```
else if (d) { m=m*10+c-'0'; o*=0.1; } else n = n * 10 + c - '0':
    General
                              7 Graphs
    Algorithms
                              8 2D Geometry
                                                             n = s * (n + m * o):
    Structures
                              9 3D Geometry
    Strings
                                                            void read(double& n) {
                              10 Optimization
                                                             ld m; read(m); n = m;
    Greedy
                              11 Additional
                                                            void read(float& n) {
  ld m; read(m); n = m;
    Math
     General
                                                             void read(string& s) {
g++ -g -02 -std=gnu++17 -static prog.cpp
./a.exe
                                                             char c: s = ""
                                                             while((c=getchar_unlocked())!=' '&&c!='\n')
                                                              s += c:
                                                            bool readline(string& s) {
# compile and test all *.in and *.ans
g++ -g -02 -std=gnu++17 -static prog.cpp
                                                             char c: s = ""
                                                             while(c=getchar_unlocked()) {
for i in *.in; do f=${i%.in}
                                                              if (c == '\n') return true;
if (c == EOF) return false;
 ./a.exe < $i > "$f.out"
diff -b -q "$f.ans" "$f.out"
                                                               s += c:
done
                                                             return false:
Header
                                                            void print(unsigned int n) {
// use better compiler options
                                                             if (n / 10) print(n / 10);
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
                                                             putchar unlocked(n % 10 + '0'):
// include everything
                                                             void print(int n) {
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <bits/extc++.h>
#include <sys/resource.h>
                                                             if (n < 0) { putchar_unlocked('-'); n*=-1; }</pre>
                                                             print((unsigned int)n);
// namespaces
using namespace std;
                                                            Common Structs
using namespace __gnu_cxx; // rope
                                                            // n-dimension vectors
// Vec<2, int> v(n, m) = arr[n][m]
// Vec<2, int> v(n, m, -1) default init -1
template<int D, typename T>
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio
                                                            struct Vec : public vector<Vec<D-1, T>> {
\label{eq:control_state} \rightarrow ios\_base::sync\_with\_stdio(0);cin.tie(0); \\ \textit{\#define nostacklim rlimit}
                                                               template<typename... Args>
                                                               Vec(int n=0, Args... args) : vector<Vec<D-1,
     RZ; getrlimit(3, &RZ); RZ.rlim_cur=-
                                                                T \gg (n, Vec < D-1, T \gg (args...)) {}
\(\Rightarrow\) 1; setrlimit(3,\&RZ); \(\text{#define DEBUG(v) cerr<<_LINE__<<": "<<\#v<<" =
                                                             témplate<typename T>
struct Vec<1, T> : public vector<T> {
                                                               Vec(int n=0, T val=T()) : vector<T>(n, val)
→ cerr<<1.0*clock()/CLOCKS_PER_SEC<<"s\n";
#define ll long long
#define ull unsigned ll
                                                                {}
#define i128 __int128
#define u128 unsigned i128
                                                                 Algorithms
#define ld long double
                                                            Min/Max Subarray
// global variables
                                                             // max - compare = a < b, reset = a < 0
mt19937 rng((uint32_t)chrono::steady
                                                                min - compare = a > b, reset = a > 0

    clock::now().time since epoch().count()):

                                                            // returns {sum, {start, end}}
pair<int, pair<int, int>>
                                                                 ContiguousSubarrav(int* a. int size.
                                                                 bool(*compare)(int, int),
#define getchar_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
                                                             bool(*reset)(int), int defbest = 0) {
int best = defbest, cur = 0, start = 0, end =
                                                             void read(unsigned int& n) {
 char c; n = 0;
while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                               cur += a[i];
                                                               if ((*compare)(best, cur)) { best = cur;
 n = n * 10 + c - 0';
                                                                start = s; end = i; }
void read(int& n) {
   char c; n = 0; int s = 1;
   if ((c=getchar_unlocked())=='-') s = -1;
                                                              if ((*reset)(cur)) { cur = 0; s = i + 1; }
                                                             return {best, {start, end}};
 else n = c - \sqrt{0}:
 while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                             Quickselect
 n = n * 10 + c -
                                                             #define QSNE -999999
                                                            int partition(int arr[], int 1, int r)
void read(ld& n) {
 char c; n = 0;

.ld m = 0, o = 1; bool d = false; int s = 1;

.if ((c=getchar_unlocked())=='-') s = -1;
                                                              int x = arr[r], i = 1;
                                                             for (int j = 1; j <= r - 1; j++)
if (arr[j] <= x)
 else if (c == '.') d = true;
else n = c - '0';
                                                               swap(arr[i++], arr[j]);
 while ((c=getchar_unlocked())!=' '&&c!='\n') {
                                                             swap(arr[i], arr[r]);
  if (c == '.') d = true;
                                                             return i;
```

```
\frac{1}{1} find k'th smallest element in unsorted array,
\hookrightarrow only if all distinct
int gselect(int arr[], int 1, int r, int k)
 if (!(k > 0 && k <= r - 1 + 1)) return QSNE;
swap(arr[1 + rng() % (r-1+1)], arr[r]);
 int pos = partition(arr, 1, r);
 if (pos-l==k-1) return arr[pos];
 if (pos-1>k-1) return qselect(arr,1,pos-1,k);
return qselect(arr, pos+1, r, k-pos+1-1);
// TODO: compare against std::nth element()
Saddleback Search
// search for v in 2d array arr[x][y], sorted
→ on both axis
pair<int, int> saddleback search(int** arr, int
