

Use the Rational Zero Theorem to list all possible rational zeros for each given function.

1.  $f(x) = x^3 + x^2 - 4x - 4$

2.  $f(x) = 3x^4 - 11x^3 - x^2 + 19x + 6$

3.  $f(x) = 4x^4 - x^3 + 5x^2 - 2x - 6$

For the next problems, (a) List all possible rational zeros; (b) Use synthetic division to test the possible rational zeros and find an actual zero; (c) Use the quotient from part (b) to find the remaining zeros of the polynomial function.

4.  $f(x) = 2x^3 - 3x^2 - 11x + 6$

5.  $f(x) = x^3 + 4x^2 - 3x - 6$

6.  $f(x) = xx^3 + 6x^2 + 5x + 2$

7.  $f(x) = x^3 - 10x - 12$

8.  $f(x) = 6x^3 + 25x^2 - 24x + 5$

9.  $f(x) = x^4 - 2x^3 - 5x^2 + 8x + 4$

**Find an  $n$ -th degree polynomial function with real coefficients satisfying the given conditions.**

10.  $n = 3$ ;  $-1$  and  $5i$  are zeros;  $f(-1) = -104$

11.  $n = 3$ ;  $-5$  and  $4 + 3i$  are zeros;  $f(2) = 91$

12.  $n = 4$ ;  $i$  and  $3i$  are zeros;  $f(-1) = 20$

**Find all zeros of the polynomial function or solve the given polynomial equation.  
Then write the function equation in factored form**

13.  $2x^3 - x^2 - 9x - 4 = 0$

14.  $f(x) = x^4 - 2x^3 + x^2 + 12x + 8$