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1 General

```
run.sh
g++ -g -O2 -std=gnu++17 -static prog.cpp
./a.exe
```

test.sh

```
# compile and test all *.in and *.ans
g++ -g -O2 -std=gnu++17 -static prog.cpp
for i in *.in; do
    f=${i%.in}
    ./a.exe < $i > "$f.out"
    diff -b -q "$f.ans" "$f.out"
done
```

Header

```
// use better compiler options
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
// include everything
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <sys/resource.h>
// namespaces
using namespace std;
using namespace __gnu_cxx; // rope
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio
    ios_base::sync_with_stdio(0);cin.tie(0);
    #define nostacklim rlimit RZ;getrlimit(3,&RZ)
    #define DEBUG(v) cerr<<_LINE_<<": "<<#v<<" = "<<v<<'\n';
    #define TIMER
    cerr<<1.0*clock()/CLOCKS_PER_SEC<<"s\n";
    #define ll long long
    #define ull unsigned ll
    #define i128 __int128
    #define ui128 unsigned i128
    #define ld long double
    // global variables
mt19937 rng((uint32_t)chrono::steady)
    _clock::now().time_since_epoch().count());
```

Fast IO

```
#ifdef _WIN32
#define getchar_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
#endif
void read(unsigned int& n) {
    char c; n = 0;
    while ((c=getchar_unlocked())!=' ' && c!='\n')
        n = n * 10 + c - '0';
}
void read(int& n) {
    char c; n = 0; int s = 1;
    if ((c=getchar_unlocked())=='-') s = -1;
    else n = c - '0';
    while ((c=getchar_unlocked())!=' ' && c!='\n')
        n = n * 10 + c - '0';
    n *= s;
}
void read(ld& n) {
    char c; n = 0;
    ld m = 0, o = 1; bool d = false; int s = 1;
    if ((c=getchar_unlocked())=='-') s = -1;
    else if (c == '.') d = true;
    else n = c - '0';
    while ((c=getchar_unlocked())!=' ' && c!='\n') {
        if (c == '.') d = true;
```

```
    else if (d) { m=m*10+c-'0'; o*=0.1; }
    else n = n * 10 + c - '0';
}
n = s * (n + m * o);
void read(double& n) {
    ld m; read(m); n = m;
}
void read(float& n) {
    ld m; read(m); n = m;
}
void read(string& s) {
    char c; s = "";
    while((c=getchar_unlocked())!=' ' && c!='\n')
        s += c;
}
bool readline(string& s) {
    char c; s = "";
    while(c=getchar_unlocked()) {
        if (c == '\n') return true;
        if (c == EOF) return false;
        s += c;
    }
    return false;
}
void print(unsigned int n) {
    if (n / 10) print(n / 10);
    putchar_unlocked(n % 10 + '0');
}
void print(int n) {
    if (n < 0) { putchar_unlocked('-'); n*=-1; }
    print((unsigned int)n);
}
```

Common Structs

```
// n-dimension vectors
Vec<2, int> v(n, m) = arr[n][m]
// Vec<2, int> v(n, m, -1) default init -1
template<int D, typename T>
struct Vec : public vector<Vec<D-1, T>> {
    template<typename... Args>
    Vec(int n=0, Args... args) : vector<Vec<D-1, T>>(n, Vec<D-1, T>(args...)) {}
};
template<typename T>
struct Vec<1, T> : public vector<T> {
    Vec(int n=0, T val=T()) : vector<T>(n, val) {}
};
```

2 Algorithms

Binary Search

```
// search for k in [p,n)
template<typename T>
int binsearch(T x[], int k, int n, int p = 0) {
    for (int i = n; i >= 1; i /= 2)
        while (p+i < n && x[p+i] <= k) p += i;
    return p; // bool: x[p] == k;
}
```

Min/Max Subarray

```
// max - compare = a < b, reset = a < 0
// min - compare = a > b, reset = a > 0
// returns {sum, {start, end}}
pair<int, pair<int, int>>
ContiguousSubarray(int* a, int size,
    bool(*compare)(int, int),
    bool(*reset)(int), int defbest = 0) {
    int best = defbest, cur = 0, start = 0, end = 0, s = 0;
    for (int i = 0; i < size; i++) {
        cur += a[i];
        if ((*compare)(best, cur)) { best = cur;
            start = s; end = i; }
        if ((*reset)(cur)) { cur = 0; s = i + 1; }
    }
    return {best, {start, end}};
}
```

Quickselect

```
#define QSNE -999999
int partition(int arr[], int l, int r)
{
    int x = arr[r], i = l;
    for (int j = l; j <= r - 1; j++)
        if (arr[j] <= x)
            swap(arr[i++], arr[j]);
    swap(arr[i], arr[r]);
    return i;
}
// find k'th smallest element in unsorted array,
// only if all distinct
int qselect(int arr[], int l, int r, int k)
{
    if (!(k > 0 && k <= r - l + 1)) return QSNE;
    swap(arr[l + rng() % (r-l+1)], arr[r]);
    int pos = partition(arr, l, r);
    if (pos-l==k-1) return arr[pos];
    if (pos-l>k-1) return qselect(arr, l, pos-1, k);
    return qselect(arr, pos+1, r, k-pos-l-1);
}
// TODO: compare against std::nth_element()
```

Saddleback Search

```
// search for v in 2d array arr[x][y], sorted
// on both axis
pair<int, int> saddleback_search(int** arr, int
    x, int y, int v) {
    int i = x-1, j = 0;
    while (i >= 0 && j < y) {
        if (arr[i][j] == v) return {i, j};
        (arr[i][j] > v)? i--: j++;
    }
    return {-1, -1};
}
```

Ternary Search

```
// < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {
    while (b-a > 4) {
        int m = (a+b)/2;
        if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
        else b = m+1;
    }
    for (int i = a+1; i <= b; i++)
        if (TERNCOMP((*f)(a), (*f)(i)))
            a = i;
    return a;
}
#define TERNPREC 0.000001
double ternsearch(double a, double b, double
    (*f)(double)) {
    while (b-a > TERNPREC * 4) {
        double m = (a+b)/2;
        if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
            = m;
        else b = m + TERNPREC;
    }
    for (double i = a + TERNPREC; i <= b; i +=
        TERNPREC)
        if (TERNCOMP((*f)(a), (*f)(i)))
            a = i;
    return a;
}
```

Golden Section Search

```
// < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
double goldsection(double a, double b, double
    (*f)(double)) {
    double r = (sqrt(5)-1)/2, eps = 1e-7;
    double x1 = b - r*(b-a), x2 = a + r*(b-a);
    double f1 = f(x1), f2 = f(x2);
    while (b-a > eps)
        if (TERNCOMP(f2, f1)) {
            b = x2; x2 = x1; f2 = f1;
            x1 = b - r*(b-a); f1 = f(x1);
        } else {
            a = x1; x1 = x2; f1 = f2;
```

```
        x2 = a + r*(b-a); f2 = f(x2);
    }
    return a;
}
3 Structures
Fenwick Tree
// Fenwick tree, array of cumulative sums -
// O(log n) updates, O(log n) gets
struct Fenwick {
    int n; ll* tree;
    void update(int i, int val) {
        ++i;
        while (i <= n) {
            tree[i] += val;
            i += i & (-i);
        }
}
Fenwick(int size) {
    n = size;
    tree = new ll[n+1];
    for (int i = 1; i <= n; i++)
        tree[i] = 0;
}
Fenwick(int* arr, int size) : Fenwick(size) {
    for (int i = 0; i < n; i++)
        update(i, arr[i]);
}
-Fenwick() { delete[] tree; }
ll operator[](int i) {
    if (i < 0 || i > n) return 0;
    ll sum = 0;
    ++i;
    while (i>0) {
        sum += tree[i];
        i -= i & (-i);
    }
    return sum;
}
ll getRange(int a, int b) { return
    operator[](b) - operator[](a-1); }
};
```

Hashtable

```
// similar to unordered_map, but faster
struct chash {
    const uint64_t C = (1ll)(2e18 * M_PI) + 71;
    ll operator()(ll x) const { return
        __builtin_bswap64(x*C); }
};
int main() {
    gp_hash_table<ll,int,chash>
        hashtable({},{},{},{},{},{1<16});
    for (int i = 0; i < 100; i++)
        hashtable[i] = 200+i;
    if (hashtable.find(10) != hashtable.end())
        cout << hashtable[10];
}
```

Ordered Set

```
template<typename T>
using oset = tree<T,null_type,less<T>,rb_tree>
    _tag,tree_order_statistics_node_update>;
template<typename T, typename D>
using omap = tree<T,D,less<T>,rb_tree>
    _tag,tree_order_statistics_node_update>;
int main()
{
    oset<int> o_set;
    o_set.insert(5); o_set.insert(1);
    o_set.insert(3);
    // get second smallest element
    cout << *(o_set.find_by_order(1));
    // number of elements less than k=4
    cout << ' ' << o_set.order_of_key(4) << '\n';
    // equivalent with ordered map
    omap<int,int> o_map;
    o_map[5]=1;o_map[1]=2;o_map[3]=3;
    cout << (*(o_map.find_by_order(1))).first;
    cout << ' ' << o_map.order_of_key(4) << '\n';
}
```