\stackrel{\cdot}{\hookrightarrow} x, int y, int v) {
int i = x-1, j = 0;

while (i >= 0 && j < y) {

if (arr[i][j] == v) return {i, j};
  (arr[i][i] > v)? i--: i++:
 return {-1, -1};
Ternary Search
// < max, > min, or any other unimodal func #define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {
 while (b-a > 4) {
  int m = (a+b)/2;
if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
  else b = m+1:
 for (int i = a+1; i <= b; i++)
if (TERNCOMP((*f)(a), (*f)(i)))
 ...a = i;
return a:
#define TERNPREC 0.000001
double ternsearch (double a, double b, double
 \rightarrow (*f)(double)) {
 while (b-a > TERNPREC * 4) {
   double m = (a+b)/2;
  if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
 → = m;
else b = m + TERNPREC;
 for (double i = a + TERNPREC; i <= b; i +=
    TERNPREC)
      if (TERNCOMP((*f)(a), (*f)(i)))
   a = i;
 return a;
3 Structures
Fenwick Tree
// Fenwick tree, array of cumulative sums -
 \hookrightarrow O(log n) updates, O(log n) gets
struct Fenwick { int n: ll* tree:
  void update(int i, int val) {
  .++i:
  while (i <= n) {
   tree[i] += val;
   i += i & (-i):
 Fenwick(int size) {
  n = size;
  tree = new ll[n+1];
for (int i = 1; i <= n; i++)
   tree[i] = 0:
 Fenwick(int* arr, int size) : Fenwick(size) {
  for (int i = 0; i < n; i++)
update(i, arr[i]);</pre>
```

```
.ll operator[](int i) {
  if (i < 0 || i > n) return 0;
  while (i>0)
   sum += tree[i];
i -= i & (-i);
  return sum:
 ll getRange(int a, int b) { return
    operator[](b) - operator[](a-1); }
Hashtable
 // similar to unordered map, but faster
| struct chash {
| const uint64 t C = (11)(2e18 * M_PI) + 71;
| ll operator()(11 x) const { return
    __builtin_bswap64(x*C); }
int main() {
  gp_hash_table<11,int,chash>
 \rightarrow hashtable({},{},{},{},{1<<16});
 for (int i = 0; i < 100; i++)
. hashtable[i] = 200+i;
.if (hashtable.find(10) != hashtable.end())
. cout << hashtable[10];</pre>
Ordered Set
using oset = tree<T,null_type,less<T>,rb_tree
tag, tree_order_statistics_node_update>; template <typename T, typename D> using omap = tree<T,D,less<T>,rb_tree |

→ _tag,tree_order_statistics_node update>;

int main()
 coset<int> o_set;
o_set.insert(5); o_set.insert(1);
 → o_set.insert(3);
// get second smallest element
 cout << *(o_set.find_by_order(1));</pre>
 // number of elements less than k=4
 cout << ' ' << o set.order of kev(4) << '\n':
  // equivalent with ordered map
 omap<int,int> o_map;
 o_map[5]=1;o_map[1]=2;o_map[3]=3;
 cout << (*(o map.find by order(1))).first;</pre>
 cout << ' ' << o_map.order_of_key(4) << '\n';</pre>
Rope
 // ar{	extsf{O}}(\log n) insert, delete, concatenate
int main() {
 // generate rope
 rope<int> v;
 for (int i = 0; i < 100; i++)
...v.push_back(i);
  // move range to front
 rope<int> copy = v.substr(10, 10);
v.erase(10, 10);
 v.insert(copy.mutable_begin(), copy);
 // print elements of rope
 for (auto it : v) cout << it << " ";
Segment Tree
 //max(a,b), min(a,b), a+b, a*b, gcd(a,b), a\hat{b}
struct SegmentTree {
 typedef int T;
 static constexpr T UNIT = INT_MIN;
 T f(T a, T b) {
    if (a == UNIT) return b;
    if (b == UNIT) return a;
  return max(a,b);
 int n; vector<T> s;
SegmentTree(int n, T def=UNIT) : s(2*n, def),
```

```
SegmentTree(vector<T> arr) :

→ SegmentTree(arr.size()) {
 for (int i=0;i<arr.size();i++)

→ update(i,arr[i]);

 void update(int pos, T val) {
 for (s[pos += n] = val; pos /= 2;)
  s[pos] = f(s[pos * 2], s[pos*2+1]);
 T query(int b, int e) { // query [b, e) }
T ra = UNIT, rb = UNIT;
 for (b+=n, e+=n; b<e; b/=2, e/=2) {
    if (b % 2) ra = f(ra, s[b++]);
    if (e % 2) rb = f(s[--e], rb);
 return f(ra, rb);
 T get(int p) { return query(p, p+1); }
Trie
typedef trie<string, null_type,

→ trie string access traits<>,

 .pat_trie_tag, trie_prefix_search_node_update>

→ trie_type;

int main() {
   // generate trie
 trie_type trie;
 for (int i = 0; i < 20; i++)
 trie.insert(to_string(i)); // true if new,
\hookrightarrow false if old
 // print things with prefix "1"
 auto range = trie.prefix_range("1");
for (auto it = range.first; it !=
\hookrightarrow range.second; it++)
 .cout << *it << "
```

```
4 Strings
Aho Corasick
// range of alphabet for automata to consider
// MAXC = 26. OFFC = 'a' if only lowercase
const int MAXC = 256;
const int OFFC = 0:
struct aho_corasick {
 struct state
  set<pair<int, int>> out:
 int fail; vector<int> go;
  state(): fail(-1), go(MAXC, -1) {}
 };
 vector<state> s;
 int id = 0;
 aho_corasick(string* arr, int size) : s(1) {
 for (int i = 0: i < size: i++) {
   int cur = 0;
  .for (int c : arr[i]) {
...if (s[cur].go[c-OFFC] == -1) {
   s[cur].go[c-OFFC] = s.size();
    s.push back(state());
    cur = s[cur].go[c-OFFC];
   s[cur].out.insert({arr[i].size(), id++});
  for (int c = 0; c < MAXC; c++)
if (s[0].go[c] == -1)
   ..s[0].go[\tilde{c}] = 0;
  queue<int> sq;
 for (int c = 0; c < MAXC; c++) {
    if (s[0].go[c] != 0) {
        s[s[0].go[c]].fail = 0;
    sq.push(s[0].go[c]);
  while (sq.size()) {
 int e = sq.front(); sq.pop();
 for (int c = 0; c < MAXC; c++) {
...if (s[e].go[c] != -1) {
```

```
int failure = s[e].fail;
while (s[failure].go[c] == -1)
      failure = s[failure].fail;
failure = s[failure].go[c];
      s[s[e].go[c]].fail = failure;
  for (auto length : s[failure].out)
s[s[e].go[c]].out.insert(length);
      sq.push(s[e].go[c]);
 // list of {start pos, pattern id}
 vector<pair<int, int>> search(string text)
  vector<pair<int, int>> toret;
  int cur = 0;
  for (int i = 0; i < text.size(); i++) {
   while (s[cur].go[text[i]-OFFC] == -1)
    .cur = s[cur].fail;
   cur = s[cur].go[text[i]-OFFC];
    if (s[cur].out.size())
    for (auto end : s[cur].out)
  toret.push_back({i - end.first + 1,
     end.second});
  return toret:
Bover Moore
struct defint { int i = -1; };
vector<int> boyermoore(string txt, string pat)
 vector<int> toret; unordered_map<char, defint> Longest Common Prefix (array)
 → badchar:
 int m = pat.size(), n = txt.size();
 for (int i = 0; i < m; i++) badchar[pat[i]].i
 \rightarrow = i;
int s = 0:
 while (s \leq n - m) {
  int j = m - 1;
  while (j \ge 0) && pat[j] == txt[s + j]) j--;
  if (i < 0) {
   .toret.push back(s);
   s += (s + m < n) ? m - badchar[txt[s +
  \rightarrow mll.i : 1:
  .} else
   s += max(1, j - badchar[txt[s + j]].i);
 return toret;
English Conversion
const string ones[] = {"", "one", "two",
"three", "four", "five", "six", "seven",

"eight", "nine";

const string teens[] ={"ten", "eleven",
   "twelve", "thirteen", "fourteen",
"fifteen", "sixteen", "seventeen",
"eighteen", "nineteen"};
const string tens[] = {"twenty", "thirty",
"forty", "fifty", "sixty", "seventy", 
\(\Rightarrow\) "eighty", "ninety"};
const string mags[] = {"thousand", "million",
     "billion", "trillion", "quadrillion",
     "quintillion", "sextillion",
string convert(int num, int carry) {
 if (num < 0) return "negative " +
     convert(-num, 0);
     (num < 10) return ones[num];
(num < 20) return teens[num % 10];</pre>
     (\text{num} < 100) \text{ return tens}[(\text{num} / 10) - 2] +
     (num%10==0?"":" ") + ones[num % 10];
     (num < 1000) return ones[num / 100]
     (num/100=0?"":" ") + "hundred" + (num%100=0?"":" ") + convert(num % 100,
```

```
return convert(num / 1000, carry + 1) + " " + |...while (i >= j && i + j + 1 < n && s[(i-j)/2]
     mags[carry] + " " + convert(num % 1000.
