

Joint Base Station Selection and Adaptive Slicing in Virtualized Wireless Networks: A Stochastic Optimization Framework

Kory Teague¹, Mohammad J. Abdel-Rahman^{1,2}, and Allen B. MacKenzie¹

¹Department Electrical and Computer Engineering, Virginia Tech, Blacksburg ,VA 24061, USA

²Electrical and Energy Engineering Department, Al Hussein Technical University (HTU), Amman 11821, Jordan

{koryt, mo7ammad, mackenab}@vt.edu

Abstract

Wireless network virtualization is a promising avenue of research for next-generation 5G cellular networks. Virtualization focuses on the concept of active resource sharing and the building of a network designed for specific demands, decreasing operational expenditures and improving demand satisfaction of cellular networks. This work investigates the problem of selecting base stations (BSs) to construct a virtual network that meets the the specific demands of a service provider, and the adaptive slicing of the resources between the service provider's demand points. A two-stage stochastic optimization framework is introduced to model the problem of joint BS selection and adaptive slicing. We present two methods for determining a solution for the two-stage stochastic optimization model. The first method uses a sampling approach applied to the deterministic equivalent program of the stochastic model, providing a tight approximation with sufficient computation time. The second method uses a genetic algorithm to approximate BS selection for the network, allowing for adaptive slicing to be determined by a simpler, single-stage linear optimization problem. To test these methods we generated a number of scenarios using a log-normal model designed to emulate demand from real world cellular networks. The results from these simulations present promising results that can be expounded upon with further investigation.

Index Terms

Wireless network virtualization, resource allocation, two-stage stochastic optimization, genetic algorithm.

I. INTRODUCTION

Resource infrastructure sharing has been a common practice between mobile network operators (MNOs) to fulfill two separate needs. First, MNOs needed to offer coverage for their users in regions where they had no infrastructure, leading to the creation of roaming agreements. Second, the cost to maintain the wireless infrastructure became high in some areas. Passive sharing of infrastructure, such as physical sites, tower

masts, power, and air-conditioning, led to considerable cost savings [1]. These benefits motivated the use of more active sharing approaches, such as the reuse of backhaul and the sharing of radio access networks (RANs) in the form of base stations (BSs) and antenna systems. The technologies developed for MNO sharing have allowed for the rise of mobile virtual network operators (MVNOs), which provide MNO-like mobile services without directly owning a physical RAN.

Wireless virtualization is one of the most promising approaches for efficient sharing of radio resources in next-generation mobile networks [2]. In [3], [4], the opportunities for cost saving and additional flexibility are the motivations behind introducing virtualization schemes for LTE networks, focusing on resource sharing. Doyle *et al.* [5] presented the Network without Borders (NwoB) paradigm which broadly explores the concepts of virtualization. The authors proposed removing the traditional constraints on spectrum and presented a virtualization-centric structure for mobile wireless networks. In this paradigm, a service provider (SP) is an MVNO that provides a specified service to its users, which could be in the form of traditional general data, voice, and messaging services or a more specific application (e.g., emergency services, Internet of things, or video streaming). The virtual network builder (VNB) aggregates and selects resources from resource providers (RPs) to build virtual networks designed for the needs of the SPs. RPs, such as traditional MNOs, are the owners and maintainers of the physical resources and infrastructure that are provided for the virtualized wireless networks (VWNs) via contracts established with VNBs.

Considering the uncertainty of user equipment (demand point) locations, in this paper we consider solving two problems. Stochastic programming provides a powerful mathematical tool to handle optimization under uncertainty. It had been recently exploited to optimize resource allocation in various types of wireless networks operating under uncertainties (examples include [6]–[12]). We establish a stochastic optimization problem from the perspective of the VNB to determine the optimal selection of resources to be leased from the RPs and adaptively sliced and allocated to form VWNs that satisfy the demands of the SPs. Then, we develop two approaches that would be run in the VNB to reach a near-optimal solution of the stochastic optimization problem. We consider two optimality criteria: maximizing demand satisfaction of SP users and minimizing the cost of the BS resources to satisfy the demand. Finally, we consider the efficacy of the approaches with a single SP with log-normal spatially-correlated demand modeled to mimic real cellular networks.

The rest of this paper is organized as follows. In Section II, we detail and define the system model assumed for our resource allocation methods. In Section III, we consider our stochastic optimization problem and resource selection and demand allocation approaches. In Section IV, we simulate the described approaches and evaluate their performance. Finally, in Section V, we discuss our conclusions and directions of future research.