Rope

```
// O(log n) insert, delete, concatenate
int main() {
    // generate rope
    rope<int> v;
    for (int i = 0; i < 100; i++)
        v.push_back(i);
    // move range to front
    rope<int> copy = v.substr(10, 10);
    v.erase(10, 10);
    v.insert(copy.mutable_begin(), copy);
    // print elements of rope
    for (auto it : v)
        cout << it << " ";
}
```

Segment Tree

```
//max(a,b), min(a,b), a+b, a*b, gcd(a,b), a^b
struct SegmentTree {
    typedef int T;
    static constexpr T UNIT = INT_MIN;
    T f(T a, T b) {
        if (a == UNIT) return b;
        if (b == UNIT) return a;
        return max(a, b);
    }
    int n; vector<T> s;
    SegmentTree(int n, T def=UNIT) : s(2*n, def),
        n(n) {}
    SegmentTree(vector<T> arr) :
        SegmentTree(arr.size()) {}
    for (int i=0; i<arr.size(); i++)
        update(i, arr[i]);
    void update(int pos, T val) {
        for (s[pos += n] = val; pos /= 2;)
            s[pos] = f(s[pos * 2], s[pos*2+1]);
    }
    T query(int b, int e) { // query [b, e)
        T ra = UNIT, rb = UNIT;
        for (b += n, e += n; b < e; b /= 2, e /= 2) {
            if (b % 2) ra = f(ra, s[b++]);
            if (e % 2) rb = f(s[--e], rb);
        }
        return f(ra, rb);
    }
    T get(int p) { return query(p, p+1); }
};
```

Sparse Table

```
template<class T> struct SparseTable {
    vector<vector<T>> m;
    SparseTable(vector<T> arr) {
        m.push_back(arr);
        for (int k = 1; (1<<(k)) <= size(arr); k++) {
            m.push_back(vector<T>(size(arr)-(1<<(k)+1)));
            for (int i = 0; i < size(arr)-(1<<(k)+1); i++)
                m[k][i] = min(m[k-1][i],
                    m[k-1][i+(1<<(k-1))]);
        }
        // min of range [l, r]
        T query(int l, int r) {
            int k = __lg(r-l+1);
            return min(m[k][l], m[k][r-(1<<(k)+1)]);
        }
    };
};
```

Trie

```
typedef trie<string, null_type,
    trie_string_access_traits<>,
    pat_trie_tag, trie_prefix_search_node_update>
    trie_type;
int main() {
    // generate trie
    trie_type trie;
    for (int i = 0; i < 20; i++)
        trie.insert(to_string(i)); // true if new,
        false if old
}
```

```
// print things with prefix "1"
auto range = trie.prefix_range("1");
for (auto it = range.first; it !=
    range.second; it++)
    cout << *it << " ";
}
```

Wavelet Tree

```
using iter = vector<int>::iterator;
struct WaveletTree {
    Vec<2, int> C; int s;
    // sigma = highest value + 1
    WaveletTree(vector<int>& a, int sigma) :
        s(sigma), C(sigma*2, 0) {
        build(a.begin(), a.end(), 0, s-1, 1);
    }
    void build(iter b, iter e, int L, int U, int
        u) {
        if (L == U) return;
        int M = (L+U)/2;
        C[u].reserve(e-b+1); C[u].push_back(0);
        for (auto it = b; it != e; ++it)
            C[u].push_back(C[u].back() + (*it<=M));
        auto p = stable_partition(b, e, [=](int
            i){return i<=M;});
        build(b, p, L, M, u*2);
        build(p, e, M+1, U, u*2+1);
    }
    // number of occurrences of x in [0, i)
    int rank(int x, int i) {
        int L = 0, U = s-1, u = 1, M, r;
        while (L != U) {
            M = (L+U)/2;
            r = C[u][i]; u *= 2;
            if (x <= M) i = r, U = M;
            else i -= r, L = M+1, ++u;
        }
        return i;
    }
    // number of occurrences of x in [l, r)
    int count(int x, int l, int r) {
        return rank(x, r) - rank(x, l);
    }
    // kth smallest in [l, r)
    int kth(int k, int l, int r) const {
        int L = 0, U = s-1, u = 1, M, ri, rj;
        while (L != U) {
            M = (L+U)/2;
            ri = C[u][l]; rj = C[u][r]; u *= 2;
            if (k <= rj-ri) l = ri, r = rj, U = M;
            else k -= rj-ri, l -= ri, r -= rj,
                L = M+1, ++u;
        }
        return U;
    }
    // # elements between [x,y] in [l, r)
    mutable int L, U;
    int range(int x, int y, int l, int r) const {
        if (y < x or r <= l) return 0;
        L = x; U = y;
        return range(l, r, 0, s-1, 1);
    }
    int range(int l, int r, int x, int y, int u)
        const {
        if (y < L or U < x) return 0;
        if (L <= x and y <= U) return r-l;
        int M = (x+y)/2, ri = C[u][l], rj = C[u][r];
        return range(ri, rj, x, M, u*2) + range(l-ri,
            r-rj, M+1, y, u*2+1);
    }
    // # elements <= x in [l, r)
    int lte(int x, int l, int r) {
        return range(INT_MIN, x, l, r);
    }
};
```

4 Strings

Aho Corasick

```
// range of alphabet for automata to consider
// MAXC = 26, OFFC = 'a' if only lowercase
```

```
const int MAXC = 256;
const int OFFC = 0;
struct aho_corasick {
    struct state {
        set<pair<int, int>> out;
        int fail; vector<int> go;
        state() : fail(-1), go(MAXC, -1) {}
    };
    vector<state> s;
    int id = 0;
    aho_corasick(string* arr, int size) : s(1) {
        for (int i = 0; i < size; i++) {
            int cur = 0;
            for (int c : arr[i]) {
                if (s[cur].go[c-OFFC] == -1) {
                    s[cur].go[c-OFFC] = s.size();
                    s.push_back(state());
                }
                cur = s[cur].go[c-OFFC];
            }
            s[cur].out.insert({arr[i].size(), id++});
        }
        for (int c = 0; c < MAXC; c++)
            if (s[0].go[c] == -1)
                s[0].go[c] = 0;
        queue<int> sq;
        for (int c = 0; c < MAXC; c++) {
            if (s[0].go[c] != 0) {
                s[s[0].go[c]].fail = 0;
                sq.push(s[0].go[c]);
            }
            while (sq.size()) {
                int e = sq.front(); sq.pop();
                for (int c = 0; c < MAXC; c++) {
                    if (s[e].go[c] != -1) {
                        int failure = s[e].fail;
                        while (s[failure].go[c] == -1)
                            failure = s[failure].fail;
                        failure = s[failure].go[c];
                        s[s[e].go[c]].fail = failure;
                        for (auto length : s[failure].out)
                            s[s[e].go[c]].out.insert(length);
                        sq.push(s[e].go[c]);
                    }
                }
            }
        }
        // list of {start pos, pattern id}
        vector<pair<int, int>> search(string txt) {
            vector<pair<int, int>> toret;
            int cur = 0;
            for (int i = 0; i < txt.size(); i++) {
                while (s[cur].go[txt[i]-OFFC] == -1)
                    cur = s[cur].fail;
                cur = s[cur].go[txt[i]-OFFC];
                if (s[cur].out.size())
                    for (auto end : s[cur].out)
                        toret.push_back({i - end.first + 1,
                            end.second});
            }
            return toret;
        };
    };
};
```

Boyer Moore

```
struct definit { int i = -1; };
vector<int> boyermore(string txt, string pat) {
    {
        vector<int> toret; unordered_map<char, definit>
            badchar;
        int m = pat.size(), n = txt.size();
        for (int i = 0; i < m; i++) badchar[pat[i]].i
            = i;
        int s = 0;
        while (s <= n - m) {
            int j = m - 1;
            while (j >= 0 && pat[j] == txt[s + j]) j--;
            if (j < 0) {
                toret.push_back(s);
                s += m;
            }
        }
    }
}
```

```
toret.push_back(s);
s += (s + m < n) ? m - badchar[txt[s +
    m]].i : 1;
} else
    s += max(1, j - badchar[txt[s + j]].i);
}
return toret;
}
```

English Conversion

```
const string ones[] = {"", "one", "two",
    "three", "four", "five", "six", "seven",
    "eight", "nine"};
const string teens[] = {"ten", "eleven",
    "twelve", "thirteen", "fourteen",
    "fifteen", "sixteen", "seventeen",
    "eighteen", "nineteen"};
const string tens[] = {"twenty", "thirty",
    "forty", "fifty", "sixty", "seventy",
    "eighty", "ninety"};
const string mags[] = {"thousand", "million",
    "billion", "trillion", "quadrillion",
    "quintillion", "sextillion",
    "septillion"};
string convert(int num, int carry) {
    if (num < 0) return "negative " +
        convert(-num, 0);
    if (num < 10) return ones[num];
    if (num < 20) return teens[num % 10];
    if (num < 100) return tens[(num / 10) - 2] +
        (num%10==0?"": " ") + ones[num % 10];
    if (num < 1000) return ones[num / 100] +
        (num/100==0?"": " ") + "hundred" +
        (num%100==0?"": " ") + convert(num % 100,
            0);
    return convert(num / 1000, carry + 1) + " " +
        mags[carry] + " " + convert(num % 1000,
            0);
}
string convert(int num) {
    return (num == 0) ? "zero" : convert(num, 0);
}
```

