

Let $A \subset X$. If d is a metric for the topology of X show that $d|_{A \times A}$ is a metric for the subspace topology on A

1. for $x, y \in A$ $d(x, y) \geq 0$, and $d(x, y) = 0 \Leftrightarrow x = y$. This is true for $x, y \in X$ and thus for $x, y \in A$

2. $d(x, y) = d(y, x)$ since $x, y \in X$

3. let $x, y, z \in A$ then $x, y, z \in X$ thus
 $d(x, z) \leq d(x, y) + d(y, z)$