```
else n = n * 10 + c - '0':
    General
                             7 Graphs
    Algorithms
                              8 2D Geometry
                                                            n = s * (n + m * o):
    Structures
                              9 3D Geometry
                                                           void read(double& n) {
    Strings
                                                            ld m; read(m); n = m;
                              10 Optimization
    Greedy
                              11 Additional
                                                           void read(float& n) {
 ld m: read(m): n = m:
    Math
     General
                                                            void read(string& s) {
                                                            char c; s = "
g++ -g -02 -std=gnu++17 -static prog.cpp
./a.exe
run.sh
                                                            while((c=getchar unlocked())!=' '&&c!='\n')
                                                            bool readline(string& s) {
                                                            char c; s = "";
while(c=getchar unlocked()) {
# compile and test all *.in and *.ans
g++ -g -02 -std=gnu++17 -static prog.cpp
for i in *.in; do
                                                             if (c == '\n') return true;
if (c == EOF) return false;
s += c;
 f=${i%.in}
 ./a.exe < $i > "$f.out"
diff -b -q "$f.ans" "$f.out"
                                                            return false;
done
                                                            void print(unsigned int n) {
Header
                                                            if (n / 10) print(n / 10);
// use better compiler options
                                                            putchar_unlocked(n % 10 + '0');
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
                                                            void print(int n) {
// include everything
                                                            if (n < 0) { putchar_unlocked('-'); n*=-1; }
 #include <bits/stdc++.h>
                                                            print((unsigned int)n);
#include <bits/extc++.h>
#include <sys/resource.h>
// namespaces
                                                           Common Structs
using namespace std;
                                                               n-dimension vectors
using namespace __gnu_cxx; // rope
                                                               Vec<2, int>v(n, m) = arr[n][m]
using namespace __gnu_pbds; // tree/trie
                                                            // Vec<2, int> v(n, m, -1) default init -1
                                                            template<int D, typename T>
// common defines
#define fastio
                                                            struct Vec : public vector < Vec < D-1, T >> {
                                                              template<typename... Args>

→ ios base::sync with stdio(0);cin.tie(0);
                                                              Vec(int n=0, Args... args) : vector<Vec<D-1,
#define nostacklim rlimit RZ; getrlimit(3,&RZ
                                                            \rightarrow T>>(n, Vec<D-1, T>(args...)) {}
    ):RZ.rlim cur=-1:setrlimit(3.&RZ):
#define DEBUG(v) cerr<< LINE <<": "<<#v<<" =
                                                           template<typename T>
\Rightarrow "<<v<<'\n'; #define TIMER
                                                           struct Vec<1, T> : public vector<T> {
                                                              Vec(int n=0, T val=T()) : vector<T>(n, val)

→ cerr<<1.0*clock()/CLOCKS_PER_SEC<<"s\n";
#define ll long long
#define ull unsigned ll
#define i128 __int128
#define u128 unsigned i128
                                                               {}
                                                                Algorithms
#define ld long double
                                                           Min/Max Subarray
// global variables
                                                              max - compare = a < b, reset = a < 0
mt19937 rng((uint32_t)chrono::steady
                                                            \frac{1}{min} - compare = a > b, reset = a > 0

    clock::now().time since epoch().count());

                                                           // returns {sum, {start, end}}
pair<int, pair<int, int>>
Fast IO
                                                                ContiguousSubarray(int* a, int size,
#ifdef _WIN32
                                                                bool(*compare)(int, int),
#define getchar_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
                                                            bool(*reset)(int), int defbest = 0) {
int best = defbest, cur = 0, start = 0, end =
                                                            0, s = 0;
for (int i = 0; i < size; i++) {
  cur += a[i];</pre>
void read(unsigned int& n) {
 char c; n = 0;
while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                              if ((*compare)(best, cur)) { best = cur;
  n = n * 10 + c - 0';
                                                            \rightarrow start = s; end = i; }
void read(int& n) {
  char c; n = 0; int s = 1
                                                             if ((*reset)(cur)) { cur = 0; s = i + 1; }
 if ((c=getchar_unlocked())=='-') s = -1;
                                                            return {best, {start, end}}:
 else n = c - '0';
while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                            Quickselect
 n = n * 10 + c - 0';
                                                           #define OSNE -999999
                                                           int partition(int arr[], int 1, int r)
void read(ld& n) {
 char c; n = 0;
ld m = 0, o = 1; bool d = false; int s = 1;
if ((c=getchar_unlocked())=='-') s = -1;
                                                            int x = arr[r], i = 1;
for (int j = 1; j <= r - 1; j++)
...if (arr[j] <= x)
...swap(arr[i++], arr[j]);</pre>
 else if (c == .'.') d = true;
else n = c - '0';
 while ((c=getchar_unlocked())!=' '&&c!='\n') {
                                                            swap(arr[i], arr[r]);
 if (c == '.') d = true;
else if (d) { m=m*10+c-'0'; o*=0.1; }
                                                            return i:
```

```
// find k'th smallest element in unsorted array, void update(int i, int val) {
→ only if all distinct
int gselect(int arr[], int 1, int r, int k)
 if (!(k > 0 && k <= r - l + 1)) return QSNE;
swap(arr[1 + rng() % (r-l+1)], arr[r]);
 int pos = partition(arr, 1, r);
if (pos-l==k-1) return arr[pos];
 if (pos-1>k-1) return qselect(arr,1,pos-1,k);
 return qselect(arr, pos+1, r, k-pos+1-1);
// TODO: compare against std::nth_element()
Saddleback Search
// search for v in 2d array arr[x][y], sorted

    on both axis
pair<int, int> saddleback_search(int** arr, int
 \rightarrow x, int y, int v) {
 int i = x-1, j = 0;
 while (i >= 0 && j < y) {
  if (arr[i][j] == v) return {i, j};
  (arr[i][j] > v)? i--: j++;
 return {-1, -1};
Ternary Search
 // < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {</pre>
 while (b-a > 4) {
    int m = (a+b)/2;
    if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
  else b = m+1:
 for (int i = a+1; i <= b; i++)
if (TERNCOMP((*f)(a), (*f)(i)))
   a = i;
 return a;
#define TERNPREC 0.000001
double ternsearch (double a. double b. double
 \leftrightarrow (*f)(double)) {
while (b-a > TERNPREC * 4) {
  double m = (a+b)/2;
  if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
  else b = m + TERNPREC;
 for (double i = a + TERNPREC: i <= b: i +=
     TERNPREC)
      if (TERNCOMP((*f)(a), (*f)(i)))
 return a;
Golden Section Search
// < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
double goldsection(double a, double b, double
 while (b-a > eps)
  while (b-a > eps)

if (TERNCOMP(f2,f1)) {

   b = x2; x2 = x1; f2 = f1;

   x1 = b - r*(b-a); f1 = f(x1);
  } else {
   a = x1; x1 = x2; f1 = f2;

x2 = a + r*(b-a); f2 = f(x2);
 return a:
3 Structures
Fenwick Tree
// Fenwick tree, array of cumulative sums -
```

