140210e-02	2.12289652e-02	-1.79607760e-02
-2.20404529e-02	-1.11672821e-02	-5.30621084e-02	9.34300821e-03
1.83625686e-03	1.66758756e-02	-1.47400731e-01	-6.10764180e-01
4.03792916e-14	6.48449512e-15	4.25530518e-15	-6.74037263e-01
1.67844952e-01	2.25941586e-02	-8.85053906e-02	7.25145926e-02
-3.58382594e-02	5.00568473e-03	-2.72535815e-02	-4.91354993e-03
-4.56896716e-02	-1.39108544e-02	-1.80468775e-02	-3.17183546e-02
-1.37951641e-02	-4.01226467e-03	4.11089472e-03	3.87584387e-02
-8.91965524e-03	4.45736982e-02	3.25695059e-03	-1.01384643e-01
2.72593517e-02	-1.41423179e-01	2.49092543e-01	4.43747443e+00
-1.87988856e-14	4.01403062e-15	-1.03446502e-14	5.74024081e-01
7.10073769e-02	-1.14904287e-03	-1.36248522e-01	-5.52168592e-02
-1.05269463e-01	-5.52386399e-02	-4.80398149e-02	-6.66121557e-02
-2.69727298e-02	-6.47967538e-02	-3.07931417e-02	-4.40256645e-02
-1.10227227e-02	-3.02929742e-02	-3.42579844e-02	-2.18200615e-02
1.09956572e-02	-7.18229144e-02	8.45752821e-03	1.42200871e-01
-1.70038171e-01	-1.81931548e-01	-4.97548713e-01	-4.23939234e+00
0.00000000e+00	0.00000000e+00	0.00000000e+00	0.00000000e+00
-9.25135496e-01	2.61352157e-01	-2.06542730e-01	7.77944182e-03
-9.17599613e-02	-4.73427311e-02	-1.16567776e-01	-4.30764643e-02
-1.01269701e-01	-3.37441281e-02	-9.01871025e-02	-4.68745660e-02
-9.76980636e-02	-5.40824984e-02	-3.27357791e-02	-7.45309295e-02
-7.49540276e-03	8.34344478e-03	-1.55967392e-01	-6.34283335e-02
-2.63607005e-01	2.06109092e+00	-2.73970042e-01	0.00000000e+00
0.00000000e+00	0.00000000e+00	0.00000000e+00	0.00000000e+00
0.00000000e+00	8.04406795e-01	2.37610340e-02	-3.77192111e-01
6.07099203e-02	-1.29168168e-01	-1.13140632e-01	-3.49107977e-02
-1.77844159e-02	-1.36109932e-01	-7.60964262e-03	-1.35766440e-01
-2.44375949e-02	-4.33457087e-02	-1.14834013e-01	-4.48240493e-02
1.13894563e-02	-1.02555619e-01	1.83726663e-01	-3.49763778e-01

-2.08560473e+00 0.00000000e+00 0.00000000e+00 0.00000000e+00
0.00000000e+00]

2. Compute True Positive, False Positive, True Negative, False Negative based on the computed optimal model parameter using training dataset

```
In [41]: truthZeroCount = collections.Counter(list_label)[0]
truthNotZeroCount = len(list_label) - truthZeroCount
answerZeroCount_y = 0
answerZeroCount_n = 0
answerNotZeroCount_y = 0
answerNotZeroCount_n = 0

for x in range(len(xn)):
    value = np.dot(xn[x],X)
    if value >= 0.0:
        if list_label[x] == 0:
            answerZeroCount_y = answerZeroCount_y + 1
        else:
            answerZeroCount_n = answerZeroCount_n + 1
    else:
        if list_label[x] != 0:
            answerNotZeroCount_y = answerNotZeroCount_y + 1
        else:
            answerNotZeroCount_n = answerNotZeroCount_n + 1

TP = answerZeroCount_y/truthZeroCount
FP = answerZeroCount_n/truthNotZeroCount
FN = answerNotZeroCount_n/truthZeroCount
TN = answerNotZeroCount_y/truthNotZeroCount

print("TP : " + str(TP))
print("FP : " + str(FP))
print("FN : " + str(FN))
print("TN : " + str(TN))

TP : 0.8723619787269965
FP : 0.003310094864729922
FN : 0.12763802127300355
TN : 0.9966899051352701
```

2. Compute True Positive, False Positive, True Negative, False Negative based on the computed optimal model parameter using training dataset

```

In [42]: file_data    = "mnist_test.csv"
         handle_file = open(file_data, "r")
         data        = handle_file.readlines()
         handle_file.close()
         count = 0
         num_image   = len(data)
         list_label  = np.empty(num_image, dtype=int)
         zero_data = []
         for line in data:
             line_data = line.split(',')
             label      = line_data[0]
             im_vector  = np.asfarray(line_data[1:])
             im_vector  = normalize(im_vector)
             im_vector = np.insert(im_vector, 0, 1)
             zero_data.append(im_vector)
             list_label[count] = label
             count += 1
         xn = np.array(zero_data, dtype=float)

         truthZeroCount = collections.Counter(list_label)[0]
         truthNotZeroCount = len(list_label) - truthZeroCount
         answerZeroCount_y = 0
         answerZeroCount_n = 0
         answerNotZeroCount_y = 0
         answerNotZeroCount_n = 0

         for x in range(len(xn)):
             value = np.dot(xn[x], X)
             if value >= 0.0:
                 if list_label[x] == 0:
                     answerZeroCount_y = answerZeroCount_y + 1
                 else:
                     answerZeroCount_n = answerZeroCount_n + 1
             else:
                 if list_label[x] != 0:
                     answerNotZeroCount_y = answerNotZeroCount_y + 1
                 else:
                     answerNotZeroCount_n = answerNotZeroCount_n + 1

         TP = answerZeroCount_y/truthZeroCount
         FP = answerZeroCount_n/truthNotZeroCount
         FN = answerNotZeroCount_n/truthZeroCount
         TN = answerNotZeroCount_y/truthNotZeroCount

         print("TP : " + str(TP))
         print("FP : " + str(FP))
         print("FN : " + str(FN))
         print("TN : " + str(TN))

```

```

TP : 0.8836734693877552
FP : 0.004767184035476719
FN : 0.11632653061224489
TN : 0.9952328159645233

```

In []: