

## CS-GY 6133

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**(a) Data-flow graph**

In our graph,  $\text{fa}(n)$  means that register a contains value n. After the code executes, the result should be:

**R[f0]=0, R[f1]=1, R[f2]=0, R[f3]=3, R[f4]=4, R[f5]=5.**

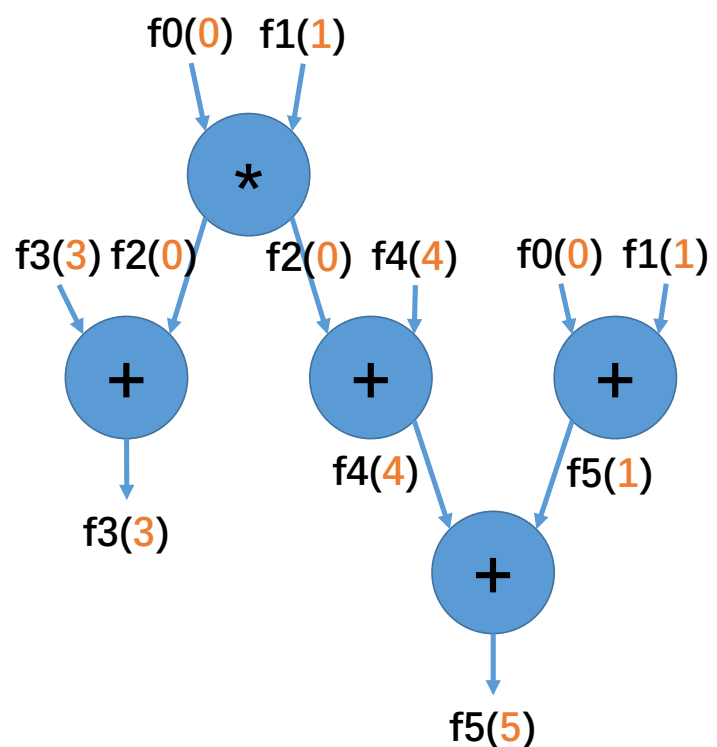
**T0:** `muld f0, f1, f2`

**T1:** `addd  $f_0$ ,  $f_1$ ,  $f_5$`

**T2:** `adddd  $f_2, f_3, f_3$`

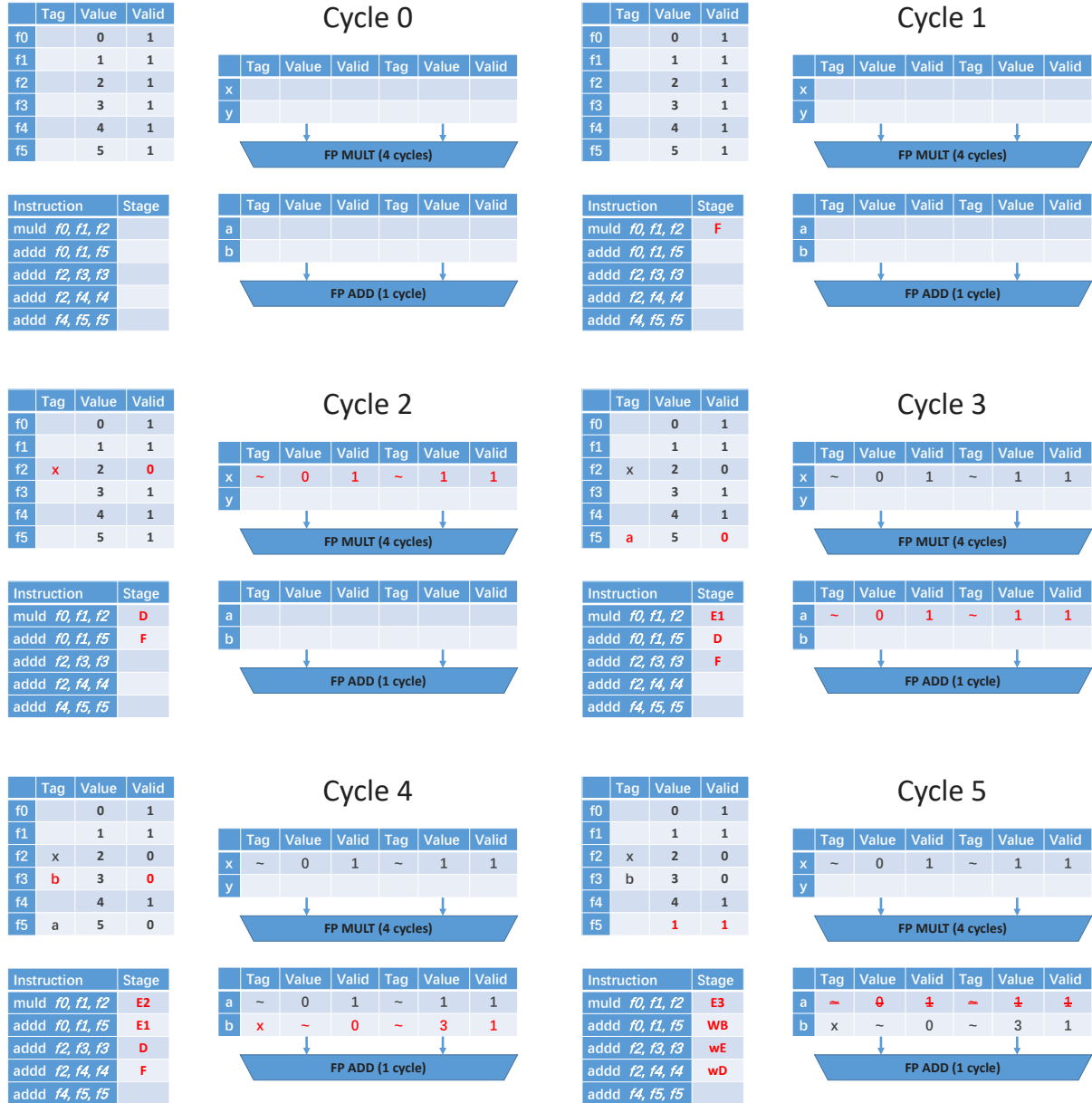
**T3:** `addd f2, f4, f4`

**T4:** `addd f4, f5, f5`



**(b) Simulate cycle-by-cycle**

In the table below, '**wE**' means waiting to execute (RAW dependency, waiting in reservation stations); '**wD**' means waiting to decode/dispatch (reservation stations are full, instruction stalling).



	Tag	Value	Valid
f0		0	1
f1		1	1
f2	x	2	0
f3	b	3	0
f4	a	4	0
f5		1	1

## Cycle 6

	Tag	Value	Valid	Tag	Value	Valid
x	~	0	1	~	1	1
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	E4
add f0, f1, f5	~
add f2, f3, f3	wE
add f2, f4, f4	D
add f4, f5, f5	F

	Tag	Value	Valid	Tag	Value	Valid
a	x	~	0	~	4	1
b	x	~	0	~	3	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3	b	3	0
f4	a	4	0
f5		1	1

## Cycle 7

	Tag	Value	Valid	Tag	Value	Valid
x	~	0	1	~	1	1
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	WB
add f0, f1, f5	~
add f2, f3, f3	wE
add f2, f4, f4	wE
add f4, f5, f5	wD

	Tag	Value	Valid	Tag	Value	Valid
a	~	0	1	~	4	1
b	~	0	1	~	3	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3	b	3	0
f4	a	4	0
f5		1	1

## Cycle 8

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	E1
add f2, f4, f4	wE
add f4, f5, f5	wD

	Tag	Value	Valid	Tag	Value	Valid
a	~	0	1	~	4	1
b	~	0	1	~	3	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4	a	4	0
f5		1	1

## Cycle 9

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	WB
add f2, f4, f4	E1
add f4, f5, f5	wD

	Tag	Value	Valid	Tag	Value	Valid
a	~	0	1	~	4	1
b	~	0	1	~	3	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	b	1	0

## Cycle 10

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	~
add f2, f4, f4	WB
add f4, f5, f5	D