 $\hookrightarrow$  O(log n) updates, O(log n) gets

struct Fenwick { int n; ll\* tree;

```
while (i <= n) {
   tree[i] += val;
   i += i & (-i);
 Fenwick(int size) {
  n = size;
  tree = new ll[n+1];
for (int i = 1; i <= n; i++)
   .tree[i] = 0;
 Fenwick(int* arr, int size) : Fenwick(size) {
  for (int i = 0; i < n; i++)
...update(i, arr[i]);
 ~Fenwick() { delete[] tree; }
 ll operator[](int i) {
  if (i < 0 || i > n) return 0;
  \overline{11} \ \overline{sum} = 0;
  while (i>0)
   sum += tree[i];
   i -= i & (-i):
  return sum:
 ll getRange(int a, int b) { return

    operator[](b) - operator[](a-1); }

Hashtable
// similar to unordered map, but faster
struct chash {
    const uint64 t C = (11)(2e18 * M PI) + 71;
 ll operator()(ll x) const { return
    builtin bswap64(x*C); }
int main() {
  gp_hash_table<11,int,chash>
 \rightarrow hashtable({},{},{},{},{1<<16});
 for (int i = 0; i < 100; i++)
hashtable[i] = 200+i;
 if (hashtable.find(10) != hashtable.end())
   cout << hashtable[10];</pre>
Ordered Set
template <typename T>
using oset = tree<T,null_type,less<T>,rb_tree
    _tag,tree_order_statistics_node_update>;
template <typename T, typename D> using omap = tree<T,D,less<T>,rb_tree
    _tag,tree_order_statistics_node_update>;
int main()
 oset<int> o_set;
o_set.insert(5); o_set.insert(1);
 → o_set.insert(3);
// get second smallest element
 cout << *(o set.find by order(1));</pre>
 // number of elements less than k=4
cout << ' ' << o_set.order_of_key(4) << '\n';</pre>
 // equivalent with ordered map
 omap<int,int> o_map;
o_map[5]=1;o_map[1]=2;o_map[3]=3;
 cout << (*(o_map.find_by_order(1))).first;</pre>
 cout << ' ' << o map.order of key(4) << '\n';
Rope
// O(log n) insert, delete, concatenate
int main() {
 // generate rove
 rope<int> v;
 for (int i = 0: i < 100: i++)
  v.push_back(i);
 // move range to front
 rope<int> copy = v.substr(10, 10);
 v.erase(10, 10);
```

```
v.insert(copy.mutable_begin(), copy);
                                                           cur = s[cur].go[c-OFFC]:
 // print elements of rope
for (auto it : v)
cout << it << "":
                                                         s[cur].out.insert({arr[i].size(), id++}):
                                                        for (int c = 0; c < MAXC; c++)
if (s[0].go[c] == -1)
Segment Tree
                                                          s[0].go[c] = 0;
//max(a,b), min(a,b), a+b, a*b, acd(a,b), a^b
                                                        queue:int> sq;
for (int c = 0; c < MAXC; c++) {
    if (s[0].go[c] != 0) {
struct SegmentTree {
 typedef int T;
 static constexpr T UNIT = INT MIN;
                                                          s[s[0].go[c]].fail = 0;
 T f(T a, T b) {
                                                           sq.push(s[0].go[c]);
 if (a == UNIT) return b;
if (b == UNIT) return a:
  return max(a,b);
                                                         while (sq.size()) {
                                                         int e = sq.front(); sq.pop();
for (int c = 0; c < MAXC; c++) {</pre>
 int n: vector<T> s:
 SegmentTree(int n, T def=UNIT) : s(2*n, def),
                                                           if (s[e].go[c] != -1) {
\rightarrow n(n) {}
                                                            int failure = s[e].fail;
 SegmentTree(vector<T> arr) :
                                                            while (s[failure].go[c] == -1)

→ SegmentTree(arr.size()) {
                                                              failure = s[failure].fail;
  for (int i=0; i < arr. size(); i++)
                                                            failure = s[failure].go[c];

→ update(i,arr[i]);

                                                            s[s[e].go[c]].fail = failure;
                                                            for (auto length : s[failure].out)
  s[s[e].go[c]].out.insert(length);
 void update(int pos, T val) {
  for (s[pos += n] = val; pos /= 2;)
   s[pos] = f(s[pos * 2], s[pos*2+1]);
                                                            sq.push(s[e].go[c]);
 T query(int b, int e) { // query [b, e)
  T ra = UNIT, rb = UNIT;
 for (b+=n, e+=n; b<=; b/=2, e/=2) {
    if (b % 2) ra = f(ra, s[b++]);
    if (e % 2) rb = f(s[--e], rb);
                                                        // list of {start pos, pattern id}
                                                        vector<pair<int, int>> search(string text)
                                                         vector<pair<int, int>> toret;
  return f(ra, rb);
                                                         int cur = 0:
                                                        for (int i = 0; i < text.size(); i++) {
  while (s[cur].go[text[i]-OFFC] == -1)
 T get(int p) { return query(p, p+1); }
                                                          cur = s[cur].fail:
Trie
                                                          cur = s[cur].go[text[i]-OFFC];
typedef trie<string, null_type,
                                                          if (s[cur].out.size())

trie_string_access_traits<>,

trie_string_access_traits<>,
                                                           for (auto end : s[cur].out)
toret.push back({i - end.first + 1,
 pat_trie_tag, trie_prefix_search_node_update>
                                                           end.second});
int main() {
                                                         return toret:
 // generate trie
 trie_type trie;
 for (int i = 0; i < 20; i++)
 trie.insert(to_string(i)); // true if new,
                                                       Bover Moore
\hookrightarrow false if old
                                                       struct defint { int i = -1; };
 // print things with prefix "1"
                                                       vector<int> boyermoore(string txt, string pat)
 auto range = trie.prefix_range("1");
 for (auto it = range.first; it !=
                                                       vector<int> toret: unordered map<char, defint>Longest Common Prefix (array)

→ range.second; it++)

                                                        → badchar:
  cout << *it <<
                                                       int m = pat.size(), n = txt.size();
                                                       for (int i = 0; i < m; i++) badchar[pat[i]].i
                                                        \rightarrow = i;
4 Strings
                                                        while (s \le n - m) {
Aho Corasick
                                                        int j = m - 1;
// range of alphabet for automata to consider
                                                         while (j \ge 0) && pat[j] == txt[s + j]) j--;
// MAXC = 26, OFFC = 'a' if only lowercase
                                                         if (i < 0) {
const int MAXC = 256;
const int OFFC = 0:
                                                         toret.push back(s):
                                                         s += (s + m < n) ? m - badchar[txt[s +
struct aho corasick {
                                                          mll.i : 1:
 struct state
  set<pair<int, int>> out:
                                                         s += max(1, j - badchar[txt[s + j]].i);
  int fail; vector<int> go;
                                                       return toret:
  state() : fail(-1), go(MAXC, -1) {}
 vector<state> s;
                                                       English Conversion
 int id = 0;
                                                      const string ones[] = {"", "one", "two",
 aho_corasick(string* arr, int size) : s(1) {
                                                       "three", "four", "five", "six", "seven", "ieight", "nine";
 for (int i = 0: i < size: i++) {
  int cur = 0:
 ...for (int c : arr[i]) {
...if (s[cur].go[c-0FFC] == -1) {
                                                       const string teens[] ={"ten", "eleven",
```

s[cur].go[c-OFFC] = s.size();

...s.push back(state());

"twelve", "thirteen", "fourteen",
"fifteen", "sixteen", "seventeen",
"eighteen", "nineteen"};

```
|const string tens[] = {"twenty", "thirty",
    "forty", "fifty", "sixty", "seventy",
    "eighty", "ninety"};
const string mags[] = {"thousand", "million";
    "billion", "trillion", "quadrillion",
    "quintillion", "sextillion",
    "septillion"}:
string convert(int num, int carry) {
 if (num < 0) return "negative " +
    convert(-num, 0);
if (num < 10) return ones[num];
if (num < 20) return teens[num % 10];
if (num < 100) return tens[(num / 10) - 2] +
     (num\%10==0?"":"") + ones[num \% 10];
 if (num < 1000) return ones[num / 100]
     (num/100==0?"":" ") + "hundred" +
    (num%100==0?"":" ") + convert(num % 100,
   0):
 return convert(num / 1000, carry + 1) + " " +
    mags[carry] + " " + convert(num % 1000,
   0):
string convert(int num) {
 return (num == 0) ? "zero" : convert(num, 0):
Knuth Morris Pratt
vector<int> kmp(string txt, string pat) {
    vector<int> toret;
 int m = txt.length(), n = pat.length();
 int next[n + 1];
 for (int i = 0; i < n + 1; i++)
 next[i] = 0;
for (int i = 1; i < n; i++) {
  int j = next[i + 1];
  while (j > 0 && pat[j] != pat[i])
  .j = next[j];
  if (j > 0 | pat[j] == pat[i])
  next[i + 1] = j + 1;
 for (int i = 0, j = 0; i < m; i++) {
  if (txt[i] == pat[j]) {
   if (++j == n)
    toret.push_back(i - j + 1);
  .} else if (j > 0) {
  .j = next[j];
 return toret;
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =

→ false) {
if (n == 0) return "";
if (!sorted) sort(arr, arr + n);
string r = ""; int v = 0;
 while (v < arr[0].length() && arr[0][v] ==
 → arr[n-1][v])
  r += arr[0][v++];
 return r;
Longest Common Subsequence
string lcs(string a, string b) {
 int m = a.length(), n = b.length();
 int L[m+1][n+1];
for (int i = 0: i <= m: i++) {</pre>
 for (int j = 0; j <= n; j++) {
    if (i == 0 || j == 0) L[i][j] = 0;
    else if (a[i-1] == b[j-1]) L[i][j] =
   L[i-1][j-1]+1;
   else L[i][j] = max(L[i-1][j], L[i][j-1]);
 // return L[m][n]; // length of lcs
```

```
string out = "";
int i = m - 1, j = n - 1;
 while (i >= 0 && i >= 0) {
 if (a[i] == b[i]) {
   out = a[i--] + out;
  else if (L[i][j+1] > L[i+1][j]) i--;
 else j--;
return out;
Longest Common Substring
// l is array of palindrome length at that
\rightarrow index
int manacher(string s, int* 1) {
int n = s.length() * 2;
for (int i = 0, j = 0, k; i < n; i += k, j =
 \rightarrow max(j-k, 0)) {
 while (i \ge j \&\& i + j + 1 < n \&\& s[(i-j)/2]
 \rightarrow == s[(i+j+1)/2]) j++;
 1[i] = j;
 for (k = 1; i >= k \&\& i >= k \&\& 1[i-k] !=
   i-k: k++)
  l[i+k] = min(l[i-k], j-k);
return *max element(1, 1 + n):
Cyclic Rotation (Lyndon)
// simple strings = smaller than its nontrivial
// lyndon factorization = simple strings
   factorized
// "abaaba" -> "ab", "aab", "a"
vector<string> duval(string s) {
int n = s.length();
 vector<string> lyndon;
for (int i = 0; i < n;) {
   int j = i+1, k = i;
   for (; j < n && s[k] <= s[j]; j++)
  if (s[k] < s[j]) k = i;
   else k++:
 for (; i <= k; i += j - k)
  lyndon.push_back(s.substr(i,j-k));
return lyndon;
// lexicographically smallest rotation
int minRotation(string s) {
 int n = s.length(); s += s;
 auto d = duval(s); int i = 0, a = 0;
 while (a + d[i].length() < n) a +=
→ d[i++].length();
while (i && d[i] == d[i-1]) a -=

→ d[i--].length();

return a:
Subsequence Count
   "banana", "ban" \gg 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
int m = subs.length(), n = body.length();
if (m > n) return 0:
 ull** arr = new ull*[m+1];
for (int i = 0; i \le m; i++) arr[i] = new
 \rightarrow ull[n+1];
for (int i = 1; i <= m; i++) arr[i][0] = 0;
for (int i = 0; i <= n; i++) arr[o][i] = 1;
for (int i = 1; i <= m; i++)
 for (int j = 1; j <= n; j++)
arr[i][j] = arr[i][j-1] + ((body[j-1] ==
```