    0):
string convert(int num) {
return (num == 0) ? "zero" : convert(num, 0);
Knuth Morris Pratt
vector<int> kmp(string txt, string pat) {
     vector<int> toret;
 int m = txt.length(), n = pat.length();
 int next[n + 1];
for (int i = 0; i < n + 1; i++)
   next[i] = 0;</pre>
 int i = 1; i < n; i++) {
  int j = next[i + 1];
  while (j > 0 && pat[j] != pat[i])
   j = next[j];
  if (j > 0 || pat[j] == pat[i])
  next[i + 1] = i + 1;
 for (int i = 0, j = 0; i < m; i++) {
  if (txt[i] == pat[j]) {
   if (++j == n)
    toret.push_back(i - j + 1);
  .} else if (j > 0) {
  .j = next[j];
 return toret:
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
false) {
if (n == 0) return "";
 if (!sorted) sort(arr, arr + n);
string r = ""; int v = 0;
 while (v < arr[0].length() && arr[0][v] ==

    arr[n-1][v])
    r += arr[0][v++];

 return r;
Longest Common Subsequence
string lcs(string a, string b) {
 int m = a.length(), n = b.length();
 int L[m+1][n+1];
 for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
        if (i == 0 || j == 0) L[i][j] = 0;
        else if (a[i-1] == b[j-1]) L[i][j] =
 \rightarrow L[i-1][j-1]+1;
   else L[i][j] = \max(L[i-1][j], L[i][j-1]);
 // return L[m][n]; // length of lcs
 string out = "":
 int i = m - 1, j = n - 1;
while (i >= 0 && j >= 0) {
   if (a[i] == b[j]) {
   out = a[i--] + out;
  else if (L[i][j+1] > L[i+1][j]) i--;
  else j--;
 return out;
Longest Common Substring
// l is array of palindrome length at that
→ index
int manacher(string s. int* 1) {
 int n = s.length() * 2;
 for (int i = \overline{0}, j = 0, k; i < n; i += k, j =
```

 \rightarrow max(i-k, 0)) {

```
\Rightarrow == s[(i+j+1)/2]) j++;
 1[i] = j;
  for (k = 1; i >= k && j >= k && l[i-k] !=
 \rightarrow j-k; k++)
  1[i+k] = min(1[i-k], j-k);
return *max_element(1, 1 + n);
Cyclic Rotation (Lyndon)
// simple strings = smaller than its nontrivial
   suffixes
// lyndon factorization = simple strings
→ factorized
// "abaaba" -> "ab", "aab", "a"
vector<string> duval(string s) {
int n = s.length();
vector<string> lyndon;
for (int i = 0; i < n;) {
 int j = i+1, k = i;

int j = i+1, k = i;

for (; j < n && s[k] <= s[j]; j++)

if (s[k] < s[j]) k = i;
   else k++:
  for (; i \le k; i += j - k)
  lyndon.push back(s.substr(i,j-k));
return lyndon;
// lexicographically smallest rotation
int minRotation(string s) {
int n = s.length(); s += s;
auto d = duval(s); int i = 0, a = 0;
while (a + d[i].length() < n) a +=</pre>
 \rightarrow d[i++].length();
while (i && d[i] == d[i-1]) a -=
→ d[i--].length();
return a;
Subsequence Count
// "banana", "ban" >> 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
int m = subs.length(), n = body.length();
if (m > n) return 0;
 ull** arr = new ull*[m+1];
for (int i = 0; i \le m; i++) arr[i] = new
\hookrightarrow ull[n+1];
for (int i = 1; i <= m; i++) arr[i][0] = 0;
for (int i = 0; i <= n; i++) arr[o][i] = 1;
for (int i = 1; i <= m; i++)
 for (int j = 1; j <= n; j++)
arr[i][j] = arr[i][j-1] + ((body[j-1] ==
\hookrightarrow subs[i-1])? arr[i-1][j-1] : 0);
return arr[m][n]:
Suffix Array + LCP
struct SuffixArray {
vector<int> sa, 1cp;
SuffixArray(string& s, int lim=256) {
   int n = s.length() + 1, k = 0, a, b;
   vector<int> x(begin(s), end(s)+1), y(n),
 \rightarrow ws(max(n, lim)), rank(n);
 sa = lcp = y;
iota(begin(sa), end(sa), 0);
  for (int j = 0, p = 0; p < n; j = max(1, j *
\rightarrow 2), lim = p) {
   p = j; iota(begin(y), end(y), n - j);
  for (int i = 0; i < (n); i++)
if (sa[i] >= j)
y[p++] = sa[i] - j;
```

fill(begin(ws), end(ws), 0);

→ ws[i - 1]:

for (int i = 0; i < (n); i++) ws[x[i]]++; for (int i = 1; i < (lim); i++) ws[i] +=

```
...for (int i = n; i--;) sa[--ws[x[y[i]]]] =
                                                         Combinatorics (nCr, nPr)

    y[i];

                                                         // can optimize by precomputing factorials, and int phi(int n) {
   swap(x, y); p = 1; x[sa[0]] = 0;
                                                              fact[n]/fact[n-r]
   for (int i = 1; i < (n); i++) {
   a = sa[i - 1]; b = sa[i];
   x[b] = (y[a] == y[b] && y[a + j] == y[b +
                                                         ull nPr(ull n, ull r) {
                                                          ull v = 1;
for (ull i = n-r+1; i <= n; i++)
   j]) ? p - 1 : p++;
                                                          ..v *= i;
return v:
  for (int i = 1; i < (n); i++) rank[sa[i]] =
                                                         ull_nPr(ull n, ull r, ull m) {
                                                          ull v = 1;
for (ull i = n-r+1; i <= n; i++)
 for (int i = 0, j; i < n - 1; lcp[rank[i++]]
                                                           v = (v * i) \% m;
                                                          return v;
for (k \&\& k--, j = sa[rank[i] - 1];
     s[i + k] == s[j + k]; k++);
                                                         ull nCr(ull n, ull r) {
                                                          long double v = 1;
                                                          for (ull i = 1; i <= r; i++)
                                                          v = v * (n-r+i) /i;
return (ull)(v + 0.001);
String Utilities
void lowercase(string& s) {
 transform(s.begin(), s.end(), s.begin(),
                                                         // requires modulo math
^{\prime\prime} can optimize by precomputing mfac and
void uppercase(string& s) {
                                                         ull nCr(ull n, ull r, ull m) {
   return mfac(n, m) * minv(mfac(k, m), m) % m *
 transform(s.begin(), s.end(), s.begin(),
minv(mfac(n-k, m), m) \% m;
void trim(string &s) {
                                                         Chinese Remainder Theorem
 s.erase(s.begin(),find_if_not(s.begin(),s
                                                         bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
     .end(), [](int c){return
   isspace(c);}));
                                                          ll x, y, d; mo = m[0]; re = r[0];
for (int i = 1; i < n; i++) {
 s.erase(find_if_not(s.rbegin(),s.rend(),[](int