II. SYSTEM MODEL

We consider a geographical area of width X (m) and length Y (m) that contains a set $\mathcal{S} = \{1, 2, \dots, S\}$ of BSs available to be leased to the VNB by a set of $\mathcal{N} = \{1, 2, \dots, N\}$ RPs. The rate capacity of BS $s \in \mathcal{S}$

is denoted by r_s , its cost is denoted by c_s , and its coverage radius is denoted by b_s .

A Service Provider (SP) seeking a virtualized wireless network from the VNB is assumed to know the distribution of traffic demand within the region the VWN would cover. It has been shown that a log-normal distribution or a mixture of log-normal distributions can approximate traffic demand in real-world cellular networks [13], [14]. It has also been shown that traffic distribution is spatially correlated [14], [15]. We model the spatial traffic demand of a single SP using a similar, continuous form of the SSLT (Scalable, Spatially-correlated, and Log-normally distributed Traffic) model as proposed by Lee, Zhou, and Niu [16].

To generate this spatial distribution over the area of consideration, an initial Gaussian field, $\rho^G = \rho^G(x, y)$, $x \in [0, X]$, $y \in [0, Y]$, is generated by

$$\rho^G(x, y) = \frac{1}{L} \sum_{l=1}^L \cos(i_l x + \phi_l) \cos(j_l y + \psi_l) \quad (1)$$

where $\mathcal{L} \stackrel{\text{def}}{=} \{1, 2, \dots, L\}$ is a set of the products of two cosines with angular frequencies $i_l, j_l \sim \mathcal{U}(0, \omega_{\max})$, $l \in \mathcal{L}$ and phases $\phi_l, \psi_l \sim \mathcal{U}(0, 2\pi)$, $l \in \mathcal{L}$. As L increases, ρ^G approaches a Gaussian random field with a spatial autocorrelation dependent on ω_{\max} according to the central limit theorem.

The approximate Gaussian distribution ρ^G is then normalized to $\rho^S = \rho^S(x, y)$, $x \in [0, X]$, $y \in [0, Y]$, which has a standard normal distribution. The final log-normal distribution, $\rho = \rho(x, y)$, $x \in [0, X]$, $y \in [0, Y]$, is determined by assigning location and scale parameters μ and σ

$$\rho(x, y) = \exp(\sigma \rho^S(x, y) + \mu) \quad (2)$$

$\rho(x, y)$ can be sampled over the space into individual pixels as per Lee with each pixel's value indicating the number of homogeneous demand points within the pixel [16]. In contrast, we allow $\rho(x, y)$ to provide a continuous, spatially-correlated log-normal distribution depicting the demand density over the region for the SP.

Let $\mathcal{M} \stackrel{\text{def}}{=} \{1, 2, \dots, M\}$ be the set of the SP's demand points seeking to connect to the VWN; the value of total traffic demand at each point is denoted by d_m . Further, let $u_{ms} \in [0, 1]$, $m \in \mathcal{M}$, $s \in \mathcal{S}$, represent the normalized capacity (with respect to r_s) of BS s at point m , i.e., the normalized maximum rate that a user can receive at point m from BS s . $u_{ms} = 0$ when m is outside the coverage area of s and $u_{ms} = 1$ when m is within a small distance of s . The specific position of point m , and therefore the value of u_{ms} , is determined stochastically by the demand field ρ .

We assume that a BS $s \in \mathcal{S}$ can be allocated between multiple demand points, and $\delta_{ms} \in [0, r_s]$, $m \in \mathcal{M}$, $s \in \mathcal{S}$, represents the rate of BS s that is allocated to point m .

Throughout this paper, stochastic variables will be differentiated from deterministic variables with a tilde (\sim) placed above the symbol.

III. SOLUTION APPROACH

In this section, we detail our approaches for selecting the subset of resources within \mathcal{S} to create a virtual network with the minimum cost while allocating the selected resources to the demand points within the

region such that it maximizes demand satisfaction. First, we formulate the problem of BS selection and their allocation to individual demand points as a two-stage stochastic optimization problem. Second, the optimization problem is converted to its deterministic equivalent program to remove the stochastic variables then approximated using a sampling method. Finally, a genetic algorithm is used as a separate approximation to the BS selection portion of the problem. In Section IV, we will consider the efficacy of these latter two approaches.

A. Problem Formulation

We formulate the presented problem as a two-stage stochastic optimization problem. We introduce $z_s, s \in \mathcal{S}$ as a binary decision variable defined as

$$z_s = \begin{cases} 1, & \text{if BS } s \text{ is selected for the created network,} \\ 0, & \text{otherwise} \end{cases}$$

To balance the interest of maximizing demand satisfaction against minimizing cost, we introduce the positive real number α as a weighting coefficient between the two stages.