 $\rightarrow$  subs[i-1])? arr[i-1][j-1] : 0);

return arr[m][n]:

```
Suffix Array + LCP
                                                                           for(int c=0; c<ALPHA; c++) if
                                                                                                                                                   Combinatorics (nCr, nPr)
                                                                                                                                                                                                                              .c = (c * an) \% m;
                                                                             (t[node][c]!=-1)
mask |= lcs(t[node][c]. i1. i2. len):
struct SuffixArray {
                                                                                                                                                   // can optimize by precomputing factorials, and
 vector<int> sa. lcp:
                                                                                                                                                         fact[n]/fact[n-r]
                                                                                                                                                                                                                             for (int i = 0; i <= n; i++) {
   if (dlogc.count(c)) return (dlogc[c] * n - i</pre>
                                                                            if (mask==3)
 SuffixArray(string& s, int lim=256) {
int n = s.length() + 1, k = 0, a, b;
                                                                              best=max(best, {len,r[node]-len});
                                                                                                                                                   ull nPr(ull n, ull r) {
                                                                                                                                                    ull v = 1;
for (ull i = n-r+1: i <= n: i++)
                                                                            return mask;
                                                                                                                                                                                                                             + m - 1) \% (m-1);
c = (c * a) \% m;
  vector<int> x(begin(s), end(s)+1), y(n),
 \rightarrow ws(max(n, lim)), rank(n);
                                                                           static pair<int, int> LCS(string s, string t)
                                                                                                                                                    return v;
                                                                                                                                                                                                                             return -1;
   iota(begin(sa), end(sa), 0);
                                                                            SuffixTree
                                                                                                                                                   ull nPr(ull n, ull r, ull m) {
                                                                           \rightarrow st(s+(char)('z'+1)+t+(char)('z'+2));
  for (int j = 0, p = 0; p < n; j = max(1, j *
                                                                                                                                                    \overline{ull} v = 1;
                                                                            st.lcs(0, s.size(), s.size()+t.size()+1, 0);
return st.best;
                                                                                                                                                                                                                            Euler Phi / Totient
 \rightarrow 2), lim = p) {
                                                                                                                                                    for (ull i = n-r+1; i \le n; i++)
 p = j; iota(begin(y), end(y), n - j);
for (int i = 0; i < (n); i++)
if (sa[i] >= j)
                                                                                                                                                     v = (v * i) \% m;
                                                                                                                                                                                                                             int phi(int n) {
                                                                                                                                                                                                                            int r = n;

for (int i = 2; i * i <= n; i++) {

    if (n % i == 0) r -= r / i;

    while (n % i == 0) n /= i;
                                                                                                                                                    return v:
                                                                                                                                                   ull nCr(ull n, ull r) {
      y[p++] = sa[i] - j
                                                                         String Utilities
   fill(begin(ws), end(ws), 0);
for (int i = 0; i < (n); i++) ws[x[i]]++;
for (int i = 1; i < (lim); i++) ws[i] +=
                                                                                                                                                    long double v = 1;
                                                                                                                                                    for (ull i = 1; i <= r; i++)
                                                                         void lowercase(string& s) {
                                                                                                                                                     v = v * (n-r+i) /i;
                                                                                                                                                                                                                              if (n > 1) r = r / n:
                                                                           transform(s.begin(), s.end(), s.begin(),
                                                                                                                                                    return (ull)(v + 0.001):
                                                                                                                                                                                                                             return r;
                                                                               ::tolower);
 \hookrightarrow ws[i - 1];
 for (int i = n; i--;) sa[-ws[x[v[i]]]] =
                                                                                                                                                                                                                            #define n 100000
                                                                                                                                                   // requires modulo math
                                                                          void uppercase(string& s) {
                                                                                                                                                                                                                            ll phi[n+1];

y[i];

                                                                                                                                                   // can optimize by precomputing mfac and
                                                                           transform(s.begin(), s.end(), s.begin(),
                                                                                                                                                                                                                            void computeTotient() {
    swap(x, y); p = 1; x[sa[0]] = 0;
                                                                          \rightarrow ::toupper);
                                                                                                                                                                                                                             for (int i=1; i<=n; i++) phi[i] = i;
    for (int i = 1; i < (n); i++) {
   a = sa[i - 1]; b = sa[i];
                                                                                                                                                   ull nCr(ull n, ull r, ull m) {
                                                                                                                                                                                                                             for (int p=2; p<=n; p++) {
                                                                                                                                                    return mfac(n, m) * minv(mfac(k, m), m) % m *
                                                                         void trim(string &s) {
     x[b] = (y[a] == y[b] && y[a + j] == y[b +
                                                                                                                                                                                                                              if (phi[p] == p) {
                                                                                                                                                   \rightarrow minv(mfac(n-k, m), m) % m:
                                                                           s.erase(s.begin(),find_if_not(s.begin(),s
     j]) ? p - 1 : p++;
                                                                                                                                                                                                                                phi[p] = p-1;
                                                                                .end(),[](int c){return
                                                                                                                                                                                                                                for (int i = 2*p; i<=n; i += p) phi[i] =
                                                                                                                                                   Multinomials
                                                                               isspace(c);}));
                                                                                                                                                                                                                                  (phi[i]/p) * (p-1);
                                                                          | Simplified to the state of th
   for (int i = 1; i < (n); i++) rank[sa[i]] =
                                                                               c){return isspace(c);}).base(),s.end());
                                                                                                                                                   for(int i = 1; i < v.size(); i++)

for (int j = 0; j < v[i]; j++)

...c = c * ++m / (j+1);
 for (int i = 0, j; i < n - 1; lcp[rank[i++]]
                                                                         vector<string> split(string& s, char token) {
 for (k \&\& k--, j = sa[rank[i] - 1];
                                                                                                                                                                                                                            Factorials
                                                                               vector<string> v; stringstream ss(s);
                                                                                                                                                    return c:
                                                                                                                                                                                                                            // digits in factorial
       s[i + k] == s[j + k]; k++);
                                                                                for (string e;getline(ss,e,token);)
                                                                                                                                                                                                                            #define kamenetsky(n) (floor((n * log10(n /
                                                                                      v.push_back(e);
};
                                                                                                                                                                                                                             \hookrightarrow M_E)) + (log10(2 * M_PI * n) / 2.0)) + 1)
                                                                                                                                                   Chinese Remainder Theorem
                                                                               return v;
                                                                                                                                                                                                                             // approximation of factorial
