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General

Header

```
// use better compiler options
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
// include everything
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <sys/resource.h>
// namespaces
using namespace std;
using namespace __gnu_cxx; // rope
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio ios base::sync with stdio(0);
\hookrightarrow cin.tie(0):
#define nostacklim rlimit RZ;getrlimit(3,&RZ);

    RZ.rlim cur=-1; setrlimit(3,&RZ);
#define DEBUG(v) cout<<"DEBUG: "<<#v<<" = "<<v</pre>
\hookrightarrow <<' \setminus n';
#define 11 long long
#define ull unsigned 11
#define i128 int128
#define u128 unsigned i128
#define ld long double
// global variables
mt19937 rng((uint32 t)chrono::steady clock::
→ now().time since epoch().count()):
```

Fast IO

```
void readn(unsigned int& n) {
char c; n = 0;
while ((c = getchar_unlocked()) != ' ' && c
\hookrightarrow != '\n'
 n = n * 10 + c - '0';
void readn(int& n) {
char c: n = 0: int s = 1:
if ((c = getchar unlocked()) == '-') s = -1;
else n = c - 0:
while ((c = getchar_unlocked()) != ' ' && c
\hookrightarrow != '\n'
```

```
n = n * 10 + c - '0';
n *= s:
void readn(long double& n) {
char c: n = 0:
\hookrightarrow s = 1:
if ((c = getchar unlocked()) == '-') s = -1;
else if (c == '.') d = true;
else n = c - 0:
while ((c = getchar unlocked()) != ' ' && c
\hookrightarrow != '\n') {
 if (c == '.') d = true:
 else if (d) { m = m * 10 + c - '0'; o *=

→ 0.1: }

 else n = n * 10 + c - '0';
n = s * (n + m * o);
void readn(double& n) {
long double m; readn(m); n = m;
void readn(float& n) {
long double m; readn(m); n = m;
void readn(string& s) {
char c: s = "":
while((c = getchar unlocked()) != ' ' && c !=
\hookrightarrow '\n')
 s += c:
bool readline(string& s) {
char c; s = "";
while(c = getchar unlocked()) {
 if (c == '\n') return true;
 if (c == EOF) return false;
 s += c:
return false:
void printn(unsigned int n) {
if (n / 10) printn(n / 10);
putchar unlocked(n % 10 + '0');
void printn(int n) {
if (n < 0) { putchar unlocked('-'): n *= -1:
\hookrightarrow }
printn((unsigned int)n);
```

Algorithms

```
Min/Max Subarray
                                               // max subarray - compare = a < b, reset = a <
                                               // min subarray - compare = a > b, reset = a > |}
                                               م حا
                                                                                                Ternary Search
                                               // returns {sum, {start, end}}
long double m = 0, o = 1; bool d = false; int |pair<int, pair<int, int>> ContiguousSubarray(
                                                                                               // < for max. > for min. or any other unimodal
                                                → int* a, int size, bool(*compare)(int, int), → func

→ bool(*reset)(int), int defbest = 0) {
                                                                                                #define TERNCOMP(a,b) (a)<(b)</pre>
                                                int best = defbest, cur = 0, start = 0, end =
                                                                                                int ternary_search(int a, int b, int (*f)(int)
                                                \rightarrow 0. s = 0:
                                                                                                → ) {
                                                for (int i = 0: i < size: i++) {</pre>
                                                 cur += a[i]:
                                                 if ((*compare)(best, cur)) { best = cur;
                                                 \hookrightarrow start = s: end = i: }
                                                 if ((*reset)(cur)) { cur = 0; s = i + 1; }
                                                return {best, {start, end}};
                                               Quickselect
                                               #define QSNE -999999
                                               int partition(int arr[], int 1, int r)
                                                int x = arr[r], i = 1;
                                                for (int j = 1; j <= r - 1; j++)
                                                if (arr[i] <= x)</pre>
                                                 swap(arr[i++], arr[j]);
                                                swap(arr[i]. arr[r]):
                                                return i;
                                               // find k'th smallest element in unsorted
                                               int quickselect(int arr[], int 1, int r, int k
                                               \hookrightarrow )
                                                if (!(k > 0 \&\& k \le r - 1 + 1)) return QSNE:
                                                swap(arr[l + rng() % (r-l+1)], arr[r]);
                                                int pos = partition(arr, 1, r);
                                                if (pos-l == k-1) return arr[pos];
                                                if (pos-l > k-1) return quickselect(arr, l,
                                                \hookrightarrow pos-1, k):
                                                return quickselect(arr, pos+1, r, k-pos+1-1);
                                               // TODO: compare against std::nth element()
                                               Saddleback Search
                                               // search for v in 2d array arr[x][y], sorted

→ on both axis

                                               pair<int, int> saddleback search(int** arr,
                                               \hookrightarrow int x, int y, int v) {
                                                int i = x-1, j = 0;
                                                while (i >= 0 && i < v) {
                                                if (arr[i][j] == v) return {i, j};
```

```
int m = (a+b)/2:
 if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
 else b = m+1:
for (int i = a+1; i <= b; i++)</pre>
 if (TERNCOMP((*f)(a), (*f)(i)))
  a = i;
return a;
#define TERNPREC 0.000001
double ternary search(double a. double b.

    double (*f)(double)) {
while (b-a > TERNPREC * 4) {
 double m = (a+b)/2;
 if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
 \hookrightarrow = m:
 else b = m + TERNPREC;
for (double i = a + TERNPREC; i <= b; i +=</pre>

→ TERNPREC)

    if (TERNCOMP((*f)(a), (*f)(i)))
return a;
3 Data Structures
Fenwick Tree
// Fenwick tree, array of cumulative sums - 0(
\hookrightarrow log n) updates, O(log n) gets
struct Fenwick {
 int n: 11* tree:
void update(int i. int val) {
 ++i:
 while (i \le n) {
  tree[i] += val:
  i += i & (-i);
 }
Fenwick(int size) {
 n = size:
 tree = new ll[n+1];
```

