Adaptive LL(*) Parsing: The Power of Dynamic Analysis

Technical Report

Terence Parr University of San Francisco parrt@cs.usfca.edu Sam Harwell
University of Texas at Austin
samharwell@utexas.edu

Kathleen Fisher
Tufts University
kfisher@eecs.tufts.edu

Abstract

Despite the advances made by modern parsing strategies such as PEG, LL(*), GLR, and GLL, parsing is not a solved problem. Existing approaches suffer from a number of weaknesses, including difficulties supporting side-effecting embedded actions, slow and/or unpredictable performance, and counter-intuitive matching strategies. This paper introduces the ALL(*) parsing strategy that combines the simplicity, efficiency, and predictability of conventional top-down LL(k) parsers with the power of a GLR-like mechanism to make parsing decisions. The critical innovation is to move grammar analysis to parse-time, which lets ALL(*) handle any non-left-recursive context-free grammar. ALL(*) is $O(n^4)$ in theory but consistently performs linearly on grammars used in practice, outperforming general strategies such as GLL and GLR by orders of magnitude. ANTLR 4 generates ALL(*) parsers and supports direct left-recursion through grammar rewriting. Widespread ANTLR 4 use (5000 downloads/month in 2013) provides evidence that ALL(*) is effective for a wide variety of applications.

1. Introduction

Computer language parsing is still not a solved problem in practice, despite the sophistication of modern parsing strategies and long history of academic study. When machine resources were scarce, it made sense to force programmers to contort their grammars to fit the constraints of deterministic LALR(k) or LL(k) parser generators. As machine resources grew, researchers developed more powerful, but more costly, nondeterministic parsing strategies following both "bottom-up" (LR-style) and "top-down" (LL-style) approaches. Strategies include GLR [24], Parser Expression Grammar (PEG) [9], LL(*) [18] from ANTLR 3, and recently, GLL [23], a fully general top-down strategy.

Although these newer strategies are much easier to use than LALR(k) and LL(k) parser generators, they suffer from a variety of weaknesses. First, nondeterministic parsers sometimes have unanticipated behavior. GLL and GLR return multiple parse trees (forests) for ambiguous grammars because they were designed to handle natural language grammars, which are often intentionally ambiguous. For computer languages, ambiguity is almost always an error. One can certainly walk the constructed parse forest to disambiguate it, but that approach costs extra time, space, and machinery for the uncommon case. PEGs are unambiguous by definition but have a quirk where rule $A \rightarrow a \mid ab$ (meaning "A matches either a or ab") can never match ab since PEGs choose the first alternative that matches a prefix of the remaining input. Nested backtracking makes debugging PEGs difficult.

Second, side-effecting programmer-supplied actions (mutators) like print statements should be avoided in any strategy that continuously speculates (PEG) or supports multiple interpretations of the input (GLL and GLR) because the action may never really take place [16]. (Though DParser [22] supports "final" actions when the programmer is certain a reduction is part of an unambiguous final parse.) Without side effects, actions must buffer data for all interpretations in

immutable data structures or provide undo actions. The former mechanism is limited by memory size and the latter is not always easy or possible. The typical approach to avoiding mutators is to construct a parse tree for post-parse processing, but such artifacts fundamentally limit parsing to input files that fit in memory. Parsers that build parse trees cannot analyze large data files or infinite streams, such as network traffic, unless the input can be processed in logical chunks.

Third, our experiments (Section 7) show that GLL and GLR can be slow and unpredictable in time and space. Their complexities are, respectively, $O(n^3)$ and $O(n^{p+1})$ where p is the length of the longest production in the grammar [13]. (GLR is typically quoted as $O(n^3)$ because Kipps [14] gave such an algorithm, albeit with a constant so high as to be impractical.) In theory, general parsers should handle deterministic grammars in near-linear time. In practice, we found GLL and GLR to be ~135x slower than ALL(*) on a corpus of 12,920 Java source files (123M) and 6 orders of magnitude slower on a single 3.2M Java file, respectively.

LL(*) addresses these weaknesses by providing a mostly deterministic parsing strategy that uses regular expressions, represented as deterministic finite automata (DFA), to potentially examine the entire remaining input rather than the fixed k-sequences of LL(k). Using DFA for lookahead limits LL(*) decisions to distinguishing alternatives with regular lookahead languages, even though lookahead languages (set of all possible remaining input phrases) are often context-free. But the main problem is that the LL(*) grammar condition is statically undecidable and grammar analysis sometimes fails to find regular expressions that distinguish between alternative productions. ANTLR 3's static analysis detects and avoids potentially-undecidable situations, failing over to backtracking parsing decisions instead. This gives LL(*) the same $a \mid ab$ quirk as PEGs for such decisions. Backtracking decisions that choose the first matching alternative also cannot detect ambiguities such $A \to \alpha \mid \alpha$ where α is some sequence of grammar symbols that makes $\alpha \mid \alpha \text{ non-}LL(*)$.

1.1 Dynamic grammar analysis

In this paper, we introduce *Adaptive LL(*)*, or *ALL(*)*, parsers that combine the simplicity of deterministic top-down parsers with the power of a GLR-like mechanism to make parsing decisions. LL parsing suspends at each prediction decision point (nonterminal) and then resumes once the prediction mechanism has chosen the appropriate production to expand. The critical innovation is to move grammar analysis to parse-time; no static grammar analysis is needed. This choice lets us avoid the undecidability of static LL(*) grammar analysis and lets us generate correct parsers for any non-left-recursive context-free grammar (CFG). While static analysis must consider all possible input sequences, dynamic analysis need only consider one actual input sequence at a time.

The idea behind the *ALL(*)* prediction mechanism is to launch subparsers at a decision point, one per alternative production. The subparsers operate in pseudo-parallel to explore all possible paths. Subparsers die off as their paths fail to match the remaining input. The subparsers advance through the input in lockstep so analysis can declare a sole survivor at the minimum lookahead depth that uniquely predicts

¹ We use the term *deterministic* in the way that deterministic finite automata (*DFA*) differ from nondeterministic finite automata (*NFA*): The next symbol(s) uniquely determine action.

a production. If multiple subparsers merge back together or survive to reach the end of file, the predictor announces an ambiguity and resolves it in favor of the lowest production number associated with a surviving subparser. (Productions are numbered to express precedence as an automatic means of resolving ambiguities.) Programmers can also embed *semantic predicates* [20] to choose between ambiguous interpretations.

ALL(*) parsers memoize analysis results, incrementally and dynamically building up a cache of DFA that maps lookahead phrases to production numbers predicted for each decision. We use the term analysis in the sense that ALL(*) analysis yields lookahead DFA like static LL(*) analysis. The parser can make future predictions at the same parser decision and lookahead phrase quickly by consulting the cache. Unfamiliar input phrases trigger the grammar analysis mechanism, simultaneously predicting an alternative and updating the DFA. DFA are suitable for recording prediction results, despite the fact that lookahead languages at a given decision forms a context-free language. Dynamic analysis only needs to consider the finite context-free language subsets encountered during a parse and any finite set is regular.

To avoid the exponential nature of nondeterministic subparsers, prediction uses a *graph-structured stack* (GSS) [23] to avoid redundant computations. This is essentially the strategy GLR uses except that ALL(*) just predicts productions with subparsers whereas GLR actually parses with them. GLR must push terminals onto the GSS but ALL(*) does not. ALL(*) also makes decisions at the left edge of productions not the right edge like GLR.

ALL(*) parsers handle the mundane task of matching terminals and expanding nonterminals with the simplicity and O(n) speed of LL but have $O(n^4)$ theoretical time complexity because in the worst-case, the parser must make a prediction at each input symbol and each prediction must examine the entire remaining input; examining an input symbol can cost $O(n^2)$. $O(n^4)$ is in line with the complexity of GLR. In Section 9, we show that ALL(*) parsers for common languages are efficient and exhibit linear behavior in practice.

Parsers embedded in long-lived and multi-threaded applications such as servers and development environments benefit greatly from ALL(*) parsing. First, these parsers often see the same or similar input phrases and will, therefore, frequently get hits from the prediction cache. Consider a C compiler in a development environment that must constantly reparse the preprocessed output of header files such as stdio.h. Second, all instances of the same parser share a prediction cache so multiple threads can operate in parallel to speed construction of the lookahead DFA.

The advantages of ALL(*) stem from moving grammar analysis to parse time, but this choice places an additional burden on grammar functional testing. As with all dynamic approaches, programmers must cover as many grammar position and input sequence combinations as possible to find grammar ambiguities. Standard source code coverage tools can help programmers measure grammar coverage for ALL(*) parsers. High coverage in the generated code corresponds to high grammar coverage.

The ALL(*) algorithm is the foundation of the ANTLR 4 parser generator (ANTLR 3 is based upon LL(*)). ANTLR 4 was released in January 2013 and gets about 5000 downloads/month (source, binary, or ANTLRworks2 development environment). (Counting non-robot entries in web logs with unique IP addresses to get a lower bound.) Such activity provides evidence that ALL(*) is useful and usable.

The remainder of this paper is organized as follows. We begin by introducing the ANTLR 4 parser generator (Section 2) and discussing the *ALL(*)* parsing strategy (Section 3). Next, we define *predicated grammars* (Section 4) and their *augmented transition network* (Section 5) representation. Then, we describe *ALL(*)* grammar analysis and present the parsing algorithm itself (Section 6). Finally, we support our claims regarding *ALL(*)* efficiency (Section 7), give key *ALL(*)* theorems (Section 8), and examine related work (Section 9).

2. ANTLR 4

ANTLR 4 accepts as input any context-free grammar that does not contain indirect or hidden left-recursion (more on left-recursion below). From the grammar, ANTLR 4 generates a recursive-descent parser that uses an *ALL*(*) production prediction function (Section 3). ANTLR currently generates parsers in Java or C#. ANTLR 4 grammars use *yacc*-like syntax with extended BNF (EBNF) operators such as Kleene star (*) and token literals in single quotes. Grammars contain both lexical and syntactic rules in a combined specification for convenience. ANTLR 4 generates both a lexer and a parser from the combined specification. By using individual characters as input symbols, ANTLR 4 grammars can be scannerless and composable because *ALL*(*) languages are closed under union (Section 8), providing the benefits of modularity described by Grimm [10]. (We will henceforth refer to ANTLR 4 as ANTLR and explicitly mark earlier versions.)

Programmers can embed side-effecting actions (*mutators*), written in the host language of the parser, into the grammar. The actions have access to the current state of the entire parser. The parser ignores mutators during speculation to prevent actions from "launching missiles" speculatively. Actions typically extract information from the input stream and create data structures.

ANTLR also supports *semantic predicates*, which are arbitrary Boolean-valued expressions written in the host language that determine the semantic viability of a particular production. Semantic predicates that evaluate to false during the parse render the surrounding production nonviable, dynamically altering the language generated by the grammar at parse-time. Predicates significantly increase the strength of a parsing strategy because predicates can examine their surrounding context to provide an informal context-sensitive parsing capability. Semantic actions and predicates typically work together to alter the parse based upon previously-discovered information. For example, a C grammar could have embedded actions that define type symbols from constructs, such as typedef int i32;, and predicates to distinguish type names from other identifiers in future definitions like i32 x;.

Previous versions of ANTLR supported *syntactic predicates* [20], which are a form of arbitrary context-free lookahead implemented via backtracking. Syntactic predicates are given as grammar fragments that must match the upcoming input. The *LL(*)* parsing strategy of ANTLR 3 needs syntactic predicates to handle decisions where static grammar analysis fails and to specify precedence order. ANTLR does not support syntactic predicates since *ALL(*)* can handle all non-left-recursive grammars without backtracking; precedence is production-order-based by default (unless altered with semantic predicates).

2.1 Sample grammar

To illustrate ANTLR's yacc-like metalanguage, consider the ANTLR 4 grammar in Figure 1 for a simple programming language with assignment and expression statements terminated by semicolons. There are two grammar features that render this grammar non-LL(*) and, hence, unacceptable to ANTLR 3. First, rule expr is left recursive. ANTLR 4 automatically rewrites the rule to be non-left-recursive and unambiguous, as described in the next section. Second, the alternative productions of rule stat have a common recursive prefix (expr), which is sufficient to render stat undecidable from an LL(*) perspective. ANTLR 3 would detect recursion on the left edge of productions and fail over to a decision that backtracked at runtime.

Predicate {!enum_is_keyword}? in rule id allows or disallows enum as a valid identifier according to the expression value at the moment of prediction. When the predicate is false, the parser treats id as just id: ID; disallowing enum as an id as the lexer matches enum as a separate token from ID. This example demonstrates how predicates allow a single grammar to describe subsets or variations of the same language.