                                                                                                                                                   bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
Suffix Tree (Ukkonen's)
                                                                                                                                                                                                                            #define stirling(n) ((n == 1) ? 1 : sqrt(2 *
struct SuffixTree {
                                                                                                                                                    11 x, y, d; mo = m[0]; re = r[0];
                                                                                Greedy
                                                                                                                                                                                                                             \hookrightarrow M_PI * n) * pow(n / M_E, n))
 .// n = 2*len+10 or so
enum { N = 50010, ALPHA = 26 };
int toi(char c) { return c - 'a'; }
                                                                                                                                                    for (int i = 1: i < n: i++) {
                                                                                                                                                                                                                             // natural log of factorial
                                                                                                                                                     d = egcd(mo, m[i], x, y);
                                                                         Interval Cover
                                                                                                                                                                                                                            #define lfactorial(n) (lgamma(n+1))
                                                                                                                                                     if ((r[i] - re) % d != 0) return false;

x = (r[i] - re) / d * x % (m[i] / d);

re += x * mo;
                                                                           // L,R = interval [L,R], in = {{l,r}, index}
\rightarrow t[N][ALPHA],1[N],r[N],p[N],s[N],v=0,q=0,m=2 // does not handle case where L==R string a; vector<int> intervalCover(double L, double R,
                                                                                                                                                                                                                             Prime Factorization
                                                                                                                                                                                                                            // do not call directlu
                                                                                                                                                     mo = mo / d * m[i];
                                                                                                                                                                                                                            11 pollard_rho(ll n, ll s) {
 void ukkadd(int i, int c) { suff:

    vector<pair<double,double>,int>> in) {
                                                                                                                                                     re %= mo;
  if (r[v]<=q) {
                                                                                                                                                                                                                             .11 x, y;
                                                                               int i = 0; pair<double,int> pos = {L,-1};
   if (t[v][c]==-1) { t[v][c]=m; l[m]=i;
    p[m++]=v; v=s[v]; q=r[v]; goto suff; }
                                                                                                                                                                                                                             x = y = rand() \% (n - 1) + 1;
                                                                               vector<int> a;
                                                                                                                                                    \check{r}e = (re + mo) \% mo;
                                                                                                                                                                                                                             int head = 1, tail = 2;
while (true) {
                                                                               sort(begin(in), end(in));
                                                                                                                                                    return true:
    v=t[v][c]; q=l[v];
                                                                                while (pos.first < R) {
                                                                                                                                                                                                                              x = mult(x, x, n);
                                                                                      double cur = pos.first;
   if (q==-1 || c==toi(a[q])) q++; else {
    l[m+1]=i; p[m+1]=m; l[m]=l[v]; r[m]=q;
                                                                                                                                                   Count Digit Occurences
                                                                                                                                                                                                                              x = (x + s) \% n;
if (x == y) return n;
                                                                                      while (i < (int)in.size() &&
                                                                                                                                                   /stcount(n,d) counts the number of occurences of
                                                                               in[i].first.first <= cur)</pre>
    p[m]=p[v]; t[m][c]=m+1; t[m][toi(a[q])]=v;
l[v]=q; p[v]=m; t[p[m]][toi(a[l[m]])]=m;
v=s[p[m]]; q=l[m];
                                                                                                                                                                                                                              11 d = gcd(max(x - y, y - x), n);
if (1 < d && d < n) return d;
                                                                                                                                                    \rightarrow a digit d in the range [0,n]*/
                                                                               max(pos,{in[i].first.second,in[i].second}), | 11 digit count(11 n, 11 d) {
                                                                                                                                                                                                                               if (++head == tail) y = x, tail <<= 1;
                                                                              i++;
if (pos.first == cur) return {};
                                                                                                                                                    11 result = 0;
    while (q < r[m]) { v = t[v][toi(a[q])];
                                                                                                                                                    while (n != 0)
                                                                                                                                                     result += ((n\%10) == d ? 1 : 0);
 \rightarrow q+=r[v]-l[v]; }
                                                                                      a.push_back(pos.second);
                                                                                                                                                                                                                            // call for prime factors
                                                                                                                                                     n /= 10;
    if (q==r[m]) s[m]=v; else s[m]=m+2;
                                                                                                                                                                                                                            void factorize(ll n, vector<ll> &divisor) {
                                                                               return a;
    q=r[v]-(q-r[m]); m+=2; goto suff;
                                                                                                                                                                                                                             if (n == 1) return;
                                                                                                                                                    return result;
                                                                                                                                                                                                                             if (isPrime(n)) divisor.push_back(n);
                                                                                                                                                   ll count(ll n. ll d) {
                                                                                Math
 SuffixTree(string a) : a(a) {
                                                                                                                                                    if (n < 10) return (d > 0 \&\& n >= d);
  fill(r,r+N,(int)(a).size());
                                                                                                                                                                                                                              while (d'>= n) d = pollard_rho(n, rand() % (n
                                                                                                                                                    if ((n % 10) != 9) return digit_count(n, d) +
                                                                         Catalan Numbers
  memset(s, 0, sizeof s);

memset(t, -1, sizeof t);

fill(t[1],t[1]+ALPHA,0);

s[0]=1;1[0]=1[1]=-1;r[0]=r[1]=p[0]=p[1]=0;
                                                                                                                                                                                                                             \rightarrow -1) +1);
factorize(n / d, divisor);
                                                                                                                                                    \hookrightarrow count(n-1, d);
                                                                         ull* catalan = new ull[1000000];
                                                                                                                                                    return 10*count(n/10, d) + (n/10) + (d > 0):
                                                                         void genCatalan(int n, int mod) {
                                                                                                                                                                                                                             factorize(d, divisor);
                                                                          catalan[0] = catalan[1] = 1;
for (int_i = 2; i <= n; i++) {
  for(int i=0; i < a. size(); i++)
                                                                                                                                                   Discrete Logarithm
                                                                            catalan[i] = 0;

    ukkadd(i,toi(a[i]));

                                                                                                                                                   unordered_map<int, int> dlogc;
                                                                            for (int j = i - 1; j >= 0; j--) {
                                                                                                                                                                                                                            Farey Fractions
                                                                                                                                                   int discretelog(int a, int b, int m) {
                                                                              catalan[i] += (catalan[j] * catalan[i-j-1])
 // Longest Common Substring between 2 strings
                                                                                                                                                                                                                                 generate 0 \le a/b \le 1 ordered, b \le n
                                                                                                                                                    dlogc.clear();
 // returns {length, offset from first string}
                                                                                                                                                                                                                            // farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