                                                           d = \operatorname{egcd}(mo, m[i], x, y);

→ c){return isspace(c):}).base().s.end()):
                                                           if ((r[i] - re) % d!= 0) return false;

x = (r[i] - re) / d * x % (m[i] / d);

re += x * mo;
vector<string> split(string& s, char token) {
    vector<string> v; stringstream ss(s);
                                                           mo = mo / d * m[i];
    for (string e;getline(ss,e,token);)
                                                           re %= mo;
         v.push back(e);
    return v;
                                                          \acute{r}e = (re + mo) \% mo:
                                                          return true;
5 Greedy
                                                         Count Digit Occurences
Interval Cover
                                                         /*count(n.d) counts the number of occurrences of
   L,R = interval [L,R], in = \{\{l,r\}, index\}
                                                          \rightarrow a digit d in the range [0,n]*/
// does not handle case where L == R
                                                         ll digit_count(ll n, ll d) {
vector<int> intervalCover(double L, double R,
                                                         ill tdft_count(i n, ii a,
ill result = 0;
while (n != 0) {
   result += ((n%10) == d ? 1 : 0);

    vector<pair<pair<double,double>,int>> in)

    int i = 0; pair<double,int> pos = {L,-1};

    vector<int>
    a;

                                                           n /= 10;
    sort(begin(in), end(in));
    while (pos.first < R) {
                                                          return result;
         double cur = pos.first;
while (i < (int)in.size() &&</pre>
                                                         ll count(ll n, ll d) {
    if (n < 10) return (d > 0 && n >= d);
    if ((n % 10) != 9) return digit_count(n, d) +
   in[i].first.first <= cur)</pre>
    max(pos,{in[i].first.second,in[i].second})
                                                             count(n-1, d):
                                                          return 10*count(n/10, d) + (n/10) + (d > 0);
    i++;
          if (pos.first == cur) return {};
         a.push_back(pos.second);
                                                         Discrete Logarithm
                                                         unordered_map<int, int> dlogc;
    return a;
                                                         int discretelog(int a, int b, int m) {
                                                          dlogc.clear();
6 Math
                                                         ll n = sqrt(m)+1, an = 1;
for (int i = 0; i < n; i++)
an = (an * a) % m;
Catalan Numbers
ull* catalan = new ull[1000000];
void genCatalan(int n, int mod) {
                                                          11 c = an;
catalan[0] = catalan[1] = 1;
for (int i = 2; i <= n; i++) {
   catalan[i] = 0;
                                                          for (int i = 1; i <= n; i++) {
    if (!dlogc.count(c)) dlogc[c] = i;
                                                           c = (c * an) \% m;
  for (int j = i - 1; j \ge 0; j - -) {
   catalan[i] += (catalan[j] * catalan[i-j-1])
                                                          c = b;
for (int i = 0; i <= n; i++) {
                                                           if (dlogc.count(c)) return (dlogc[c] * n - i
 if (catalan[i] >= mod)
catalan[i] -= mod;
                                                          \rightarrow + m \overline{\phantom{a}}1) % (m-1);
                                                          c = (c * a) \% m;
\mathcal{Y}' // TODO: consider binomial coefficient method
                                                          return -1:
```

```
Euler Phi / Totient
 int r = n;
for (int i = 2; i * i <= n; i++) {
   if (n % i == 0) r -= r / i;</pre>
  while (n % i == 0) n /= i;
 if (n > 1) r = r / n:
 return r;
#define n 100000
ll phi[n+1];
void computeTotient() {
 for (int i=1; i<=n; i++) phi[i] = i;
 for (int p=2; p<=n; p++) {
  .if (phi[p] == p) {
   phi[p] = p-1;
for (int i = 2*p; i<=n; i += p) phi[i] =</pre>
    (phi[i]/p) * (p-1);
Factorials
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
 \rightarrow ME)) + (log10(2 * MPI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
 \hookrightarrow M PI * n) * pow(n / M_E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
Prime Factorization
// do not call directly
ll pollard rho(ll n, ll s) {
 .11 x, y;
 x = y = rand() \% (n - 1) + 1;
 int head = 1. tail = 2:
 while (true) {
 x = mult(x, x, n);

x = (x + s) \% n;
  if (x == y) return n;
  11 d = _gcd(max(x - y, y - x), n);
if (1 < d && d < n) return d;
  if (++head == tail) y = x, tail <<= 1;
// call for prime factors
void factorize(ll n, vector<ll> &divisor) {
 if (n == 1) return:
 if (isPrime(n)) divisor.push back(n);
 else {
    11 d = n:
  while (d'>= n) d = pollard_rho(n, rand() % (n)
 \rightarrow -1) + 1);
  factorize(n / d, divisor);
factorize(d, divisor);
Farey Fractions
    generate 0 \le a/b \le 1 ordered. b \le n
// farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1 // length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farev(int n) {
 int h = 0, k = 1, x = 1, y = 0, r;
 vector<pair<int, int>> v;
 do {
  v.push_back({h, k});
  r = (n-y)/k;
  y += r*k; x' += r*h;
 x = -x; y = -y;

while (k > 1);
```

v.push_back({1, 1});

.return v;

```
Fast Fourier Transform
#define cd complex<double>
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert) {
int n = a.size();
for (int i = 1, j = 0; i < n; i++) {
  int bit = n >> 1:
 for (; j & bit; bit >>= 1) j ^= bit;
j ^= bit;
 if (i < j) swap(a[i], a[j]);
for (int len = 2; len <= n; len <<= 1) {
   double ang = 2 * PI / len * (invert ? -1 :
 cd wlen(cos(ang), sin(ang));
 for (int i = 0; i < n; i += len) {
  for (int j = 0; j < len / 2; j++) {
    cd u = a[i+j], v = a[i+j+len/2] * w;
   a[i+j] = u + v;
   a[i+j+len/2] = u - v;
   .w *= wlen;
 if (invert)
 for (auto& x : a)
  x /= n;
vector<int> fftmult(vector<int> const& a.
