Give an example showing that a Hausdorff space with a countable basis need not be metrizable.

R_k has a countable basis. It is not regular $\Rightarrow$ not normal $\Rightarrow$ not metrizable

(every metrizable space is normal.)