                                                                                                                                                    ll n = sqrt(m)+1, an = 1;
                                                                             if (catalan[i] >= mod)
   catalan[i] -= mod;
 pair<int, int> best;
                                                                                                                                                    for (int i = 0; i < n; i++)
an = (an * a) % m;
 int los(int node, int i1, int i2, int olen) {
   if (1[node] <= i1 && i1 < r[node]) return 1;
   if (1[node] <= i2 && i2 < r[node]) return 2;</pre>
                                                                                                                                                                                                                             int h = 0, k = 1, x = 1, y = 0, r;
                                                                                                                                                    11 c = an;
                                                                                                                                                    for (int i = 1; i \le n; i++)
                                                                                                                                                                                                                             vector<pair<int, int>> v;
                                                                             TODO: consider binomial coefficient method
                                                                                                                                                     if (!dlogc.count(c)) dlogc[c] = i;
                                                                                                                                                                                                                             do {

→ len=node?olen+(r[node]-l[node]):0:
```

```
v.push_back({h, k});
 r = (n-y)/k;
y += r*k; x += r*h;
swap(x,h); swap(y,k);
x = -x; y = -y;
} while (k > 1);
 v.push_back(\{1, 1\});
Fast Fourier Transform
#define cd complex<double>
const double PI = acos(-1):
void fft(vector<cd>& a, bool invert) {
int n = a.size();
for (int i = 1, j = 0; i < n; i++) {
  int bit = n >> 1;
  for (; j & bit; bit >>= 1) j ^= bit;
  i ^= bit:
  if (i < j) swap(a[i], a[j]);
 for (int len = 2; len <= n; len <<= 1) {
    double ang = 2 * PI / len * (invert ? -1 :
  cd wlen(cos(ang), sin(ang));
  for (int i = 0; i < n; i += len) {
   cd w(1);
   for (int j = 0; j < len / 2; j++) {
  cd u = a[i+j], v = a[i+j+len/2] * w;
    a[i+j] = u + v;
    a[i+j+len/2] = u - v;
    w = wlen:
 if (invert)
 for (auto& x : a)
  ..x /= n;
vector<int> fftmult(vector<int> const& a.

    vector<int> const& b) {

vector<cd> fa(a.begin(), a.end()),

    fb(b.begin(), b.end());

int n = 1 << (32 - _builtin_clz(a.size() +

→ b.size() - 1));
fa.resize(n); fb.resize(n);
fft(fa, false); fft(fb, false);
for (int i = 0; i < n; i++) fa[i] *= fb[i];</pre>
 fft(fa, true);
 vector<int> toret(n);
 for (int i = 0; i < n; i++) toret[i] =

→ round(fa[i].real());

return toret:
Greatest Common Denominator
ll egcd(ll a, ll b, ll& x, ll& y) {
if (b == 0) { x = 1; y = 0; return a; }
ll gcd = egcd(b, a % b, x, y);
 x = a / b * y;
swap(x, y);
return gcd;
Josephus Problem
// 0-indexed, arbitrary k
int josephus(int n, int k) {
if (n == 1) return 0;
 if (k == 1) return n-1:
 if (k > n) return (josephus(n-1,k)+k)%n;
 int res = josephus(n-n/k,k)-n\%k;
 return res + ((res<0)?n:res/(k-1));
^{
m N}_{\rm min} fast case if k=2, traditional josephus
int josephus(int n) {
return 2*(n-(1<<(32-_builtin_clz(n)-1)));
Least Common Multiple
#define lcm(a,b) ((a*b)/_gcd(a,b))
```

```
Modulo Operations
#define MOD 1000000007
#define madd(a,b,m) (a+b-((a+b-m>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a < b)?m:0))
ll mpow(ll b. ll e. ll m) {
 11 x = 1;
 while (e > 0) {
  if (e % 2) x = (x * b) % m;
 b = (b * b) \% m;
  e /= 2:
 return x % m:
ull mfac(ull n, ull m) {
 ull f = 1;
for (int i = n: i > 1: i--)
  f = (f * i) \% m;
 return f:
// if m is not quaranteed to be prime
11 minv(ll b, ll m) {
 11 x = 0, y = 0;

if (egcd(b, m, x, y) != 1) return -1;
 return (x % m + m) % m;
11 mdiv_compmod(int a, int b, int m) {
 if (__gcd(b, m) != 1) return -1;
 return mult(a, minv(b, m), m);
// if m is prime (like 10^9+7)
ll mdiv_primemod (int a, int b, int m) {
 return mult(a, mpow(b, m-2, m), m);
Modulo Tetration
11 tetraloop(ll a, ll b, ll m) {
 if(b == 0 | a == 1) return 1;
11 w = tetraloop(a,b-1,phi(m)), r = 1;
 for (;w;w/=2) {
 if (w&1) {
    r *= a; if (r >= m) r -= (r/m-1)*m;
  a *= a; if (a >= m) a -= (a/m-1)*m;
 return r:
int tetration(int a, int b, int m) {
  if (a == 0 || m == 1) return ((b+1)&1)%m;
 return tetraloop(a,b,m) % m;
Matrix
template<typename T>
struct Mat : public Vec<2, T> {
 int w, h;
 Mat(int x, int y) : Vec<2, T>(x, y), w(x),
 \rightarrow h(v) {}
 static Mat<T> identity(int n) { Mat<T> m(n,n);
    for (int i=0;i<n;i++) m[i][i] = 1; return
    m; }
 Mat<\hat{T}>\& operator+=(const Mat<T>\& m) {
  for (int i = 0; i < w; i++)

for (int j = 0; j < h; j++)

(*this)[i][j] += m[i][j];
  return *this:
 Mat<T>& operator-=(const Mat<T>& m) {
 for (int i = 0; i < w; i++)
for (int j = 0; j < h; j++)
(*this)[i][j] -= m[i][j];
  return *this;
 Mat<T> operator*(const Mat<T>& m) {
  Mat<T>z(w,m.h);
  for (int i = 0; i < w; i++)
   for (int j = 0; j < h; j++)

for (int k = 0; k < m.h; k++)

z[i][k] += (*this)[i][j] * m[j][k];
```

```
.Mat<T> operator+(const Mat<T>& m) { Mat<T>
 → a=*this; return a+=m; }
 Mat<T> operator-(const Mat<T>& m) { Mat<T>
 → a=*this; return a-=m; }
 Mat<T>& operator*=(const Mat<T>& m) { return
 \rightarrow *this = (*this)*m; }
 Mat<T> power(int n) {
 Mat<T> a = Mat<T>::identity(w), m=*this;
 for (;n;n/=2,m*=m) if (n&1) a *= m; return a:
Matrix Exponentiation
//F(n) = c[0]*F(n-1) + c[1]*F(n-2) + ...
 // b is the base cases of same length c
ll matrix_exponentiation(ll n, vector<ll> c,
→ vector<ll> b) {
    if (nth < b.size()) return b[nth-1];
    Mat<ll> a(c.size(), c.size()); ll s = 0;
    for (int i = 0; i < c.size(); i++) a[i][0] =
c[i];
for (int i = 0; i < c.size() - 1; i++)</pre>
 \rightarrow a[i][i+1] = 1;
a = a.power(nth - c.size());
 for (int i = 0; i < c.size(); i++)
s += a[i][0] * b[i];
return s;
Matrix Subarray Sums
template < class T> struct MatrixSum {
 Vec<2, T> p;
 MatrixSum(Vec<2, T>& v) {
 p[i+1][j] - p[i][i];
 T sum(int u, int 1, int d, int r) {
return p[d][r] - p[d][l] - p[u][r] + p[u][l];
Nimber Arithmetic
\#define\ nimAdd(a,b)\ ((a)^(b))
ull nimMul(ull a, ull b, int i=6) {
static const ull M[]={INT_MIN>>32,
M[0]^(M[0]<<16), M[1]^(M[1]<<8),

M[2]^(M[2]<<4), M[3]^(M[3]<<2),

M[4]^(M[4]<<1)};
  if (i--==0) return a&b;
  int k=1<<i;
  ull s=nimMul(a,b,i), m=M[5-i],
     t=nimMul(((a^(a>>k))&m)|(s&~m),
     ((b^{(b)}k))&m)|(m&(\sim m>>1))<< k, i);
  return ((s^t)\&m) << k | ((s^(t>>k))\&m);
Permutation
// c = array size, n = nth perm, return index
vector<int> gen_permutation(int c, int n) {
 vector<int> idx(c), per(c), fac(c); int i;
 for (i = 0; i < c; i++) idx[i] = i;
for (i = 1; i <= c; i++) fac[i-1] = n%i, n/=i;
for (i = c - 1; i >= 0; i--)
per[c-i-1] = idx[fac[i]],
                                                           Simpson's / Approximate Integrals
  idx.erase(idx.begin() + fac[i]);
// get what nth permutation of vector
int get_permutation(vector<int>& v) {
 int use = 0, i = 1, r = 0;
 for (int e : v) {
  r = r * i++ + __builtin_popcount(use &
 \rightarrow -(1<<e));
  use |= 1 << e:
 return r;
```

```
Permutation (string/multiset)
string freq2str(vector<int>& v) {
 string s;
for (int i = 0; i < v.size(); i++)
for (int j = 0; j < v[i]; j++)
s += (char)(i + 'A');
return s;
// nth perm of multiset, n is 0-indexed
string gen_permutation(string s, ll n) {
  vector<int> freq(26, 0);
 for (auto e : s) freq[e - 'A']++;
 for (int i = 0; i < 26; i++) if (freq[i] > 0)
  freq[i]--; ll v = multinomial(freq);
  if (n < v) return (char)(i+'A') +
gen_permutation(freq2str(freq), n);
freq[i]++; n -= v;
return "":
Miller-Rabin Primality Test
// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
  if (n < 2) return false;</pre>
if (n == 2) return true;

if (n % 2 == 0) return false;

ull s = n - 1;

while (s % 2 == 0) s /= 2;

for (int i = 0; i < 10; i++) {
  ull temp = s:
  ull a = rand() \% (n - 1) + 1;
  ull mod = mpow(a, temp, n);
  while (temp!=n-1\&\&mod!=1\&\&mod!=n-1) {
   mod = mult(mod, mod, n):
   temp *= 2;
  if (mod!=n-1&&temp%2==0) return false;
 }
return true;
Sieve of Eratosthenes
bitset<100000001> sieve;
// generate sieve - O(n log n)
void genSieve(int n) {
void gensieve(int in ;
sieve[0] = sieve[1] = 1;
for (ull i = 3; i * i < n; i += 2)
    if (!sieve[i])
    for (ull j = i * 3; j <= n; j += i * 2)</pre>
    sieve[j] = 1;
// query sieve after it's generated - 0(1)
bool quervSieve(int n) {
 return n == 2 || (n % 2 != 0 && !sieve[n]);
```

```
// integrate f from a to b, k iterations
double Simpsons (double a, double b, int k,
double (*f)(double)) {
double dx = (b-a)/(2.0*k), t = 0;
for (int i = 0; i < k; i++)
...t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
\leftrightarrow (*f)(a+(2*i+1)*dx);
return (t + (*f)(b)) * (b-a) / 6.0 / k;
```

```
Common Equations Solvers
// ax^2 + bx + c = 0, find x
vector < double > solve Eq (double a, double b,
double c) {
vector<double> r;
double z = b * b - 4 * a * c;
if (z == 0)
 r.push_back(-b/(2*a));
 else if (z > 0) {
 r.push back((sqrt(z)-b)/(2*a));
  r.push_back((sqrt(z)+b)/(2*a));
 return r;
// ax^3 + bx^2 + cx + d = 0, find x
vector < double > solve Eq (double a, double b,

    double c, double d) {
    vector<double> res;

 long double a1 = b/a, a2 = c/a, a3 = d/a;
long double q = (a1*a1 - 3*a2)/9.0, sq =
\rightarrow -2*sqrt(q);
long double r = (2*a1*a1*a1 - 9*a1*a2 +
\hookrightarrow 27*a3)/54.0;
long double z = r*r-q*q*q, theta;
 if (z \le 0) {
  theta = acos(r/sqrt(q*q*q));
  res.push_back(sq*cos(theta/3.0) - a1/3.0);
 res.push_back(sq*cos((theta+2.0*PI)/3.0) -
res.push back(sq*cos((theta+4.0*PI)/3.0) -
\rightarrow a1/3.0);
 res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
res[0] = (res[0] + q / res[0]) *
\rightarrow ((r<0)?1:-1) - a1 / 3.0;
 return res;
}
// linear diophantine equation ax + by = c,
\hookrightarrow find x and y
// infinite solutions of form x+k*b/g, y-k*a/g bool solveEq(11 a, 11 b, 11 c, 11 &x, 11 &y, 11
 g = \operatorname{egcd}(\operatorname{abs}(a), \operatorname{abs}(b), x, y);
if (c % g) return false;

x *= c / g * ((a < 0) ? -1 : 1);

y *= c / g * ((b < 0) ? -1 : 1);

return true;
^{\prime}// m = # equations, n = # variables, a[m][n+1]
\Rightarrow = coefficient matrix
// a[i][0]x + a[i][1]y + ... + a[i][n]z =
\rightarrow a[i][n+1]
// find a solution of some kind to linear
\rightarrow equation
const double eps = 1e-7:
bool zero(double a) { return (a < eps) && (a >
vector < double > solve Eq (double **a, int m, int
 for (int i = 0; i < n; i++) {
 for (int j = cur; j < m; j++) {
...if (!zero(a[j][i])) {
 if (j != cur) swap(a[j], a[cur]);
    for (int sat = 0; sat < m; sat++) {
  if (sat == cur) continue;
double num = a[sat][i] / a[cur][i];
   for (int sot = 0; sot <= n; sot++)
a[sat][sot] -= a[cur][sot] * num;
    }
cur++;
    break
 for (int j = cur; j < m; j++)
 if (!zero(a[i][n])) return vector < double > ();
```

```
vector<double> ans(n,0);
for (int i = 0, sat = 0; i < n; i++)
   if (sat < m && !zero(a[sat][i]))
      ans[i] = a[sat][n] / a[sat++][i];
return ans;</pre>
// solve A[n][n] * x[n] = b[n] linear equation
// rank < n is multiple solutions, -1 is no
→ solutions

// `alls` is whether to find all solutions, or
const double eps = 1e-12:
int solveEq(Vec<2, double>& A, Vec<1, double>&
 \rightarrow b. Vec<1. double>& x. bool alls=false) {
 int n = A.size(), m = x.size(), rank = 0, br,
 vector<int> col(m); iota(begin(col), end(col)
 for(int i = 0; i < n; i++) {
   double v, bv = 0;
   for(int r = i; r < n; r++)</pre>
  for(int c = i; c < n; c++)
    if ((v = fabs(A[r][c])) > bv)
        br = r, bc = c, bv = v;
    if (bv <= eps) {
   for(int j = i; j < n; j++)
if (fabs(b[j]) > eps)
       return -1;
  swap(A[i], A[br]);
swap(b[i], b[br]);
swap(col[i], col[bc]);
  for(int j = 0; j < n; j++)
. swap(A[j][i], A[j][bc]);
bv = 1.0 / A[i][i];
for(int j = (alls)?0:i+1; j < n; j++) {</pre>
   if (j != i) {
     double fac = A[j][i] * bv;
    b[j] = fac * b[i];
    for(int k = i+1; k < m; k++)
A[j][k] -= fac*A[i][k];
 rank++;
 if (alls) for (int i = 0; i < m; i++) x[i] =
     -DBL MAX:
 for (int i = rank; i--;) {
   bool isGood = true:
   if (alls)
   if or (int j = rank; isGood && j < m; j++)
if (fabs(A[i][j]) > eps)
  ...isGood = false;
.b[i] /= A[i][i];
.if (isGood) x[col[i]] = b[i];
  if (!alls)
  for(int j = 0; j < i; j++)
b[j] -= A[j][i] * b[i];
 return rank:
Gravcode Conversions
ull graycode2ull(ull n) {
 ull i = 0;
for (; n; n = n >> 1) i ^= n;
ull ull2graycode(ull n) {
  return n ^ (n >> 1);
Unix/Epoch Time
// O-indexed month/time, 1-indexed day
 // minimum 1970, 0, 1, 0, 0, 0
ull toEpoch(int year, int month, int day, int
 → hour, int minute, int second) {
struct tm t; time_t epoch;

t.tm_year = year - 1900; t.tm_mon = month;

t.tm_mday = day; t.tm_hour = hour;
 t.tm_min = minute; t.tm_sec = second;
```

```
t.tm_isdst = 0; // 1 = daylights savings
 epoch = mktime(&t);
return (ull)epoch;
vector<int> toDate(ull epoch) {
time t e=epoch: struct tm t=*localtime(&e):
 return {t.tm vear+1900.t.tm mon.t.tm mdav.t
    .tm hour.t.tm min.t.tm sec}:
int getWeekday(ull epoch) {
 time t e=epoch: struct tm t=*localtime(&e):
 return t.tm wday; // 0-6, 0 = sunday
int getDayofYear(ull epoch) {
time_t e=epoch; struct tm t=*localtime(&e);
return t.tm yday; // 0-365
const int months[] =
\rightarrow {31,28,31,30,31,30,31,30,31,30,31};
bool validDate(int year, int month, int day) {
    bool leap = !(year%(year%25?4:16));
if (month >= 12) return false;
    return day <= months[month] + (leap &&
   month == 1);
```