→ vector<int> const& b) {
vector<cd> fa(a.begin(), a.end()),

    fb(b.begin(), b.end());

int n = 1 < (32 - \_builtin_clz(a.size() +
\rightarrow b.size() - 1));
fa.resize(n); fb.resize(n);
fft(fa, false); fft(fb, false);
for (int i = 0; i < n; i++) fa[i] *= fb[i];</pre>
fft(fa, true);
 vector<int> toret(n);
for (int i = 0; i < n; i++) toret[i] =

→ round(fa[i].real());

return toret;
Greatest Common Denominator
ll egcd(ll a, ll b, ll& x, ll& y) {
if (b == 0) { x = 1; y = 0; return a; }
11 gcd = egcd(b, a \% b, x, y);
x = a / b * y;
swap(x, y);
return gcd;
Josephus Problem
// 0-indexed, arbitrary k
int josephus(int n, int k) {
if (n == 1) return 0;
if (k == 1) return n-1;
 if (k > n) return (josephus(n-1,k)+k)%n;
 int res = josephus(n-n/k,k)-n\%k;
return res + ((res<0)?n:res/(k-1)):
// fast case if k=2, traditional josephus
int josephus (int n) {
return 2*(n-(1<<(32-\_builtin_clz(n)-1)));
Least Common Multiple
```

#define lcm(a,b) ((a*b)/qcd(a,b))

```
Modulo Operations
 #define MOD 1000000007
 #define madd(a,b,m) (a+b-((a+b-m>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a<b)?m:0))
11 mpow(11 b, 11 e, 11 m) {
Il mpow(11 b, 11 s, --- s, ---
                                                                                                            → double (*f)(double)) {
   e /= 2;
 return x % m;
ull mfac(ull n, ull m) {
                                                                                                           Common Equations Solvers
  ull f = 1;
  for (int i = n; i > 1; i--)
                                                                                                           // ax^2 + bx + c = 0, find x
   f = (f * i) % m;
 return f;

    double c) {
    vector<double> r:
}
 // if m is not guaranteed to be prime
                                                                                                            double z = b * b - 4 * a * c;
if (z == 0)
11 minv(ll b, ll m) {
  \overline{11} x = 0, y = 0;
                                                                                                              r.push back(-b/(2*a));
 if (egcd(b, m, x, y) != 1) return -1;
return (x % m + m) % m;
                                                                                                             else if^-(z > 0) {
11 mdiv_compmod(int a, int b, int m) {
  if (\underline{gcd}(b, m) != 1) return -1;
                                                                                                            return r;
  return mult(a, minv(b, m), m);
 // if m is prime (like 10^9+7)
11 mdiv primemod (int a. int b. int m) {
 return mult(a, mpow(b, m-2, m), m);
Permutation
                                                                                                                  -2*sqrt(q);
 //c = array \ size, \ n = nth \ perm, \ return \ index
vector<int> gen_permutation(int c, int n) {
 vector<int> idx(c), per(c), fac(c); int i;
  for (i = 0; i < c; i++) idx[i] = i;
for (i = 1; i <= c; i++) fac[i-1] = n%i, n/=i;
                                                                                                            if (z \le 0) {
                                                                                                               theta = acos(r/sqrt(q*q*q));
 for (i = c - 1; i >= 0; i--)
per[c-i-1] = idx[fac[i]],
    idx.erase(idx.begin() + fac[i]);
  return per;
                                                                                                                  a1/3.0);
                                                                                                                   a1/3.0);
Miller-Rabin Primality Test
 // Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
  if (n < 2) return false;</pre>
  if (n == 2) return true;
if (n == 2) return true;
if (n % 2 == 0) return false;
ull s = n - 1;
while (s % 2 == 0) s /= 2;
for (int i = 0; i < 10; i++) {
    ull temp = s;</pre>
                                                                                                             \rightarrow - a1 / 3.0:
                                                                                                            return res;
                                                                                                                  find x and u
    ull a = rand() \% (n - 1) + 1:
    ull mod = mpow(a, temp, n);
    while (temp!=n-1\&\&mod!=1\&\&mod!=n-1) {
                                                                                                            mod = mult(mod, mod, n);
                                                                                                            g = egcd(abs(a), abs(b), x, y);
      temp *= 2;
                                                                                                             if (c % g) return false;
    if (mod!=n-1&&temp%2==0) return false;
  return true:
                                                                                                            return true;
Sieve of Eratosthenes
                                                                                                                = coefficient matrix
bitset<100000001> sieve;
 // generate sieve - O(n log n)
                                                                                                           \hookrightarrow a[i][n+1]
void genSieve(int n) {
                                                                                                           const double eps = 1e-7;
 sieve[0] = sieve[1] = 1;
for (ull i = 3; i * i < n; i += 2)
    if (!sieve[i])
    if (ull j = i * 3; j <= n; j += i * 2)</pre>
                                                                                                            → -eps): }
        .sieve[j] = 1;
                                                                                                            \rightarrow n) {
}
// query sieve after it's generated - O(1)
bool querySieve(int n) {
                                                                                                              if (!zero(a[j][i])) {
return n == 2 || (n % 2 != 0 && !sieve[n]);
```

```
.for (int sat = 0; sat < m; sat++) {