2.2 Left-recursion removal

The *ALL*(*) parsing strategy itself does not support left-recursion, but ANTLR supports direct left-recursion through grammar rewriting prior

Figure 1. Sample left-recursive ANTLR 4 predicated-grammar Ex

to parser generation. Direct left-recursion covers the most common cases, such as arithmetic expression productions, like $E \to E$. id , and C declarators. We made an engineering decision not to support indirect or hidden left-recursion because these forms are much less common and removing all left recursion can lead to exponentially-big transformed grammars. For example, the C11 language specification grammar contains lots of direct left-recursion but no indirect or hidden recursion. Indirectly left-recursive rules call themselves through another rule; e.g., $A \to B$, $B \to A$. Hidden left-recursion occurs when an empty production exposes left recursion; e.g., $A \to BA$, $B \to \epsilon$.

As an illustration, consider how ANTLR translates rule expr from Figure 1, inserting semantic predicates to resolve ambiguities according to the order of productions [2]:

ANTLR replaces expr references in other nonterminals with expr [0]. The predicates resolve ambiguities by comparing the precedence of the current operator to the precedence of the previous operator. An expansion of $\exp[pr]$ can match only those subexpressions whose precedence meets or exceeds pr.

3. Introduction to ALL(*) parsing

The strength of a top-down parsing strategy is related to how the strategy chooses which alternative production to expand for the current nonterminal. Unlike LL(k) and LL(*) parsers, ALL(*) parsers always choose the alternative that leads to a valid parse. All non-left-recursive grammars are therefore ALL(*).

Instead of relying on static grammar analysis, an ALL(*) parser adapts to the input sentences presented to it at parse-time. The parser analyzes the current decision point (nonterminal with multiple productions) using a GLR-like mechanism to explore all possible decision paths with respect to the current "call" stack and the remaining input *on-demand*. The parser incrementally and dynamically builds a lookahead DFA per decision that records a mapping from lookahead sequence to predicted production number. If the DFA constructed to date matches the current lookahead, the parser can skip analysis and immediately expand the predicted alternative. Experiments in Section 7 show that ALL(*) parsers get DFA cache hits most of the time and that DFA are critical to performance.

Because ALL(*) differs from deterministic top-down methods only in the prediction mechanism, we can construct conventional recursive-descent LL parsers but with an important twist. ALL(*) parsers call a special prediction function, adaptivePredict, that analyzes the grammar to construct lookahead DFA instead of simply comparing the lookahead to a statically-computed token set. Function adaptivePredict takes a nonterminal (decision) and parser call stack as parameters and returns the predicted production number or throws an exception if there is no viable production. For example, rule stat from the example in Section 2.1 yields a parsing procedure similar to Figure 2.

```
void stat() { // parse according to rule stat
    switch (adaptivePredict("stat", callStack)) {
    case 1 : // predict production I
        expr(); match('='); expr(); match(';');
        break;
    case 2 : // predict production 2
        expr(); match(';'); break;
    }
}
```

Figure 2. Recursive-descent code for stat in grammar Ex

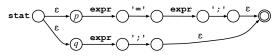


Figure 3. ATN for ANTLR rule stat in grammar Ex

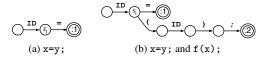


Figure 4. Prediction DFA for decision stat

ALL(*) prediction has a structure similar to the well-known NFAto-DFA subset construction algorithm. The goal is to discover the set of "execution" states the parser could reach after having seen some or all of the remaining input relative to the current decision. As in subset construction, an ALL(*) DFA state is the set of parser configurations possible after matching the input leading to that state. Instead of an NFA, ALL(*) simulates the actions of an augmented recursive transition network (ATN) [25] representation of the grammar because ATNs closely mirror grammar structure. (ATNs look just like syntax diagrams that can have actions and semantic predicates.) LL(*)'s static analysis also operates on an ATN for the same reason. Figure 3 shows the ATN submachine for rule stat. An ATN configuration represents the execution state of a subparser and tracks the ATN state, predicted production number, and ATN call stack. The configuration includes the predicted production so it can guide parsing rather than simply answer whether a lookahead sequence is valid. Unlike static LL(*) analysis, ALL(*) incrementally builds DFA considering just the lookahead sequences it has seen instead of all possible sequences.

When parsing reaches a decision for the first time, adaptivePredict initializes the lookahead DFA for that decision by creating a DFA start state. Start state construction begins by launching subparsers at production left edges. For example, the start state for nonterminal stat in Figure 3 initializes subparsers with ATN configurations (p, 1, [])and (q, 2, []) where p and q are production 1 and 2's left edges and is the empty parser call stack (stat is the start symbol). Analysis then computes a new DFA state indicating where ATN simulation could reach after consuming the first lookahead symbol and connects the two DFA states with an edge labeled with that symbol. Analysis continues, adding new DFA states, until all ATN configurations in a newly-created DFA state predict the same production. Function adaptivePredict marks that state as an accept state and returns to the parser with that production number. Figure 4a shows the lookahead DFA for decision stat after adaptivePredict has analyzed input sentence x=y;. The DFA stops after seeing = because = is sufficient to uniquely predict the first alternative. (Notation: 1 means "predict production 1.")

In the typical case, adaptivePredict finds an existing DFA for a particular decision. The goal is to find or build a path through the DFA to an accept state. If adaptivePredict reaches a (non-accept) DFA state without an edge for the current lookahead symbol, it switches to ATN simulation to extend the DFA (without rewinding the input). For example, to analyze a second input phrase for stat such as f(x);, adaptivePredict finds an existing ID edge from the start state and jumps to s_1 without ATN simulation. There is no existing edge from s_1 for the left parenthesis so analysis simulates the ATN to complete a path to an accept state predicting the second production, as shown in Fig-

ure 4b. Note that because sequence ID(ID) predicts both productions, analysis continues until the DFA has edges for the = or; symbols.

If ATN simulation computes a new target state that already exists in the DFA, simulation adds a new edge targeting the existing state and switches back to DFA simulation mode starting at that state. Targeting existing states is how cycles can appear in the DFA. Extending the DFA to handle unfamiliar phrases empirically decreases the likelihood of future ATN simulation, thereby increasing parsing speed (Section 7).

3.1 Predictions sensitive to the call stack

Parsers cannot always rely upon lookahead DFA to make correct decisions. To handle all non-left-recursive grammars, ALL(*) prediction must occasionally consider the parser call stack available at the start of prediction (denoted γ_0 in Section 6.1). To illustrate stack-sensitive predictions, consider that predictions made while recognizing a Java method definition might depend on whether the method was defined within an interface or class definition. (Java interface methods cannot have bodies.) Here is a simplified grammar that exhibits a stack-sensitive decision in nonterminal A:

$$S \to xB \mid yC \quad B \to Aa \quad C \to Aba \quad A \to b \mid \epsilon$$

Without the parser stack, no amount of lookahead can uniquely distinguish between A's productions. Lookahead ba predicts $A \to b$ when B invokes A but predicts $A \to \epsilon$ when C invokes A. If prediction ignores the parser call stack, there is a prediction conflict upon ba.

Parsers that ignore the parser call stack for prediction are called $Strong\ LL\ (SLL)$ parsers. The recursive-descent parsers programmers build by hand are in the SLL class. By convention, the literature refers to SLL as LL but we distinguish the terms since "real" LL is needed to handle all grammars. The above grammar is LL(2) but not SLL(k) for any k, though duplicating A for each call site renders the grammar SLL(2). ALL(*) must consider the parser stack during prediction to handle every non-left-recursive grammar.

Creating a different lookahead DFA for each possible parser call stack is not feasible since the number of stack permutations is exponential in the stack depth. Instead, we take advantage of the fact that most decisions are not stack-sensitive and build lookahead DFA ignoring the parser call stack. If SLL ATN simulation finds a prediction conflict (Section 6.4), it cannot be sure if the lookahead phrase is ambiguous or stack-sensitive. In this case, adaptivePredict must re-examine the lookahead using the parser stack γ_0 .

This hybrid or "optimized *LL* mode" improves performance by caching stack-insensitive prediction results in lookahead DFA when possible while retaining full stack-sensitive prediction power. Optimized *LL* mode applies on a per-decision basis, but *two-stage parsing*, described next, can often avoid *LL* simulation completely. (In the remainder we use *SLL* to indicate stack-insensitive parsing and *LL* to indicate stack-sensitive.)

3.2 Two-stage *ALL*(*) parsing

SLL is weaker but faster than LL. Since we have found that most decisions are SLL in practice, it makes sense to attempt parsing entire inputs in "SLL only mode." Without having to consider the call stack, ALL(*) can augment the lookahead DFA to continuously improve prediction performance. If, however, SLL mode finds a syntax error, it might have found an SLL weakness or a real syntax error, so we have to retry the entire input using optimized LL mode, as described in the previous section. This counterintuitive strategy, which potentially parses entire inputs twice, can dramatically increase speed over a single optimized LL mode stage. For example, two-stage parsing with the Java grammar (Section 7) is 8x faster than one-stage optimized LL mode to parse a 123M corpus. This two-stage strategy relies on the fact that SLL either behaves like LL or gets a syntax error (Theorem 8.3). For invalid sentences, there is no derivation for the input regardless of how the parser chooses productions. For valid sentences, SLL chooses productions as LL would or picks a production that ultimately leads to a syntax error (LL finds that choice nonviable). Even in the presence of ambiguities, SLL often resolves conflicts as LL would. For example,

despite a few ambiguities in our Java grammar, *SLL* mode correctly parses all inputs we have tried without failing over to *LL*. Nonetheless, the second (*LL*) stage must remain to ensure correctness.

3.3 Lexical analysis with ALL(*)

Because of the DFA prediction cache, ALL(*) is fast enough to handle lexing (tokenizing) as well as parsing. ANTLR uses a variation of ALL(*) for lexing that fully matches tokens instead of just predicting productions like ALL(*) parsers do. After warm-up, the lexer will have built a DFA similar to what regular-expression based tools such as lex would create statically. The key difference is that ALL(*) lexers are predicated context-free grammars not just regular expressions so they can recognize context-free tokens such as nested comments and can gate tokens in and out according to semantic context.

ALL(*) is also suitable for scannerless parsing because of its recognition power, which comes in handy for context-sensitive lexical problems like merging C and SQL into a single language. Such a union has no clear lexical sentinels demarcating lexical regions:

```
int next = select ID from users where name='Raj'+1;
int from = 1, select = 2;
int x = select * from;
```

See grammar code/extras/CSQL in [?] for a proof of concept.

4. Predicated grammars

To describe ALL(*) parsing, we first need to formally define the predicated grammars from which they are derived. A predicated grammar $G = (N, T, P, S, \Pi, \mathcal{M})$ has elements:

- N is the set of nonterminals (rule names)
- T is the set of terminals (tokens)
- P is the set of productions
- $S \in N$ is the start symbol
- \bullet Π is a set of side-effect-free semantic predicates
- M is a set of actions (mutators)

Predicated ALL(*) grammars differ from those of LL(*) [18] only in that ALL(*) grammars do not need or support syntactic predicates. Predicated grammars in the formal sections of this paper use the notation shown in Figure 5. The derivation rules in Figure 6 define the meaning of a predicated grammar. To support semantic predicates and mutators, the rules reference state \mathbb{S} , which abstracts user state during parsing. The judgment form $(\mathbb{S},\alpha) \Rightarrow (\mathbb{S}',\beta)$ may be read: "In machine state \mathbb{S} , grammar sequence α reduces in one step to modified state \mathbb{S}' and grammar sequence β ." The judgment $(\mathbb{S},\alpha) \Rightarrow^* (\mathbb{S}',\beta)$ denotes repeated applications of the one-step reduction rule. These reduction rules specify a leftmost derivation. A production with a semantic predicate π_i is viable only if π_i is true of the current state \mathbb{S} . Finally, an action production uses the specified mutator μ_i to update the state.

Formally, the language generated by grammar sequence α is $L(\mathbb{S},\alpha)=\{w\,|\,(\mathbb{S},\alpha)\Rightarrow^*(\mathbb{S}',w)\}$ and the language of grammar G is $L(\mathbb{S}_0,G)=\{w\,|\,(\mathbb{S}_0,S)\Rightarrow^*(\mathbb{S},w)\}$ for initial user state \mathbb{S}_0 (\mathbb{S}_0 can be empty). If u is a prefix of w or equal to w, we write $u\preceq w$. Language L is ALL(*) iff there exists an ALL(*) grammar for L. Theoretically, the language class of L(G) is recursively enumerable because each mutator could be a Turing machine. In practice, grammar writers do not use this generality so we consider the language class to be the context-sensitive languages instead. The class is context-sensitive rather than context-free because predicates can examine the call stack and terminals to the left and right.