Problem 1 (Two-Stage Stochastic Optimization Problem)

$$\underset{\{z_s, s \in \mathcal{S}\}}{\text{minimize}} \left\{ \sum_{s \in \mathcal{S}} c_s z_s + \alpha \mathbb{E} [h(\mathbf{z}, \tilde{\mathbf{u}})] \right\} \quad (3)$$

subject to:

$$z_s \in \{0, 1\}, \forall s \in \mathcal{S} \quad (4)$$

where $h(\mathbf{z}, \tilde{\mathbf{u}})$ is the optimal value of the second-stage problem, which is given by:

$$\underset{\{\delta_{ms}, m \in \mathcal{M}, s \in \mathcal{S}\}}{\text{minimize}} \left\{ - \sum_{m \in \mathcal{M}} \sum_{s \in \mathcal{S}} \delta_{ms} \tilde{u}_{ms} \right\} \quad (5)$$

subject to:

$$z_s = \mathbb{1}_{\{\sum_{m \in \mathcal{M}} \delta_{ms} > 0\}}, \forall s \in \mathcal{S} \quad (6)$$

$$\sum_{s \in \mathcal{S}} \delta_{ms} \tilde{u}_{ms} \leq d_m, \forall m \in \mathcal{M} \quad (7)$$

$$\sum_{m \in \mathcal{M}} \delta_{ms} \leq r_s, \forall s \in \mathcal{S} \quad (8)$$

The first stage objective function (3) minimizes the total cost of the selected network in context to that network's ability to satisfy the demand contained within the region, as determined by ρ . The second stage objective function (5) maximizes demand satisfaction by maximizing the total demand allocated to the resources comprising the network, as specified by δ_{ms} as the decision variable of the second stage. In this

context, we define demand satisfaction as the ratio of the total demand allocated to the selected network to the total demand contained within the region.

Constraints (4), (6), and (8) implement the defined ranges and values of the decision variables z_s and δ_{ms} , with (6) ensuring that demand is allocated only to selected resources. For constraint (6), $\mathbb{1}_{\{*\}}$ is defined by

$$\mathbb{1}_{\{*\}} = \begin{cases} 1, & \text{if condition } * \text{ is true,} \\ 0, & \text{otherwise} \end{cases}$$

Constraint (7) ensures a demand point $m \in \mathcal{M}$ is not allocated more resource capacity than it demands.

B. Deterministic Equivalent Reformulation

In order to solve the two-stage stochastic optimization formulation (Problem 1), we need to convert it to a deterministic equivalent program (DEP) that does not contain any stochastic variables (only deterministic variables) [17].

Let $\Omega \stackrel{\text{def}}{=} \{1, 2, \dots, |\Omega|\}$ be defined as the set of discrete scenarios, each of which contains a sampled version of the stochastic variables within Problem 1. As $|\Omega|$ approaches infinity, Ω contains the entire scope of the stochastic variables. The probability a given scenario $\omega \in \Omega$ occurs is denoted by $p^{(\omega)}$, $\omega \in \Omega$, where $\sum_{\omega \in \Omega} p^{(\omega)} = 1$. Variables that are dependent on Ω are shown with a superscript (ω) with the specific scenario it is dependent on indicated by ω .

Problem 2 (Deterministic Equivalent Program of Problem 1)

$$\begin{aligned} & \underset{\substack{z_s, \delta_{ms}^{(\omega)} \\ s \in \mathcal{S}, m \in \mathcal{M}, \\ \omega \in \Omega}}{\text{minimize}} \quad \sum_{s \in \mathcal{S}} c_s z_s - \alpha \sum_{\omega \in \Omega} p^{(\omega)} \left(\sum_{m \in \mathcal{M}} \sum_{s \in \mathcal{S}} \delta_{ms}^{(\omega)} u_{ms}^{(\omega)} \right) \end{aligned} \quad (9)$$

subject to:

$$\sum_{s \in \mathcal{S}} \delta_{ms}^{(\omega)} u_{ms}^{(\omega)} \leq d_m, \quad \forall m \in \mathcal{M}, \quad \forall \omega \in \Omega \quad (10)$$

$$\sum_{m \in \mathcal{M}} \delta_{ms}^{(\omega)} \leq r_s z_s, \quad \forall s \in \mathcal{S}, \quad \forall \omega \in \Omega \quad (11)$$

$$z_s \in \{0, 1\}, \quad \forall s \in \mathcal{S} \quad (12)$$

The objective function (9) combines both objective functions (3) and (5) of the initial formulation into a deterministic form. Constraints (10) and (11) ensure demand is not overallocated and is only allocated to selected resources and within capacity for all scenarios.