### Theorems and Formulae

Montmort Numbers count the number of derangements (permutations where no element appears in its original position) of a set of size n. !0 = 1, !1 = 0, !n = (n+1)(!(n-1)) $|1)+!(n-2), !n=n!\sum_{i=0}^{n}\frac{(-1)^{i}}{i!}, !n=[\frac{n!}{e}]$ In a partially ordered set, a chain is a subset of elements that are all comparable to eachother

parable. Dilworth's theorem states the size of a max-| ⇒ imal antichain equals the size of a minimal chain cover of a partially ordered set S. The width of S is the maximum size of an antichain in S, which is equal to the minimum number of chains needed to cover S, or the minimum

Rosser's Theorem states the *nth* prime ; number is greater than n \* ln(n) for n > 1.

Nicomachi's Theorem states  $1^3 + 2^3 + \dots + \frac{\text{const 11 inf = 1LL } < 62;}{\text{m}^3 = (1 + 2 + \dots + n)^2}$  and is equivalent to void floydWarshall(Vec<2, 11>& m) {  $(n^{\frac{n+1}{2}})^2$ .

Lagrange's Four Square Theorem states every natural number is the sum of the squares of four non-negative integers. This is a special case of the Fermat Polygonal Number **Theorem** where every positive integer is a sum of at most n s-gonal numbers. The  $nth \mapsto m[i][j] = -inf;$ s-gonal number  $P(s,n) = (s-2)\frac{n(n-1)}{2} + n$ 

# 7 Graphs

at least one chain.

```
struct edge {
int u.v.w:
 edge (int u,int v,int w) : u(u),v(v),w(w) {}
edge (): u(0), v(0), w(0) {}
```

```
bool operator < (const edge &e1, const edge
bool operator > (const edge &e1, const edge
struct subset { int p, rank; };
```

```
Eulerian Path
                                                   #define edge_list vector<edge>
#define adj_sets vector<set<int>>>
                                                   struct EulerPathGraph {
                                                   adj_sets graph; // actually indexes incident
                                                   edge_list edges; int n; vector<int> indeg;
                                                   EulerPathGraph(int n): n(n) {
                                                    indeg = *(new vector<int>(n,0));
                                                    graph = *(new adj_sets(n, set<int>()));
                                                   void add_edge(int u, int v) {
                                                    graph[u].insert(edges.size());
                                                     indeg[v]++;
                                                    edges.push_back(edge(u,v,0));
                                                   bool eulerian_path(vector<int> &circuit) {
                                                    if(edges.size()==0) return false:
                                                    stack<int> st:
                                                    bool b = indeg[v] > graph[v].size();
if (abs(((int)indeg[v])-((int)graph[v])
                                                       .size())) > 1) return
                                                      false; if (a[b] != -1) return false;
                                                      a[b] = v;
                                                     int s = (a[0]!=-1 \&\& a[1]!=-1 ? a[0] :
                                                      (a[0]=-1 \&\& a[1]=-1 ? edges[0].u : -1));
                                                    if(s==-1) return false;
An antichain is a subset where no two are com-
                                                    while(!st.empty() || !graph[s].empty()) {
   if (graph[s].empty()) {
                                                      circuit.push_back(s); s = st.top();
                                                      st.pop(); }
                                                      else {
                                                      int w = edges[*graph[s].begin()].v;
                                                      graph[s].erase(graph[s].begin());
                                                      st.push(s); s = w;
                                                    circuit.push back(s):
number of chains such that all elements are in
                                                    return circuit.size()-1==edges.size();
```

## Floyd Warshall

```
int n = m.size();

FOR(i,n) m[i][i] = min(m[i][i], OLL);

FOR(k,n) FOR(i,n) FOR(j,n) if (m[i][k] != inf
   && m[k][j] != inf)
 auto newDist = max(m[i][k] + m[k][i]. -inf):
 m[i][j] = min(m[i][j], newDist);
fOR(k,n) if (m[k][k] < 0) FOR(i,n) FOR(j,n)
if (m[i][k] != inf && m[k][j] != inf)
```

## Minimum Spanning Tree

```
returns vector of edges in the mst
// graph[i] = vector of edges incident to
→ vertex i
// places total weight of the mst in &total
// if returned vector has size != n-1, there is
```

```
vector<edge> mst(vector<vector<edge>> graph,
                                                     polygon(vector<point> points) :
\hookrightarrow 11 &total) {
                                                        points(points) {}
 total = 0;
                                                     polygon(triangle a) {
priority_queue<edge, vector<edge>,
                                                      points.push_back(a.a); points.push_back(a.b);

    greater < edge >> pq;
    vector < edge >> MST;
                                                        points.push back(a.c);
 bitset<20001> marked; // change size as needed
                                                     polygon(rectangle a)
 marked[0] = 1:
                                                      points.push_back(a.tl);
for (edge ep : graph[0]) pq.push(ep);
while(MST.size()!=graph.size()-1 &&
                                                         points.push back({real(a.tl),
                                                         imag(a.br)});

→ pq.size()!=0) {
                                                      points.push_back(a.br);
 edge e = pq.top(); pq.pop();
int u = e.u, v = e.v, w = e.w;
if(marked[u] && marked[v]) continue;
                                                         points.push back({real(a.br),
                                                         imag(a.tl)});
 else if(marked[u]) swap(u, v);
for(edge_ep : graph[u]) pq.push(ep);
                                                     polygon(convex polygon a) {
  marked[u] = 1:
                                                      for (point v : a.points)
  MST.push_back(e);
                                                       points.push_back(v);
  total += e.w;
 return MST:
                                                       triangle methods
                                                     double area heron(double a, double b, double
                                                     \rightarrow c) {
if (a < b) swap(a, b):
Union Find
int uf_find(subset* s, int i) {
  if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
                                                     if (a < c) swap(a, c);
                                                     if (b < c) swap(b, c);
return s[i].p;
                                                     if (a > b + c) return -1;
return sqrt((a+b+c)*(c-a+b)*(c+a-b)*(a+b-c)
void uf_union(subset* s, int x, int y) {
                                                        /16.0);
 int xp = uf_find(s, x), yp = uf_find(s, y);
 if (s[xp].rank > s[yp].rank) s[yp].p = xp;
                                                     // segment methods
else if (s[xp].rank < s[yp].rank) s[xp].p =
                                                     double lengthsq(segment a) { return
else { s[yp].p = xp; s[xp].rank++; }
                                                         sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
                                                         imag(a.b)); }
                                                     double length(segment a) { return
2D Grid Shortcut
                                                         sqrt(lengthsq(a)); }
#define inbound(x,n) (0<=x\mathcal{E}\mathcal{E}x<n)
                                                        circle methods
#define fordir(x,y,n,m) for(auto[dx,dy]:dir)if
                                                    double circumference(circle a) { return 2 * a.r|_{1}^{2}
                                                     → * M_PI; }
\hookrightarrow (inbound(x+dx,n)&inbound(y+dy,m))
                                                     double area(circle a) { return sq(a.r) * M PI:
const pair<int,int> dir[] =
\rightarrow {{1,0},{0,1},{-1,0},{0,-1}};
                                                     // rectangle methods
                                                     double width(rectangle a) { return
    2D Geometry

→ abs(real(a.br) - real(a.tl)); }

#define point complex<double>
                                                     double height(rectangle a) { return
#define EPS 0.0000001

→ abs(imag(a.br) - real(a.tl)); }

#define sq(a) ((a)*(a))
                                                     double diagonal(rectangle a) { return
#define cb(a) ((a)*(a)*(a))

    sqrt(sq(width(a)) + sq(height(a))); }

double dot(point a, point b) { return
                                                     double area (rectangle a) { return width(a) *

→ real(conj(a)*b); }

                                                     → height(a); }
double cross(point a, point b) { return
                                                     double perimeter(rectangle a) { return 2 *

    imag(conj(a)*b); }