This formalism has various syntactic restrictions not present in actual ANTLR grammars, for example, forcing mutators into their own rules and disallowing the common Extended BNF (EBNF) notation such as α^* and α^+ closures. We can make these restrictions without loss of generality because any grammar in the general form can be translated into this more restricted form.

4.1 Resolving ambiguity

An ambiguous grammar is one in which the same input sequence may be recognized in multiple ways. The rules in Figure 6 do not preclude

$A \in N$	Nonterminal
$a, b, c, d \in T$	Terminal
$X \in (N \cup T)$	Production element
$\alpha, \beta, \delta \in X^*$	Sequence of grammar symbols
$u,v,w,x,y\in T^*$	Sequence of terminals
ϵ	Empty string
\$	End of file "symbol"
$\pi \in \Pi$	Predicate in host language
$\mu \in \mathcal{M}$	Action in host language
$\lambda \in (N \cup \Pi \cup \mathcal{M})$	Reduction label
$\vec{\lambda} = \lambda_1 \lambda_n$	Sequence of reduction labels
Production Rules:	
$A \to \alpha_i$	i^{th} context-free production of A
$A \to \{\pi_i\}$? α_i	<i>i</i> th production predicated on semantics
$A \to \{\mu_i\}$	<i>i</i> th production with mutator

Figure 5. Predicated Grammar Notation

$Prod \ \frac{A \to \alpha}{(\mathbb{S}, uA\delta) \Rightarrow (\mathbb{S}, u\alpha\delta)}$			
$\pi(\mathbb{S})$			
$Sem \ \frac{A \to \{\pi'\}? \ \alpha}{(\mathbb{S}, uA\delta) \Rightarrow (\mathbb{S}, u\alpha\delta)} Action \ \frac{A \to \{\mu\}}{(\mathbb{S}, uA\delta) \Rightarrow (\mu(\mathbb{S}), u\delta)}$			
Closure $(\mathbb{S}, \alpha) \Rightarrow (\mathbb{S}', \alpha'), (\mathbb{S}', \alpha') \Rightarrow^* (\mathbb{S}'', \beta)$ $(\mathbb{S}, \alpha) \Rightarrow^* (\mathbb{S}'', \beta)$			

Figure 6. Predicated Grammar Leftmost Derivation Rules

ambiguity. However, for a practical parser, we want each input to correspond to a unique parse. To that end, ANTLR uses the order of the productions in the grammar to resolve ambiguities in favor of the production with the lowest number. This strategy resolves the well-known *if-then-else* ambiguity in the usual way by associating the *else* with the most recent *if*.

To resolve ambiguities that depend on the current state \mathbb{S} , programmers can insert semantic predicates but must make them mutually exclusive for all potentially ambiguous input sequences to render such productions unambiguous. Statically, mutual exclusion cannot be enforced because predicates are written in a Turing-complete language. At parse-time, however, ALL(*) evaluates predicates and dynamically reports input phrases for which multiple, predicated productions are viable. If the programmer fails to satisfy mutual exclusivity, ANTLR uses production order to resolve the ambiguity. This policy matches that of PEGs and is useful for concisely representing precedence.

5. Augmented transition networks

Given predicated grammar $G = (N, T, P, S, \Pi, \mathcal{M})$, the corresponding ATN $M_G = (Q, \Sigma, \Delta, E, F)$ has elements [18]:

- Q is the set of states
- Σ is the edge alphabet $N \cup T \cup \Pi \cup \mathcal{M}$
- Δ is the transition relation mapping $Q \times (\Sigma \cup \epsilon) \to Q$
- $E \in Q = \{p_A \mid A \in N\}$ is the set of submachine entry states
- $F \in Q = \{p'_A \mid A \in N\}$ is the set of submachine final states

ATNs resemble the syntax diagrams used to document programming languages, with an ATN submachine for each nonterminal. Figure 7 shows how to construct the set of states Q and edges Δ from grammar productions. The start state for A is $p_A \in Q$ and targets $p_{A,i}$, created from the left edge of α_i , with an edge in Δ . The last state created from α_i targets p_A' . Nonterminal edges $p \xrightarrow{A} q$ are like function calls. They transfer control of the ATN to A's submachine, pushing return state q onto a state call stack so it can continue from q after reaching the stop state for A's submachine, p_A' . Figure 8 gives the ATN for a simple grammar. The language matched by the ATN is the same as the language of the original grammar.

ALL(*) parsers record prediction results obtained from ATN simulation with *lookahead DFA*, which are DFA augmented with accept states that yield predicted production numbers. There is one accept state per decision production.

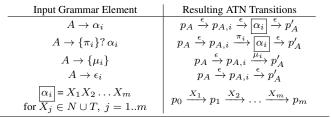


Figure 7. Predicated Grammar to ATN transformation



Figure 8. ATN for G with $P = \{S \rightarrow Ac \mid Ad, A \rightarrow aA \mid b\}$

Definition 5.1. Lookahead DFA are DFA with augmented accept states that yield predicted production numbers. For predicated grammar $G = (N, T, P, S, \Pi, \mathcal{M})$, DFA $M = (Q, \Sigma, \Delta, D_0, F)$ where:

- Q is the set of states
- $\Sigma = T$ is the edge alphabet
- Δ is the transition function mapping $Q \times \Sigma \to Q$
- $D_0 \in Q$ is the start state
- $F \in Q = \{f_1, f_2, \dots, f_n\}$ final states, one f_i per production i

A transition in Δ from state p to state q on symbol $a \in \Sigma$ has the form $p \xrightarrow{a} q$ and we require $p \xrightarrow{a} q'$ implies q = q'.

6. *ALL*(*) parsing algorithm

ALL(*) parsers are identical to conventional top-down LL(k) parsers except that ALL(*) predicts productions according to a special function called adaptivePredict, instead of the usual "switch on next k token types" mechanism. Function parse simulates an ATN representation of the original predicated grammar, factoring prediction and grammar analysis into adaptivePredict. We assume that user state $\mathbb S$ and the input are in scope to all algorithm functions, semantic predicates, and grammar actions.

```
Function 1: parse(S)
\gamma := []; a := input.curr(); i := adaptivePredict(S, \gamma); p := p_{S,i};
while true do
  if p = p'_B (i.e., p is rule stop state) then
      if B = S (i.e., finished matching start rule S) then return;
      else let \gamma = q\gamma' in \gamma := \gamma'; p := q;
   else
      switch t where p \xrightarrow{t} q do
         case b: (i.e., atom transition)
            if b = a then p := q; a := input.next();
            else throw mismatched-token-exception;
         case B: \gamma := q\gamma; i := adaptivePredict(B, \gamma); p := p_{B,i};
         case \mu: \mathbb{S} := \hat{\mu}(\mathbb{S}); p := q;
         case \pi: if \pi(\mathbb{S}) then p := q else throw failed-\pi;
         case \epsilon: p := q;
      endsw
```

Function parse takes start rule S as a parameter and initializes γ to an empty parsing stack and sets "cursor" p to the left edge in the ATN of the predicted production, $p_{S,i}$. The function loops until the cursor reaches p_S' , the submachine stop state for S. If the cursor reaches submachine stop state, p_B' , parse simulates a "return" by popping the return state q off the call stack and moving p to q.

If the cursor is not at a stop state, parse processes ATN transition t emanating from p. There can be only one transition from p because of the way ATNs are constructed. If t is a terminal edge and matches the current input symbol, parse transitions the edge and moves to the next symbol. If t is a nonterminal edge referencing B, parse simulates a submachine call by pushing return state q onto the stack and choosing the appropriate production left edge in B. For action edges, μ , parse

updates the state and transitions to q. Function parse only transitions predicate edges if π evaluates to true. Upon ϵ edge, parse moves to q. Function parse does not explicitly check that parsing stops at end-of-file because applications like development environments need to parse input subphrases.

6.1 ALL(*) grammar analysis

The goal of ALL(*) prediction is to choose an α_i production to expand for decision point $A \to \alpha_1 \mid \ldots \mid \alpha_n$, given current parser call stack γ_0 and remaining input w_r . Predicting α_i means α_i will lead to a successful parse of w_r . Grammar analysis yields the prediction and incrementally updates the lookahead DFA cache.

As with *parse*, the ALL(*) analysis algorithm operates at parsetime to simulate the actions of an ATN. Like GLR, ALL(*) makes decisions by launching subparsers to explore all possible parses, but ALL(*) chooses the path associated with the minimum production number if more than one is viable. Simulation of the ATN uses its own stack (GSS) and does not alter the parser stack. An *ATN configuration* for prediction purposes is a tuple (p, i, γ) that uniquely identifies a subparser location (comprised of ATN state p and prediction call stack γ) and predicted production number i. Component i does not exist in the machine configurations of GLL, GLR, or Earley [8].

The simplest way to implement ALL(*) prediction would be a classic backtracking approach, launching a subparser for each α_i . Subparsers would run independently, each with their own ATN call stack initialized with a copy of γ_0 . Subparsers that encountered syntax errors would die off, leaving subparsers associated with viable alternatives alive to consume w_r . The subparsers would consume all remaining input because backtracking subparsers do not know when to stop parsing—they are unaware of other subparsers' status. There are two issues with this approach. First, it is a waste to allow subparsers to examine all of w_r when most decisions need only a few lookahead symbols. Second, naive backtracking has exponential time complexity because of redundant computations.

We address both issues by having the prediction subparsers advance in lockstep through w_r . Prediction terminates after consuming prefix $u \leq w_r$ when all subparsers but one die off or when prediction identifies a conflict (Section 6.4). Operating in lockstep also lets prediction operate from a single work list of ATN configurations, providing an opportunity to share call stacks to avoid redundant computations.

6.2 Graph-structured call stacks

Two subparsers at state p that share the same ATN stack top, $q\gamma_1$ and $q\gamma_2$ (stacks grow to the left), will mirror each other's behavior until simulation pops q from their stacks. Prediction can treat those subparsers as a single subparser by merging stacks. We merge stacks for all configurations in the work list of the form (p,i,γ_1) and (p,i,γ_2) , forming a general configuration (p,i,Γ) with a graph-structured stack (GSS) [23] component $\Gamma = \gamma_1 \uplus \gamma_2$ where \uplus means graph merge. Γ can be the empty stack [], a special stack # used for SLL prediction (addressed shortly), an individual stack, or a graph of stack nodes. Merging individual stacks into a GSS reduces the potential size from exponential to linear complexity (Section 8). We use an immutable graph data structure with maximal sharing of nodes. Here are two examples that share the parser stack γ_0 at the bottom of the stack:

$$p\gamma_0 \uplus q\gamma_0 = \bigvee_{\boxed{\gamma_0}}^{p-q} \qquad q\Gamma\gamma_0 \uplus q\Gamma'\gamma_0 = \bigcap_{\boxed{\Gamma}}^{q}$$

In the functions that follow, all additions to configuration lists, such as with operator +=, implicitly merge stacks.

There is a special case related to the stack condition at the start of prediction. Γ must distinguish between an empty stack and no stack information. For LL prediction, the initial ATN simulation stack is the current parser call stack γ_0 . The initial stack is only empty, $\gamma_0 = []$, when the decision entry rule is the start symbol. Stack-insensitive SLL prediction, on the other hand, ignores the parser call stack and uses an

initial stack of #, indicating no stack information. This distinction is important when computing the *closure* (Function 7) of configurations representing submachine stop states. Without parser stack information, a subparser that returns from decision entry rule A must consider all possible invocation sites; i.e., *closure* sees configuration $(p'_A, -, \#)$.

The empty stack [] is treated like any other node for LL prediction: $\Gamma \uplus []$ yields the graph equivalent of set $\{\Gamma, []\}$, meaning that both Γ and the empty stack are possible. Pushing state p onto [] yields p[] not p because popping p must leave the [] empty stack symbol. For SLL prediction, $\Gamma \uplus \# = \#$ for any graph Γ because # acts like a wildcard and represents the set of all stacks. The wildcard therefore contains any Γ . Pushing state p onto # yields p#.

6.3 ALL(*) prediction algorithm

Prediction for nonterminal A begins in adaptive Predict (Function 2) and is a function of the decision A and the parser stack γ_0 . We assume that the ATN corresponding to input grammar G and nonterminal A are in scope for all functions of the algorithm. Given the similarity of ATN and DFA machine elements, we explicitly label transition maps and state sets needed by the algorithm: Δ_{ATN} , Δ_{DFA} , and Q_{DFA} . Our discussion follows a top-down order with the key algorithm functions appearing in boxes.