While Problem 2 provides an equivalent deterministic form of Problem 1, it only remains so while Ω contains the entire scope of the stochastic variables (i.e., Ω contains every scenario that the stochastic variables can take with their associated probabilities occurring). For Problem 2 to be in a generally tractable form, Ω needs to be sampled. We sample Ω with a finite number of scenarios, $|\Omega|$. With sufficiently large $|\Omega|$,

Ω approaches a tight approximation of the scope of the stochastic variables. Within each scenario $\omega \in \Omega$, the SSLT demand field ρ is sampled to provide a set of M discrete demand points. Each sampling of ρ is generated by creating a non-stationary 2D Poisson point process (PPP) with M points over the region using ρ as the spatial intensity function. To generate this non-stationary PPP, we use an acceptance-rejection method. That is, each point of a stationary PPP with an intensity of $\rho_{\max} = \max_i \rho(x_i, y_i)$ is retained with probability $\frac{\rho(x_i, y_i)}{\rho_{\max}}$, where x_i and y_i are the x- and y-coordinates of the i^{th} point of the stationary PPP.

C. Adaptive Slicing within a Formed VWN

After the solution to the sampled DEP of Section III-B has been found, the VNB has determined the joint BS selection that forms the VWN and a proposed resource slicing of considered possible scenarios, Ω , that allocates the resources to the SP's demand points. Since $|\Omega|$ is not infinite, any given scenario present in the formed VWN is exceedingly unlikely to be an element of Ω . Further, as demand points move between BSs or enter or exit the VWN, a new scenario $\omega \notin \Omega$ is formed with a possibly new set $\mathcal{M}' \triangleq \{1, 2, \dots, M'\}$. The VWN must adapt its resource slicing to these new demand points to maintain maximal demand satisfaction. With the VWN built, the joint BS selection, z_s , becomes a constant of the network, simplifying Problem 2 to a single-stage optimization problem

Problem 3 (Deterministic Adaptive Slicing)

$$\begin{aligned} \underset{\left\{ \begin{array}{l} \delta_{ms}^{\{\omega\}}, s \in \mathcal{S}, \\ m \in \mathcal{M}', \omega \in \Omega' \end{array} \right\}}{\text{minimize}} & - \sum_{\omega \in \Omega'} p^{(\omega)} \left(\sum_{m \in \mathcal{M}'} \sum_{s \in \mathcal{S}} \delta_{ms}^{\{\omega\}} u_{ms}^{\{\omega\}} \right) \end{aligned} \quad (13)$$

subject to:

$$\sum_{s \in \mathcal{S}} \delta_{ms}^{\{\omega\}} u_{ms}^{\{\omega\}} \leq d_m, \forall m \in \mathcal{M}', \forall \omega \in \Omega' \quad (14)$$

$$\sum_{m \in \mathcal{M}'} \delta_{ms}^{\{\omega\}} \leq r_s z_s, \forall s \in \mathcal{S}, \forall \omega \in \Omega' \quad (15)$$

where $\Omega' \triangleq \{1, 2, \dots, |\Omega'|\}$ is the set of $|\Omega'|$ scenarios independent of the original set Ω . In practice, $|\Omega'| = 1$ with $p^{(1)} = 1$, as only the currently existing scenario of the network is of interest for slicing the resources at that moment. Higher values of $|\Omega'|$ are useful for simulating multiple scenarios with a homogeneous \mathcal{M}' . It is worth noting that Problem 3 is more tractable than Problem 2 as it only contains the single decision variable for resource slicing, simplifying the objective function (13) and constraint (15).

D. Genetic Algorithm Approach

The full sampled DEP formulation is notably intractable as its components increase in size. Most importantly, the accuracy of the sampled DEP is directly dependent on the size of Ω , directly causing a trade off between the accuracy of the sampled DEP and its computability in a reasonable amount of time. In this subsection, we reformulate the problem of joint BS selection for the VWN as a genetic algorithm,

circumventing the need to discretize demand or to establish Ω , thereby simplifying the original problem into a more scalable form.

A genetic algorithm is an iterative metaheuristic in which an approximate solution to a given optimization problem is arrived at via a series of progressive generations. Each generation contains a number of candidate solutions, called individuals, each of which is defined by a chromosome. During a given generation, each individual is assessed a fitness heuristic based on its chromosome. Then individuals are selected at random, with more fit individuals being selected with greater probability. Pairs of selected individuals will crossover with probability p_{cov} , a process similar to genetic recombination in biology. The resulting chromosomes then have probability p_{mut} to mutate, altering the chromosome slightly. Once enough new individual chromosomes have been selected and possibly undergone crossover and mutation, this set of new individuals, called children, forms the next generation to repeat the process.