                                                         (width(a) + height(a)); }
struct line { point a, b; };
                                                        check if `a` fit's inside `b
struct circle { point c; double r; };
                                                     // swap equalities to exclude tight fits
struct segment { point a, b; };
                                                     bool doesfitInside(rectangle a, rectangle b) {
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
                                                     int x = width(a), w = width(b), y = height(a)
                                                      → h = height(b);
struct convex_polygon {
                                                     if (x > y) swap(x, y);
if (w > h) swap(w, h);
vector<point points;
 convex_polygon(vector<point> points) :
                                                     if (w < x) return false;

→ points(points) {}
                                                     if (y <= h) return true;
 convex polygon(triangle a) {
                                                     double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
 points.push_back(a.a); points.push_back(a.b);
                                                     return sq(a) \le sq(b) + sq(c);
→ points.push_back(a.c);
.}:
                                                        polygon methods
 convex_polygon(rectangle a) {
                                                     // negative area = CCW, positive = CW
 points.push_back(a.tl);
                                                     double area(polygon a) {
    points.push_back({real(a.tl),
                                                       double area = 0.0; int n = a.points.size();
    imag(a.br)});
                                                       for (int i = 0, j = 1; i < n; i++, j = (j - 1)
  points.push_back(a.br);
                                                         area += (real(a.points[j]-a.points[i]))*
    points.push back({real(a.br),
    imag(a.tl)});
                                                        (imag(a.points[j]+a.points[i]));
                                                      return area / 2.0:
struct polygon {
                                                       aet both unsigned area and centroid
vector <point > points;
```

```
int n = a.points.size();
 double area = 0:
point c(0, 0);
 for (int i = n - 1, j = 0; j < n; i = j++) {
 double v = cross(a.points[i], a.points[j]) /
  c += (a.points[i] + a.points[i]) * (v / 3):
 c /= area;
return {area, c}:
Intersection
// -1 coincide, 0 parallel, 1 intersection
int intersection(line a, line b, point& p) {
if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
   p = cross(b.a - a.a, b.b - a.b) / cross(a.b)
 \rightarrow - a.a. b.b - b.a) * (b - a) + a:
 return 1:
 if (abs(cross(a.b - a.a, a.b - b.a)) > EPS)

→ return 0:

return -1:
// area of intersection
double intersection(circle a, circle b) {
 double d = abs(a.c - b.c);
if (d <= b.r - a.r) return area(a);</pre>
 if (d <= a.r - b.r) return area(b);
 if (d >= a.r + b.r) return 0;
double alpha = acos((sq(a.r) + sq(d) -
 \rightarrow sq(b.r)) / (2 * a.r * d));
 double beta = acos((sq(b.r) + sq(d) - sq(a.r))
 \rightarrow / (2 * b.r * d)):
 return sq(a.r) * (alpha - 0.5 * sin(2 *
    alpha) + sq(b.r) * (beta - 0.5 * sin(2 *
 // -1 outside. O inside. 1 tangent. 2
int intersection circle a. circle b.
→ vector<point>& inter) {
 double d2 = norm(b.c - a.c), rS = a.r + b.r,
\rightarrow rD = a.r - b.r;
 if (d2 > sq(rS)) return -1;
 if (d2 < sq(rD)) return 0;
 double ca = 0.5 * (1 + rS * rD / d2);
 point z = point(ca, sqrt(sq(a.r) / d2 -
 \rightarrow sq(ca));
 inter.push_back(a.c + (b.c - a.c) * z);
 if (abs(imag(z)) > EPS) inter.push_back(a.c
\rightarrow (b.c - a.c) * coni(z)):
return inter.size();
// points of intersection
vector<point> intersection(line a, circle c) {
 vector<point> inter;
c.c -= a.a;
a.b -= a.a;
point m = a.b * real(c.c / a.b);
double d2 = norm(m - c.c);
 if (d2 > sq(c.r)) return 0;
 double l = sqrt((sq(c.r) - d2) / norm(a.b));
 inter.push_back(a.a + m + 1 * a.b);
 if (abs(1) > EPS) inter.push back(a.a + m - 1
\rightarrow * a.b);
return inter:
double x1 = max(real(a.tl), real(b.tl)), y1 =
 → max(imag(a.tl), imag(b.tl));
 double x2 = min(real(a.br), real(b.br)), y2 =
 → min(imag(a.br), imag(b.br));
return (x2 <= x1 | | y2 <= y1) ? 0 :
    (x2-x1)*(y2-y1);
```

```
pair double, point area_centroid(polygon a) { Convex Hull
                                                         bool cmp(point a, point b) {
  if (abs(real(a) - real(b)) > EPS) return
                                                             real(a) < real(b);
                                                          if (abs(imag(a) - imag(b)) > EPS) return
                                                         \hookrightarrow imag(a) < imag(b);
                                                         return false;
                                                         convex_polygon convexhull(polygon a) {
                                                          sort(a.points.begin(), a.points.end(), cmp);
                                                          vector<point> lower, upper;
                                                          for (int i = 0; i < a.points.size(); i++) {
   while (lower.size() >= 2 &&
                                                             cross(lower.back() - lower[lower.size() -
                                                             2], a.points[i] - lower.back()) < EPS)
                                                            lower.pop_back();
                                                           while (upper.size() >= 2 &&
                                                              cross(upper.back() - upper[upper.size() -
                                                             2], a.points[i] - upper.back()) > -EPS)
                                                           ..upper.pop_back();
.lower.push_back(a.points[i]);
                                                           upper.push back(a.points[i]);
                                                          lower.insert(lower.end(), upper.rbegin() + 1,

    upper.rend());

                                                         return convex polygon(lower);
                                                            3D Geometry
                                                         struct point3d {
                                                         double x, y, z;
                                                          point3d operator+(point3d a) const { return
                                                         \hookrightarrow {x+a.x, y+a.y, z+a.z}; }
                                                          point3d operator*(double a) const { return
                                                          \rightarrow {x*a, y*a, z*a}; }
                                                          point3d operator-() const { return {-x, -y,
                                                         \stackrel{-}{\hookrightarrow} -z}; }
                                                         point3d operator-(point3d a) const { return

    *this + -a; }

                                                         point3d operator/(double a) const { return
                                                          → *this * (1/a); }
double norm() { return x*x + y*y + z*z; }
                                                          double abs() { return sqrt(norm()); }
                                                          point3d normalize() { return *this /
                                                        this->abs(); }
                                                         double dot(point3d a, point3d b) { return
                                                         \rightarrow a.x*b.x + a.y*b.y + a.z*b.z; }
                                                         point3d cross(point3d a, point3d b) { return
                                                             {a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,}
                                                         \Rightarrow a.x*b.y - a.y*b.x}; } struct line3d { point3d a, b; };
                                                         struct plane { double a, b, c, d; } // a*x +
                                                         \Rightarrow b*y + c*z + d = 0
                                                        struct sphere { point3d c; double r; };
                                                         #define sq(a) ((a)*(a))
                                                         #define cb(a) ((a)*(a)*(a))
                                                         double surface(circle a) { return 4 * sq(a.r) *

    M_PI; }

                                                         double volume(circle a) { return 4.0/3.0 *
                                                         \hookrightarrow cb(a.r) * M PI; }
                                                         10 Optimization
                                                         Snoob
                                                          // SameNumberOfOneBits, next permutation
                                                        // example usage
int main() {
  char 11[] = {'1', '2', '3', '4',
  char 12[] = {'a', 'b', 'c', 'd'};
  int d1 = 5, d2 = 4;
  // prints 12345abcd, 1234a5bcd, ...
```