(arr[i][j] > v)? i--: j++;

return {-1, -1};

while (b-a > 4) {

```
for (int i = 1; i <= n; i++)</pre>
  tree[i] = 0:
 Fenwick(int* arr, int size) : Fenwick(size) {
 for (int i = 0: i < n: i++)
  update(i, arr[i]):
 ~Fenwick() { delete[] tree; }
11 operator[](int i) {
 if (i < 0 || i > n) return 0;
 11 sum = 0;
 ++i:
 while (i>0) {
  sum += tree[i];
  i -= i & (-i):
 return sum;
11 getRange(int a, int b) { return operator
};
```

Hashtable

```
// similar to unordered map, but faster
struct chash {
const \ uint64 \ t \ C = (11)(2e18 * M PI) + 71;
11 operator()(11 x) const { return
⇒ builtin bswap64(x*C); }
}:
int main() {
gp_hash_table<11,int,chash> hashtable
for (int i = 0; i < 100; i++)</pre>
 hashtable[i] = 200+i;
if (hashtable.find(10) != hashtable.end())
 cout << hashtable[10];</pre>
```

Ordered Set

```
typedef tree<int,null_type,less<int>,
\hookrightarrow rb tree tag,

    → tree order statistics node update>

→ ordered set;
int main()
   ordered_set o_set;
   o set.insert(5): o set.insert(1): o set.
   \hookrightarrow insert(3):
   // get second smallest element
   cout << *(o set.find by order(1)) << '\n';</pre>
   // number of elements less than k=4
   cout << o set.order of kev(4) << '\n':
```

```
Rope
// O(log n) insert, delete, concatenate
int main() {
// generate rope
rope<int> v:
 for (int i = 0: i < 100: i++)</pre>
 v.push back(i);
// move range to front
rope<int> copy = v.substr(10, 10);
v.erase(10, 10):
v.insert(copy.mutable_begin(), copy);
// print elements of rope
for (auto it : v)
 cout << it << " ":
Trie
typedef trie<string, null_type,
trie_string_access_traits<>,
 pat_trie_tag, trie_prefix_search_node_update
 \hookrightarrow > trie type:
int main() {
// generate trie
trie type trie;
for (int i = 0; i < 20; i++)</pre>
 trie.insert(to string(i)): // true if new.
 \hookrightarrow false if old
// print things with prefix "1"
```

