

## <시험 암기 및 정리>

### Ch\_5

1. If  $F$  is empty, then return
2. Traverse the subtrees of  $F$  in forest postorder
3. Traverse the remaining trees of  $F$  in forest postorder
4. Visit the root of the first tree of  $F$

### Ch\_6

※  $\langle u, v \rangle$   $u$ : tail(cause),  $v$ : head(effect)

※ complete graph:

undirected:  $n(n-1)/2$

directed:  $n(n-1)$

※ adjacent & incident  $(u, v)$ ,  $\langle u, v \rangle$

undirected:

$u$  and  $v$  are adjacent

$(u, v)$  is incident on  $u$  and  $v$

directed:

$u$  is adjacent to  $v$

$v$  is adjacent from  $u$

$\langle u, v \rangle$  is incident on  $u$  on  $v$

※ path: edge의 열거

a path from  $u$  to  $v$

length of path is the number of edges

simple path: a path where vertices are all distinct

※ cycle:

a simple path which the first and last nodes are same

※ connected:

$u$  and  $v$  are connected if there is a path between  $u$  and  $v$

※ connected graph:

if all pairs of nodes in  $G$  are connected,

then  $G$  is a connected graph

※ connected component:

a maximal connected subgraph which

※ Tree: a graph which has no cycle

※ strongly connected:

directed graph에서 모든 node pairs에 대하여 u에서 v로 가는 path, v에서 u로 가는 path가 존재하면 그 directed graph는 strongly connected graph이다.

※ strongly connected component (clique):

a maximal subgraph that is strongly connected

※ degree:

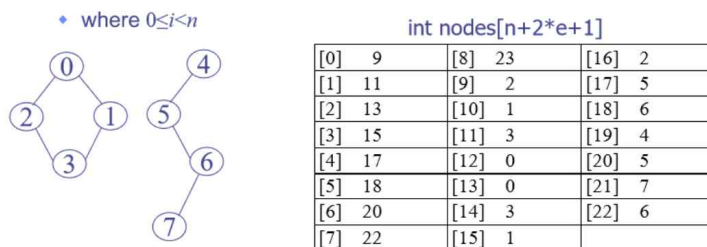
$$e = (\sum_{i=0}^{n-1} d_i) / 2$$

in-degree: edge where v is head

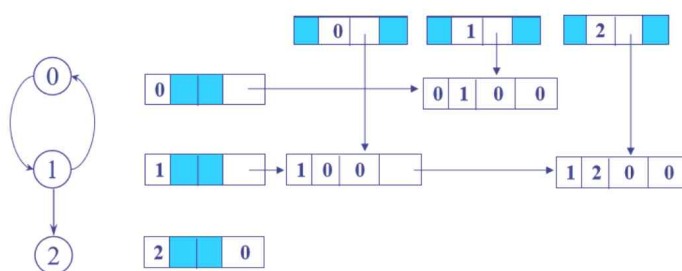
out-degree: edge where v is tail

※ adjacency matrix  $O(n^2) = n^2 - n$

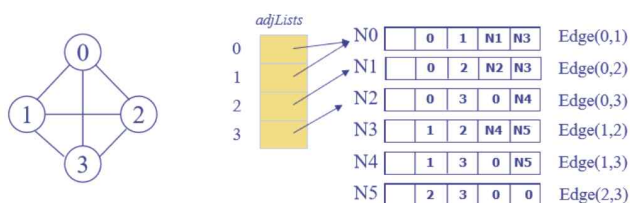
※ adjacency list



tail	head	Column link for head	Row link for tail
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※ adjacency multilist



※ Activity Networks

processor -> successor

## Ch\_7

- ※ sequential search -> 일일이 하나씩 찾음 ->  $O(n)$
- ※ binary search -> order를 이용하여 찾음 ->  $O(\log n)$
- ※ list 비교 -> no order  $O(mn)$
- ※ list 비교 -> order  $O(\max(n \log n, m \log m))$

### ※ decision tree

- > input length =  $n$ ,  $n!$  possible outputs
- >  $n!$  leaves
- >  $\log_2(n!) + 1$  height

### ※ merge sort

recursive: 1을 기준으로 큰 덩어리를 자른다.

iterative:

(십진수, 3자리수 기준)

- ※ radix sort의 TC는  $O(d(n+r))$

Method	Worst	Average
Insertion sort	$n^2$	$n^2$
Heap sort	$n \log n$	$n \log n$
Merge sort	$n \log n$	$n \log n$
Quick sort	$n^2$	$n \log n$

- ※ radix sort에서  $r$ 은 10,  $d$ 는 3,  $n$ 은 element의 수이다.

