

Show that if A is closed in X and B closed in Y then $A \times B$ is closed in $X \times Y$

$$(A \times B)^c = (X \times B^c) \cup (A^c \times Y)$$

This is a union of open sets so open

$A \times B$ is closed \square