For the genetic algorithm, ρ is not sampled for discrete demand points. Instead, we assume that all demand over the region is allocated to the closest resource. The subset of \mathcal{S} , \mathcal{S}' , that is selected for a given possible VWN forms a Voronoi tessellation from the point locations of the selected resources. The total demand allocated to a selected resource $s \in \mathcal{S}' \subseteq \mathcal{S}$ is $\iint_{V_s} \rho(x, y) dx dy$, where V_s is the region bounded by the cell of resource s in the Voronoi tessellation. If the total demand allocated to s exceeds r_s , s is considered to be *overcapacity*. If V_s is not wholly contained within the coverage area of resource s , s is considered to be *overcoverage*.

Let $\mathcal{G} \stackrel{\text{def}}{=} \{1, 2, \dots, G\}$ be the set of generations used in the genetic algorithm and $\mathcal{J}_g \stackrel{\text{def}}{=} \{1, 2, \dots, I\}$, $g \in \mathcal{G}$ be the set of individuals within generation g . Each individual $i \in \mathcal{J}_{g \in \mathcal{G}}$ has a binary chromosome $z^{\{ig\}}$ of length S . $z_s^{\{ig\}}$, $s \in \mathcal{S}$, denoting each individual bit of the chromosome, is defined as follows:

$$z_s^{\{ig\}} = \begin{cases} 1, & \text{if BS } s \text{ is selected for the VWN for individual } i \text{ in generation } g, \\ 0, & \text{otherwise} \end{cases}$$

The fitness heuristic of each individual chromosome, $z^{\{ig\}}$, is assessed as the reciprocal of the chromosome's cost, which is defined as

$$\text{fitness}(z^{\{ig\}}) = \frac{1}{\text{cost}(z^{\{ig\}})} \quad (16)$$

$$\text{cost}(z^{\{ig\}}) = \sum_{s \in \mathcal{S}} \left(c_s z_s^{\{ig\}} + c_{\text{cov}} \mathbb{1}_{\{V_s \not\subseteq R_s\}} + (c_{\text{cap}}^g - 1) \max \left(0, \iint_{R_s} \rho(x, y) dx dy - r_s \right) \right) \quad (17)$$

where R_s is the coverage area region of resource $s \in \mathcal{S}$.

The cost function (17) indicates cost increases not only based on the cost of the resources selected, but also with imperfection costs c_{cov} and c_{cap} , the costs of a selected resource being overcoverage or overcapacity, respectively. The overcapacity cost grows with each successive generation. For early generations, this allows for imperfect solutions to temporarily exist to seed later generations and improve diversity to increase the probability of finding a better final approximate solution.

Elitism is used, where the n most fit individuals of a given generation are automatically selected without crossover or mutation to be the first children of the next generation. Selection occurs via the roulette wheel selection method. Every individual i of a given generation g has a probability of being selected given by

$$\frac{\text{fitness}(z^{\{ig\}})}{\sum_{i \in \mathcal{I}} \text{fitness}(z^{\{ig\}})}$$

When crossover is performed on selected individuals, it is via the uniform crossover method with a mixing ratio of 0.5. That is, if two selected parent individuals crossover, each equivalent bit in the parents will swap with a probability of 50%. It has been suggested that uniform crossover is more exploratory than n -point crossover (*cite*). Mutation occurs on a bit-by-bit level, with each bit mutating (i.e., flipping) with probability $\frac{1}{S}$. The uniqueness property is then enforced on the resulting children to ensure diversity; if a child chromosome is identical to another child chromosome in the next generation, the child is discarded and a new child generated, ensuring that each individual of any given generation is unique within that generation.

The genetic algorithm iterates for a number of generations G . If the genetic algorithm settles on a single individual for a number of continuous generations, G_{halt} , it will halt and present that individual's chromosome as the final approximate solution for z_s . Otherwise, the chromosome of the fittest individual of generation G determines z_s .

The genetic algorithm only determines an approximate solution to the BS selection forming the VWN, informing the VNB of which BSs to obtain from the RPs. With this selection, z_s , the SP's demand points can be dynamically allocated resource slices as described by Problem 3 in Section III-C.

IV. SIMULATION AND EVALUATION

In this section, we evaluate the sampled DEP and genetic algorithm approaches as approximations of Problem 1. We will compare the cost, demand satisfaction, and time to generate of the resultant networks.