. if (sat == cur) continue;</pre>
Simpson's / Approximate Integrals
 // integrate f from a to b, k iterations // error <= (b-a)/18.0*M*((b-a)/2k)^4
                                                                 double num = a[sat][i] / a[cur][i];
for (int sot = 0; sot <= n; sot++)
a[sat][sot] -= a[cur][sot] * num;</pre>
// where M = max(abs(f)) for x in [a,b] // "f" is a function "double func(double x)"
                                                                cur++;
double Simpsons (double a, double b, int k,
                                                                break;
double dx = (b-a)/(2.0*k), t = 0;

for (int i = 0; i < k; i++)

t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
                                                            for (int j = cur; j < m; j++)
 if (!zero(a[i][n])) return vector < double > ():
                                                             vector<double> ans(n,0);
                                                            for (int i = 0, sat = 0; i < n; i++)

if (sat < m && !zero(a[sat][i]))

...ans[i] = a[sat][n] / a[sat++][i];

return ans;
vector<double> solveEq(double a, double b,
                                                           Graycode Conversions
                                                           ull graycode2ull(ull n) {
                                                            ull i = 0:
                                                            for (; n; n = n >> 1) i ^= n; return i;
 r.push_back((sqrt(z)-b)/(2*a));
                                                           ull ull2graycode(ull n) {
  r.push_back((sqrt(z)+b)/(2*a));
                                                            return n ^ (n >> 1);
                                                           Unix/Epoch Time
\frac{1}{1/a} ax^3 + bx^2 + cx + d = 0, find x
                                                           // O-indexed month/time, 1-indexed day
vector<double> solveEq(double a, double b,
double c, double d) {
vector < double > res;
long double a1 = b/a, a2 = c/a, a3 = d/a;
                                                           // minimum 1970, 0, 1, 0, 0, 0
ull toEpoch(int year, int month, int day, int

    hour, int minute, int second) {
    struct tm t; time_t epoch;
    t.tm_year = year - 1900; t.tm_mon = month;
}

 long double q = (a1*a1 - 3*a2)/9.0, sq =
                                                            t.tm_mday = day; t.tm_hour = hour;
t.tm_min = minute; t.tm_sec = second;
t.tm_isdst = 0; // 1 = daylights savings
 long double r = (2*a1*a1*a1 - 9*a1*a2 +
 \rightarrow 27*a3)/54.0;
long double z = r*r-q*q*q, theta;
                                                            epoch = mktime(&t);
                                                            return (ull)epoch;
  res.push_back(sq*cos(theta/3.0) - a1/3.0);
                                                           vector<int> toDate(ull epoch) {
  res.push_back(sq*cos((theta+2.0*PI)/3.0) -
                                                            time t e=epoch; struct tm t=*localtime(&e);
                                                            return {t.tm_year+1900,t.tm_mon,t.tm_mday,t_
  res.push back(sq*cos((theta+4.0*PI)/3.0) -

    .tm_hour,t.tm_min,t.tm_sec};
                                                           int getWeekday(ull epoch) {
                                                            time_t e=epoch; struct tm t=*localtime(&e);
  res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
  res[\hat{0}] = (res[\hat{0}] + \hat{q} / res[\hat{0}]) * ((r<0)?1:-1) | return t.tm_wday; // 0-6, 0 = sunday
                                                           int getDavofYear(ull epoch) {
                                                            time_t e=epoch; struct tm t=*localtime(&e);
                                                            return t.tm_yday; // 0-365
// linear diophantine equation ax + by = c,
// infinite solutions of form x+k*b/g, y-k*a/g Craph bool solveEq(11 a, 11 b, 11 c, 11 &x, 11 &y, 11 struct edge {
                                                                Graphs
                                                            int u, v, w;
                                                             edge (int u,int v,int w) : u(u),v(v),w(w) {}
                                                            edge (): u(0), v(0), w(0) {}
 x *= c / g * ((a < 0) ? -1 : 1);
                                                           bool operator < (const edge &e1, const edge
 y *= c / g * ((b < 0) ? -1 : 1);
                                                           \rightarrow &e2) { return e1.w < e2.w; }
                                                           bool operator > (const edge &e1, const edge
 ^{\prime}// m = # equations, n = # variables, a[m][n+1]
                                                            \rightarrow &e2) { return e1.w > e2.w: }
                                                           struct subset { int p, rank; };
// a[i][0]x + a[i][1]y + ... + a[i][n]z =
                                                           Eulerian Path
                                                           #define edge_list vector<edge>
#define adj sets vector<set<int>>>
bool zero(double a) { return (a < eps) && (a >
                                                           struct EulerPathGraph {
                                                            adj_sets graph; // actually indexes incident
vector < double > solveEq(double **a, int m, int
edge_list edges; int n; vector<int> indeg;
                                                             EulerPathGraph(int n): n(n) {
                                                             indeg = *(new vector<int>(n,0));
                                                             graph = *(new adj_sets(n, set<int>()));
  ...if (j != cur) swap(a[j], a[cur]);
```

```
void add_edge(int u, int v) {
 graph[u].insert(edges.size());
  indeg[v]++;
  edges.push back(edge(u,v,0));
 bool eulerian_path(vector<int> &circuit) {
 if(edges.size()==0) return false;
 stack<int> st;
int a[] = {-1, -1};
for(int v=0;v<n;v++)
   if(indeg[v]!=graph[v].size()) {