4 String

Aho Corasick

→ second; it++)

cout << *it << " ";

```
// range of alphabet for automata to consider
// MAXC = 26. OFFC = 'a' if only lowercase
→ letters
const int MAXC = 256:
const int OFFC = 0;
struct aho corasick {
 struct state
 set<pair<int, int>> out;
 int fail; vector<int> go;
 state() : fail(-1), go(MAXC, -1) {}
};
```

auto range = trie.prefix range("1");

for (auto it = range.first; it != range.

```
vector<state> s:
int id = 0:
aho_corasick(string* arr, int size) : s(1) { };
for (int i = 0: i < size: i++) {</pre>
 int cur = 0:
 for (int c : arr[i]) {
  if (s[cur].go[c-OFFC] == -1) {
   s[cur].go[c-OFFC] = s.size();
   s.push back(state()):
  cur = s[cur].go[c-OFFC]:
 s[cur].out.insert({arr[i].size(), id++});
for (int c = 0; c < MAXC; c++)
 if (s[0],go[c] == -1)
  s[0].go[c] = 0;
queue<int> sq;
for (int c = 0: c < MAXC: c++) {
 if (s[0].go[c] != 0) {
  s[s[0].go[c]].fail = 0:
  sq.push(s[0].go[c]);
}
while (sq.size()) {
 int e = sq.front(); sq.pop();
 for (int c = 0; c < MAXC; c++) {</pre>
  if (s[e].go[c] != -1) {
   int failure = s[e].fail:
   while (s[failure].go[c] == -1)
     failure = s[failure].fail;
   failure = s[failure].go[c]:
   s[s[e].go[c]].fail = failure;
   for (auto length : s[failure].out)
    s[s[e].go[c]].out.insert(length);
   sq.push(s[e].go[c]);
 }
}
// list of {start pos, pattern id}
vector<pair<int, int>> search(string text)
vector<pair<int, int>> toret:
int cur = 0:
for (int i = 0: i < text.size(): i++) {</pre>
 while (s[cur].go[text[i]-OFFC] == -1)
  cur = s[cur].fail:
 cur = s[cur].go[text[i]-OFFC];
 if (s[cur].out.size())
  for (auto end : s[cur].out)
   toret.push_back({i - end.first + 1, end.
```

```
→ second});
 }
 return toret:
Boyer Moore
struct defint { int i = -1: }:
vector<int> boyermoore(string txt, string pat)
← {
vector<int> toret; unordered map<char, defint
→ > badchar:
int m = pat.size(), n = txt.size();
for (int i = 0; i < m; i++) badchar[pat[i]].i</pre>
int s = 0:
while (s \le n - m) {
 int i = m - 1:
 while (i >= 0 \&\& pat[i] == txt[s + i]) i--;
 if (i < 0) {
  toret.push back(s):
  s += (s + m < n) ? m - badchar[txt[s + m]].

→ i : 1:

  s += max(1, j - badchar[txt[s + j]].i);
return toret;
English Conversion
const string ones[] = {"", "one", "two", "

    three", "four", "five", "six", "seven", "

⇔ eight". "nine"}:
const string teens[] ={"ten", "eleven", "

→ twelve", "thirteen", "fourteen", "fifteen",
→ "sixteen", "seventeen", "eighteen", "
const string tens[] = {"twenty", "thirty", "
→ forty", "fifty", "sixty", "seventy", '

    eighty", "ninety"};
const string mags[] = {"thousand", "million",
→ "billion". "trillion". "quadrillion". "
string convert(int num, int carry) {
if (num < 0) return "negative " + convert(-</pre>
\hookrightarrow num. 0):
if (num < 10) return ones[num]:
if (num < 20) return teens[num % 10];</pre>
if (num < 100) return tens[(num / 10) - 2] +</pre>

    (num%10==0?"":" ") + ones[num % 10]:
if (num < 1000) return ones[num / 100] + (num
return convert(num / 1000, carry + 1) + " " +
→ mags[carrv] + " " + convert(num % 1000.
```

 \hookrightarrow 0);

Knuth Morris Pratt

```
vector<int> kmp(string txt, string pat) {
   vector<int> toret:
int m = txt.length(), n = pat.length();
int next[n + 1]:
for (int i = 0; i < n + 1; i++)
 next[i] = 0:
 for (int i = 1; i < n; i++) {</pre>
 int i = next[i + 1]:
 while (j > 0 && pat[j] != pat[i])
  j = next[i];
 if (j > 0 || pat[j] == pat[i])
  next[i + 1] = i + 1;
 for (int i = 0, j = 0; i < m; i++) {</pre>
 if (txt[i] == pat[j]) {
  if (++i == n)
   toret.push_back(i - j + 1);
 } else if (i > 0) {
  i = next[i];
  i--;
return toret:
```