A. Setup

Unless stated otherwise, we use the default parameter values shown in Table I. BS locations are determined as a stationary PPP. Demand point locations are generated independently for each scenario as a non-stationary PPP using $\rho(x, y)$, $x \in [0, X]$, $y \in [0, Y]$, as the spatial intensity function, as described in Section II. Fig. 1 provides a visualization of the simulation network area. (1a) shows the BS locations of \mathcal{S} with the associated Voronoi Tessellation showing the coverage areas of the BSs when all are active with respect to the genetic algorithm. (1b) shows the SSLT demand density field with one example scenario of demand points, which acts as a single sample of the demand density field. To compute $u_{ms}^{\{\omega\}}$, it is assumed that there is perfect propagation between the demand points and BSs. Unlike as described in Section II, $u_{ms}^{\{\omega\}} = 1$ if the distance between demand point $m \in \mathcal{M}$ of scenario $\omega \in \Omega$ and BS $s \in \mathcal{S}$ is less than b_s , and 0 otherwise. To compute the integral of the fitness function (17), $\rho(x, y)$ is discretized into a grid of congruent pixels, and the demands of all pixels within a Voronoi cell of interest are summed together.

TABLE I: Numerical Values of Relevant Parameters

Parameter	Value
Width of Geographic Area (X)	2 km
Height of Geographic Area (Y)	2 km
Number of BSs (S)	60
Number of Demand Points (M)	75
Number of Scenarios ($ \Omega $)	$\{5, 10, \dots, 50\}$
BS cost ($c_s, \forall s \in \mathcal{S}$)	1
BS capacity ($r_s, \forall s \in \mathcal{S}$)	1.50 Mbps
BS range ($b_s, \forall s \in \mathcal{S}$)	500 m
Demand Point Demand ($d_m, \forall m \in \mathcal{M}$)	0.178 Mbps
Set of Two-Stage Model Weights (α)	20
SSLT Approximation Depth (L)	50
SSLT Maximum Angular Frequency (ω_{\max})	$\frac{2\pi}{30}$
SSLT Location Parameter (σ)	0
SSLT Scale Parameter (μ)	1
Pixel Grid Size	100 x 100, 20 m side
Maximum Number of Generations (G)	3000
Minimum Number of Generations	300
Number of Unchanged Generations Before Halt (G_{halt})	150
Number of Individuals per Generation (I)	80
Number of Elite Individuals per Generation	4
Probability of Crossover (p_{cov})	0.7
Probability of Mutation per bit (p_{mut})	$\frac{1}{S} = 0.0167$
Overcoverage Cost (c_{cov})	3
Overcapacity Cost (c_{cap})	1.015

We ran our simulations on an Intel Core i7-4790K 4.00 GHz 4 real/8 virtual core CPU with 16 GB of DDR3 RAM. We used CPLEX [18] to solve the sampled DEP optimization problems and we used MATLAB to simulate the genetic algorithm and to generate the demand field and stochastic data (i.e., $\rho(x, y)$ and $u_{ms}^{\{\omega\}}$). During the simulations, extraneous processes were culled to allow maximal use of computer resources. Average values for the performance of the genetic algorithm are provided from 50 independent runs using the identical data set except for the set of initial individuals. The sampled DEP solutions were solved across multiple values of α as cost, time, and demand satisfaction are directly dependent on α .

B. Results

In Fig. 2 is a comparison of the approach run times. It shows the run times of both the DEP and genetic algorithm in terms of the speedup ratio and in absolute number of seconds. As the number of scenarios sampled increases, the CPU run time of the sampled DEP increases exponentially, and fails to converge to a final solution with 50 scenarios within the time limit of 15 minutes. Except for the 5 scenario case, the genetic algorithm converges to a solution in less CPU time (125.8 seconds) than the sampled DEP. When