   bool b = indeg[v] > graph[v].size();
    if (abs(((int)indeg[v])-((int)graph[v]
    .size())) > 1) return
   false;
if (a[b] != -1) return false;
   a[b] = v;
  int s = (a[0]!=-1 \&\& a[1]!=-1 ? a[0] :
 \rightarrow (a[0]==-1 && a[1]==-1 ? edges[0].u : -1));
 if(s==-1) return false;
  while(!st.empty() || !graph[s].empty()) {
  if (graph[s].empty()) {
    circuit.push back(s): s = st.top():
   st.pop(); }
   else {
    int w = edges[*graph[s].begin()].v;
    graph[s].erase(graph[s].begin());
    st.push(s); s = w:
 circuit.push back(s):
 return circuit.size()-1==edges.size();
Floyd Warshall
const ll inf = 1LL << 62;
#define FOR(i,n) for (int i = 0; i < n; i++)
void floydWarshall(Vec<2, 11>& m) {
int n = m.size();
FOR(i,n) m[i][i] = min(m[i][i], OLL);
FOR(k,n) FOR(i,n) FOR(j,n) if (m[i][k] != inf
 \rightarrow && m[k][j] != inf)
 auto newDist = max(m[i][k] + m[k][j], -inf);
m[i][j] = min(m[i][j], newDist);
 FOR(k,n) if (m[k][k] < 0) FOR(i,n) FOR(j,n)
 if (m[i][k] != inf && m[k][j] != inf)

→ m[i][i] = -inf:

Minimum Spanning Tree
// returns vector of edges in the mst
// graph[i] = vector of edges incident to
   vertex i places total weight of the mst in &total
// if returned vector has size != n-1, there is
vector<edge> mst(vector<vector<edge>> graph,

→ 11 &total) {

priority_queue<edge, vector<edge>,

    greater<edge>> pq;
vector<edge> MST;
bitset<20001> marked; // change size as needed
marked[0] = 1:
for (edge ep : graph[0]) pq.push(ep); while (MST.size()!=graph.size()-1 &&
   pq.size()!=0) {
  edge e = pq.top(); pq.pop();
 int u = e.u, v = e.v, w = e.w;

if(marked[u] && marked[v]) continue;

else if(marked[u]) swap(u, v);
  for(edge ep : graph[u]) pq.push(ep);
  marked[u] = 1;
  MST.push back(e);
```

```
total += e.w:
 return MST:
Union Find
int uf_find(subset* s, int i) {
  if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
return s[i].p;
void uf_union(subset* s, int x, int y) {
int xp = uf_find(s, x), yp = uf_find(s, y);
 if (s[xp].rank > s[yp].rank) s[yp].p = xp;
 else if (s[xp].rank < s[yp].rank) s[xp].p =
else { s[yp].p = xp; s[xp].rank++; }
    2D Geometry
#define point complex<double>
#define EPS 0.0000001
#define sq(a) ((a)*(a))
#define c\bar{b}(a) ((a)*(a)*(a))
double dot(point a, point b) { return

    real(coni(a)*b): }

double cross(point a, point b) { return
\rightarrow imag(conj(a)*b); }
struct line { point a, b; };
struct circle { point c; double r; };
struct segment { point a, point b; };
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
struct convex_polygon {
vector<point points;
 convex_polygon(vector<point> points) :

→ points(points) {}
 convex_polygon(triangle a) {
 points.push_back(a.a); points.push_back(a.b);
→ points.push_back(a.c);
 convex polygon(rectangle a) {
 points.push back(a.tl);
    points.push back({real(a.tl),
    imag(a.br)}):
 points.push back(a.br);
    points.push back({real(a.br),
    imag(a.tl)});
struct polygon {
vector <point > points;
 polygon(vector point points) : points(points) pair double, point area_centroid(polygon a) {
polygon(triangle a) {
 points.push_back(a.a); points.push_back(a.b);

→ points.push_back(a.c);

 polygon(rectangle a) {
 points.push_back(a.tl);
    points.push_back({real(a.tl),
    imag(a.br)});
  points.push_back(a.br);
    points.push back({real(a.br),
    imag(a.tl)});
 polygon(convex_polygon a) {
  for (point v : a.points)
   points.push_back(v);
   triangle methods
double area_heron(double a, double b, double c)
\stackrel{\hookrightarrow}{} {
if (a < b) swap(a, b);
if (a < c) swap(a, c);
 if (b < c) swap(b, c);
```

```
if (a > b + c) return -1;
return sqrt((a+b+c)*(c-a+b)*(c+a-b)*(a+b-c)
// segment methods
double lengthsq(segment a) { return
    sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
   imag(a.b)): }
double length(segment a) { return
   sqrt(lengthsq(a)); }
  circle methods
double circumference(circle a) { return 2 * a.r.
→ * M_PI; }
double area(circle a) { return sq(a.r) * M PI;
→ }
// rectangle methods
double width(rectangle a) { return

    abs(real(a.br) - real(a.tl)): }

double height (rectangle a) { return

→ abs(imag(a.br) - real(a.tl)); }

double diagonal (rectangle a) { return

    sqrt(sq(width(a)) + sq(height(a))); }

double area (rectangle a) { return width(a) *
\rightarrow height(a); }
double perimeter(rectangle a) { return 2 *
   (width(a) + height(a)); }
// check if `a` fit's inside `b`
// swap equalities to exclude tight fits
bool doesFitInside(rectangle a, rectangle b) {
int x = width(a), w = width(b), y = height(a)
\rightarrow h = height(b);
if (x > y) swap(x, y);
if (w > h) swap(w, h);
if (w < x) return false;
if (y <= h) return true;</pre>
double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
return sq(a) \le sq(b) + sq(c);
  polygon methods
// negative area = CCW, positive = CW
double area(polygon a) {
  double area = 0.0; int n = a.points.size();
  for (int i = 0, i = 1; i < n; i++, i = (i)
    (real(a.points[j]-a.points[i]))*(imag(a |
    .points[j]+a.points[i]));
 return area / 2.0;
  get both unsigned area and centroid
int n = a.points.size():
double area = 0;
point c(0, 0);
 for (int i = n - 1, j = 0; j < n; i = j++) {
 double v = cross(a.points[i], a.points[j]) /
 area += v:
 c += (a.points[i] + a.points[j]) * (v / 3);
c /= area:
return {area, c};
Intersection
// -1 coincide, 0 parallel, 1 intersection
int intersection(line a, line b, point& p) {
if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
 p = cross(b.a - a.a, b.b - a.b) / cross(a.b)
 \rightarrow a.a, b.b - b.a) * (b - a) + a;
 return 1:
if (abs(cross(a.b - a.a. a.b - b.a)) > EPS)
   return 0;
return -1;
  area of intersection
```

```
double intersection(circle a, circle b) {
double d = abs(a.c - b.c);
 if (d <= b.r - a.r) return area(a);
 if (d <= a.r - b.r) return area(b);
if (d >= a.r + b.r) return 0;
 double alpha = acos((sq(a.r) + sq(d) -
 \rightarrow sg(b.r)) / (2 * a.r * d)):
 double beta = acos((sq(b.r) + sq(d) - sq(a.r))
 \rightarrow / (2 * b.r * d)):
 return sq(a.r) * (alpha - 0.5 * sin(2 *
    alpha) + sq(b.r) * (beta - 0.5 * sin(2 *
// -1 outside. O inside. 1 tangent. 2

    intersection
int intersection(circle a, circle b,
→ vector<point>& inter) {
double d2 = norm(b.c - a.c), rS = a.r + b.r,
 \rightarrow rD = a.r - b.r:
