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1 General

run.sh
```bash
g++ -g -O2 -std=gnu++17 -static prog.cpp
./a.exe
```

test.sh
```bash
# compile and test all *.in and *.ans
g++ -g -O2 -std=gnu++17 -static prog.cpp
for i in *.in; do
 f=${i%.in}
 ./a.exe < $i > "$f.out"
 diff -b -q "$f.ans" "$f.out"
done
```

Header
```cpp
// use better compiler options
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
// include everything
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <sys/resource.h>
// namespaces
using namespace std;
using namespace __gnu_cxx; // rope
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio \
  ios_base::sync_with_stdio(0);cin.tie(0);
#define nostacklim rlimit \
  RZ;getrlimit(3,&RZ);RZ.rlim_cur=- \
  1;setrlimit(3,&RZ);
#define DEBUG(v) cerr<<__LINE__<<": "<<#v<<" = " \
  "<<v<<'\n';
#define TIMER \
  cerr<<1.0*clock()/CLOCKS_PER_SEC<<"s\n";
#define ll long long
#define ull unsigned ll
#define i128 __int128
#define u128 unsigned i128
#define ld long double
// global variables
mt19937 rng((uint32_t)chrono::steady_clock::now().time_since_epoch().count());
```

Fast IO
```cpp
#ifdef _WIN32
#define getchar_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
#endif
void read(unsigned int& n) {
 char c; n = 0;
 while ((c=getchar_unlocked())!=' '&&c!='\n')
 n = n * 10 + c - '0';
}
void read(int& n) {
 char c; n = 0; int s = 1;
 if ((c=getchar_unlocked())=='-') s = -1;
 else n = c - '0';
 while ((c=getchar_unlocked())!=' '&&c!='\n')
 n = n * 10 + c - '0';
 n *= s;
}
void read(ld& n) {
 char c;
 ld m = 0, o = 1; bool d = false; int s = 1;
 if ((c=getchar_unlocked())=='-') s = -1;
 else if (c == '.') d = true;
 else n = c - '0';
 while ((c=getchar_unlocked())!=' '&&c!='\n') {
 if (c == '.') d = true;
 else if (d) { m=m*10+c-'0'; o*=0.1; }
```
```cpp
 else n = n * 10 + c - '0';
 }
 n = s * (n + m * o);
}
void read(double& n) {
 ld m; read(m); n = m;
}
void read(float& n) {
 ld m; read(m); n = m;
}
void read(string& s) {
 char c; s = "";
 while((c=getchar_unlocked())!=' '&&c!='\n')
 s += c;
}
bool readline(string& s) {
 char c; s = "";
 while(c=getchar_unlocked()) {
 if (c == '\n') return true;
 if (c == EOF) return false;
 s += c;
 }
 return false;
}
void print(unsigned int n) {
 if (n / 10) print(n / 10);
 putchar_unlocked(n % 10 + '0');
}
void print(int n) {
 if (n < 0) { putchar_unlocked('-'); n*=-1; }
 print((unsigned int)n);
}
```

Common Structs
```cpp
// n-dimension vectors
// Vec<2, int> v(n, m) = arr[n][m]
// Vec<2, int> v(n, m, -1) default init -1
template<int D, typename T>
struct Vec : public vector<Vec<D-1, T>> {
 template<typename... Args>
 Vec(int n=0, Args... args) : vector<Vec<D-1,
 T>>(n, Vec<D-1, T>(args...)) {}
};
template<typename T>
struct Vec<1, T> : public vector<T> {
 Vec(int n=0, T val=T()) : vector<T>(n, val)
 {}
};
```

2 Algorithms

Min/Max Subarray
```cpp
// max - compare = a < b, reset = a < 0
// min - compare = a > b, reset = a > 0
// returns {sum, {start, end}}
pair<int, pair<int, int>>
 ContiguousSubarray(int* a, int size,
 bool(*compare)(int, int),
 bool(*reset)(int), int defbest = 0) {
 int best = defbest, cur = 0, start = 0, end =
 0, s = 0;
 for (int i = 0; i < size; i++) {
 cur += a[i];
 if ((*compare)(best, cur)) { best = cur;
 start = s; end = i; }
 if ((*reset)(cur)) { cur = 0; s = i + 1; }
 }
 return {best, {start, end}};
}
```