Knuth Morris Pratt

```
vector<int> kmp(string txt, string pat) {
    vector<int> toret;
    int m = txt.length(), n = pat.length();
    int next[n + 1];
    for (int i = 0; i < n + 1; i++)
        next[i] = 0;
    for (int i = 1; i < n; i++) {
        int j = next[i + 1];
        while (j > 0 && pat[j] != pat[i])
            j = next[j];
        if (j > 0 || pat[j] == pat[i])
            next[i + 1] = j + 1;
    }
    for (int i = 0, j = 0; i < m; i++) {
        if (txt[i] == pat[j]) {
            if (++j == n)
                toret.push_back(i - j + 1);
        } else if (j > 0) {
            j = next[j];
        }
    }
    return toret;
}
```

Longest Common Prefix (array)

```
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
    false) {
    if (n == 0) return "";
    if (!sorted) sort(arr, arr + n);
    string r = ""; int v = 0;
    while (v < arr[0].length() && arr[0][v] ==
        arr[n-1][v])
        r += arr[0][v++];
    return r;
}
```

Longest Common Subsequence

```
string lcs(string a, string b) {
    int m = a.length(), n = b.length();
    int L[m+1][n+1];
    for (int i = 0; i <= m; i++) {
        for (int j = 0; j <= n; j++) {
            if (i == 0 || j == 0) L[i][j] = 0;
            else if (a[i-1] == b[j-1]) L[i][j] =
                L[i-1][j-1] + 1;
            else L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    }
    // return L[m][n]; // length of lcs
    string out = "";
    int i = m - 1, j = n - 1;
    while (i >= 0 && j >= 0) {
        if (a[i] == b[j]) {
            out = a[i--] + out;
            j--;
        }
        else if (L[i][j+1] > L[i+1][j]) i--;
        else j--;
    }
    return out;
}
```

Longest Common Substring

```
// l is array of palindrome length at that
// index
int manacher(string s, int* l) {
    int n = s.length() * 2;
    for (int i = 0, j = 0, k; i < n; i += k, j =
        max(j-k, 0)) {
        while (i >= j && i + j + 1 < n && s[(i-j)/2]
            == s[(i+j+1)/2]) j++;
        l[i] = j;
        for (k = 1; i >= k && j >= k && l[i-k] !=
            j-k; k++)
            l[i+k] = min(l[i-k], j-k);
    }
    return *max_element(l, l + n);
}
```

Cyclic Rotation (Lyndon)

```
// simple strings = smaller than its nontrivial
// suffixes
// lyndon factorization = simple strings
// factorized
// "abaaba" -> "ab", "aab", "a"
vector<string> duval(string s) {
    int n = s.length();
    vector<string> lyndon;
    for (int i = 0; i < n; i) {
        int j = i+1, k = i;
        for (; j < n && s[j] <= s[i]; j++)
            if (s[j] < s[i]) k = j;
        else k++;
        for (; i <= k; i += j - k)
            lyndon.push_back(s.substr(i, j-k));
    }
    return lyndon;
}
// lexicographically smallest rotation
int minRotation(string s) {
    int n = s.length(); s += s;
    auto d = duval(s); int i = 0, a = 0;
    while (a + d[i].length() < n) a +=
        d[i++].length();
    while (i && d[i] == d[i-1]) a -=
        d[i--].length();
    return a;
}
```

Hashing

```
#define HASHER 27
ull basicHash(string s) {
    ull v = 0;
```

```
    for (auto c : s) v = (c - 'a' + 1) + v *
        HASHER;
    return v;
}
const int MAXN = 1000001;
ull base[MAXN] = {1};
void genBase(int n) {
    for (int i = 1; i <= n; i++)
        base[i] = base[i-1] * HASHER;
}
struct advHash {
    ull v, l; vector<ull> wip;
    advHash(string& s): v(0) {
        wip = vector<ull>(s.length()+1);
        wip[0] = 0;
        for (int i = 0; i < s.length(); i++)
            wip[i+1] = (s[i] - 'a' + 1) + wip[i] *
                HASHER;
        l = s.length(); v = wip[l];
    }
    ull del(int pos, int len) {
        return v - wip[pos+len]*base[l-pos-len] +
            wip[pos]*base[l-pos-len];
    }
    ull substr(int pos, int len) {
        return del(pos+len, (l-pos-len)) -
            wip[pos]*base[len];
    }
    ull replace(int pos, char c) {
        return v - wip[pos+1]*base[l-pos-1] + ((c -
            'a' + 1) + wip[pos] *
            HASHER)*base[l-pos-1];
    }
    ull replace(int pos, string s) {
        // can't increase total string size
        ull r = v -
            wip[pos+s.size()*base[l-pos-s.size()]] *
            wip[pos];
        for (int i = 0; i < s.size(); i++)
            c = (s[i] - 'a' + 1) + c * HASHER;
        return r + c * base[l-pos-s.size()];
    }
};
```

Subsequence Count

```
// "banana", "ban" >> 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
    int m = subs.length(), n = body.length();
    if (m > n) return 0;
    ull* arr = new ull*[m+1];
    for (int i = 0; i <= m; i++) arr[i] = new
        ull[n+1];
    for (int i = 1; i <= m; i++) arr[i][0] = 0;
    for (int i = 0; i <= n; i++) arr[0][i] = 1;
    for (int i = 1; i <= m; i++)
        for (int j = 1; j <= n; j++)
            arr[i][j] = arr[i][j-1] + ((body[j-1] ==
                subs[i-1])? arr[i-1][j-1] : 0);
    return arr[m][n];
}
```

Suffix Array + LCP

```
struct SuffixArray {
    vector<int> sa, lcp;
    SuffixArray(string& s, int lim=256) {
        int n = s.length() + 1, k = 0, a, b;
        vector<int> x(begin(s), end(s)+1), y(n),
            ws(max(n, lim)), rank(n);
        sa = lcp = y;
        iota(begin(sa), end(sa), 0);
        for (int j = 0, p = 0; p < n; j = max(1, j *
            2), lim = p) {
            p = j; iota(begin(y), end(y), n - j);
            for (int i = 0; i < (n); i++)
                if (sa[i] >= j)
                    y[p++] = sa[i] - j;
            fill(begin(ws), end(ws), 0);
            for (int i = 0; i < (n); i++) ws[x[i]]++;
```

```
            for (int i = 1; i < (lim); i++) ws[i] +=
                ws[i-1];
            for (int i = n; i--;) sa[--ws[x[y[i]]]] =
                y[i];
            swap(x, y); p = 1; x[sa[0]] = 0;
            for (int i = 1; i < (n); i++) {
                a = sa[i-1]; b = sa[i];
                x[b] = (y[a] == y[b] && y[a + j] == y[b +
                    j]) ? p - 1 : p++;
            }
            for (int i = 1; i < (n); i++) rank[sa[i]] =
                i;
            for (int i = 0, j; i < n - 1; lcp[rank[i++]]
                = k)
                for (k && k--, j = sa[rank[i] - 1];
                    s[i + k] == s[j + k]; k++);
        }
        // smallest cyclic shift
        int cyclic() { return sa[0]; }
        // longest repeated substring
        pair<int, int> lrs() {
            int length = -1, index = -1;
            for (int i = 0; i < lcp.size(); i++) {
                if (lcp[i] > length) {
                    length = lcp[i];
                    index = sa[i];
                }
            }
            return {index, length};
        }
        // count distinct substrings, excluding empty
        int distincts() {
            int n = sa.size() - 1, r = n - sa[0];
            for (int i = 1; i < lcp.size(); i++)
                r += (n - sa[i]) - lcp[i-1];
            return r;
        }
        // count repeated substrings, excluding empty
        int repeateds() {
            int r = 0;
            for (int i = 1; i < lcp.size(); i++)
                r += max(lcp[i] - lcp[i-1], 0);
            return r;
        }
};
```

Suffix Tree (Ukkonen's)

```
struct SuffixTree {
    // n = 2*len+10 or so
    enum { N = 50010, ALPHA = 26 };
    int toi(char c) { return c - 'a'; }
    int
        t[N][ALPHA], l[N], r[N], p[N], s[N], v=0, q=0, m=2;
    string a;
    void ukkadd(int i, int c) { suff:
        if (r[v]<q) {
            if (t[v][c]==-1) { t[v][c]=m; l[m]=i;
                p[m]=p[v]; t[m][c]=m+1; t[m][toi(a[q])] = v;
                l[v]=q; p[v]=m; t[p[m]][toi(a[l[m]])]=m;
                v=s[p[m]]; q=l[m];
                while (q<r[m]) { v=t[v][toi(a[q])];
                    q=r[r[m]]; }
                if (q==r[m]) s[m]=v; else s[m]=m+2;
                q=r[v]-q-r[m]; m+=2; goto suff;
            }
        }
        SuffixTree(string a) : a(a) {
            fill(r, r+N, (int)(a.size()));
            memset(s, 0, sizeof s);
            memset(t, -1, sizeof t);
            fill(t[1], t[1]+ALPHA, 0);
            s[0]=1; l[0]=l[1]=-1; r[0]=r[1]=p[0]=p[1]=0;
            for (int i=0; i<a.size(); i++)
                ukkadd(i, toi(a[i]));
```

```
        }
        // Longest Common Substring between 2 strings
        // returns {length, offset from first string}
        pair<int, int> best;
        int lcs(int node, int i1, int i2, int olen) {
            if (l[node] <= i1 && i1 < r[node]) return 1;
            if (l[node] <= i2 && i2 < r[node]) return 2;
            int mask=0;
            len=node?olen+(r[node]-l[node]):0;
            for (int c=0; c<ALPHA; c++) if
                (t[node][c]!=-1)
                    mask |= lcs(t[node][c], i1, i2, len);
            if (mask==3)
                best=max(best, {len, r[node]-len});
            return mask;
        }
        static pair<int, int> LCS(string s, string t)
        {
            SuffixTree
                st(s+(char)('z'+1)+t+(char)('z'+2));
            st.lcs(0, s.size(), s.size()+t.size()+1, 0);
            return st.best;
        }
};
```