int min = (1 << d1) - 1, max = min << d2;

```
Limits
                                                                          \pm 2147483647|\ \pm 2^{31}-1|10^9
                                                       int
                                                                                            \overline{2}^{32} - 1|10^9
   cout << ((v & 1) ? 11[p1++] : 12[p2++]);
                                                                            4294967295
                                                       uint
                                                                                          \pm \tilde{2}^{63} - \tilde{1}|\tilde{10}^{18}
   v /= 2;
                                                              \pm 9223372036854775807
                                                      cout << '\n';
                                                                                           \frac{1}{2}<sup>128</sup> -\frac{1}{1}<sup>1038</sup>
                                                      |u128| 340282366920938463...|
Powers
                                                      Complexity classes input size (per second):
bool isPowerOf2(11 a) {
                                                       O(n^n) or O(n!)
 return a > 0 \&\& ! (a \& a-1);
                                                      |O(2^n)|
                                                                                                    n \leq 30
bool isPowerOf3(11 a) {
   return a>0&&!(12157665459056928801ull%a);
                                                      O(n^3)
                                                                                                 n < 1000
                                                      O(n^2)
bool isPower(ll a, ll b) {
  double x = log(a) / log(b);
  return abs(x-round(x)) < 0.00000000001;</pre>
                                                                                                n < 30000
                                                      O(n\sqrt{n})
                                                                                                  n < 10^6
                                                                                                  n \le 10^7
                                                      |O(n \log n)|
                                                                                                  n < 10^9
11 Additional
                                                      |O(n)|
Judge Speed
 // kattis: 0.50s
 // codeforces: 0.421s
// atcoder: 0.455s
#include <bits/stdc++.h>
using namespace std;
int v = 1e9/2, p = 1;
int main() {
  for (int i = 1; i <= v; i++) p *= i;</pre>
 cout << p;
Judge Pre-Contest Checks
- int128 and float128 support?
-does extra or missing whitespace cause WA?
-documentation up to date?
-printer usage available and functional?
// each case tests a different fail condition
// try them before contests to see error codes
struct g { int arr[1000000]; g(){}};
vector<g> a;
 // O=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
if (n == 3) while(1) putchar_unlocked('a');
 if (n == 4) assert(0);
 if (n == 5) 0 / 0;
if (n == 6) *(int*)(0) = 0;
 return n + judge(n + 1);
GCC Builtin Docs
 // 128-bit integer
__int128 a;
unsigned __int128 b;
// 128-bit float
 // minor improvements over long double
__float128 c;
// log2 floor
__lg(n);
// number of 1 bits
// can add ll like popcountll for long longs
 __builtin_popcount(n);
// number of trailing zeroes
builtin_ctz(n);
// number of leading zeroes
builtin_clz(n);
// 1-indexed least significant 1 bit
__builtin_ffs(n);
// parity of number
__builtin_parity(n);
```