	Tag	Value	Valid	Tag	Value	Valid
a	~	0	1	~	4	1
b	~	4	1	~	1	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	b	1	0

## Cycle 11

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	~
add f2, f4, f4	~
add f4, f5, f5	E1

	Tag	Value	Valid	Tag	Value	Valid
a						
b	~	4	1	~	1	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

## Cycle 12

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	~
add f2, f4, f4	~
add f4, f5, f5	WB

	Tag	Value	Valid	Tag	Value	Valid
a						
b	~	4	1	~	1	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

## Cycle 13

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

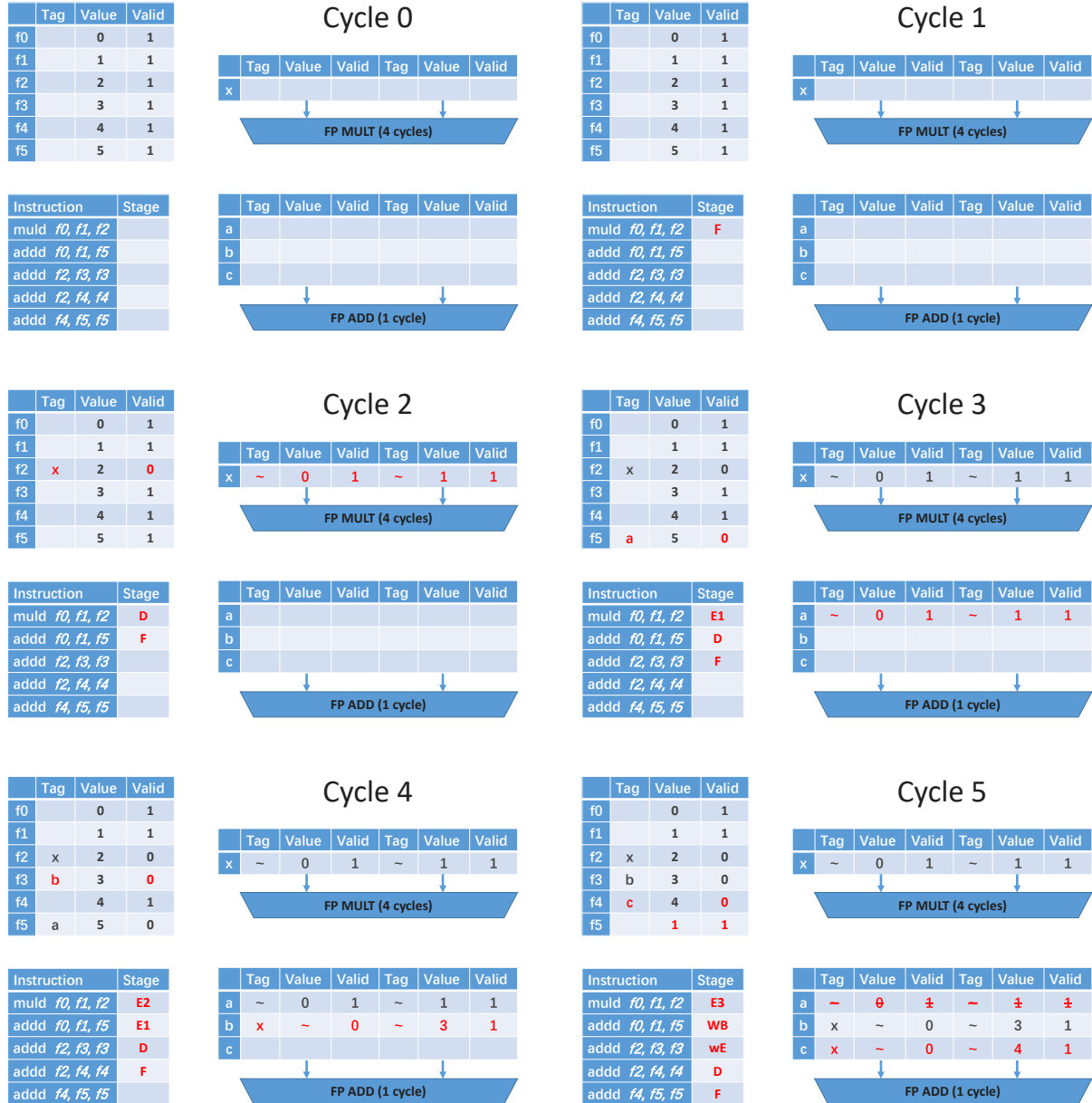
Instruction	Stage
muld f0, f1, f2	~
add f0, f1, f5	~
add f2, f3, f3	~
add f2, f4, f4	~
add f4, f5, f5	~