String Utilities

```
void lowercase(string& s) {
    transform(s.begin(), s.end(), s.begin(),
        ::tolower);
}
void uppercase(string& s) {
    transform(s.begin(), s.end(), s.begin(),
        ::toupper);
}
void trim(string &s) {
    s.erase(s.begin(), find_if_not(s.begin(), s]
        .end(), [](int c){return
            isspace(c);}));
    s.erase(find_if_not(s.rbegin(), s.rend(), [](int
        c){return isspace(c);}).base(), s.end());
}
vector<string> split(string& s, char token) {
    vector<string> v; stringstream ss(s);
    for (string e; getline(ss, e, token);)
        v.push_back(e);
    return v;
}
```

5 Greedy

Interval Cover

```
// L, R = interval [L, R], in = {{l, r}, index}
// does not handle case where L == R
vector<int> intervalCover(double L, double R,
    vector<pair<pair<double, double>, int>> in) {
    int i = 0; pair<double, int> pos = {L, -1};
    vector<int> a;
    sort(begin(in), end(in));
    while (pos.first < R) {
        double cur = pos.first;
        while (i < (int)in.size() &&
            in[i].first.first <= cur)
            pos =
                max(pos, {in[i].first.second, in[i].second});
        i++;
        if (pos.first == cur) return {};
        a.push_back(pos.second);
    }
    return a;
}
```

6 Math

Catalan Numbers

```
ull* catalan = new ull[1000000];
void genCatalan(int n, int mod) {
    catalan[0] = catalan[1] = 1;
    for (int i = 2; i <= n; i++) {
        catalan[i] = 0;
        for (int j = i - 1; j >= 0; j--) {
```



```

.. catalan[i] += (catalan[j] * catalan[i-j-1])
↪ % mod;
.. if (catalan[i] >= mod)
.. catalan[i] -= mod;
.. }
}
// TODO: consider binomial coefficient method

```

Combinatorics (nCr, nPr)

```

// can optimize by precomputing factorials, and
↪ fact[n]/fact[n-r]
ull nPr(ull n, ull r) {
    ull v = 1;
    for (ull i = n-r+1; i <= n; i++)
        v *= i;
    return v;
}
ull nPr(ull n, ull r, ull m) {
    ull v = 1;
    for (ull i = n-r+1; i <= n; i++)
        v = (v * i) % m;
    return v;
}
ull nCr(ull n, ull r) {
    long double v = 1;
    for (ull i = 1; i <= r; i++)
        v = v * (n-r+i) / i;
    return (ull)(v + 0.001);
}
// requires modulo math
// can optimize by precomputing mfac and
↪ minv-mfac
ull nCr(ull n, ull r, ull m) {
    return mfac(n, m) * minv(mfac(k, m), m) % m *
    ↪ minv(mfac(n-k, m), m) % m;
}

```

Multinomials

```

ll multinomial(vector<int>& v) {
    ll c = 1, m = v.empty() ? 1 : v[0];
    for(int i = 1; i < v.size(); i++)
        for (int j = 0; j < v[i]; j++)
            c = c * ++m / (j+1);
    return c;
}

```

Chinese Remainder Theorem

```

bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
{
    ll x, y, d; mo = m[0]; re = r[0];
    for (int i = 1; i < n; i++) {
        d = egcd(mo, m[i], x, y);
        if ((r[i] - re) % d != 0) return false;
        x = (r[i] - re) / d * x % (m[i] / d);
        re += x * mo;
        mo = mo / d * m[i];
        re %= mo;
    }
    re = (re + mo) % mo;
    return true;
}

```

Count Digit Occurences

```

/*count(n,d) counts the number of occurences of
↪ a digit d in the range [0,n]*/
ll digit_count(ll n, ll d) {
    ll result = 0;
    while (n != 0) {
        result += ((n%10) == d ? 1 : 0);
        n /= 10;
    }
    return result;
}
ll count(ll n, ll d) {
    if (n < 10) return (d > 0 && n >= d);
    if ((n % 10) != 9) return digit_count(n, d) +
    ↪ count(n-1, d);
    return 10*count(n/10, d) + (n/10) + (d > 0);
}

```

Discrete Logarithm

```

int discretelog(int a, int b, int m) {
    ll n = sqrt(m) + 1, an = 1;
    for (ll i = 0; i < n; ++i)
        an = (an * a) % m;
    unordered_map<ll, ll> vals;
    for (ll q = 0, cur = b; q <= n; q++) {
        vals[cur] = q;
        cur = (cur * a) % m;
    }
    for (ll p = 1, cur = 1; p <= n; p++) {
        cur = (cur * an) % m;
        if (vals.count(cur)) {
            int ans = n * p - vals[cur];
            return ans;
        }
    }
    return -1;
}

```

Euler Phi / Totient

```

int phi(int n) {
    int r = n;
    for (int i = 2; i * i <= n; i++) {
        if (n % i == 0) r = r / i;
        while (n % i == 0) n /= i;
    }
    if (n > 1) r = r / n;
    return r;
}
#define n 100000
ll phi[n+1];
void computeTotient() {
    for (int i=1; i<=n; i++) phi[i] = i;
    for (int p=2; p<=n; p++) {
        if (phi[p] == p) {
            phi[p] = p-1;
            for (int i = 2*p; i<=n; i += p) phi[i] =
            ↪ (phi[i/p] * (p-1));
        }
    }
}

```

Factorials

```

// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
↪ M_E)) + (log10(2 * M_PI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
↪ M_PI * n) * pow(n / M_E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))

```

Prime Factorization

```

// do not call directly
ll pollard_rho(ll n, ll s) {
    ll x, y;
    x = y = rand() % (n - 1) + 1;
    int head = 1, tail = 2;
    while (true) {
        x = mult(x, x, n);
        x = (x + s) % n;
        if (x == y) return n;
        ll d = __gcd(max(x - y, y - x), n);
        if (1 < d && d < n) return d;
        if (++head == tail) y = x, tail <= 1;
    }
    // call for prime factors
void factorize(ll n, vector<ll> &divisor) {
    if (n == 1) return;
    if (isPrime(n)) divisor.push_back(n);
    else {
        ll d = n;
        while (d >= n) d = pollard_rho(n, rand() % (n
        ↪ - 1) + 1);
        factorize(n / d, divisor);
        factorize(d, divisor);
    }
}

```

Farey Fractions

```

// generate 0 <= a/b <= 1 ordered, b <= n
// farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
    int h = 0, k = 1, x = 1, y = 0, r;
    vector<pair<int, int>> v;
    do {
        v.push_back({h, k});
        r = (n-y)/k;
        y += r*k; x += r*h;
        swap(x,h); swap(y,k);
        x = -x; y = -y;
        while (k > 1)
            v.push_back({1, 1});
        return v;
    }
}

```

Fast Fourier Transform

```

#define cd complex<double>
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert) {
    int n = a.size();
    for (int i = 1, j = 0; i < n; i++) {
        int bit = n >> 1;
        for (; j < bit; bit >>= 1) j ^= bit;
        if (i < j) swap(a[i], a[j]);
    }
    for (int len = 2; len <= n; len <= 1) {
        double ang = 2 * PI / len * (invert ? -1 :
        ↪ 1);
        cd wlen(cos(ang), sin(ang));
        for (int i = 0; i < n; i += len) {
            cd w(1);
            for (int j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
        if (invert)
            for (auto& x : a)
                x /= n;
    }
    vector<int> fftmult(vector<int> const& a,
    ↪ vector<int> const& b) {
        vector<cd> fa(a.begin(), a.end()),
        ↪ fb(b.begin(), b.end());
        int n = 1 << (32 - __builtin_clz(a.size() +
        ↪ b.size() - 1));
        fa.resize(n); fb.resize(n);
        fft(fa, false); fft(fb, false);
        for (int i = 0; i < n; i++) fa[i] *= fb[i];
        fft(fa, true);
        vector<int> toret(n);
        for (int i = 0; i < n; i++) toret[i] =
        ↪ round(fa[i].real());
        return toret;
    }
}

```

Greatest Common Denominator

```

ll egcd(ll a, ll b, ll& x, ll& y) {
    if (b == 0) { x = 1; y = 0; return a; }
    ll gcd = egcd(b, a % b, x, y);
    x -= a / b * y;
    swap(x, y);
    return gcd;
}

