

Artificial Intelligence I

Lab 6 - Winter Semester 2023 / 2024

<https://moodle.haw-landshut.de/course/view.php?id=10282>

1. Given the datasets

- $S_1 = (\text{yes, yes, yes, no, no, yes, yes, yes, yes, no, no})$
- $S_2 = (\text{yes, yes, yes, no, no, no}) \Rightarrow 3/6 \Rightarrow \text{am Wochenende}$

compute the corresponding entropy values. Which one has the greater entropy and thus more uncertainty?

2. Given the following data set for the skiing classification problem

Day	Snow	Dist	Weekend	Sun	Skiing
1	≤ 100		yes	yes	yes
2	≤ 100		yes	yes	yes
3	≤ 100		yes	no	yes
4	≤ 100		no	yes	yes
5	> 100		yes	yes	yes
6	> 100		yes	yes	yes
7	> 100		yes	yes	no
8	> 100		yes	no	no
9	> 100		no	yes	no
10	> 100		no	yes	no
11	> 100		no	no	no

generate the corresponding decision tree using the ID3-algorithm.

(Handwritten)

$$IG(S, \text{Snow-Dist}) = I(S) - \frac{4}{11} I(S \leq 100) - \frac{7}{11} I(S > 100) = 0,994 - \frac{4}{11} \cdot 0 - \frac{7}{11} \cdot 0,863 = 0,445$$

$$I(S) = -\frac{6}{11} \log_2\left(\frac{6}{11}\right) - \frac{5}{11} \log_2\left(\frac{5}{11}\right) = 0,994$$

$$I(S \leq 100) = 0 = -0 \cdot \log_2(0) - \frac{4}{4} \cdot \log_2\left(\frac{4}{4}\right) \quad (\text{weil immer yes bei Skiing})$$

$$I(S > 100) = -\frac{5}{7} \log_2\left(\frac{5}{7}\right) - \frac{2}{7} \log_2\left(\frac{2}{7}\right) = 0,863$$

$$IG(S, \text{Weekend}) = 0,994 - \frac{7}{11} I(\text{Weekend}_{\text{yes}}) - \frac{4}{11} I(\text{Weekend}_{\text{no}}) = 0,994 - \frac{7}{11} \cdot 0,863 - \frac{4}{11} \cdot 0,811 = 0,15$$

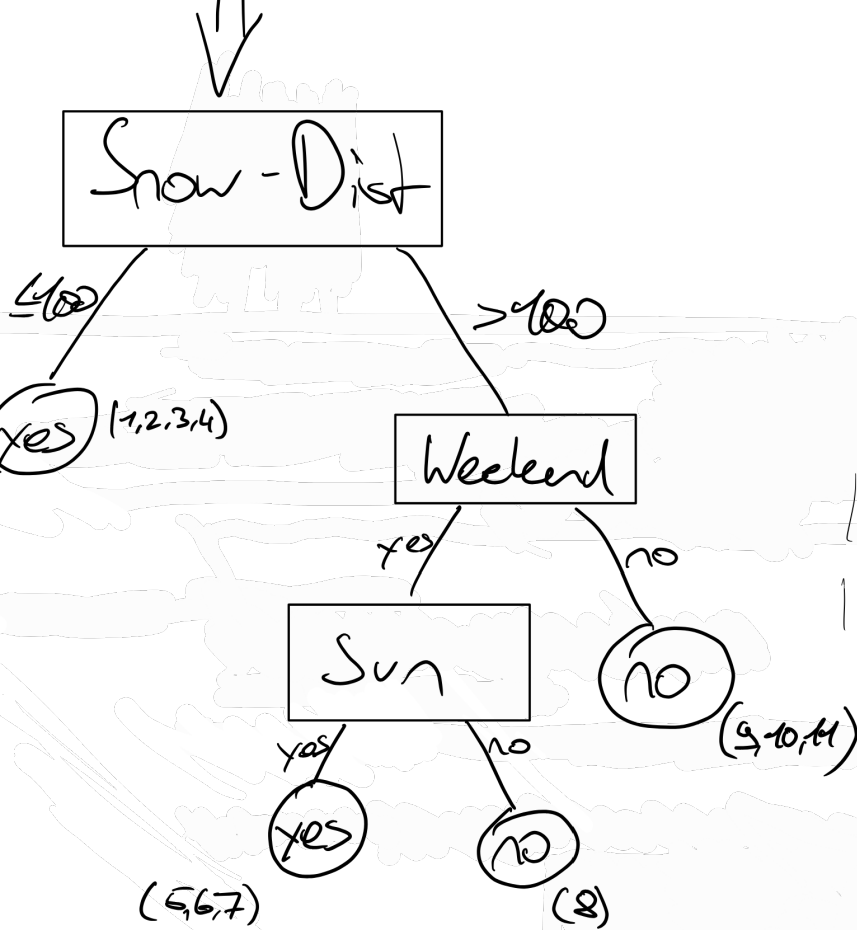
$$\hookrightarrow -\frac{5}{7} \log_2\left(\frac{5}{7}\right) - \frac{2}{7} \log_2\left(\frac{2}{7}\right) = 0,863$$

$$\hookrightarrow -\frac{3}{4} \log_2\left(\frac{3}{4}\right) - \frac{1}{4} \log_2\left(\frac{1}{4}\right) = 0,811$$

$$IG(S, \text{Sun}) = 0,994 - \frac{8}{11} I(\text{Sun}_{\text{yes}}) - \frac{3}{11} I(\text{Sun}_{\text{no}}) = 0,994 - \frac{8}{11} \cdot 0,954 - \frac{3}{11} \cdot 0,918 = 0,049$$

$$\hookrightarrow -\frac{5}{8} \log_2\left(\frac{5}{8}\right) - \frac{3}{8} \log_2\left(\frac{3}{8}\right) = 0,954$$

$$\hookrightarrow -\frac{1}{3} \log_2\left(\frac{1}{3}\right) - \frac{2}{3} \log_2\left(\frac{2}{3}\right) = 0,918$$



Weekend	Sun	Skiing
yes	yes	yes
yes	yes	yes
yes	yes	no
yes	no	no
no	yes	no
no	yes	no
no	no	no

$$I(S) - \frac{4}{7} I(W_{yes}) - \frac{3}{7} I(W_{no}) = 0,292$$

$$I(\text{Snow-Dist}, \text{Sun}) = 0,17$$