Let ACX show that if C is a connected subspace of X that intersects both A and XIA then Cintersects Bd A Bd A = A n Ac

Arque contra positively. assume that C does not intersect Bd A A=intAUBdA so CnintA # 1

Similarly Coint AC + I but X = int A U int AC U Bd A

so C = (CnintA) U (CnintAc) U (CnBdA) = (CnintA)U(CnintAc) but these are disjoint open sets so C is not connected