Longest Common Prefix

Longest Common Subsequence

```
}
// return L[m][n]; // length of lcs

string out = "";
int i = m - 1, j = n - 1;
while (i >= 0 && j >= 0) {
   if (a[i] == b[j]) {
     out = a[i--] + out;
     j--;
   }
   else if (L[i][j+1] > L[i+1][j]) i--;
   else j--;
}

return out;
}
```

Longest Common Substring

Subsequence Count

Math

Catalan Numbers

```
ull* catalan = new ull[1000000];
```

Combinatorics (nCr, nPr)

```
// can optimize by precomputing factorials,

    and fact[n]/fact[n-r]

ull nPr(ull n. ull r) {
ull v = 1:
for (ull i = n-r+1; i <= n; i++)</pre>
 v *= i:
 return v:
ull nPr(ull n, ull r, ull m) {
ull v = 1;
 for (ull i = n-r+1: i <= n: i++)</pre>
 v = (v * i) % m;
return v:
ull nCr(ull n. ull r) {
long double v = 1;
 for (ull i = 1; i <= r; i++)</pre>
 v = v * (n-r+i) /i:
return (ull)(v + 0.001);
// requires modulo math
// can optimize by precomputing mfac and minv-
ull nCr(ull n, ull r, ull m) {
```

Chinese Remainder Theorem

 \hookrightarrow minv(mfac(n-k, m), m) % m;

return mfac(n, m) * minv(mfac(k, m), m) % m *

```
mo = mo / d * m[i];
re %= mo;
}
re = (re + mo) % mo;
return true;
}
```

Count Digit Occurences

Discrete Logarithm

Euler Phi / Totient

```
int phi(int n) {
  int r = n;
  for (int i = 2; i * i <= n; i++) {
   if (n % i == 0) r -= r / i;
  while (n % i == 0) n /= i;</pre>
```

```
if (n > 1) r = r / n:
return r:
#define n 100000
ll phi[n+1]:
void computeTotient() {
   for (int i=1; i<=n; i++) phi[i] = i;</pre>
   for (int p=2; p<=n; p++) {</pre>
       if (phi[p] == p) {
           phi[p] = p-1;
           for (int i = 2*p; i<=n; i += p) phi
           \hookrightarrow [i] = (phi[i]/p) * (p-1);
       }
   }
```

Factorials

```
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
\hookrightarrow M E)) + (log10(2 * M PI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
\hookrightarrow M PI * n) * pow(n / M E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
```

Prime Factorization

```
// do not call directly
ll pollard rho(ll n. ll s) {
11 x, y;
x = y = rand() \% (n - 1) + 1;
int head = 1. tail = 2:
while (true) {
 x = mult(x, x, n);
 x = (x + s) \% n:
 if (x == y) return n;
 11 d = _{gcd}(max(x - y, y - x), n);
 if (1 < d && d < n) return d:
 if (++head == tail) y = x, tail <<= 1;</pre>
// call for prime factors
void factorize(ll n, vector<ll> &divisor) {
if (n == 1) return;
if (isPrime(n)) divisor.push back(n):
else {
 11 d = n:
 while (d >= n) d = pollard rho(n, rand() % (
 \hookrightarrow n - 1) + 1);
 factorize(n / d. divisor):
 factorize(d, divisor);
```

Farev Fractions

```
// generate 0 <= a/b <= 1 ordered, b <= n
// farev(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farev(int n) {
 int h = 0, k = 1, x = 1, y = 0, r;
 vector<pair<int, int>> v;
 do {
 v.push back({h, k});
 r = (n-v)/k:
 v += r*k; x += r*h;
 swap(x,h); swap(y,k);
 x = -x; y = -y;
 } while (k > 1);
 v.push_back({1, 1});
 return v;
```

Fast Fourier Transform

```
#define cd complex<double>
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert) {
int n = a.size():
for (int i = 1, j = 0; i < n; i++) {
 int bit = n \gg 1;
 for (: i & bit: bit >>= 1) i ^= bit:
 j ^= bit;
 if (i < j) swap(a[i], a[j]);</pre>
for (int len = 2; len <= n; len <<= 1) {</pre>
 double ang = 2 * PI / len * (invert ? -1 :
 \hookrightarrow 1):
 cd wlen(cos(ang), sin(ang));
 for (int i = 0; i < n; i += len) {</pre>
  cd w(1):
  for (int j = 0; j < len / 2; j++) {</pre>
   cd u = a[i+i], v = a[i+i+len/2] * w:
   a[i+j] = u + v;
   a[i+j+len/2] = u - v;
   w *= wlen:
  }
 }
if (invert)
 for (auto& x : a)
  x /= n;
```