```

Josephus Problem

```

// 0-indexed, arbitrary k
int josephus(int n, int k) {
    if (n == 1) return 0;
    if (k == 1) return n-1;
    if (k > n) return (josephus(n-1,k)+k)%n;
    int res = josephus(n-n/k,k)-n%k;
    return res + ((res<0)?n:res/(k-1));
}

```

```

// fast case if k=2, traditional josephus
int josephus(int n) {
    return 2*(n-(1<<(32-__builtin_clz(n)-1)));
}

```

Least Common Multiple

```

#define lcm(a,b) ((a*b)/__gcd(a,b))

```

Modulo Operations

```

#define MOD 1000000007
#define madd(a,b,m) (a+b-((a+b-m)>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msb(a,b,m) (a-b+((a-b)>=0)?m:0))
ll mpow(ll b, ll e, ll m) {
    ll x = 1;
    while (e > 0) {
        if (e % 2) x = (x * b) % m;
        b = (b * b) % m;
        e /= 2;
    }
    return x % m;
}
ull mfac(ull n, ull m) {
    ull f = 1;
    for (int i = n; i > 1; i--)
        f = (f * i) % m;
    return f;
}
// if m is not guaranteed to be prime
ll minv(ll b, ll m) {
    ll x = 0, y = 0;
    if (egcd(b, m, x, y) != 1) return -1;
    return (x % m + m) % m;
}
ll mdiv_compmod(int a, int b, int m) {
    if (__gcd(b, m) != 1) return -1;
    return mult(a, minv(b, m), m);
}
// if m is prime (like 10^9+7)
ll mdiv_primemod (int a, int b, int m) {
    return mult(a, mpow(b, m-2, m), m);
}
// tonelli shanks = sqrt(n) % m, m is prime
ll legendre(ll a, ll m){
    if (a % m==0) return 0;
    if (m == 2) return 1;
    return mpow(a, (m-1)/2, m);
}
ll msqrt(ll n, ll m) {
    ll s = __builtin_ctzll(m-1), q = (m-1ll)>>s,
    ↪ z = rand()%(m-1)+1;
    if (m == 2) return 1;
    if (s == 1) return mpow(n, (m+1)/4, m);
    while (legendre(z,m)!=m-1) z = rand()%(m-1)+1;
    ll c = mpow(z,q,m), r = mpow(n, (q+1)/2, m), t
    ↪ = mpow(n,q,m), M = s;
    while (t != 1) {
        ll i=1, ts = (t * t) % m;
        while (ts != 1) i++, ts = (ts * ts) % m;
        ll b = c;
        for (int j = 0; j < M-i-1; j++) b = (b * b) %
        ↪ m;
        r = r * b % m; c = b * b % m; t = t * c % m;
        M = i;
    }
    return r;
}
}

```

Modulo Tetration

```

ll tetraloop(ll a, ll b, ll m) {
    if (b == 0 || a == 1) return 1;
    ll w = tetraloop(a,b-1,phi(m)), r = 1;
    for (;w;/=2) {
        if (w&1) {
            r *= a; if (r >= m) r -= (r/m-1)*m;
        }
        a *= a; if (a >= m) a -= (a/m-1)*m;
    }
    return r;
}
int tetration(int a, int b, int m) {

```

```

    if (a == 0 || m == 1) return ((b+1)&1)%m;
    return tetraloop(a,b,m) % m;
}

```

Matrix

```

template<typename T>
struct Mat : public Vec<2, T> {
    int w, h;
    Mat(int x, int y) : Vec<2, T>(x, y), w(x),
        h(y) {}
    static Mat<T> identity(int n) { Mat<T> m(n,n);
        for (int i=0;i<n;i++) m[i][i] = 1; return
        m; }
    Mat<T>& operator+=(const Mat<T>& m) {
        for (int i = 0; i < w; i++)
            for (int j = 0; j < h; j++)
                (*this)[i][j] += m[i][j];
        return *this;
    }
    Mat<T>& operator-=(const Mat<T>& m) {
        for (int i = 0; i < w; i++)
            for (int j = 0; j < h; j++)
                (*this)[i][j] -= m[i][j];
        return *this;
    }
    Mat<T> operator*(const Mat<T>& m) {
        Mat<T> z(w,m.h);
        for (int i = 0; i < w; i++)
            for (int j = 0; j < h; j++)
                for (int k = 0; k < m.h; k++)
                    z[i][k] += (*this)[i][j] * m[j][k];
        return z;
    }
    Mat<T> operator+(const Mat<T>& m) { Mat<T>
        a=*this; return a+m; }
    Mat<T> operator-(const Mat<T>& m) { Mat<T>
        a=*this; return a-m; }
    Mat<T>& operator*=(const Mat<T>& m) { return
        *this = (*this)*m; }
    Mat<T> power(int n) {
        Mat<T> a = Mat<T>::identity(w),m=*this;
        for (;n;n/=2,m*=m) if (n&1) a *= m;
        return a;
    }
};

```

Matrix Exponentiation

```

// F(n) = c[0]*F(n-1) + c[1]*F(n-2) + ...
// b is the base cases of same length c
ll matrix_exponentiation(ll n, vector<ll> c,
    vector<ll> b) {
    if (nth < b.size()) return b[nth-1];
    Mat<ll> a(c.size(), c.size()); ll s = 0.
    for (int i = 0; i < c.size(); i++) a[i][0] =
        c[i];
    for (int i = 0; i < c.size() - 1; i++)
        for (int i = 0; i < c.size() - 1; i++)
            a[i][i+1] = 1;
    a = a.power(nth - c.size());
    for (int i = 0; i < c.size(); i++)
        s += a[i][0] * b[i];
    return s;
}

```

Matrix Subarray Sums

```

template<class T> struct MatrixSum {
    Vec<2, T> p;
    MatrixSum(Vec<2, T>& v) {
        p = Vec<2,T>(v.size()+1, v[0].size()+1);
        for (int i = 0; i < v.size(); i++)
            for (int j = 0; j < v[0].size(); j++)
                p[i+1][j+1] = v[i][j] + p[i][j+1] +
                p[i+1][j] - p[i][j];
    }
    T sum(int u, int l, int d, int r) {
        return p[d][r] - p[d][l] - p[u][r] + p[u][l];
    }
};

```

Mobius Function

```

const int MAXN = 10000000;
// mu[n] = 0 iff n has no square factors

```

```

// 1 = even number prime factors, -1 = odd
short mu[MAXN] = {0,1};
void mobius() {
    for (int i = 1; i < MAXN; i++)
        if (mu[i])
            for (int j = i + i; j < MAXN; j += i)
                mu[j] -= mu[i];
}

```

Nimber Arithmetic

```

#define nimAdd(a,b) ((a)^(b))
ull nimMul(ull a, ull b, int i=6) {
    static const ull M[]={INT_MIN>>32,
        M[0]^M[0]<<16), M[1]^M[1]<<8),
        M[2]^M[2]<<4), M[3]^M[3]<<2),
        M[4]^M[4]<<1)};
    if (i-- == 0) return a&b;
    int k=1<<i;
    ull s=nimMul(a,b,i), m=M[5-i],
        t=nimMul(((a^(a>>k))&m)|(s&m),
        ((b^(b>>k))&m)|(m&(~m>>1))<<k, i);
    return ((s^t)&m)<<k|((s^(t>>k))&m);
}

```

Permutation

```

// c = array size, n = nth perm, return index
vector<int> gen_permutation(int c, int n) {
    vector<int> idx(c), per(c), fac(c); int i;
    for (i = 0; i < c; i++) idx[i] = i;
    for (i = 1; i <= c; i++) fac[i-1] = n/i, n/=i;
    for (i = c - 1; i >= 0; i--)
        per[c-i-1] = idx[fac[i]],
        idx.erase(idx.begin() + fac[i]);
    return per;
}
// get what nth permutation of vector
int get_permutation(vector<int>& v) {
    int use = 0, i = 1, r = 0;
    for (int e : v) {
        r = r * i++ + __builtin_popcount(use &
            ~(1<<e));
        use |= 1<< e;
    }
    return r;
}

```

Permutation (string/multiset)

```

string freq2str(vector<int>& v) {
    string s;
    for (int i = 0; i < v.size(); i++)
        for (int j = 0; j < v[i]; j++)
            s += (char)(i + 'A');
    return s;
}
// nth perm of multiset, n is 0-indexed
string gen_permutation(string s, ll n) {
    vector<int> freq(26, 0);
    for (auto e : s) freq[e - 'A']++;
    for (int i = 0; i < 26; i++) if (freq[i] > 0)
        {
            freq[i]--; ll v = multinomial(freq);
            if (n < v) return (char)(i+'A') +
                gen_permutation(freq2str(freq), n);
            freq[i]++; n -= v;
        }
    return "";
}

```

Miller-Rabin Primality Test

```

// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
    if (n < 2) return false;
    if (n == 2) return true;
    if (n % 2 == 0) return false;
    ull s = n - 1;
    while (s % 2 == 0) s /= 2;
    for (int i = 0; i < 10; i++) {
        ull temp = s;
        ull a = rand() % (n - 1) + 1;
        ull mod = mpow(a, temp, n);
        while (temp!=n-1&&mod!=1&&mod!=n-1) {