Function adaptivePredict delegates to predictLL (Function 6), described below, for LL prediction if at least one of the productions is predicated.² For unpredicated decisions, adaptivePredict creates a DFA with start state D_0 for decision A, if one does not already exist, in preparation for adding paths to the DFA. D_0 is the set of ATN configurations for all positions reachable without traversing a terminal edge. Function adaptivePredict then invokes predictSLL (Function 4) to predict a production.

```
Function 2: adaptivePredict(A, \gamma_0) returns int alt start := input.index(); if \exists A \to \pi_i \alpha_i then return predictLL(A, \gamma_0); if \nexists dfa_A then

F_{DEA} := \{f_i \mid f_i := \text{DFA\_State}(i) \ \forall A \to \alpha_i\};
D_0 := startState(A, \#);
D_{error} := \text{DFA\_State}(-);
Q_{DEA} := F_{DEA} \cup D_0 \cup D_{error};
dfa_A := DFA(Q_{DEA}, \Sigma_{DEA} = T, \Delta_{DEA} = \varnothing, D_0, F_{DEA});
alt := predictSLL(D<sub>0</sub>, start, \gamma_0);
input.seek(start); (i.e., undo stream position changes)
return alt;
```

To create DFA start state D_0 , startState (Function 3) adds configurations $(p_{A,i},i,\gamma)$ for each $A \to \alpha_i$ and $A \to \pi_i \alpha_i$, if π_i evaluates to true. When called from predictLL, the ATN call stack γ is the initial parser stack γ_0 . When called from adaptivePredict, γ is special symbol # needed by SLL prediction, indicating "no parser stack information." Computing closure (Function 7) of the configurations completes D_0 .

```
Function 3: startState(A, \gamma) returns DFA_State D_0

D_0 := \emptyset; for each p_A \xrightarrow{\epsilon} p_{A,i} \in \Delta_{ATN} do

if p_A \xrightarrow{\epsilon} p_{A,i} \xrightarrow{\pi_i} p then \pi := \pi_i else \pi := \epsilon;

if \pi = \epsilon or eval(\pi_i) then D_0 += closure(\{\}, D_0, (p_{A,i}, i, \gamma)); return D_0;
```

Function predictSLL (Function 4) performs both DFA and SLL ATN simulation, incrementally adding paths to the DFA. In the best case, there is already a DFA path from D_0 to an accept state, f_i , for prefix $u \leq w_r$ and some production number i. In the worst-case, ATN simulation is required for all a in sequence u. The main loop in predictSLL finds an existing edge emanating from D upon

² SLL prediction does not incorporate predicates for clarity in this exposition, but in practice, ANTLR incorporates predicates into DFA accept states (Section ??). ANTLR 3 DFA used predicated edges not predicated accept states.

a or computes a new one via target (Function 5). It is possible that target will compute a target state that already exists in the DFA, \underline{D}' , in which case function target returns \underline{D}' because \underline{D}' may already have a computed outgoing edge; it is inefficient to discard work by replacing \underline{D}' . At the next iteration, predictSLL will consider edges from \underline{D}' , effectively switching back to DFA simulation.

```
Function 4: predictSLL(D_0, start, \gamma_0) returns int prod a := input.curr(); D = D_0; while true do

let D' be DFA target D \xrightarrow{a} D'; if \nexists D' then D' := target(D, a); if D' = D_{error} then throw no-viable-alternative; if D' stack sensitive then input.seek(start); return predictLL(A, \gamma_0); if D' = f_i \in F then return i; D := D'; a := input.next();
```

Once predictSLL acquires a target state, D', it checks for errors, stack sensitivity, and completion. If D' is an error state, the algorithm throws an exception. If D' has been marked as stack-sensitive by target, prediction requires full LL simulation so predictSLL re-examines lookahead w_r using parser stack information via predictLL. If D' is accept state f_i for some i, predictSLL returns i. A DFA state is an accept state when all of its configurations predict the same production; further analysis is unnecessary and the algorithm can stop. For any other D', the algorithm jumps to D', gets the next input symbol, and repeats.

Function *target* uses a combined *move-closure* operation to discover the set of ATN configurations reachable from D upon a single terminal symbol $a \in T$. Function *move* computes the configurations reachable directly upon a by traversing a terminal edge:

$$move(D, a) = \{(q, i, \Gamma) \mid p \xrightarrow{a} q, (p, i, \Gamma) \in D\}$$

The algorithm then adds the closure of those configurations to form D'. If D' is empty, no viable alternative can match a from the current state and target returns DFA error state $D_{error}.$ If all configurations in D' predict the same production number i, target adds edge $D \stackrel{a}{\rightarrow} f_i$ and returns accept state $f_i.$ If SLL ATN simulation finds a conflict, target marks D' as stack-sensitive. The conflict could be an ambiguity or a weakness stemming from SLL's lack of parser stack information. (Conflicts along with functions getConflictSetsPerLoc and getConflictSetsPerState are described in Section 6.4.) The function finishes by adding state D', if an equivalent state is not already in the DFA, and adds edge $D \stackrel{a}{\rightarrow} D'.$

```
Function 5: target(D, a) returns DFA_State D'
mv := move(D, a); D' := \bigcup_{\substack{c \in mv \\ c \in mv}} closure(\{\}, c);

if D' = \varnothing then \Delta_{DFA} += D \xrightarrow{a} D_{error}; return D_{error};

if \{j \mid (-, j, -) \in D'\} = \{i\} then \Delta_{DFA} += D \xrightarrow{a} f_i; return f_i;

// Look for a conflict among configurations of D'

a\_conflict := \exists alts \in getConflictSetsPerLoc(D') : |alts| > 1;

viablealt := \exists alts \in getConflictSetsPerState(D') : |alts| = 1;

if a\_conflict and not viablealt then mark D' as stack sensitive;

if D' = \underline{D'} \in Q_{DFA} then D' := \underline{D'}; else Q_{DFA} += D';

\Delta_{DFA} += D \xrightarrow{a} D';

return D';
```

Function predictLL performs LL ATN simulation and returns the predicted production number. Function predictLL is similar to predictSLL and also uses a local variable called D' for consistency but does not update the DFA. LL prediction continues until either D' uniquely predicts an alternative, $D' = \emptyset$, or D' has a conflict. If D' from LL simulation has a conflict as SLL did, the algorithm reports u as an ambiguous phrase and resolves to the minimum production number among the conflicting configurations. Otherwise, the algorithm moves to D' and the next input symbol.

```
Function 6: predictLL(A, \gamma_0) returns int alt
D := D_0 := startState(A, \gamma_0); a := input.curr();
while true do
mv := move(D, a); D' := \bigcup_{c \in mv} closure(\{\}, c);
if D' = \varnothing then throw no-viable-alternative;
if \{j \mid (-, j, -) \in D'\} = \{i\} then return i;
/* If all p, \Gamma pairs predict > 1 alt and all such production sets are same, input ambiguous. */
subsets := getConflictSetsPerLoc(D');
if x = y and |x| > 1 \ \forall x, y \in subsets then
x := any set in subsets;
reportAmbiguity(x, start, input.index());
return min(x);
D := D'; a := input.next();
```

The closure operation (Function 7) chases through all ϵ edges reachable from p, the ATN state projected from configuration parameter c and also simulates the call and return of submachines. Function closure treats μ and π edges as ϵ edges. Mutators should not be executed during prediction and predicates are only evaluated during start state computation. From parameter $c=(p,i,\Gamma)$ and edge $p\stackrel{\epsilon}{\to}q, closure$ adds (q,i,Γ) to local working set C. For submachine call edge $p\stackrel{E}{\to}q, closure$ adds the closure of $(p_B,i,q\Gamma)$. Returning from a submachine stop state p_B' adds the closure of configuration (q,i,Γ) for $c=(p_B',i,q\Gamma)$. In general, a configuration stack Γ is a graph representing multiple individual stacks. Function closure must simulate a return from each of the Γ stack tops. The algorithm uses notation $q\Gamma'\in\Gamma$ to represent all stack tops q of Γ .

```
Function 7: closure(busy, c = (p, i, \Gamma)) returns set C C := \{c\}; if c \in busy then return \varnothing; else busy += c; if p = p_B' (i.e., p is any stop state including p_A') then if \Gamma = \# (i.e., stack is SLL wildcard) then C += \bigcup closure(busy, (p_2, i, \#)); // call site closure \forall p_2 : p_1 \xrightarrow{A} p_2 \in \Delta_{ATN} else // nonempty SLL or LL stack for q\Gamma' \in \Gamma (i.e., each stack top q in graph \Gamma) do C += closure(busy, (q, i, \Gamma')); // "return" to q return C; end foreach p \xrightarrow{edge} q do switch edge do case B: C += closure(busy, (p_B, i, q\Gamma)); case \pi, \mu, \epsilon: C += closure(busy, (q, i, \Gamma)); return C;
```

When analysis returns out of the decision entry rule, A, LL and SLL predictions behave differently. LL prediction simply continues up the stack into the parser call stack inherited as γ_0 . SLL prediction, on the other hand, has no access to the parser call stack and must consider all possible A invocation sites. Function closure finds $\Gamma=\#$ in this situation because startState will have marked the initial stack with # not γ_0 . The return behavior at the decision entry rule is what differentiates SLL from LL style parsing.

To avoid non-termination due to SLL right recursion and ϵ edges in closure subrules such as ()+, closure uses a busy set that is shared among all closure operations used to compute the same D'.

6.4 Conflict and ambiguity detection

The notion of conflicting configurations is central to ALL(*) analysis. Conflicts trigger failover to full LL prediction during SLL prediction and signal an ambiguity during LL prediction. A sufficient condition for a conflict between configurations is when they differ only in the predicted alternative: (p,i,Γ) and (p,j,Γ) . Detecting conflicts is aided by two functions. The first, getConflictSetsPerLoc (Function 8), collects the sets of production numbers associated with all $(p,-,\Gamma)$ configurations. If a p,Γ pair predicts more than a single production, a conflict exists. Here is a sample configuration set and the associated set of conflict sets:

$$\{\underbrace{(p,1,\Gamma),(p,2,\Gamma),(p,3,\Gamma)}_{\{1,2,3\}},\underbrace{(p,1,\Gamma'),(p,2,\Gamma')}_{\{1,2\}},\underbrace{(r,2,\Gamma'')}_{\{2\}}\}$$

These conflicts sets indicate that location p, Γ is reachable from productions $\{1, 2, 3\}$, location p, Γ' is reachable from productions $\{1, 2\}$, and r, Γ'' is reachable from production $\{2\}$.

/* For each p, Γ get set of alts $\{i\}$ from $(p, -, \Gamma) \in D$ configs */ Function 8: getConflictSetsPerLoc(D) returns set of int sets $s := \varnothing$; for $(p, -, \Gamma) \in D$ do $prods := \{i \mid (p, i, \Gamma)\}; s := s \cup prods;$ return s;

/* For each p return set of alts i from $(p,-,-) \in D$ configs. */ Function 9: getConflictSetsPerState(D) returns set of int sets $s := \varnothing$; for $(p,-,-) \in D$ do $prods := \{i \mid (p,i,-)\}; s := s \cup prods;$ return s;

The second function, *getConflictSetsPerState* (Function 9), is similar but collects the production numbers associated with just ATN state *p*. For the same configuration set, *getConflictSetsPerState* computes these conflict sets:

$$\{\underbrace{(p,1,\Gamma),(p,2,\Gamma),(p,3,\Gamma),(p,1,\Gamma'),(p,2,\Gamma')}_{\{1,2,3\}},\underbrace{(r,2,\Gamma'')}_{\{2\}}\}$$

A sufficient condition for failing over to LL prediction (predictLL) from SLL would be when there is at least one set of conflicting configurations: getConflictSetsPerLoc returns at least one set with more than a single production number. E.g., configurations (p, i, Γ) and (p, j, Γ) exist in parameter D. However, our goal is to continue using SLL prediction as long as possible because SLL prediction updates the lookahead DFA cache. To that end, SLL prediction continues if there is at least one nonconflicting configuration (when getConflict-SetsPerState returns at least one set of size 1). The hope is that more lookahead will lead to a configuration set that predicts a unique production via that nonconflicting configuration. For example, the decision for $S \to a|a|a \bullet_p b$ is ambiguous upon input a between productions 1 and 2 but is unambiguous upon ab. (Location \bullet_n is the ATN state between a and b.) After matching input a, the configuration set would be $\{(p'_S, 1, []), (p'_S, 2, []), (p, 3, [])\}$. Function getConflictSetsPerLoc returns $\{\{1,2\}, \{3\}\}$. The next move-closure upon b leads to nonconflicting configuration set $\{(p'_S, 3, [])\}$ from (p, 3, []), bypassing the conflict. If all conflict sets returned from getConflictSetsPerLoc predict more than one alternative, no amount of lookahead will lead to a unique prediction. Analysis must try again with the call stack via *predictLL*.