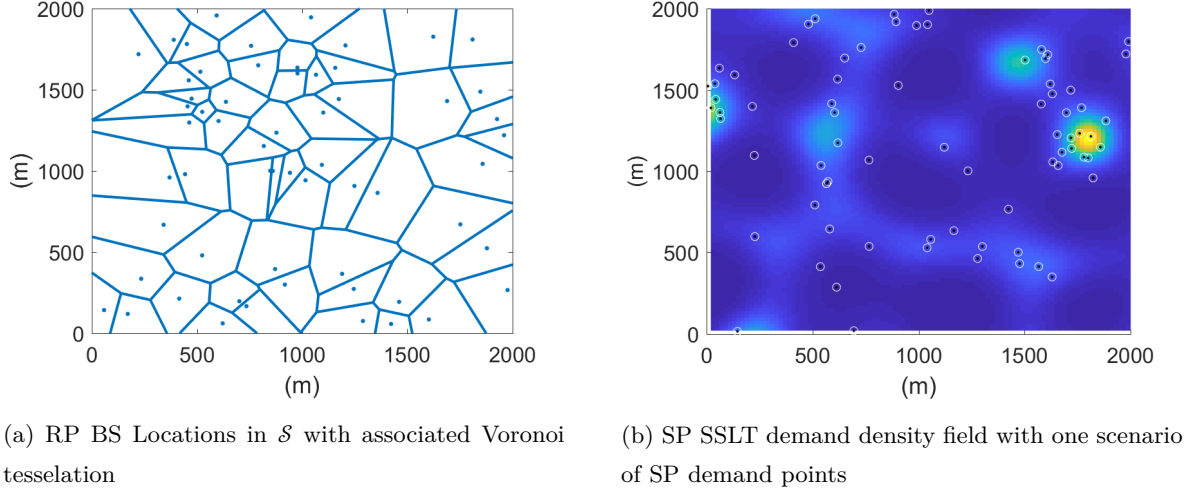


Fig. 1: Visualization of network area. (1a) visualizes the resources available to VNB for creating the VWN, and (1b) visualizes the demand to be satisfied by the VWN.

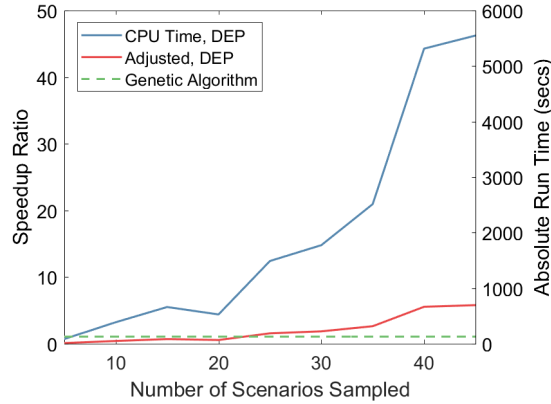


Fig. 2: Absolute run time and speedup ratio of the genetic algorithm and sampled DEP approaches. Speedup ratio is the ratio between the average genetic algorithm and sampled DEP run times. Adjusted time is the minimum wall run time accounting for CPLEX utilizing 8 threads. CPLEX did not converge to a final solution within the time limit (15 minutes) in the 50 scenario case.

20 scenarios are sampled, the DEP takes approximately 440% of the time as the genetic algorithm; at 45 scenarios, this has increased to 4,630%. CPLEX is capable of parallelizing across the 8 CPU cores, allowing for the real run time to be, at minimum, one-eighth the CPU run time. In terms of the adjusted approximate "wall" time, the genetic algorithm converges in less wall time than the sampled DEP for 25 or more sampled scenarios.

The trade off for the genetic algorithm's improved run time is that the solution provided is less optimal than the sampled DEP, as indicated by an increased cost for the VNB to build the VWN. Fig. 3a compares the

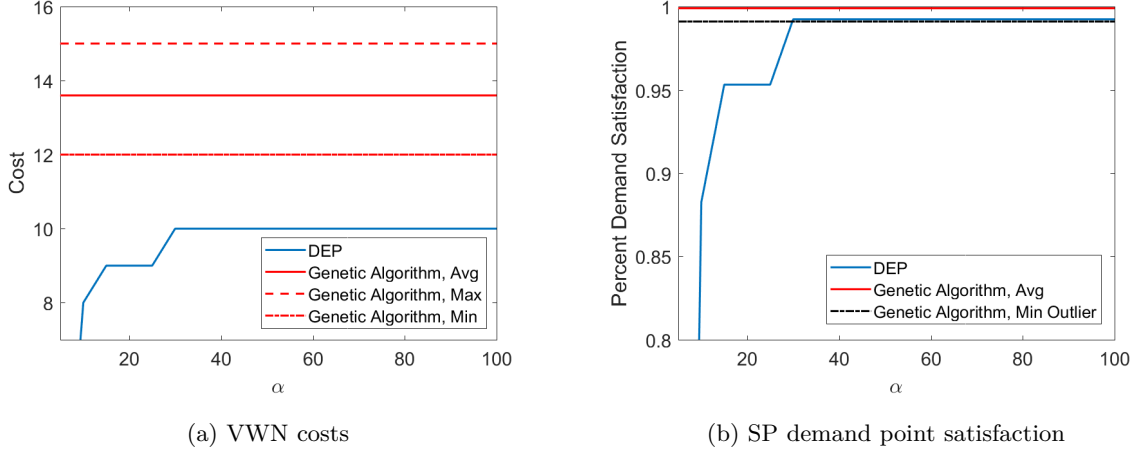


Fig. 3: Comparison of VWN costs and SP demand point satisfaction. Note that cost and demand satisfaction show a direct correlation.

