

HW 2

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

features

class

$$\text{Info}(D) = I(9,5)$$

$$= -\frac{9}{14} \log_2 \left(\frac{9}{14} \right) - \frac{5}{14} \log_2 \left(\frac{5}{14} \right) = 0.940$$

$$\begin{aligned} \text{Info}_{\text{age}}(D) &= \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,2) \\ &= 0.694 \end{aligned}$$

$$\begin{aligned} \text{Info}_{\text{income}}(D) &= \frac{4}{14} I(2,2) + \frac{6}{14} I(4,2) + \frac{4}{14} I(3,1) \\ &= 0.111 \end{aligned}$$

$$\begin{aligned} \text{Info}_{\text{student}}(D) &= \frac{9}{14} I(6,1) + \frac{7}{14} I(3,4) \\ &= 0.489 \end{aligned}$$

$$\begin{aligned} \text{Info}_{\text{credit}}(D) &= \frac{8}{14} I(6,2) + \frac{6}{14} I(3,3) \\ &= 0.892 \end{aligned}$$

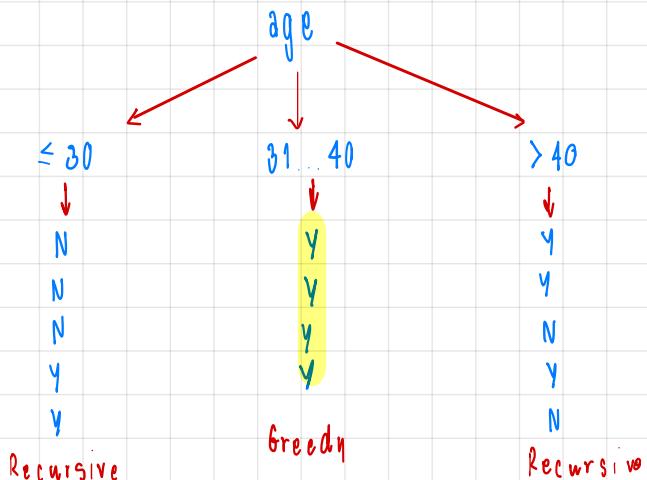
$$\text{Gain}(\text{age}) = \text{Info}(D) - \text{Info}_{\text{age}}(D)$$

$$= 0.940 - 0.694 = 0.246$$

$$\text{Gain}(\text{income}) = 0.940 - 0.911 = 0.029$$

$$\text{Gain}(\text{student}) = 0.940 - 0.989 = 0.959$$

$$\text{Gain}(\text{credit_rating}) = 0.940 - 0.892 = 0.048$$



$$\text{Info}(D) = I(2,3)$$

$$= -\frac{2}{5} \log_2 \left(\frac{2}{5} \right) - \frac{3}{5} \log_2 \left(\frac{3}{5} \right) = 0.9710$$

$$\text{Info}_{\text{income}}(D) = \frac{2}{5} I(0,2) + \frac{2}{5} I(1,1) + \frac{1}{5} I(1,0)$$

$$= 0.4$$

$$\text{Info}_{\text{student}}(D) = \frac{2}{5} I(2,0) + \frac{3}{5} I(0,3)$$

$$= 0$$

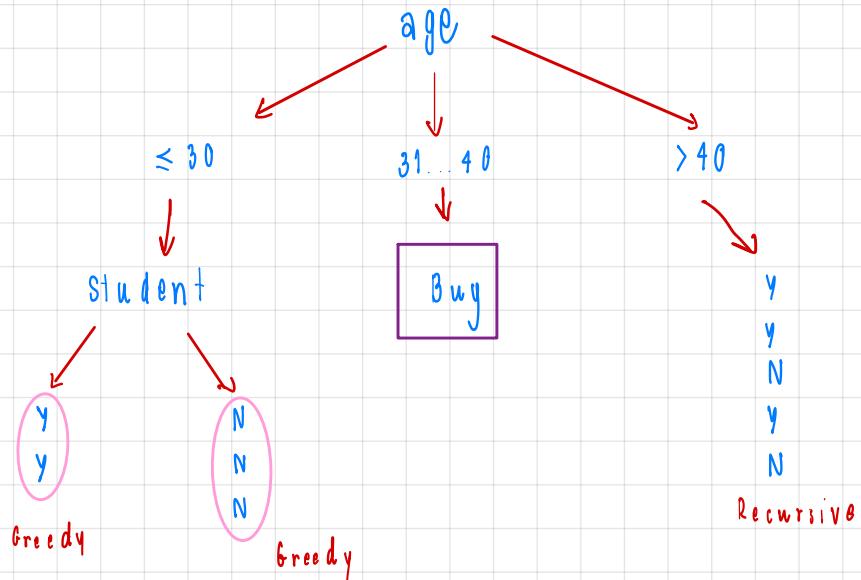
$$\text{Info}_{\text{credit}}(D) = \frac{2}{5} I(1,1) + \frac{3}{5} I(1,2)$$

$$= 0.9509$$

$$\text{Gain}(\text{income}) = 0.9710 - 0.4 = 0.5710$$

$$\text{Gain}(\text{student}) = 0.9710 - 0 = 0.9710$$

$$\text{Gain}(\text{credit_rating}) = 0.9710 - 0.9509 = 0.0201$$



$$\text{Info}(D) \sim I(3,2)$$

$$= -\frac{3}{5} \log_2 \left(\frac{3}{5} \right) - \frac{2}{5} \log_2 \left(\frac{2}{5} \right)$$

$$= 0.941$$

$$\text{Info}_{\text{income}}(D) = \frac{3}{5} I(2,1) + \frac{2}{5} I(1,1)$$

$$= 0.9509$$

$$\text{Info}_{\text{student}}(D) = \frac{3}{5} I(2,1) + \frac{2}{5} I(1,1)$$

$$= 0.9509$$

$$\text{Info}_{\text{credit}}(D) = \frac{2}{5} I(0,2) + \frac{3}{5} I(3,0)$$

$$= 0$$

$$\text{Gain}(\text{income}) = 0.9410 - 0.9509 = 0.0201$$

$$\text{Gain}(\text{student}) = 0.0201$$

$$\text{Gain}(\text{credit_rating}) = 0.9410 - 0 = 0.9410$$

Decision Tree