Conflicts during LL simulation are ambiguities and occur when each conflict set from getConflictSetsPerLoc contains more than 1 production—every location in D is reachable from more than a 1 production. Once multiple subparsers reach the same $(p, -, \Gamma)$, all future simulation derived from $(p, -, \Gamma)$ will behave identically. More lookahead will not resolve the ambiguity. Prediction could terminate at this point and report lookahead prefix u as ambiguous but predictLL continues until it is sure for which productions u is ambiguous. Consider conflict sets $\{1,2,3\}$ and $\{2,3\}$. Because both have degree greater than one, the sets represent an ambiguity, but additional input will identify whether u is ambiguous upon $\{1,2,3\}$ or $\{2,3\}$. Function predictLL continues until all conflict sets that identify ambiguities are equal; condition u0 and u1 and u2 by u3 by u4 by u5 subsets embodies this test.

To detect conflicts, the algorithm compares graph-structured stacks frequently. Technically, a conflict occurs when configurations (p,i,Γ) and (p,j,Γ') occur in the same configuration set with $i\neq j$ and at least one stack trace γ in common to both Γ and Γ' . Because checking for graph intersection is expensive, the algorithm uses equality, $\Gamma = \Gamma'$, as a heuristic. Equality is much faster because of the shared subgraphs. The graph equality algorithm can often check node identity to compare two entire subgraphs. In the worst case, the equality versus subset heuristic delays conflict detection until the GSS between conflicting configurations are simple linear stacks where graph intersection is the same as graph equality. The cost of this heuristic is deeper lookahead.

6.5 Sample DFA construction

To illustrate algorithm behavior, consider inputs bc and bd for the grammar and ATN in Figure 8. ATN simulation for decision S launches subparsers at left edge nodes $p_{S,1}$ and $p_{S,2}$ with initial D_0 configurations $(p_{S,1},1,[])$ and $(p_{S,2},2,[])$. Function closure adds three more configurations to D_0 as it "calls" A with "return" nodes p_1 and p_3 . Here is the DFA resulting from ATN simulation upon bc and then bd (configurations added by move are bold):

$$D_{0} \begin{bmatrix} (\mathbf{p_{S,1},1}, []), (p_{A}, 1, p_{1}), (p_{A,1}, 1, p_{1}), (p_{A,2}, 1, p_{1}) \\ (\mathbf{p_{S,2},2}, []), (p_{A}, 2, p_{3}), (p_{A,1}, 2, p_{3}), (p_{A,2}, 2, p_{3}) \end{bmatrix}$$

$$D' \begin{bmatrix} (\mathbf{p_{7},1}, \mathbf{p_{1}}), (p'_{A}, 1, p_{1}), (p_{1}, 1, []) \\ (\mathbf{p_{7},2}, \mathbf{p_{3}}), (p'_{A}, 2, p_{3}), (p_{3}, 2, []) \end{bmatrix}$$

$$f_{1} \begin{bmatrix} (\mathbf{p_{2},1}, []), (p'_{S}, 1, []) \end{bmatrix} \begin{bmatrix} (\mathbf{p_{4},2}, []), (p'_{S}, 2, []) \end{bmatrix} f_{2}$$

After bc prediction, the DFA has states D_0 , D', and f_1 . From DFA state D', closure reaches the end of A and pops from the Γ stacks, returning to nodes in S. State f_1 uniquely predicts production number 1. State f_2 is created and connected to the DFA (shown with dashed arrow) during prediction of the second phrase, bd. Function adaptivePredict first uses DFA simulation to get to D' from D_0 upon b. Before having seen bd, D' has no d edge so adaptivePredict must use ATN simulation to add edge $D' \xrightarrow{d} f_2$.

7. Pragmatics

This section describes some of the practical considerations associated with implementing the ALL(*) algorithm.

7.1 Semantic predicate evaluation

For clarity, the algorithm described in this paper uses pure ATN simulation for all decisions that have semantic predicates on production left edges. In practice, ANTLR uses lookahead DFA that track predicates in accept states to handle semantic-context-sensitive prediction. Tracking the predicates in the DFA allows prediction to avoid expensive ATN simulation if predicate evaluation during *SLL* simulation predicts a unique production. Semantic predicates are not common but are critical to solving some context-sensitive parsing problems; e.g., predicates are used internally by ANTLR to encode operator precedence when rewriting left-recursive rules. So it is worth the extra complexity to evaluate predicates during *SLL* prediction. Consider the predicated rule from Section 2.1:

id : ID | {!enum_is_keyword}? 'enum';

The second production is viable only when <code>!enum_is_keyword</code> evaluates to true. In the abstract, that means the parser would need two lookahead DFA, one per semantic condition. Instead, ANTLR's <code>ALL(*)</code> implementation creates a lookahead DFA (via <code>SLL</code> prediction) with edge $D_0 \stackrel{\text{enum}}{\longrightarrow} f_2$ where f_2 is an augmented DFA accept state that tests <code>!enum_is_keyword</code>. Function <code>adaptPredict</code> returns production number 2 for <code>enum_is_keyword</code> else <code>adaptPredict</code> throws a no-viable-alternative exception.

The algorithm described in this paper also does not support semantic predicates outside of the decision entry rule. In practice, ANTLR must evaluate all predicates reachable from the decision entry rule without stepping over a terminal edge in the ATN. For example, the simplified ALL(*) algorithm in this paper considers only predicates π_1 and π_2 for the productions of S in the following (ambiguous) grammar.

$$\begin{array}{l} S \to \{\pi_1\}?Ab \,|\, \{\pi_2\}?Ab \\ A \to \{\pi_3\}?a \,|\, \{\pi_4\}?a \end{array}$$

Input ab matches either alternative of S and, in practice, ANTLR evaluates " π_1 and (π_3 or π_4)" to test the viability of S's first production not just π_1 . After simulating S and A's ATN submachines, the lookahead DFA for S would be $D_0 \stackrel{a}{\to} D' \stackrel{b}{\to} f_{1,2}$. Augmented accept state $f_{1,2}$ predicts productions 1 or 2 depending on semantic contexts

 $\pi_1 \wedge (\pi_3 \vee \pi_4)$ and $\pi_2 \wedge (\pi_3 \vee \pi_4)$, respectively. To keep track of semantic context during SLL simulation, ANTLR ATN configurations contain extra element π : (p,i,Γ,π) . Element π carries along semantic context and ANTLR stores predicate-to-production pairs in the augmented DFA accept states.

7.2 Multi-threaded execution

Applications often require parallel execution of multiple parser instances, even for the same language. For example, web-based application servers parse multiple incoming XML or JSON data streams using multiple instances of the same parser. For memory efficiency, all *ALL(*)* parser instances for a given language must share lookahead DFA. The Java code that ANTLR generates uses a shared memory model and threads for concurrency, which means parsers must update shared DFA in a thread-safe manner. Multiple threads can be simulating the DFA while other threads are adding states and edges to it. Our goal is thread safety, but concurrency also provides a small speed up for lookahead DFA construction (observed empirically). For more details, see [2].

The key to thread safety in Java while maintaining high throughput lies in avoiding excessive locking (synchronized blocks). There are only two data structures that require locking: Q, the set of DFA states, and Δ , the set of edges. Our implementation factors state addition, Q += D', into an addDFAState function that waits on a lock for Q before testing a DFA state for membership or adding a state. This is not a bottleneck as DFA simulation can proceed during DFA construction without locking since it traverses edges to visit existing DFA states without examining Q.

Adding DFA edges to an existing state requires fine-grained locking, but only on that specific DFA state as our implementation maintains an edge array for each DFA state. We allow multiple readers but a single writer. A lock on testing the edges is unnecessary even if another thread is racing to set that edge. If edge $D \xrightarrow{a} D'$ exists, the simulation simply transitions to D'. If simulation does not find an existing edge, it launches ATN simulation starting from D to compute D' and then sets element edge[a] for D. Two threads could find a missing edge on a and both launch ATN simulation, racing to add $D \xrightarrow{a} D'$. D' would be the same in either case so there is no hazard as long as that specific edge array is updated safely using synchronization. To encounter a contested lock, two or more ATN simulation threads must be trying to add an edge to the same DFA state.

7.3 Reducing warm-up time

Many decisions in a grammar are LL(1) and they are easy to identify statically. Instead of always generating "switch on *adaptivePredict*" decisions in the recursive-descent parsers, ANTLR generates "switch on token type" decisions whenever possible. This LL(1) optimization does not affect the size of the generated parser but reduces the number of lookahead DFA that the parser must compute.

Originally, we anticipated "training" a parser on a large input corpus and then serializing the lookahead DFA to disk to avoid recomputing DFA for subsequent parser runs. As shown in Section 7, lookahead DFA construction is fast enough that serializing and deserializing the DFA is unnecessary.

7.4 Error reporting and recovery

ALL(*) prediction can scan arbitrarily far ahead so erroneous lookahead sequences can be long. By default, ANTLR-generated parsers print the entire sequence. To recover, parsers consume tokens until a token appears that could follow the current rule. ANTLR provides hooks to override reporting and recovery strategies.

ANTLR parsers issue error messages for invalid input phrases and attempt to recover. For mismatched tokens, ANTLR attempts single token insertion and deletion to resynchronize. If the remaining input is not consistent with any production of the current nonterminal, the parser consumes tokens until it finds a token that could reasonably follow the current nonterminal. Then the parser continues parsing as if the

current nonterminal had succeeded. ANTLR improves error recovery over ANTLR 3 for EBNF subrules by inserting synchronization checks at the start and at the "loop" continuation test to avoid prematurely exiting the subrule. For example, consider the following class definition rule.

```
classdef : 'class' ID '{' member+ '}' ;
member : 'int' ID ';' ;
```

An extra semicolon in the member list such as int i;; int j; should not force surrounding rule classdef to abort. Instead, the parser ignores the extra semicolon and looks for another member. To reduce cascading error messages, the parser issues no further messages until it correctly matches a token.

8. Empirical results

We performed experiments to compare the performance of ALL(*) Java parsers with other strategies, to examine the throughput of ALL(*) parsers for a variety of other languages, to highlight the effect of the lookahead DFA cache on parsing speed, and to provide evidence of linear ALL(*) performance in practice.

8.1 Comparing ALL(*)'s speed to other parsers

Our first experiment compared Java parsing speed across 10 tools and 8 parsing strategies: hand-tuned recursive-descent with precedence parsing, LL(k), LL(*), PEG, LALR(1), ALL(*) GLR, and GLL. Figure 9 shows the time for each tool to parse the 12,920 source files of the Java 6 library and compiler. We chose Java because it was the most commonly available grammar among tools and sample Java source is plentiful. The Java grammars used in this experiment came directly from the associated tool except for DParser and Elkhound, which did not offer suitable Java grammars. We ported ANTLR's Java grammar to the meta-syntax of those tools using unambiguous arithmetic expressions rules. We also embedded merge actions in the Elkhound grammar to disambiguate during the parse to mimic ANTLR's ambiguity resolution. All input files were loaded into RAM before parsing and times reflect the average time measured over 10 complete corpus passes, skipping the first two to ensure JIT compiler warm-up. For ALL(*). we used the two-stage parse from Section 3.2. The test machine was a 6 core 3.33Ghz 16G RAM Mac OS X desktop running the Java 7 virtual machine. Elkhound and DParser parsers were implemented in C/C++, which does not have a garbage collector running concurrently. Elkhound was last updated in 2005 and no longer builds on Linux or OS X, but we were able to build it on Windows 7 (4 core 2.67Ghz 24G RAM). Elkhound also can only read from a file so Elkhound parse times are not comparable. In an effort to control for machine speed differences and RAM vs SSD, we computed the time ratio of our Java test rig on our OS X machine reading from RAM to the test rig running on Windows pulling from SSD. Our reported Elkhound times are the Windows time multiplied by that OS X to Windows ratio.

For this experiment, ALL(*) outperforms the other parser generators and is only about 20% slower than the handbuilt parser in the Java compiler itself. When comparing runs with tree construction (marked with † in Figure 9), ANTLR 4 is about 4.4x faster than Elkhound, the fastest GLR tool we tested, and 135x faster than GLL (Rascal). ANTLR 4's nondeterministic ALL(*) parser was slightly faster than JavaCC's deterministic LL(k) parser and about 2x faster than Rats!'s PEG. In a separate test, we found that ALL(*) outperforms Rats! on its own PEG grammar converted to ANTLR syntax (8.77s vs 12.16s). The LALR(1) parser did not perform well against the LL tools but that could be SableCC's implementation rather than a deficiency of LALR(1). (The Java grammar from JavaCUP, another LALR(1)tool, was incomplete and unable to parse the corpus.) When reparsing the corpus, ALL(*) lookahead gets cache hits at each decision and parsing is 30% faster at 3.73s. When reparsing with tree construction (time not shown), ALL(*) outperforms handbuilt Javac (4.4s vs 4.73s). Reparsing speed matters to tools such as development environments.