## Ch\_8

- ※ overflow: pair를 넣을 때 bucket이 이미 꽉 차 있을 때를 의미
- ※ collision: pair를 넣을 때 bucket에 이미 뭐가 있을 때를 의미

- ※ Division:  $h(n) = ((k) \% (\text{prime\#})) \% b$

- ※ Mid-Square: 제곱해서 중간을 자름 ->  $r$ 자리수이면  $0 \sim 2^r - 1$ 가  $h(k)$ 의 범위이다.

- ※ Folding(shift folding): 1234567890129384 -> 123+456+789+012+938+4

- ※ Folding(Folding at boundaries):

1234567890129384 -> 123+456+789+012+938+4 -> 123+654+789+210+938+4

- ※ overflow handling (Open addressing)

->

- ※ linear proving ->  $ht[(h(k)+i) \% b]$  ( $0 \leq i \leq b-1$ )

-> expected key comparisons =  $p = (2-a)/(2-2a)$ ,  $a=n/sb$

-> 이미 가득 차 있으면  $ht$ 를 두배로 늘림

- ※ quadratic proving ->  $ht[(h(k)+i^2) \% b]$  ( $0 \leq i \leq (b-1)/2$ )

- ※ Rehashing: 여러 hash함수를 놓고, overflow되면 다른 걸 쓴다.

※ overflow handling (Chaining)

->the number of comparisons needed to search:  $/n$

[0]	→ acos atoi atol
[1]	→ NULL
[2]	→ char ceil cos ctime
[3]	→ define
[4]	→ exp
[5]	→ float floor
[6]	→ NULL
...	
[25]	→ NULL

1: acos, char, define, exp, float

2: atoi, ceil, floor

3: atol, cos

4: ctime

->  $1*5+2*3+3*2+4*1=5+6+6+4=21$

$21/n = 21/11$

※ Dynamic hashing

$k$	$h(k)$
A0	100 000
A1	100 001
B0	101 000
B1	101 001
C1	110 001
C2	110 010
C3	110 011
C4	110 101

->  $h(C4,4)=0101(2)=5$

$h(k, p) \rightarrow b=2^p$ , size of directory =  $2^p$ , directory depth =  $p$

overflow되면 bucket을 복제한다.

overflow된 bucket을 split하고, pointer를 duplicate한다.

Ch\_9

single-ended priority queue:

return minimum/maximum element ->  $O(1)$

Insert arbitrary element ->  $O(\log n)$

Delete minimum/maximum element ->  $O(\log n)$

double-ended priority queue:

return minimum element

return maximum element

Insert arbitrary element

Delete minimum element

Delete maximum element

meld operation은  $O(n)$ 시간이 걸리는데, Leftist tree를 이용하면  $O(\log n)$ 이 걸린다.

※  $\text{shorest}(\text{leftChild}(x)) \geq \text{shorest}(\text{rightChild}(x))$

※  $n \geq (2^{\text{shortest}(\text{root})}) - 1$

※  $\text{shortest}(\text{root}) \leq \log_2(n + 1)$

※ Weight-Biased Leftist Trees

-> 아래로 내려갈수록 node의 수가 적어진다는 보장이 있다.

Height-Biased Leftist Trees

-> top에서 bottom으로, bottom에서 top으로 가는 two step이 필요하다.

-> Weight-Biased Leftist Trees는 아래로 내려갈수록 node의 수가 적어진다는 보장이 있어서 one step만 하면 된다.