increasing cost of the sampled DEP as α increases with the cost of the various genetic algorithm solutions. On average, the genetic algorithm incurs a 36% increased cost in selecting the BSs for the VWN. At minimum, the incurred cost is only 20% than the sampled DEP, which implies the genetic algorithm might be terminating early, and a tighter solution might be found by increasing G_{halt} . It should also be noted that one unit of cost is one additional BS being selected for the VWN, and the sampled DEP selections for $\alpha \geq 30$ have a cost of only 10 BSs. Any variance that incurs one additional BS for the genetic algorithm incurs 10% increased cost. Increasing the number of BSs required to comprise the VWN would introduce additional granularity in \mathcal{S} that might decrease the inefficiency of the genetic algorithm. This was not done as this data set was chosen specifically so the sampled DEP would terminate within 15 minutes (i.e., in a reasonable amount of time); increasing the number of BSs available to the VNB drastically increases the time it would take the sampled DEP to converge to a solution.

There is a direct correlation between the number of BS in the VWN and its capability for satisfying demand. As the cost increases of the sampled DEP solution, more BS are selected, and the demand satisfaction the sampled DEP solution similarly trends towards 100%, as shown in Fig. 3. Because of this, the genetic algorithm solutions have a very high demand satisfaction, averaging 99.9% demand satisfaction, even reaching 100% for some solutions. The most expensive 10-BS sampled DEP solutions reach 99.2% demand satisfaction when slicing the same set of resources that determined the sampled DEP BS selection.

When the set of demand points change to a scenario no longer in Ω , the sampled DEP performs very similarly. Fig. 4 shows the demand satisfaction for both the sampled DEP and genetic algorithm BS selections when sliced to a new set of scenarios. Here, the number of demand points increases to 200 points per scenario, each with 66.8 kbps rate demand, across 50 independent scenarios. The demand satisfaction trend of the sampled DEP BS selection follows very closely to the original set of scenarios but hits a maximum of 99.0%

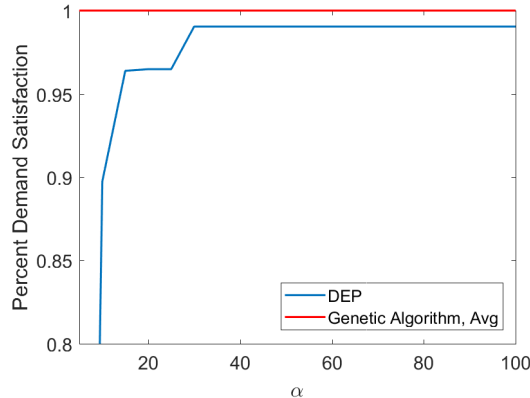


Fig. 4: Comparison of demand satisfaction with 50 scenarios of 200 SP demand points

demand satisfaction with 10 BSs. In comparison, the SP demand point scenarios are far more beneficial to the genetic algorithm, which reaches greater than 99.99% demand satisfaction for all generated VWNs. This is expected as a side effect of the increased number of points and scenarios more accurately describing a sampling of the original SSLT demand density field of the SP, $\rho(x, y)$.

V. CONCLUSION

In this work, we studied the problem of determining the optimal joint BS selection for a virtual network and the adaptive slicing of the network to the SP demand points. We introduced a two-stage stochastic optimization problem which minimizes the cost of base station selection for a virtual network while maximizing demand satisfaction of the network's demand points. We then investigated two approaches that provide a solvable form for the stochastic model: a deterministic equivalent program of the stochastic problem which is simplified to a tractable form with a sampling method, and a genetic algorithm that determines base station selection so that slicing can be found via a single-stage optimization problem.

The sampled DEP is considered to be closer to the original problem, and will provide a tight approximate solution to the original DEP or stochastic model with a sufficiently large set of scenarios and sufficient time, but trends to the intractable as these are reached. The genetic algorithm is a hybrid approach intending to simplify the first stage of the model by using a metaheuristic. All demand, known from a continuous demand density model, within a resource's cell in a Voronoi tessellation is considered allocated to that resource, a simpler process than attempting to allocate individual demand points to the entire pool of resources. The advantage of this approach is that it simplifies the search space of the original two-stage model to a single-stage model which only handles slicing demand points to the selected resources. This provides a faster solution with the introduction of error.

The simulation results indicate that the genetic algorithm approach may be an adequate avenue for a solution. This approach trends to a solution in 2% of the time, incurring 20% increased error. While the error is significant, it could decrease with larger, more computationally-intensive data sets that would

provide more resolution to both the resource and demand sets, allowing for less error to be incurred for small variations. It is important to note that increasing the size of the data set incurs a larger time cost on the sampled DEP approach than on the genetic algorithm approach. Analyzing these larger data sets, improving on the genetic algorithm formulation, or utilizing other metaheuristic algorithms could improve on these results and would be obvious avenues for further investigation.

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