 if (d2 > sq(rS)) return -1;
 if (d2 < sq(rD)) return 0;
 double ca = 0.5 * (1 + rS * rD / d2);
point z = point(ca, sqrt(sq(a.r) / d2 -
\rightarrow sq(ca))):
 inter.push back(a.c + (b.c - a.c) * z):
 if (abs(imag(z)) > EPS) inter.push_back(a.c
\hookrightarrow (b.c - a.c) * conj(z));
return inter.size();
// points of intersection
vector<point> intersection(line a, circle c) {
vector<point> inter;
c.c -= a.a;
a.b -= a.a;
point m = a.b * real(c.c / a.b):
 double d2 = norm(m - c.c):
 if (d2 > sq(c.r)) return 0;
 double l = sqrt((sq(c.r) - d2) / norm(a.b));
 inter.push_back(a.a + m + 1 * a.b);
 if (abs(1) > EPS) inter.push back(a.a + m
\rightarrow * a.b):
return inter:
 // area of intersection
double intersection(rectangle a, rectangle b) {
 double x1 = max(real(a.tl), real(b.tl)), v1 =
 → max(imag(a.tl), imag(b.tl));
 double x2 = min(real(a.br), real(b.br)), y2 =
→ min(imag(a.br), imag(b.br));
return (x2 <= x1 || y2 <= y1) ? 0 :
\hookrightarrow (x2-x1)*(v2-v1):
Convex Hull
bool cmp(point a, point b) {
 if (abs(real(a) - real(b)) > EPS) return
    real(a) < real(b);
if (abs(imag(a) - imag(b)) > EPS) return
 → imag(a) < imag(b);</pre>
return false;
convex_polygon convexhull(polygon a) {
 sort(a.points.begin(), a.points.end(), cmp);
 vector<point> lower, upper;
 for (int i = 0; i < a.points.size(); i++) {
 while (lower.size() >= 2 &&
    cross(lower.back() - lower[lower.size() -
    2], a.points[i] - lower.back()) < EPS)
  lower.pop_back();
  while (upper.size() >= 2 &&
    cross(upper.back() - upper[upper.size()
    2], a.points[i] - upper.back()) > -EPS)
   upper.pop_back();
  lower.push back(a.points[i]):
  upper.push_back(a.points[i]);
 lower.insert(lower.end(), upper.rbegin() + 1,
   upper.rend()):
```

```
return convex_polygon(lower);
     3D Geometry
struct point3d {
 double x, y, z;
 point3d operator+(point3d a) const { return
 \rightarrow {x+a.x, y+a.y, z+a.z}; }
 point3d operator*(double a) const { return
 \hookrightarrow {x*a, y*a, z*a}; }
 point3d operator-() const { return {-x, -y,
 \rightarrow -z}; }
 point3d operator-(point3d a) const { return
 \rightarrow *this + -a; }
 point3d operator/(double a) const { return
 *this * (1/a); }
double norm() { return x*x + y*y + z*z; }
 double abs() { return sqrt(norm()); }
 point3d normalize() { return *this /
this->abs(); }
double dot(point3d a, point3d b) { return
 \rightarrow a.x*b.x + a.y*b.y + a.z*b.z; }
point3d cross(point3d a, point3d b) { return
    \{a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,
 \stackrel{\hookrightarrow}{\Rightarrow} a.x*b.y - a.y*b.x}; }
struct line3d { point3d a, b; };
struct plane { double a, b, c, d; } // a*x +
 \rightarrow b*y + c*z + d = 0
 struct sphere { point3d c; double r; };
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double surface(circle a) { return 4 * sq(a.r) *

    M_PI; }

double volume(circle a) { return 4.0/3.0 *
 \rightarrow cb(a.r) * M PI; }
10
       Optimization
 Snoob
 // SameNumberOfOneBits. next permutation
 int snoob(int a) {
 int b = a & -a, c = a + b;
return c \mid ((a \hat{c}) >> 2) / b;
 // example usage
int main() {
  char l1[] = {'1', '2', '3', '4', '5', char l2[] = {'a', 'b', 'c', 'd'};
  int d1 = 5, d2 = 4;
  // prints 12345abcd, 1234a5bcd, ...
 int min = (1<<d1)-1, max = min << d2;</pre>
 for (int i = min; i <= max; i = snoob(i)) {
  int p1 = 0, p2 = 0, v = i;
  while (p1 < d1 || p2 < d2) {
   cout << ((v & 1) ? l1[p1++] : l2[p2++]);
   .v /= 2;
  cout << '\n';
Powers
 bool isPowerOf2(11 a) {
 return a > 0 \&\& !(a \& a-1):
 bool isPowerOf3(11 a) {
return a>0&&!(12157665459056928801ull%a);
 bool isPower(ll a, ll b) {
  double x = log(a) / log(b);
 return abs(x-round(x)) < 0.00000000001;
 11 Additional
 Judge Speed
    kattis: 0.50s
```

/ codeforces: 0.421s

```
// atcoder: 0.455s
#include <bits/stdc++.h>
using namespace std;
int v = 1e9/2, p = 1;
int main() {
  for (int i = 1; i <= v; i++) p *= i;</pre>
 cout << p;
Judge Pre-Contest Checks
     int128 and float128 support?
-does extra or missing whitespace cause WA?
-documentation up to date?
- printer usage available and functional?
// each case tests a different fail condition
// try them before contests to see error codes
struct g { int arr[1000000]; g(){}};
vector<g> a;
 // O=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
→ 6=SIGSEGV 7=recursive MLE int judge(int n) {
 if (n == 0) exit(0);
if (n == 1) while(1);
if (n == 2) while(1) a.push_back(g());
if (n == 3) while(1) putchar_unlocked('a');
  if (n == 4) assert(0);
 if (n == 5) 0 / 0;
if (n == 6) *(int*)(0) = 0;
 return n + judge(n + 1);
GCC Builtin Docs
 // 128-bit integer
__int128 a;
unsigned __int128 b;
 // 128-bit float
 // minor improvements over long double
_float128 c;
// log2 floor
 __lg(n);
__lg(n);
// number of 1 bits
// can add ll like popcountll for long longs
__builtin_popcount(n);
// number of trailing zeroes
__builtin_ctz(n);
// number of leading zeroes
__builtin_clz(n);
// 1-indexed least significant 1 bit
__builtin_ffs(n):
__builtin_ffs(n);
// parity of number
 __builtin_parity(n);
Limits
                         \pm 2147483647 \mid \pm 2^{31}_{-2} - 1 \mid 10^9
 int
                                                 \frac{1}{2}^{32} - \frac{1}{1} | 10^9
                            4294967295
 uint
         \pm 9223372036854775807 | \pm 2^{63} - 1|10^{18}
 11
                                                 \frac{1}{2}^{64} - \frac{1}{1}^{10}^{19}
          18446744073709551615
 ull
|\pm 170141183460469231...|\pm 2^{\tilde{1}27} - 1|10^{38}
                                              -\frac{1}{2}<sup>128</sup> -\frac{1}{1}<sup>1038</sup>
 u128 340282366920938463...
 Complexity classes input size (per second):
 O(n^n) or O(n!)
                                                          n < 10
 O(2^n)
                                                          n < 30
 O(n^3)
                                                       n \le 1000
O(n^2)
                                                     n \le 30000
                                                        n \le 10^6
 O(n\sqrt{n})
                                                        n \le 10^7
 O(n \log n)
 O(n)
                                                         n < 10^9
```