The GLR parsers we tested are up to two orders of magnitude slower at Java parsing than ALL(*). Of the GLR tools, Elkhound

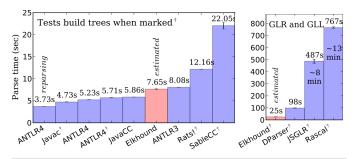


Figure 9. Comparing Java parse times for 10 tools and 8 strategies on Java 6 Library and compiler source code (smaller is faster). 12,920 files, 3.6M lines, size 123M. Tool descriptors comprise: "tool name version [strategy]." ANTLR4 4.1 [ALL(*)]; Javac 7 [handbuilt recursive-descent and precedence parser for expressions]; JavaCC 5.0 [LL(k)]; Elkhound 2005.08.22b [GLR] (tested on Windows); ANTLR3 3.5 [LL(*)]; Rats! 2.3.1 [PEG]; SableCC 3.7 [LALR(1)]; DParser 1.2 [GLR]; JSGLR (from Spoofax) 1.1 [GLR]; Rascal 0.6.1 [GLL]. Tests run 10x, average/stddev computed on last 8 to avoid JIT cost. Error bars are negligible but show some variability due to garbage collection. To avoid a log scale, we use a separate graph for GLR and GLL parse times.

Tool	Time	RAM (M)
Javac	89ms	7
ANTLR4	201ms	8
JavaCC	206ms	7
ANTLR4 [†]	360ms	8
ANTLR3	1048ms	143
SableCC [†]	1,174ms	201
Rats! [†]	1,365ms	22
JSGLR [†]	15,401ms	1,030
Rascal [†]	24,941ms	2,622
(no DFA) ANTLR4	42,512ms	27
elkhound a	3.35 min	3
DParser [†]	10.5 hours	100+
elkhound †	out of mem	5390+

Figure 10. Time and space to parse and optionally build trees for 3.2M Java file. Space is median reported after GC during parse using -XX:+PrintGC option (process monitoring for C++). Times include lexing; all input preloaded. †Building trees. ^aDisambiguating during the parse, no trees, estimated time.

has the best performance primarily because it relies on a linear LR(1) stack instead of a GSS whenever possible. Further, we allowed Elkhound to disambiguate during the parse like ALL(*). Elkhound uses a separate lexer, unlike JSGLR and DParser, which are scannerless. A possible explanation for the observed performance difference with ALL(*) is that the Java grammar we ported to Elkhound and DParser is biased towards ALL(*), but this objection is not well-founded. GLR should also benefit from highly-deterministic and unambiguous grammars. GLL has the slowest speed in this test perhaps because Rascal's team ported SDF's GLR Java grammar, which is not optimized for GLL (Variations in the grammar can affect performance.) Rascal is also scannerless. Rascal is currently the only available GLL tool.

The biggest issue with general algorithms is that they are highly unpredictable in time and space, which can make them unsuitable for some commercial applications. Figure 10 summarizes the performance of the same tools against a single 3.2M Java file. Elkhound took 7.65s to parse the 123M Java corpus, but took 3.35 minutes to parse a single 3.2M Java file. It crashed with parse forest construction on because it ran out of memory. DParser's time jumped from a corpus time of 98s to 10.5 hours on the single file. The speed of Rascal and JSGLR scale reasonably well to the large 3.2M file, but use 2.6G and 1G RAM, respectively. In contrast, *ALL*(*) parses the 3.2M file in 360ms with tree construction using 8M. ANTLR 3 is fast but is slower and takes more memory (due to backtracking memoization) than ANTLR 4.

Grammar	KB/sec
XML	45,993
Java	24,972
JSON	17,696
DOT	16,152
Lua	5,698
C	4,238
Verilog2001	1,994
Erlang	751

Figure 11. Throughput. Lexing+parsing; input preloaded.

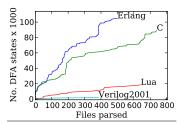


Figure 12. DFA growth rate vs no. files parsed. Files parsed in disk order.

8.2 ALL(*) performance across languages

Figure 11 gives the bytes-per-second throughput of *ALL(*)* parsers for 8 languages, including Java for comparison. The number of test files and file sizes vary greatly (according to the input we could reasonably collect); smaller files yield higher parse-time variance.

- C Derived from C11 specification; has no indirect left-recursion, altered stack-sensitive rule to render SLL (see text below): 813 preprocessed files, 159.8M source from postgres database.
- Verilog2001 Derived from Verilog 2001 spec, removed indirect leftrecursion: 385 files, 659k from [4] and web.
- JSON Derived from spec. 4 files, 331k from twitter.
- DOT: Derived from spec. 48 files 19.5M collected from web.
- Lua: Derived from Lua 5.2 spec. 751 files, 123k from github.
- XML Derived from spec. 1 file, 117M from XML benchmark.
- Erlang Derived from official LALR(1) grammar. 500 preproc'd files, 8M.

Some of these grammars yield reasonable but much slower parse times compared to Java and XML but demonstrate that programmers can convert a language specification to ANTLR's meta-syntax and get a working grammar without major modifications. (In our experience, grammar specifications are rarely tuned to a particular tool or parsing strategy and are often ambiguous.) Later, programmers can use ANTLR's profiling and diagnostics to improve performance, as with any programming task. For example, the C11 specification grammar is *LL* not *SLL* because of declarationSpecifiers, which we altered to be *SLL* in our C grammar (getting a 7x speed boost as *ALL*(*) is optimized for *SLL*).

8.3 Effect of lookahead DFA on performance

The lookahead DFA cache is critical to *ALL*(*) performance. To demonstrate the cache's effect on parsing speed, we disabled the DFA and repeated our Java experiments. Consider the 3.73s parse time from Figure 9 to reparse the Java corpus with pure cache hits. With the lookahead DFA cache disabled completely, the parser took 12 minutes (717.6s). Figure 10 also shows that disabling the cache increases parse time from 203ms to 42.5s on the 3.2M file. This performance is in line with the high cost of GLL and GLR parsers that also do not reduce parser speculation by memoizing parsing decisions. As an intermediate value, clearing the DFA cache before parsing each corpus file yields a total time of 34s instead of 12 minutes. This isolates cache use to a single file and demonstrates that cache warm-up occurs quickly even within a single file.

DFA size increases linearly as the parser encounters new lookahead phrases. Figure 12 shows the growth in the number of DFA states as the (slowest four) parsers from Figure 11 encounter new files. Languages like C that have constructs with common left-prefixes require deep lookahead in *LL* parsers to distinguish phrases; e.g., struct {...} x; and struct {...} f(); share a large left-prefix. In contrast, the Verilog2001 parser uses very few DFA states (but runs slower due to a non-*SLL* rule). Similarly, after seeing the entire 123M Java corpus, the Java parser uses just 31,626 DFA states (1.5M RAM), adding an average of 2.5 states per file parsed. DFA size does, however, continue to grow as the parser encounters unfamiliar input. Programmers can easily clear the cache and *ALL*(*) will adapt to subsequent input.

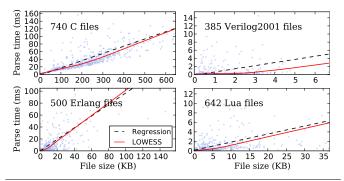


Figure 13. Linear parse time vs file size. Linear regression (dashed line) and LOWESS unconstrained curve coincide, giving strong evidence of linearity. Curves computed on (bottom) 99% of file sizes but zooming in to show detail in the bottom 40% of parse times.

8.4 Empirical parse-time complexity

Given the wide range of throughput in Figure 11, one could suspect nonlinear behavior for the slower parsers. To investigate, we plotted parse time versus file size in Figure 13 and drew least-squares regression and LOWESS [6] data fitting curves. A LOWESS curve is parametrically unconstrained (it is not required to be a line or any particular polynomial) and virtually mirrors each regression line, providing strong evidence that the relationship between parse time and input size is linear. The same methodology shows that the parser generated from the non-SLL grammar (not shown) taken verbatim from the C11 specification is also linear, despite being much slower than our SLL version.

We have yet to see nonlinear behavior in practice but the theoretical worst-case behavior of ALL(*) parsing is $O(n^4)$. Experimental parsetime data for the following contrived worst-case grammar exhibits quartic behavior for input $a, aa, aaa, ..., a^n$ (with input $n \le 120$ symbols we could test in a reasonable amount of time).

$$S \to A$$
\$ $A \to aAA \mid aA \mid a$

The generated parser requires a prediction upon each input symbol and each prediction must examine the entire remaining input. The *closure* operation for each lookahead symbol must examine the entire depth n of the GSS. Merging two GSS can take O(n) in our implementation.

From these experiments, we conclude that shifting grammar analysis to parse-time to get ALL(*) strength is not only practical but yields extremely efficient parsers, competing with the hand-tuned recursive-descent parser of the Java compiler. Memoizing analysis results with lookahead DFA is critical to such performance. Despite $O(n^4)$ theoretical complexity, ALL(*) appears to be linear in practice and does not exhibit the unpredictable performance or large memory footprint of the general algorithms.

9. Related work

For decades, researchers have worked towards increasing the recognition strength of efficient but non-general LL and LR parsers and increasing the efficiency of general algorithms such as Earley's $O(n^3)$ algorithm [8]. Parr [19] and Charles [5] statically generated LL(k) and LR(k) parsers for k > 1. Parr and Fisher's LL(*) [18] and Bermudez and Schimpf's LAR(m) [3] statically computed LL and LR parsers augmented with cyclic DFA that could examine arbitrary amounts of lookahead. These parsers were based upon LL-regular [11] and LRregular [7] parsers, which have the undesirable property of being undecidable in general. Introducing backtracking dramatically increases recognition strength and avoids static grammar analysis undecidability issues but is undesirable because it makes embedded mutators difficult, reduces performance, and complicates single-step debugging. Packrat parsers (PEGs) [9] try decision productions in order and pick the first that succeeds. PEGs are efficient because they memoize partial parsing results but suffer from the $a \mid ab$ quirk where alternative ab is silently never matchable.

To improve general parsing performance, Tomita [24] introduced GLR, a general algorithm based upon LR(k) that conceptually forks subparsers at each conflicting LR(k) state at parse-time to explore all possible paths. Tomita shows GLR to be 5x to 10x faster than Earley. A key component of GLR parsing is the graph-structured stack (GSS) [24] that prevents parsing the same input twice in the same way. (GLR pushes input symbols and LR states on the GSS whereas ALL(*) pushes ATN states.) Elkhound [17] introduced hybrid GLR parsers that use a single stack for all LR(1) decisions and flip to a GSS when necessary to match ambiguous portions of the input. (Elkhound parsers are faster than those of other GLR tools in our experiments.) GLL [23] is the LL analog of GLR and also uses subparsers and a GSS to explore all possible paths; GLL uses k=1 lookahead where possible for efficiency. GLL is $O(n^3)$ and GLR is $O(n^{p+1})$ where p is the length of the longest production in the grammar.

Earley parsers scale gracefully from O(n) for deterministic grammars to $O(n^3)$ in the worst case for ambiguous grammars but performance is not good enough for general use. LR(k) state machines can improve the performance of such parsers by statically computing as much as possible. LRE [15] is one such example. Despite these optimizations, general algorithms are still very slow compared to deterministic parsers augmented with deep lookahead.

The problem with arbitrary lookahead is that it is impossible to compute statically for many useful grammars (the LL-regular condition is undecidable.) By shifting lookahead analysis to parse-time, ALL(*) gains the power to handle any grammar without left recursion because it can launch subparsers to determine which path leads to a valid parse. Unlike GLR, speculation stops when all remaining subparsers are associated with a single alternative production, thus, computing the minimum lookahead sequence. To get performance, ALL(*) records a mapping from that lookahead sequence to the predicted production using a DFA for use by subsequent decisions. The context-free language subsets encountered during a parse are finite and, therefore, ALL(*) lookahead languages are regular. Ancona $et\ al\ [1]$ also performed parse-time analysis, but they only computed fixed LR(k) lookahead and did not adapt to the actual input as ALL(*) does. Perlin [21] operated on an RTN like ALL(*) and computed k=1 lookahead during the parse.