vector<int> fftmult(vector<int> const& a.

```
→ vector<int> const& b) {
vector<cd> fa(a.begin(), a.end()), fb(b.begin |}
\hookrightarrow (), b.end()):
int n = 1 \ll (32 - builtin clz(a.size() + b | if ( gcd(b, m) != 1) return -1;
 → .size() - 1));
fa.resize(n): fb.resize(n):
fft(fa, false); fft(fb, false);
for (int i = 0; i < n; i++) fa[i] *= fb[i];</pre>
fft(fa, true);
vector<int> toret(n);
for (int i = 0; i < n; i++) toret[i] = round( Miller-Rabin Primality Test
 \hookrightarrow fa[i].real()):
return toret;
```

Greatest Common Denominator

```
ll egcd(ll a, ll b, ll& x, ll& y) {
if (b == 0) { x = 1; y = 0; return a; }
ll gcd = egcd(b, a \% b, x, y);
x -= a / b * y;
swap(x, y);
return gcd;
```

Least Common Multiple

```
#define lcm(a,b) ((a*b)/__gcd(a,b))
```

Modulo Operations

```
#define MOD 100000007
#define madd(a,b,m) (a+b-((a+b-m>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a<b)?m:0))
ll mpow(ll b. ll e. ll m) {
11 x = 1;
 while (e > 0) {
 if (e \% 2) x = (x * b) \% m;
 b = (b * b) \% m:
 e /= 2:
 return x % m:
ull mfac(ull n. ull m) {
 ull f = 1:
 for (int i = n; i > 1; i--)
 f = (f * i) % m:
 return f;
// if m is not guaranteed to be prime
ll minv(ll b, ll m) {
11 x = 0, y = 0;
 if (egcd(b, m, x, y) != 1) return -1;
```

```
return (x % m + m) % m;
11 mdiv compmod(int a, int b, int m) {
 return mult(a, minv(b, m), m);
// if m is prime (like 10^9+7)
11 mdiv_primemod (int a, int b, int m) {
 return mult(a, mpow(b, m-2, m), m);
```

```
// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
if (n < 2) return false:
if (n == 2) return true;
if (n % 2 == 0) return false:
ull s = n - 1:
while (s \% 2 == 0) s /= 2:
for (int i = 0; i < 10; i++) {</pre>
 ull temp = s:
 ull a = rand() \% (n - 1) + 1;
 ull mod = mpow(a, temp, n):
 while (temp != n - 1 && mod != 1 && mod != n

→ - 1) {
  mod = mult(mod, mod, n):
  temp *= 2;
 if (mod != n - 1 && temp % 2 == 0) return
 \hookrightarrow false:
return true;
```

Sieve of Eratosthenes

```
bitset<100000001> sieve:
// generate sieve - O(n log n)
void genSieve(int n) {
sieve[0] = sieve[1] = 1;
for (ull i = 3: i * i < n: i += 2)
 if (!sieve[i])
 for (ull j = i * 3; j <= n; j += i * 2)
   sieve[j] = 1;
// guery sieve after it's generated - O(1)
bool querySieve(int n) {
return n == 2 || (n % 2 != 0 && !sieve[n]);
```

Simpson's / Approximate Integrals

```
// integrate f from a to b, k iterations
```