```

```

        mod = mult(mod, mod, n);
        temp *= 2;
        if (mod!=n-1&&temp%2==0) return false;
    }
    return true;
}

```

Sieve of Eratosthenes

```

bitset<100000001> sieve;
// generate sieve - O(n log n)
void genSieve(int n) {
    sieve[0] = sieve[1] = 1;
    for (ull i = 3; i * i < n; i += 2)
        if (!sieve[i])
            for (ull j = i * 3; j <= n; j += i * 2)
                sieve[j] = 1;
}
// query sieve after it's generated - O(1)
bool querySieve(int n) {
    return n == 2 || (n % 2 != 0 && !sieve[n]);
}

```

Compile-time Prime Sieve

```

const int MAXN = 100000;
template<int N>
struct Sieve {
    bool sieve[N];
    constexpr Sieve() : sieve() {
        sieve[0] = sieve[1] = 1;
        for (int i = 2; i * i < N; i++)
            if (!sieve[i])
                for (int j = i * 2; j < N; j += i)
                    sieve[j] = 1;
    }
};
bool isPrime(int n) {
    static constexpr Sieve<MAXN> s;
    return !s.sieve[n];
}

```

Simpson's / Approximate Integrals

```

// integrate f from a to b, k iterations
// error <= (b-a)/18.0 * M * ((b-a)/2k)^4
// where M = max(abs(f^(k-1)(x))) for x in [a,b]
// "f" is a function "double func(double x)"
double Simpsons(double a, double b, int k,
    double (*f)(double)) {
    double dx = (b-a)/(2.0*k), t = 0;
    for (int i = 0; i < k; i++)
        t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
        (*f)(a+(2*i+1)*dx);
    return (t + (*f)(b)) * (b-a) / 6.0 / k;
}

```

Common Equations Solvers

```

// ax^2 + bx + c = 0, find x
vector<double> solveEq(double a, double b,
    double c) {
    vector<double> r;
    double z = b * b - 4 * a * c;
    if (z == 0)
        r.push_back(-b/(2*a));
    else if (z > 0) {
        r.push_back((sqrt(z)-b)/(2*a));
        r.push_back((sqrt(z)+b)/(2*a));
    }
    return r;
}

```

```

// ax^3 + bx^2 + cx + d = 0, find x
vector<double> solveEq(double a, double b,
    double c, double d) {
    vector<double> res;
    long double a1 = b/a, a2 = c/a, a3 = d/a;
    long double q = (a1*a1 - 3*a2)/9.0, sq =
        -2*sqrt(q);
    long double r = (2*a1*a1*a1 - 9*a1*a2 +
        27*a3)/54.0;
    long double z = r*r-r*q*q, theta;
    if (z <= 0) {
        theta = acos(r/sqrt(q*q*q));

```

```

        res.push_back(sq*cos(theta/3.0) - a1/3.0);
        res.push_back(sq*cos((theta+2.0*PI)/3.0) -
            a1/3.0);
        res.push_back(sq*cos((theta+4.0*PI)/3.0) -
            a1/3.0);
    }
    else {
        res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
        res[0] = (res[0] + q / res[0]) *
            ((r<0)?1:-1) - a1 / 3.0;
    }
    return res;
}
// linear diophantine equation ax + by = c,
// find x and y
// infinite solutions of form x=k*b/g, y-k*a/g
bool solveEq(ll a, ll b, ll c, ll &x, ll &y, ll
    &g) {
    g = egcd(abs(a), abs(b), x, y);
    if (c % g) return false;
    x *= c / g * ((a < 0) ? -1 : 1);
    y *= c / g * ((b < 0) ? -1 : 1);
    return true;
}
// m = # equations, n = # variables, a[m][n+1]
// = coefficient matrix
// a[i][0]x + a[i][1]y + ... + a[i][n]z =
// a[i][n+1]
// find a solution of some kind to linear
// equation
const double eps = 1e-7;
bool zero(double a) { return (a < eps) && (a >
    -eps); }
vector<double> solveEq(double **a, int m, int
    n) {
    int cur = 0;
    for (int i = 0; i < n; i++) {
        for (int j = cur; j < m; j++) {
            if (!zero(a[j][i])) {
                if (j != cur) swap(a[j], a[cur]);
                for (int sat = 0; sat < m; sat++) {
                    if (sat == cur) continue;
                    double num = a[sat][i] / a[cur][i];
                    for (int sot = 0; sot <= n; sot++)
                        a[sat][sot] -= a[cur][sot] * num;
                }
                cur++;
                break;
            }
        }
        for (int j = cur; j < m; j++)
            if (!zero(a[j][n])) return vector<double>();
        vector<double> ans(n,0);
        for (int i = 0, sat = 0; i < n; i++)
            if (sat < m && !zero(a[sat][i]))
                ans[i] = a[sat][n] / a[sat++][i];
        return ans;
    }
    // solve A[n][n] * x[n] = b[n] linear equation
    // rank < n is multiple solutions, -1 is no
    // solutions
    // alls is whether to find all solutions, or
    // any
    const double eps = 1e-12;
    int solveEq(Vec<2, double>& A, Vec<1, double>&
        b, Vec<1, double>& x, bool alls=false) {
        int n = A.size(), m = x.size(), rank = 0, br,
            bc;
        vector<int> col(m); iota(begin(col), end(col),
            0);
        for(int i = 0; i < n; i++) {
            double v, bv = 0;
            for(int r = i; r < n; r++)
                for(int c = i; c < n; c++)
                    if ((v = fabs(A[r][c])) > bv)
                        br = r, bc = c, bv = v;
            if (bv <= eps) {
                for(int j = i; j < n; j++)

```

```

    if (fabs(b[j]) > eps)
        return -1;
    break;
}
swap(A[i], A[br]);
swap(b[i], b[br]);
swap(col[i], col[bc]);
for(int j = 0; j < n; j++)
    swap(A[j][i], A[j][bc]);
bv = 1.0 / A[i][i];
for(int j = (alls)?0:i+1; j < n; j++) {
    if (j != i) {
        double fac = A[j][i] * bv;
        b[j] -= fac * b[i];
        for(int k = i+1; k < m; k++)
            A[j][k] -= fac*A[i][k];
    }
}
rank++;
if (alls) for (int i = 0; i < m; i++) x[i] =
    -DBL_MAX;
for (int i = rank; i--;) {
    bool isGood = true;
    if (alls)
        for (int j = rank; isGood && j < m; j++)
            if (fabs(A[i][j]) > eps)
                isGood = false;
    b[i] /= A[i][i];
    if (!isGood) x[col[i]] = b[i];
    if (!alls)
        for(int j = 0; j < i; j++)
            b[j] -= A[j][i] * b[i];
}
return rank;
}

```

Graycode Conversions

```

ull graycode2ull(ull n) {
    ull i = 0;
    for (; n; n = n >> 1) i ^= n;
    return i;
}
ull ull2graycode(ull n) {
    return n ^ (n >> 1);
}

```

Date Utilities

```

// handles -4799-01-01 to 1465001-12-31
int date2int(int y, int m, int d){
    return 1461*(y+4800+(m-14)/12)/4+367*(m-2-(m-
        -14)/12*12)/12-3*((y+4900+(m-14)/12)/100)
    }
    } /4+d-32075;
}
pair<int,pair<int,int>> int2date(int x){
    int n,i,j;
    x+=68569;
    n=4*x/146097;
    x=(146097*n+3)/4;
    i=(4000*(x+1))/1461001;
    x=1461*i/4-31;
    j=80*x/2447;
    return {100*(n-49)+i+j/11, {j+2-12*(j/11),
    }
    } x-2447*j/80}};
}
int dayOfWeek(int y, int m, int d){ //0=sunday
    static int cal[]={0,3,2,5,0,3,5,1,4,6,2,4};
    y-=m<3;
    return (y+y/4-y/100+y/400+cal[m-1]+d)%7;
}

```

Unix/Epoch Time

```

// 0-indexed month/time, 1-indexed day
// minimum 1970, 0, 1, 0, 0, 0
ull toEpoch(int year, int month, int day, int
    }
    } hour, int minute, int second) {
    struct tm t; time_t epoch;
    t.tm_year = year - 1900; t.tm_mon = month;
    t.tm_mday = day; t.tm_hour = hour;
    t.tm_min = minute; t.tm_sec = second;
}

```

```

t.tm_isdst = 0; // 1 = daylights savings
epoch = mktime(&t);
return (ull)epoch;
}
vector<int> toDate(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return {t.tm_year+1900,t.tm_mon,t.tm_mday,t
    }
    } .tm_hour,t.tm_min,t.tm_sec};
}
int getWeekday(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return t.tm_wday; // 0-6, 0 = sunday
}
int getDayOfYear(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return t.tm_yday; // 0-365
}
const int months[] =
    }
    } {31,28,31,30,31,30,31,31,30,31,30,31};
bool validDate(int year, int month, int day) {
    bool leap = !(year%(year%2574:16));
    if (month >= 12) return false;
    return day <= months[month] + (leap &&
    }
    } month == 1);
}

```

Theorems and Formulae

Montmort Numbers count the number of derangements (permutations where no element appears in its original position) of a set of size n . $!0 = 1$, $!1 = 0$, $!n = (n+1)!(n-1) + !(n-2)$, $!n = n! \sum_{i=0}^n \frac{(-1)^i}{i!}$, $!n = \left[\frac{n!}{e} \right]$

In a partially ordered set, a chain is a subset of elements that are all comparable to each other. An antichain is a subset where no two are comparable.