	Tag	Value	Valid	Tag	Value	Valid
a						
b						

FP ADD (1 cycle)

**(c) Simulate cycle-by-cycle without stalling**

At (b) - cycle 7 we found that FP ADD reservation station was full. The instruction had to wait until a free station was released. So we have to add one more station to FP ADD. We can also observe that FP MULT only need one reservation station at least.



	Tag	Value	Valid
f0		0	1
f1		1	1
f2	x	2	0
f3	b	3	0
f4	c	4	0
f5	a	1	0

Cycle 6

	Tag	Value	Valid	Tag	Value	Valid
x	~	0	1	~	1	1

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	E4
addd f0, f1, f5	~
addd f2, f3, f3	wE
addd f2, f4, f4	wE
addd f4, f5, f5	D

	Tag	Value	Valid	Tag	Value	Valid
a	c	~	0	~	1	1
b	x	~	0	~	3	1
c	x	~	0	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3	b	3	0
f4	c	4	0
f5	a	1	0

Cycle 7

	Tag	Value	Valid	Tag	Value	Valid
x	~	0	1	~	1	1

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	WB
addd f0, f1, f5	~
addd f2, f3, f3	wE
addd f2, f4, f4	wE
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	c	~	0	~	1	1
b	~	0	1	~	3	1
c	~	0	1	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3	b	3	0
f4	c	4	0
f5	a	1	0

Cycle 8

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	E1
addd f2, f4, f4	wE
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	c	~	0	~	1	1
b	~	0	1	~	3	1
c	~	0	1	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4	c	4	0
f5	a	1	0

Cycle 9

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	WB
addd f2, f4, f4	E1
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	c	~	0	~	1	1
b	~	0	1	~	3	1
c	~	0	1	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	a	1	0

Cycle 10

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	WB
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b						
c	~	0	1	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	a	1	0

Cycle 11

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	E1

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b						
c						

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

Cycle 12

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	WB

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b						
c						

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

Cycle 13

	Tag	Value	Valid	Tag	Value	Valid
x						

FP MULT (4 cycles)

