

Show that if $f: X \rightarrow Y$ is X compact and Y is Hausdorff, f is a closed map.

Let $C \subset X$ be closed. Then C is compact.

Then $f(C)$ is compact as f is continuous.

Then $f(C)$ is closed as Y is Hausdorff. ▀