

Show that if A is closed in Y and Y is closed in X then A is closed in X .

$Y \setminus A$ is open

$X \setminus A = (Y \setminus A) \cup (X \setminus Y)$ both open thus

A is closed