ALL(*) is similar to Earley in that both are top-down and operate on a representation of the grammar at parse-time, but Earley is parsing not computing lookahead DFA. In that sense, Earley is not performing grammar analysis. Earley also does not manage an explicit GSS during the parse. Instead, items in Earley states have "parent pointers" that refer to other states that, when threaded together, form a GSS. Earley's SCANNER operation correspond to ALL(*)'s move function. The PREDICTOR and COMPLETER operations correspond to push and pop operations in ALL(*)'s closure function. An Earley state is the set of all parser configurations reachable at some absolute input depth whereas an ALL(*) DFA state is a set of configurations reachable from a lookahead depth relative to the current decision. Unlike the completely general algorithms, ALL(*) seeks a single parse of the input, which allows the use of an efficient LL stack during the parse.

Parsing strategies that continuously speculate or support ambiguity have difficulty with mutators because they are hard to undo. A lack of mutators reduces the generality of semantic predicates that alter the parse as they cannot test arbitrary state computed previously during the parse. *Rats!* [10] supports restricted semantic predicates and Yakker [12] supports semantic predicates that are functions of previously-parsed terminals. Because *ALL(*)* does not speculate during the actual parse, it supports arbitrary mutators and semantic predicates. Space considerations preclude a more detailed discussion of related work here; a more detailed analysis can be found in reference [18].

10. Conclusion

ANTLR 4 generates an ALL(*) parser for any CFG without indirect or hidden left-recursion. ALL(*) combines the simplicity, efficiency, and predictability of conventional top-down LL(k) parsers with the power of a GLR-like mechanism to make parsing decisions. The critical

innovation is to shift grammar analysis to parse-time, caching analysis results in lookahead DFA for efficiency. Experiments show ALL(*) outperforms general parsers (parsing Java) by orders of magnitude and exhibits linear time and space behavior in practice for 8 languages. In theory, ALL(*) is $O(n^4)$, inline with the low polynomial bound of GLR. ANTLR is widely used in practice, indicating that ALL(*) provides practical parsing power without sacrificing the flexibility and simplicity of recursive-descent parsers desired by programmers.

11. Acknowledgments

We thank Elizabeth Scott, Adrian Johnstone, and Mark Johnson for discussions on parsing algorithm complexity. Eelco Visser and Jurgen Vinju provided code for testing isolated parsers from JSGLR and Rascal. Etienne Gagnon generated the SableCC Java parser.

A. Correctness and complexity analysis

Theorem A.1. ALL(*) languages are closed under union.

Proof. Let predicated grammars $G_1 = (N_1, T, P_1, S_1, \Pi_1, \mathcal{M}_1)$ and $G_2 = (N_2, T, P_2, S_2, \Pi_2, \mathcal{M}_2)$ describe $L(G_1)$ and $L(G_2)$, respectively. For applicability to both parsers and scannerless parsers, assume that the terminal space T is the set of valid characters. Assume $N_1 \cap N_2 = \emptyset$ by renaming nonterminals if necessary. Assume that the predicates and mutators of G_1 and G_2 operate in disjoint environments, S_1 and S_2 . Construct:

$$G' = (N_1 \cup N_2, T, P_1 \cup P_2, S', \Pi_1 \cup \Pi_2, \mathcal{M}_1 \cup \mathcal{M}_2)$$

with
$$S' = S_1 | S_2$$
. Then, $L(G') = L(G_1) \cup L(G_2)$.

Lemma A.1. The ALL(*) parser for non-left-recursive G with lookahead DFA deactivated recognizes sentence w iff $w \in L(G)$.

Proof. The ATN for G recognizes w iff $w \in L(G)$. Therefore, we can equivalently prove that ALL(*) is a faithful implementation of an ATN. Without lookahead DFA, prediction is a straightforward ATN simulator: a top-down parser that makes accurate parsing decisions using GLR-like subparsers that can examine the entire remaining input and ATN submachine call stack.

Theorem A.2. (Correctness). The ALL(*) parser for non-left-recursive G recognizes sentence w iff $w \in L(G)$.

Proof. Lemma **??** shows that an ALL(*) parser correctly recognizes w without the DFA cache. The essence of the proof then is to show that ALL(*)'s adaptive lookahead DFA do not break the parse by giving different prediction decisions than straightforward ATN simulation. We only need to consider the case of unpredicated SLL parsing as ALL(*) only caches decision results in this case.

if case: By induction on the state of the lookahead DFA for any given decision A. Base case. The first prediction for A begins with an empty DFA and must activate ATN simulation to choose alternative α_i using prefix $u \leq w_r$. As ATN simulation yields proper predictions, the ALL(*) parser correctly predicts α_i from a cold start and then records the mapping from u:i in the DFA. If there is a single viable alternative, i is the associated production number. If ATN simulation finds multiple viable alternatives, i is the minimum production number associated with alternatives from that set.

Induction step. Assume the lookahead DFA correctly predicts productions for every u prefix of w_r seen by the parser at A. We must show that starting with an existing DFA, ALL(*) properly adds a path through the DFA for unfamiliar u prefix of w'_r . There are several cases:

1. $u \leq w'_r$ and $u \leq w_r$ for a previous w_r . The lookahead DFA gives the correct answer for u by induction assumption. The DFA is not updated.

- 2. $w'_r = bx$ and all previous $w_r = ay$ for some $a \neq b$. This case reduces to the cold-start base case because there is no $D_0 \xrightarrow{b} D$ edge. ATN simulation predicts α_i and adds path for $u \leq w'_r$ from D_0 to f_i .
- 3. $w_r' = vax$ and $w_r = vby$ for some previously seen w_r with common prefix v and $a \neq b$. DFA simulation reaches D from D_0 for input v. D has an edge for b but not a. ATN simulation predicts α_i and augments the DFA, starting with an edge on a from D leading eventually to f_i .

only if case: The ALL(*) parser reports a syntax error for $w \notin L(G)$. Assume the opposite, that the parser successfully parses w. That would imply that there exists an ATN configuration derivation sequence $(\mathbb{S}, p_S, [], w) \mapsto^* (\mathbb{S}', p_S', [], \epsilon)$ for w through G's corresponding ATN. But that would require $w \in L(G)$, by Definition \ref{log} . Therefore the ALL(*) parser reports a syntax error for w. The accuracy of the ALL(*) lookahead cache is irrelevant because there is no possible path through the ATN or parser. \square

Lemma A.2. The set of viable productions for LL is always a subset of SLL's viable productions for a given decision A and remaining input string w_r .

Proof. If the key *move-closure* analysis operation does not reach stop state p'_A for submachine A, SLL and LL behave identically and so they share the same set of viable productions.

If closure reaches the stop state for the decision entry rule, p_A' , there are configurations of the form $(p_A', -, \gamma)$ where, for convenience, the usual GSS Γ is split into single stacks, γ . In LL prediction mode, $\gamma = \gamma_0$, which is either a single stack or empty if A = S. In SLL mode, $\gamma = \#$, signaling no stack information. Function closure must consider all possible γ_0 parser call stacks. Since any single stack must be contained within the set of all possible call stacks, LL closure operations consider at most the same number of paths through the ATN as SLL.

Lemma A.3. For $w \notin L(G)$ and non-left-recursive G, SLL reports a syntax error.

Proof. As in the *only if case* of Theorem ??, there is no valid ATN configuration derivation for w regardless of how *adaptivePredict* chooses productions.

Theorem A.3. Two-stage parsing for non-left-recursive G recognizes sentence w iff $w \in L(G)$.

Proof. By Lemma $\ref{lem:proof:eq:lem:pro$

- 1. If $min(\mathcal{V}) = min(\mathcal{V}')$, *SLL* and *LL* choose the same production. *SLL* succeeds for w. E.g., $\mathcal{V} = \{1, 2, 3\}$ and $\mathcal{V}' = \{1, 3\}$ or $\mathcal{V} = \{1\}$ and $\mathcal{V}' = \{1\}$.
- 2. If $min(\mathcal{V}) \neq min(\mathcal{V}')$ then $min(\mathcal{V}) \notin \mathcal{V}'$ because LL finds $min(\mathcal{V})$ nonviable. SLL would report a syntax error. E.g., $\mathcal{V} = \{1, 2, 3\}$ and $\mathcal{V}' = \{2, 3\}$ or $\mathcal{V} = \{1, 2\}$ and $\mathcal{V}' = \{2\}$.

In all possible combinations of \mathcal{V} and \mathcal{V}' , SLL behaves like LL or reports a syntax error for $w \in L(G)$.

Lemma A.4. A GSS has O(n) nodes for n input symbols.

Proof. For nonterminals N and ATN states Q, there are $|N| \times |Q|$ $p \xrightarrow{A} q$ ATN transitions if every every grammar position invokes every nonterminal. That limits the number of new GSS nodes to $|Q|^2$ for a closure operation (which cannot transition terminal edges). ALL(*) performs n+1 closures for n input symbols giving $|Q|^2(n+1)$ nodes or O(n) as Q is not a function of the input.

Lemma A.5. Examining a lookahead symbol has $O(n^2)$ time.

Proof. Lookahead is a *move-closure* operation that computes new target DFA state D' as a function of the ATN configurations in D. There are $|Q| \times m \approx |Q|^2$ configurations of the form $(p,i,_) \in D$ for |Q| ATN states and m alternative productions in the current decision. The cost of *move* is not a function of input size n. Closure of D computes $closure(c) \ \forall \ c \in D$ and closure(c) can walk the entire GSS back to the root (the empty stack). That gives a cost of $|Q|^2$ configurations times $|Q|^2(n+1)$ GSS nodes (per Lemma ??) or O(n) add operations to build D'. Adding a configuration is dominated by the graph merge, which (in our implementation) is proportional to the depth of the graph. The total cost for move-closure is $O(n^2)$.

Theorem A.4. ALL(*) parsing of n input symbols has $O(n^4)$ time.

Proof. Worst case, the parser must examine all remaining input symbols during prediction for each of n input symbols giving $O(n^2)$ lookahead operations. The cost of each lookahead operation is $O(n^2)$ by Lemma ?? giving overall parsing cost $O(n^4)$.

B. Left-recursion elimination

ANTLR supports directly left-recursive rules by rewriting them to a non-left-recursive version that also removed any ambiguities. For example, the natural grammar for describing arithmetic expression syntax is one of the most common (ambiguous) left-recursive rules. The following grammar supports simple modulo and additive expressions.

$$E \rightarrow E\%E \,|\, E{+}E \,|\, \mathbf{id}$$

E is directly left-recursive because at least one production begins with E ($\exists E \Rightarrow E\alpha$), which is a problem for top-down parsers.

Grammars meant for top-down parsers must use a cumbersome non-left-recursive equivalent instead that has a separate nonterminal for each level of operator precedence:

$$E' \to M \ (+M)^*$$
 Additive, lower precedence $M \to P \ (\% \ P)^*$ Modulo, higher precedence $P \to \mathbf{id}$ Primary (\mathbf{id} means identifier)

The deeper the rule invocation, the higher the precedence. At parsetime, matching a single identifier, a, requires l rule invocations for l precedence levels.

E is easier to read than E', but the left-recursive version is ambiguous as there are two interpretations of input a+b+c as shown in (a) and (b) of Figure ??. Bottom-up parser generators such as bison use operator precedence specifiers (e.g., %left '%') to resolve such ambiguities. The non-left-recursive grammar is unambiguous because it implicitly encodes precedence rules according to the nonterminal nesting depth.

Ideally, a parser generator would support left-recursion and provide a way to resolve ambiguities implicitly with the grammar itself without resorting to external precedence specifiers. ANTLR does this by rewriting nonterminals with direct left-recursion and inserting semantic predicates to resolve ambiguities according to the order of productions. The rewriting process leads to generated parsers that mimic Clarke's [?] technique.

We chose to eliminate just direct left-recursion because general left-recursion elimination can result in transformed grammars orders of magnitude larger than the original [?] and yields parse trees only

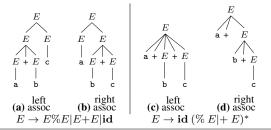


Figure 14. Parse trees for 1+2+3 in ambiguous left-recursive and non-left-recursive E nonterminals

loosely related to those of the original grammar. ANTLR automatically constructs parse trees appropriate for the original left-recursive grammar so the programmer is unaware of the internal restructuring. Direct left-recursion also covers the most common grammar cases (from long experience building grammars). This discussion focuses on grammars for arithmetic expressions, but the transformation rules work just as well for other left-recursive constructs such as C declarators: $D \to *D$, $D \to D$ [], $D \to D$ (), $D \to id$.