Common Equations Solvers

```
// ax^2 + bx + c = 0, find x
vector<double> solveEq(double a, double b.
\hookrightarrow double c) {
vector<double> r;
double z = b * b - 4 * a * c:
if (z == 0)
 r.push_back(-b/(2*a));
 else if (z > 0) {
 r.push back((sqrt(z)-b)/(2*a));
 r.push_back((sqrt(z)+b)/(2*a));
return r;
// ax^3 + bx^2 + cx + d = 0, find x
vector<double> solveEq(double a. double b.
⇔ double c, double d) {
vector<double> res:
long double a1 = b/a, a2 = c/a, a3 = d/a;
long double q = (a1*a1 - 3*a2)/9.0, sq = -2*
long double r = (2*a1*a1*a1 - 9*a1*a2 + 27*a3)
 \hookrightarrow )/54.0;
long double z = r*r-q*q*q, theta:
 if (z \le 0) {
 theta = acos(r/sqrt(q*q*q));
 res.push_back(sq*cos(theta/3.0) - a1/3.0);
 res.push back(sq*cos((theta+2.0*PI)/3.0) -
  \hookrightarrow a1/3.0):
  res.push back(sq*cos((theta+4.0*PI)/3.0) -
 \hookrightarrow a1/3.0);
}
 res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
 res[0] = (res[0] + a / res[0]) * ((r<0))
  \hookrightarrow ?1:-1) - a1 / 3.0;
```

```
// m = # equations, n = # variables, a[m][n+1]
// a[i][0]x + a[i][1]y + ... + a[i][n]z = a[i]
const double eps = 1e-7;
bool zero(double a) { return (a < eps) && (a >
vector<double> solveEq(double **a, int m, int
\hookrightarrow n) {
 int cur = 0:
 for (int i = 0; i < n; i++) {</pre>
 for (int j = cur; j < m; j++) {</pre>
  if (!zero(a[i][i])) {
   if (j != cur) swap(a[j], a[cur]);
   for (int sat = 0: sat < m: sat++) {</pre>
    if (sat == cur) continue:
    double num = a[sat][i] / a[cur][i];
    for (int sot = 0: sot <= n: sot++)</pre>
     a[sat][sot] -= a[cur][sot] * num;
   cur++;
   break:
  }
 }
 for (int j = cur; j < m; j++)</pre>
 if (!zero(a[j][n])) return vector<double>();
 vector<double> ans(n,0);
 for (int i = 0, sat = 0: i < n: i++)
  if (sat < m && !zero(a[sat][i]))</pre>
  ans[i] = a[sat][n] / a[sat++][i]:
 return ans;
    Graph
```

Setup

}

```
bool operator > (const edge &e1, const edge &
\hookrightarrow e2) { return e1.w > e2.w: }
struct subset { int p, rank; };
Eulerian Path
#define edge_list vector<edge>
#define adi sets vector<set<int>>
struct EulerPathGraph {
 adj sets graph; // actually indexes incident
 edge list edges: int n: vector<int> indeg:
 EulerPathGraph(int n): n(n) {
 indeg = *(new vector<int>(n.0));
 graph = *(new adj_sets(n, set<int>()));
 void add edge(int u, int v) {
 graph[u].insert(edges.size());
 indeg[v]++:
 edges.push back(edge(u,v,0));
 bool eulerian path(vector<int> &circuit) {
 if(edges.size()==0) return false;
 stack<int> st;
  int a[] = \{-1, -1\};
  for(int v=0:v<n:v++) {</pre>
  if(indeg[v]!=graph[v].size()) {
   bool b = indeg[v] > graph[v].size();
   if (abs(((int)indeg[v])-((int)graph[v].size
   \hookrightarrow ())) > 1) return false:
   if (a[b] != -1) return false:
   a[b] = v;
  }
 }
  int s = (a[0]!=-1 \&\& a[1]!=-1 ? a[0] : (a
  \hookrightarrow [0]==-1 && a[1]==-1 ? edges[0].u : -1));
  if(s==-1) return false:
  while(!st.empty() || !graph[s].empty()) {
  if (graph[s].empty()) { circuit.push_back(s
  \hookrightarrow ); s = st.top(); st.pop(); }
   int w = edges[*graph[s].begin()].v;
    graph[s].erase(graph[s].begin());
   st.push(s): s = w:
```

```
circuit.push_back(s);
  return circuit.size()-1==edges.size();
};
```

Minimum Spanning Tree

```
// returns vector of edges in the mst
// graph[i] = vector of edges incident to

→ vertex i

// places total weight of the mst in &total
// if returned vector has size != n-1, there
vector<edge> mst(vector<vector<edge>> graph.
→ 11 &total) {
    total = 0:
    priority_queue<edge, vector<edge>, greater<</pre>

→ edge>> pq;

    vector<edge> MST;
    bitset<20001> marked; // change size as
    \hookrightarrow needed
    marked[0] = 1:
    for (edge ep : graph[0]) pq.push(ep);
    while(MST.size()!=graph.size()-1 && pq.size
    \hookrightarrow ()!=0) {
        edge e = pq.top(); pq.pop();
        int u = e.u. v = e.v. w = e.w:
       if(marked[u] && marked[v]) continue;
        else if(marked[u]) swap(u, v);
       for(edge ep : graph[u]) pq.push(ep);
       marked[u] = 1;
       MST.push back(e):
       total += e.w:
    return MST:
```

Union Find