Dilworth's theorem states the size of a maximal antichain equals the size of a minimal chain cover of a partially ordered set S . The width of S is the maximum size of an antichain in S , which is equal to the minimum number of chains needed to cover S , or the minimum number of chains such that all elements are in at least one chain.

Rosser's Theorem states the n th prime number is greater than $n * \ln(n)$ for $n > 1$.

Nicomachi's Theorem states $1^3 + 2^3 + \dots + n^3 = (1 + 2 + \dots + n)^2$ and is equivalent to $(\frac{n^2+1}{2})^2$.

Lagrange's Four Square Theorem states every natural number is the sum of the squares of four non-negative integers. This is a special case of the Fermat Polygonal Number Theorem where every positive integer is a sum of at most n s -gonal numbers. The n th

s -gonal number $P(s, n) = (s-2) \frac{n(n-1)}{2} + n$

7 Graphs

```

struct edge {
    int u,v,w;
    edge(int u,int v,int w) : u(u),v(v),w(w) {}
    edge() : u(0), v(0), w(0) {}
};

```

```

bool operator < (const edge &e1, const edge
    }
    } &e2) { return e1.w < e2.w; }
bool operator > (const edge &e1, const edge
    }
    } &e2) { return e1.w > e2.w; }
struct subset { int p, rank; };

```

Eulerian Path

```

#define edge_list vector<edge>
#define adj_sets vector<set<int>>
struct EulerPathGraph {
    adj_sets graph; // actually indexes incident
    }
    } edges
    edge_list edges; int n; vector<int> indeg;
    EulerPathGraph(int n): n(n) {
        indeg = *(new vector<int>(n,0));
        graph = *(new adj_sets(n, set<int>()));
    }
    void add_edge(int u, int v) {
        graph[u].insert(edges.size());
        indeg[v]++;
        edges.push_back(edge(u,v,0));
    }
    bool eulerian_path(vector<int> &circuit) {
        if(edges.size()==0) return false;
        stack<int> st;
        int a[] = {-1, -1};
        for(int v=0;v<n;v++) {
            if(indeg[v]!=graph[v].size()) {
                bool b = indeg[v] > graph[v].size();
                if (abs((((int)indeg[v])-((int)graph[v]
                }
                } .size())) > 1) return
                }
                } false;
                if (a[b] != -1) return false;
                a[b] = v;
            }
        }
        int s = (a[0]!=-1 && a[1]!=-1 ? a[0] :
        }
        } (a[0]==-1 && a[1]==-1 ? edges[0].u : -1));
        if(s==-1) return false;
        while(!st.empty() || !graph[s].empty()) {
            if (graph[s].empty()) {
                circuit.push_back(s); s = st.top();
                st.pop();
            }
            else {
                int w = edges[*graph[s].begin()].v;
                graph[s].erase(graph[s].begin());
                st.push(s); s = w;
            }
        }
        circuit.push_back(s);
        return circuit.size()-1==edges.size();
    }
}

```

Floyd Warshall

```

const ll inf = 1LL << 62;
#define FOR(i,n) for (int i = 0; i < n; i++)
void floydWarshall(Vec<2, ll>&m) {
    int n = m.size();
    FOR(i,n) m[i][i] = min(m[i][i], 0LL);
    FOR(k,n) FOR(i,n) FOR(j,n) if (m[i][k] != inf
    }
    } && m[k][j] != inf) {
        auto newDist = max(m[i][k] + m[k][j], -inf);
        m[i][j] = min(m[i][j], newDist);
    }
    FOR(k,n) if (m[k][k] < 0) FOR(i,n) FOR(j,n)
    }
    } if (m[i][k] != inf && m[k][j] != inf)
        m[i][j] = -inf;
}

```

Minimum Spanning Tree

```

// returns vector of edges in the mst
// graph[i] = vector of edges incident to
// vertex i
// places total weight of the mst in &total
// if returned vector has size != n-1, there is
    }
    } no MST
vector<edge> mst(vector<vector<edge>> graph,
    }
    } ll &total) {

```

```

total = 0;
priority_queue<edge, vector<edge>,
    }
    } greater<edge>> pq;
vector<edge> MST;
bitset<20001> marked; // change size as needed
marked[0] = 1;
for (edge ep : graph[0]) pq.push(ep);
while (MST.size()!=graph.size()-1 &&
    }
    } pq.size()!=0) {
    edge e = pq.top(); pq.pop();
    int u = e.u, v = e.v, w = e.w;
    if(marked[u] && marked[v]) continue;
    else if(marked[u]) swap(u, v);
    for(edge ep : graph[u]) pq.push(ep);
    marked[u] = 1;
    MST.push_back(e);
    total += e.w;
}
return MST;
}

```

Union Find

```

int uf_find(subset* s, int i) {
    if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
    return s[i].p;
}
void uf_union(subset* s, int x, int y) {
    int xp = uf_find(s, x), yp = uf_find(s, y);
    if (s[xp].rank > s[yp].rank) s[yp].p = xp;
    else if (s[xp].rank < s[yp].rank) s[xp].p =
    }
    } yp;
    else { s[yp].p = xp; s[xp].rank++; }
}

```

2D Grid Shortcut

```

#define inbound(x,n) (0<=x&&x<n)
#define ford(x,y,n,m) for(auto [dx,dy]:dir) if
    }
    } (inbound(x+dx,n)&&inbound(y+dy,m))
const pair<int,int> dir[] =
    }
    } {{1,0},{0,1},{-1,0},{0,-1}};

```

8 2D Geometry

```

#define point complex<double>
#define EPS 0.0000001
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double dot(point a, point b) { return
    }
    } real(conj(a)*b); }
double cross(point a, point b) { return
    }
    } imag(conj(a)*b); }
struct line { point a, b; };
struct circle { point c; double r; };
struct segment { point a, b; };
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
struct convex_polygon {
    vector<point> points;
    convex_polygon(vector<point> points) :
    }
    } points(points) {}
    convex_polygon(triangle a) {
        points.push_back(a.a); points.push_back(a.b);
        points.push_back(a.c);
    };
    convex_polygon(rectangle a) {
        points.push_back(a.tl);
        points.push_back({real(a.tl),
        }
        } imag(a.br)});
        points.push_back(a.br);
        points.push_back({real(a.br),
        }
        } imag(a.tl)});
    };
}
struct polygon {
    vector<point> points;
    polygon(vector<point> points) :
    }
    } points(points) {}

```



```

polygon(triangle a) {
    points.push_back(a.a); points.push_back(a.b);
    points.push_back(a.c);
}
polygon(rectangle a) {
    points.push_back(a.tl);
    points.push_back({real(a.tl),
    imag(a.br)});
    points.push_back(a.br);
    points.push_back({real(a.br),
    imag(a.tl)});
}
polygon(convex_polygon a) {
    for (point v : a.points)
        points.push_back(v);
};
// triangle methods
double area_heron(double a, double b, double
    c) {
    if (a < b) swap(a, b);
    if (a < c) swap(a, c);
    if (b < c) swap(b, c);
    if (a > b + c) return -1;
    return sqrt((a+b+c)*(c-a+b)*(c+a-b) /
    /16.0);
}
// segment methods
double lengthsq(segment a) { return
    sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
    imag(a.b)); }
double length(segment a) { return
    sqrt(lengthsq(a)); }
// circle methods
double circumference(circle a) { return 2 * a.r
    * M_PI; }
double area(circle a) { return sq(a.r) * M_PI;
    };
// rectangle methods
double width(rectangle a) { return
    abs(real(a.br) - real(a.tl)); }
double height(rectangle a) { return
    abs(imag(a.br) - real(a.tl)); }
double diagonal(rectangle a) { return
    sqrt(sq(width(a)) + sq(height(a))); }
double area(rectangle a) { return width(a) *
    height(a); }
double perimeter(rectangle a) { return 2 *
    (width(a) + height(a)); }
// check if 'a' fit's inside 'b'
// swap equalities to exclude tight fits
bool doesFitInside(rectangle a, rectangle b) {
    int x = width(a), w = width(b), y = height(a),
    h = height(b);
    if (x > y) swap(x, y);
    if (w > h) swap(w, h);
    if (w < x) return false;
    if (y <= h) return true;
    double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
    return sq(a) <= sq(b) + sq(c);
}
// polygon methods
// negative area = CCW, positive = CW
double area(polygon a) {
    double area = 0.0; int n = a.points.size();
    for (int i = 0, j = 1; i < n; i++, j = (j +
    1) % n)
        area += (real(a.points[j]-a.points[i]))*
    (imag(a.points[j]+a.points[i]));
    return area / 2.0;
}
// get both unsigned area and centroid
pair<double, point> area_centroid(polygon a) {
    int n = a.points.size();

```

```

double area = 0;
point c(0, 0);
for (int i = n - 1, j = 0; j < n; i = j++) {
    double v = cross(a.points[i], a.points[j]) /
    2;
    area += v;
    c += (a.points[i] + a.points[j]) * (v / 3);
}
c /= area;
return {area, c};
}