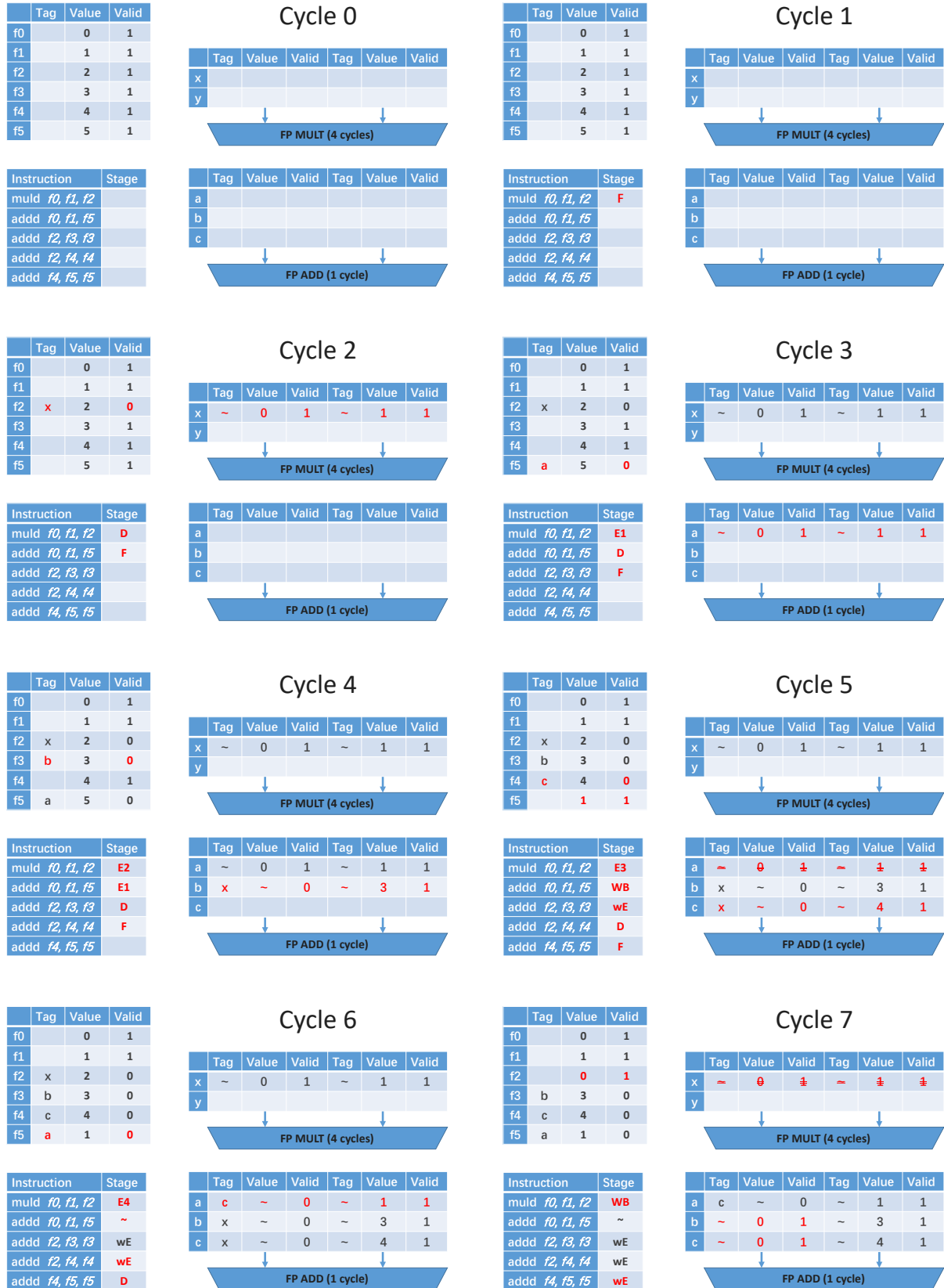
Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	~

	Tag	Value	Valid	Tag	Value	Valid
a						
b						
c						

FP ADD (1 cycle)

**(d) Simulate cycle-by-cycle with parallel FP adders**

After simulation, we found that parallel process was needed at cycle 8. Two instructions could be dispatched at the same time. Thus,  $M = 2$ .



	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3	b	3	0
f4	c	4	0
f5	a	1	0

Cycle 8

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	a	1	0

Cycle 9

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	E1
addd f2, f4, f4	E1
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	c	~	0	~	1	1
b	~	0	1	~	3	1
c	~	0	1	~	4	1

FP ADD (1 cycle)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	WB
addd f2, f4, f4	WB
addd f4, f5, f5	wE

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b	~	0	1	~	3	1
c	~	0	1	~	4	1

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5	a	1	0

Cycle 10

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

Cycle 11

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	E1

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b						
c						

FP ADD (1 cycle)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	WB

	Tag	Value	Valid	Tag	Value	Valid
a	~	4	1	~	1	1
b						
c						

FP ADD (1 cycle)

	Tag	Value	Valid
f0		0	1
f1		1	1
f2		0	1
f3		3	1
f4		4	1
f5		5	1

Cycle 12

	Tag	Value	Valid	Tag	Value	Valid
x						
y						

FP MULT (4 cycles)

Instruction	Stage
muld f0, f1, f2	~
addd f0, f1, f5	~
addd f2, f3, f3	~
addd f2, f4, f4	~
addd f4, f5, f5	~

	Tag	Value	Valid	Tag	Value	Valid
a						
b						
c						

FP ADD (1 cycle)