Eliminating direct left-recursion without concern for ambiguity is straightforward [?]. Let $A \to \alpha_j$ for j = 1...s be the non-left-recursive productions and $A \to A\beta_k$ for k = 1...r be the directly left-recursive productions where α_j , $\beta_k \not\Rightarrow^* \epsilon$. Replace those productions with:

$$A \to \alpha_1 A' | \dots | \alpha_s A' A' \to \beta_1 A' | \dots | \beta_r A' | \epsilon$$

The transformation is easier to see using EBNF:

$$\begin{array}{l} A \rightarrow A'A''^* \\ A' \rightarrow \alpha_1|...|\alpha_s \\ A'' \rightarrow \beta_1|...|\beta_r \end{array}$$

or just $A \to (\alpha_1|...|\alpha_s)(\beta_1|...|\beta_r)^*$. For example, the left-recursive E rule becomes:

$$E \to id \ (\% \ E \ | + E)^*$$

This non-left-recursive version is still ambiguous because there are two derivations for a+b+c as shown in parse trees (c) and (d) of Figure ??. (c) interprets the input as left-associative (a+b)+c whereas (d) interprets it as right-associative a+(b+c). The default ambiguity resolution policy chooses to match input as soon as possible, resulting in interpretation (d).

The difference in associativity does not matter for expressions using a single operator, but expressions with a mixture of operators must associate operands and operators according to operator precedence. For example, the parser must recognize a%b+c as (a%b)+c not a%(b+c). The two interpretations are shown in Figure ??.

To choose the appropriate interpretation, the generated parser must compare the previous operator's precedence to the current operator's precedence in the $(\% E \mid + E)^*$ "loop." In Figure $\ref{fig:precedence}$ is the critical expansion of E. It must match just \mathbf{id} and return immediately, allowing the invoking E to match the + to form the parse tree in $\mathbf{(a)}$ as opposed to $\mathbf{(b)}$.

To support such comparisons, productions get precedence numbers that are the reverse of production numbers. The precedence of the i^{th} production is n-i+1 for n original productions of E. That assigns precedence 3 to $E \to E \% E$, precedence 2 to $E \to E + E$, and precedence 1 to $E \to \mathbf{id}$.

Next, each nested invocation of E needs information about the operator precedence from the invoking E. The simplest mechanism is to pass a precedence parameter, pr, to E and require: An expansion of E[pr] can match only those subexpressions whose precedence meets or exceeds pr.

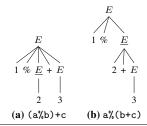


Figure 15. Parse trees for input a%b+c and $E \to id$ (% E|+E)*

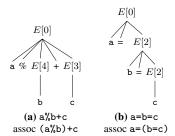


Figure 16. Nonterminal Invocation Trees for $E[pr] \rightarrow \mathbf{id}$ ($\{3 \ge pr\}$? $\%E[4] | \{2 \ge pr\}$? + E[3])*

To enforce this, the left-recursion elimination procedure inserts predicates into the $(\% E \mid +E)^*$ loop. Here is the transformed unambiguous and non-left-recursive rule:

$$E[pr] \to id (\{3 \ge pr\}? \%E[4] | \{2 \ge pr\}? + E[3])^*$$

References to E elsewhere in the grammar become E[0]; e.g., $S \to E$ becomes $S \to E[0]$. Input a%b+c yields the parse tree for E[0] shown in (a) of Figure ??.

Production " $\{3 \geq pr\}$? %E[4]" is viable when the precedence of the modulo operation, 3, meets or exceeds parameter pr. The first invocation of E has pr=0 and, since $3 \geq 0$, the parser expands "%E[4]" in E[0].

When parsing invocation E[4], predicate $\{2 \ge pr\}$? fails because the precedence of the + operator is too low: $2 \not\ge 4$. Consequently, E[4] does not match the + operator, deferring to the invoking E[0].

A key element of the transformation is the choice of E parameters, E[4] and E[3] in this grammar. For left-associative operators like % and +, the right operand gets one more precedence level than the operator itself. This guarantees that the invocation of E for the right operand matches only operations of higher precedence.

For right-associative operations, the E operand gets the same precedence as the current operator. Here is a variation on the expression grammar that has a right-associative assignment operator instead of the addition operator:

$$E \rightarrow E \% E \mid E =^{right} E \mid \mathbf{id}$$

where notation $=_{right}$ is a shorthand for the actual ANTLR syntax of '='<assoc=right>. The interpretation of a=b=c should be right associative, a=(b=c). To get that associativity, the transformed rule need differ only in the right operand, E[2] versus E[3]:

$$E[pr] \to id (\{3 \ge pr\}? \% E[4] | \{2 \ge pr\}? = E[2])^*$$

The E[2] expansion can match an assignment, as shown in **(b)** of Figure $\ref{eq:condition}$, since predicate $2\geq 2$ is true.

Unary prefix and suffix operators are fixed as right- and left-associative, respectively. Consider the following E with negation prefix and "not" suffix operators.

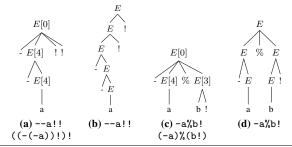


Figure 17. Nonterminal call trees and parse trees for $E \rightarrow -E \mid E \mid \mid E\%E \mid \mathbf{id}$

$$E \rightarrow -E \mid E \mid \mid E \% E \mid \mathbf{id}$$

Prefix operators are not left recursive and so they go into the first subrule whereas left-recursive suffix operators go into the predicated loop like binary operators:

$$\begin{array}{ll} E[pr] \to & (\mathbf{id} \mid -E[4]) \\ & (\{3 \geq pr\}? \: ! \mid \{2 \geq pr\}? \: \% \: E[3])^* \end{array}$$

Figure ?? illustrates the rule invocation tree (a record of the call stacks) and associated parse trees resulting from an ANTLR-generated parser. Unary operations in contiguous productions all have the same relative precedence and are, therefore, "evaluated" in the order specified. E.g., $E \rightarrow -E \mid +E \mid \text{id}$ must interpret -+a as -(+a) not +(-a).

B.1 Formal Left-Recursion Elimination Rules

ANTLR eliminates directly left-recursive nonterminals and resolves ambiguities using the rules in Figure \ref{figure} where X^{assoc} captures the associativity specified in the ANTLR meta-language for X. Nonconforming left-recursive productions $E \to E$ or $E \to \epsilon$ are rewritten without concern for ambiguity using the typical elimination technique. Hidden and indirect left-recursion results in static left-recursion errors from ANTLR.

Because of the need to resolve ambiguities with predicates and A invocation parameters, ANTLR looks for patterns within the $A \to A\beta_k$ and $A \to \alpha_j$ productions. The subscript on productions, A_i , captures the production number in the original grammar when needed. The transformation from G to G' is as follows:

- 1. strip away directly left-recursive nonterminal references
- 2. collect prefix and "other" productions into newly-created A'
- 3. collect binary, ternary, and suffix productions into newly-created $A^{\prime\prime}$
- 4. prefix productions in A'' with precedence-checking semantic predicate $\{pr(i)>= pr\}$?
- 5. rewrite A references among binary, ternary, and prefix productions as A[nextpr(i,assoc)]
- 6. rewrite any other A references within any production in P (including A' and A'') as A[0]
- 7. rewrite the original A rule as $A[pr] \rightarrow A'A''^*$

$$Binary \frac{A_i \rightarrow A \ (\mathbf{op_1}|...|\mathbf{op_m})^{assoc} \ A}{A'' \rightarrow \{pr(i) >= \mathbf{pr}\}? \ (\mathbf{op_1}|...|\mathbf{op_m}) \ A[nextpr(i,assoc)]}$$

$$Ternary \frac{A_i \rightarrow A \ \mathbf{op_1^{assoc}} \ A \ \mathbf{op_2} \ A}{A'' \rightarrow \{pr(i) >= \mathbf{pr}\}? \ \mathbf{op_1} A[0] \ \mathbf{op_2} \ A[nextpr(i,assoc)]}$$

$$Unary \ suffix \frac{A_i \rightarrow Ax}{A'' \rightarrow \{pr(i) >= \mathbf{pr}\}? \ x}$$

$$Unary \ prefix \frac{A_i \rightarrow xA}{A' \rightarrow xA[nextpr(i,right)]}$$

$$Grouping \frac{A \rightarrow xAy}{A' \rightarrow xA[0] \ y}$$

$$Other \frac{A \rightarrow \alpha, \ \alpha \neq \alpha' A\alpha''}{A' \rightarrow \alpha}$$

$$Unclassified \ ref \frac{B \rightarrow \delta \ A \ \delta', \ B \in N}{\Rightarrow B \rightarrow \delta \ A[0] \ \delta'}$$

$$Rule \ rewrite \frac{A \rightarrow A\beta_1|...|A\beta_r|\alpha_1|...|\alpha_s}{\Rightarrow A[\mathbf{p}] \rightarrow A'A''*}$$

$$pr(i) = \{n - i + 1\}$$

$$nextpr(i,assoc) = \{assoc == left? \ i + 1 : i\}$$

Figure 18. Direct Left-Recursion Elimination Rules

References

- [1] ANCONA, M., DODERO, G., GIANUZZI, V., AND MORGAVI, M. Efficient construction of LR(k) states and tables. *ACM Trans. Program. Lang. Syst. 13*, 1 (Jan. 1991), 150–178.
- [2] ANONYMOUS. Additional materials available as part of submission.
- [3] BERMUDEZ, M. E., AND SCHIMPF, K. M. Practical arbitrary lookahead *LR* parsing. *Journal of Computer and System Sciences* 41, 2 (1990).
- [4] BROWN, S., AND VRANESIC, Z. Fundamentals of Digital Logic with Verilog Design. McGraw-Hill series in ECE. 2003.
- [5] CHARLES, P. A Practical Method for Constructing Efficient LALR(k) Parsers with Automatic Error Recovery. PhD thesis, New York University, New York, NY, USA, 1991.
- [6] CLEVELAND, W. S. Robust Locally Weighted Regression and Smoothing Scatterplots. *Journal of the American Statistical Association* 74 (1979), 829–836.
- [7] COHEN, R., AND CULIK, K. LR-Regular grammars—an extension of LR(k) grammars. In SWAT '71 (Washington, DC, USA, 1971), IEEE Computer Society, pp. 153–165.
- [8] EARLEY, J. An efficient context-free parsing algorithm. Communications of the ACM 13, 2 (1970), 94–102.
- [9] FORD, B. Parsing Expression Grammars: A recognition-based syntactic foundation. In *POPL* (2004), ACM Press, pp. 111–122.
- [10] GRIMM, R. Better extensibility through modular syntax. In *PLDI* (2006), ACM Press, pp. 38–51.
- [11] JARZABEK, S., AND KRAWCZYK, T. *LL*-Regular grammars. *Information Processing Letters* 4, 2 (1975), 31 37.
- [12] JIM, T., MANDELBAUM, Y., AND WALKER, D. Semantics and algorithms for data-dependent grammars. In POPL (2010).
- [13] JOHNSON, M. The computational complexity of GLR parsing. In Generalized LR Parsing, M. Tomita, Ed. Kluwer, Boston, 1991, pp. 35–42.
- [14] KIPPS, J. Generalized LR Parsing. Springer US, 1991, pp. 43-59.
- [15] MCLEAN, P., AND HORSPOOL, R. N. A faster Earley parser. In CC (1996), Springer, pp. 281–293.
- [16] MCPEAK, S. Elkhound: A fast, practical GLR parser generator. Tech. rep., University of California, Berkeley (EECS), Dec. 2002.
- [17] MCPEAK, S., AND NECULA, G. C. Elkhound: A fast, practical GLR parser generator. In CC (2004), pp. 73–88.
- [18] PARR, T., AND FISHER, K. LL(*): The Foundation of the ANTLR Parser Generator. In *PLDI* (2011), pp. 425–436.

- [19] PARR, T. J. Obtaining practical variants of LL(k) and LR(k) for k>1 by splitting the atomic k-tuple. PhD thesis, Purdue University, West Lafayette, IN, USA, 1993.
- [20] PARR, T. J., AND QUONG, R. W. Adding Semantic and Syntactic Predicates to LL(k)—pred-LL(k). In CC (1994).
- [21] PERLIN, M. LR recursive transition networks for Earley and Tomita parsing. In *Proceedings of the 29th Annual Meeting on Association for Computational Linguistics* (1991), ACL '91, pp. 98–105.
- [22] PLEVYAK, J. DParser: GLR parser generator, Visited Oct. 2013.
- [23] SCOTT, E., AND JOHNSTONE, A. GLL parsing. *Electron. Notes Theor. Comput. Sci. 253*, 7 (Sept. 2010), 177–189.
- [24] TOMITA, M. Efficient Parsing for Natural Language. Kluwer Academic Publishers, 1986.
- [25] WOODS, W. A. Transition network grammars for natural language analysis. Communications of the ACM 13, 10 (1970), 591–606.