```

Intersection

```

// -1 coincide, 0 parallel, 1 intersection
int intersection(line a, line b, point& p) {
    if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
        p = cross(b.a - a.a, b.b - a.b) / cross(a.b
        - a.a, b.b - b.a) * (b - a) + a;
        return 1;
    }
    if (abs(cross(a.b - a.a, a.b - b.a)) > EPS)
        return 0;
    return -1;
}
// area of intersection
double intersection(circle a, circle b) {
    double d = abs(a.c - b.c);
    if (d <= b.r - a.r) return area(a);
    if (d <= a.r - b.r) return area(b);
    if (d >= a.r + b.r) return 0;
    double alpha = acos((sq(a.r) + sq(d) -
    sq(b.r)) / (2 * a.r * d));
    double beta = acos((sq(b.r) + sq(d) - sq(a.r))
    / (2 * b.r * d));
    return sq(a.r) * (alpha - 0.5 * sin(2 *
    alpha)) + sq(b.r) * (beta - 0.5 * sin(2 *
    beta));
}
// -1 outside, 0 inside, 1 tangent, 2
intersection
int intersection(circle a, circle b,
    vector<point>& inter) {
    double d2 = norm(b.c - a.c), rS = a.r + b.r,
    rD = a.r - b.r;
    if (d2 > sq(rS)) return -1;
    if (d2 < sq(rD)) return 0;
    double ca = 0.5 * (1 + rS * rD / d2);
    point z = point(ca, sqrt(sq(a.r) / d2 -
    sq(ca)));
    inter.push_back(a.c + (b.c - a.c) * z);
    if (abs(imag(z)) > EPS) inter.push_back(a.c +
    (b.c - a.c) * conj(z));
    return inter.size();
}
// points of intersection
vector<point> intersection(line a, circle c) {
    vector<point> inter;
    c.c -= a.a;
    a.b -= a.a;
    point m = a.b * real(c.c / a.b);
    double d2 = norm(m - c.c);
    if (d2 > sq(c.r)) return 0;
    double l = sqrt((sq(c.r) - d2) / norm(a.b));
    inter.push_back(a.a + m + l * a.b);
    if (abs(l) > EPS) inter.push_back(a.a + m - l
    * a.b);
    return inter;
}
// area of intersection
double intersection(rectangle a, rectangle b) {
    double x1 = max(real(a.tl), real(b.tl)), y1 =
    max(imag(a.tl), imag(b.tl));
    double x2 = min(real(a.br), real(b.br)), y2 =
    min(imag(a.br), imag(b.br));
    return (x2 <= x1 || y2 <= y1) ? 0 :
    (x2-x1)*(y2-y1);
}

```

Convex Hull

```

bool cmp(point a, point b) {
    if (abs(real(a) - real(b)) > EPS) return
    real(a) < real(b);
    if (abs(imag(a) - imag(b)) > EPS) return
    imag(a) < imag(b);
    return false;
}
convex_polygon convexhull(polygon a) {
    sort(a.points.begin(), a.points.end(), cmp);
    vector<point> lower, upper;
    for (int i = 0; i < a.points.size(); i++) {
        while (lower.size() >= 2 &&
        cross(lower.back() - lower[lower.size() -
        2], a.points[i] - lower.back()) < EPS)
            lower.pop_back();
        while (upper.size() >= 2 &&
        cross(upper.back() - upper[upper.size() -
        2], a.points[i] - upper.back()) > -EPS)
            upper.pop_back();
        lower.push_back(a.points[i]);
        upper.push_back(a.points[i]);
    }
    lower.insert(lower.end(), upper.rbegin() + 1,
    upper.rend());
    return convex_polygon(lower);
}

```

9 3D Geometry

```

struct point3d {
    double x, y, z;
    point3d operator+(point3d a) const { return
    {x+a.x, y+a.y, z+a.z}; }
    point3d operator*(double a) const { return
    {x*a, y*a, z*a}; }
    point3d operator-() const { return {-x, -y,
    -z}; }
    point3d operator-(point3d a) const { return
    *this - a; }
    point3d operator/(double a) const { return
    *this * (1/a); }
    double norm() { return sqrt(norm()); }
    double abs() { return sqrt(norm()); }
    point3d normalize() { return *this /
    this->abs(); }
};
double dot(point3d a, point3d b) { return
    a.x*b.x + a.y*b.y + a.z*b.z; }
point3d cross(point3d a, point3d b) { return
    {a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,
    a.x*b.y - a.y*b.x}; }
struct line3d { point3d a, b; };
struct plane { double a, b, c, d; } // a*x +
    b*y + c*z + d = 0
struct sphere { point3d c; double r; };
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double surface(circle a) { return 4 * sq(a.r) *
    M_PI; }
double volume(circle a) { return 4.0/3.0 *
    cb(a.r) * M_PI; }

```

10 Optimization

Snoob

```

// SameNumberOfOneBits, next permutation
int snoob(int a) {
    int b = a & -a, c = a + b;
    return c | ((a ^ c) >> 2) / b;
}
// example usage
int main() {
    char l1[] = {'1', '2', '3', '4', '5'};
    char l2[] = {'a', 'b', 'c', 'd'};
    int d1 = 5, d2 = 4;
    // prints 12345abcd, 1234a5bcd, ...
    int min = (1<<d1)-1, max = min << d2;
}

```

```

for (int i = min; i <= max; i = snoob(i)) {
    int p1 = 0, p2 = 0, v = 1;
    while (p1 < d1 || p2 < d2) {
        cout << ((v & 1) ? l1[p1++] : l2[p2++]);
        v /= 2;
    }
    cout << '\n';
}
}

```

Powers

```

bool isPowerOf2(ll a) {
    return a > 0 && !(a & a-1);
}
bool isPowerOf3(ll a) {
    return a>0&&!(12157665459056928801ull%a);
}
bool isPower(ll a, ll b) {
    double x = log(a) / log(b);
    return abs(x-round(x)) < 0.00000000001;
}

```

11 Python

Recursion Limit Removal (Basic)

```

import sys
sys.setrecursionlimit(10**6)

```

Recursion Limit Removal (Advanced)

```

# @bootstrap over recursive function
# replace 'return' with 'yield'
# for when sys method does not work
from types import GeneratorType
def bootstrap(f, stack=[]):
    def wrappedfunc(*args, **kwargs):
        if stack:
            return f(*args, **kwargs)
        else:
            to = f(*args, **kwargs)
            while True:
                if type(to) is GeneratorType:
                    stack.append(to)
                    to = next(to)
                else:
                    stack.pop()
                    if not stack:
                        break
            to = stack[-1].send(to)
    return wrappedfunc

```

Python 3 Compatibility

```

import sys
from __future__ import division, print_function
if sys.version_info[0] < 3:
    from __builtin__ import xrange as range
    from future_builtins import ascii, filter,
    hex, map, oct, zip

```

12 Additional

Judge Speed

```

// kattis: 0.50s
// codeforces: 0.421s
// atcoder: 0.455s
#include <bits/stdc++.h>
using namespace std;
int v = 1e9/2, p = 1;
int main() {
    for (int i = 1; i <= v; i++) p *= i;
    cout << p;
}

```

Judge Pre-Contest Checks

- __int128 and __float128 support?
- does extra or missing whitespace cause WA?
- documentation up to date?
- printer usage available and functional?

```
// each case tests a different fail condition
// try them before contests to see error codes
struct g { int arr[1000000]; g(){} };
vector<g> a;
// 0=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
↪ 6=SIGSEGV 7=recursive MLE
int judge(int n) {
    if (n == 0) exit(0);
    if (n == 1) while(1);
    if (n == 2) while(1) a.push_back(g());
    if (n == 3) while(1) putchar_unlocked('a');
    if (n == 4) assert(0);
    if (n == 5) 0 / 0;
    if (n == 6) *(int*)(0) = 0;
    return n + judge(n + 1);
}
```

GCC Builtin Docs

```
// 128-bit integer
__int128 a;
unsigned __int128 b;
// 128-bit float
// minor improvements over long double
float128 c;
// log2 floor
__lg(n);
// number of 1 bits
// can add ll like popcountll for long longs
__builtin_popcount(n);
// number of trailing zeroes
__builtin_ctz(n);
// number of leading zeroes
__builtin_clz(n);
// 1-indexed least significant 1 bit
__builtin_ffs(n);
// parity of number
__builtin_parity(n);
```

Limits

int	±2147483647	±2 ³¹ − 1	10 ⁹
uint	4294967295	2 ³² − 1	10 ⁹
ll	±9223372036854775807	±2 ⁶³ − 1	10 ¹⁸
ull	18446744073709551615	2 ⁶⁴ − 1	10 ¹⁹
l128	±170141183460469231...	±2 ¹²⁷ − 1	10 ³⁸
u128	340282366920938463...	2 ¹²⁸ − 1	10 ³⁸

Complexity classes input size (per second):

$O(n^n)$ or $O(n!)$	$n \leq 10$
$O(2^n)$	$n \leq 30$
$O(n^3)$	$n \leq 1000$
$O(n^2)$	$n \leq 30000$
$O(n\sqrt{n})$	$n \leq 10^6$
$O(n \log n)$	$n \leq 10^7$
$O(n)$	$n < 10^9$