Quickselect
```cpp
#define QSNE -999999
int partition(int arr[], int l, int r)
{
 int x = arr[r], i = l;
 for (int j = l; j <= r - 1; j++)
 if (arr[j] <= x)
 swap(arr[i++], arr[j]);
 swap(arr[i], arr[r]);
 return i;
}
```
```cpp
// find k'th smallest element in unsorted array,
// only if all distinct
int qselect(int arr[], int l, int r, int k)
{
 if (!(k > 0 && k <= r - l + 1)) return QSNE;
 swap(arr[l + rng() % (r-l+1)], arr[r]);
 int pos = partition(arr, l, r);
 if (pos-l==k-1) return arr[pos];
 if (pos-l>k-1) return qselect(arr,l,pos-1,k);
 return qselect(arr, pos+1, r, k-pos+l-1);
}
// TODO: compare against std::nth_element()
```

Saddleback Search
```cpp
// search for v in 2d array arr[x][y], sorted
// on both axis
pair<int, int> saddleback_search(int** arr, int
 x, int y, int v) {
 int i = x-1, j = 0;
 while (i >= 0 && j < y) {
 if (arr[i][j] == v) return {i, j};
 (arr[i][j] > v)? i-- : j++;
 }
 return {-1, -1};
}
```

Ternary Search
```cpp
// < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {
 while (b-a > 4) {
 int m = (a+b)/2;
 if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
 else b = m+1;
 }
 for (int i = a+1; i <= b; i++)
 if (TERNCOMP((*f)(a), (*f)(i)))
 a = i;
 return a;
}
#define TERNPREC 0.000001
double ternsearch(double a, double b, double
 (*f)(double)) {
 while (b-a > TERNPREC * 4) {
 double m = (a+b)/2;
 if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
 = m;
 else b = m + TERNPREC;
 }
 for (double i = a + TERNPREC; i <= b; i +=
 TERNPREC)
 if (TERNCOMP((*f)(a), (*f)(i)))
 a = i;
 return a;
}
```

3 Structures

Fenwick Tree
```cpp
// Fenwick tree, array of cumulative sums -
// O(log n) updates, O(log n) gets
struct Fenwick {
 int n; ll* tree;
 void update(int i, int val) {
 ++i;
 while (i <= n) {
 tree[i] += val;
 i += i & (-i);
 }
 }
 Fenwick(int size) {
 n = size;
 tree = new ll[n+1];
 for (int i = 1; i <= n; i++)
 tree[i] = 0;
 }
 Fenwick(int* arr, int size) : Fenwick(size) {
 for (int i = 0; i < n; i++)
 update(i, arr[i]);
 }
 ~Fenwick() { delete[] tree; }
 ll operator[](int i) {
```
```cpp
 if (i < 0 || i > n) return 0;
 ll sum = 0;
 ++i;
 while (i>0) {
 sum += tree[i];
 i -= i & (-i);
 }
 return sum;
 }
 ll getRange(int a, int b) { return
 operator[](b) - operator[](a-1); }
};
```

Hashtable
```cpp
// similar to unordered_map, but faster
struct chash {
 const uint64_t C = (ll)(2e18 * M_PI) + 71;
 ll operator()(ll x) const { return
 __builtin_bswap64(x*C); }
};
int main() {
 gp_hash_table<ll,int,chash>
 hashtable({},{},{},{},{1<<16});
 for (int i = 0; i < 100; i++)
 hashtable[i] = 200+i;
 if (hashtable.find(10) != hashtable.end())
 cout << hashtable[10];
}
```

Ordered Set
```cpp
typedef tree<int,null_type,less<int>,rb_tree
 _tag,tree_order_statistics_node_update>
 ordered_set;
int main()
{
 ordered_set o_set;
 o_set.insert(1); o_set.insert(1);
 o_set.insert(5); o_set.insert(3);
 // get second smallest element
 cout << *(o_set.find_by_order(1)) << '\n';
 // number of elements less than k=4
 cout << o_set.order_of_key(4) << '\n';
}
```

Rope
```cpp
// O(log n) insert, delete, concatenate
int main() {
 // generate rope
 rope<int> v;
 for (int i = 0; i < 100; i++)
 v.push_back(i);
 // move range to front
 rope<int> copy = v.substr(10, 10);
 v.erase(10, 10);
 v.insert(copy.mutable_begin(), copy);
 // print elements of rope
 for (auto it : v)
 cout << it << " ";
}
```

Segment Tree
```cpp
//max(a,b), min(a,b), a+b, a*b, gcd(a,b), a^b
struct SegmentTree {
 typedef int T;
 static constexpr T UNIT = INT_MIN;
 T f(T a, T b) {
 if (a == UNIT) return b;
 if (b == UNIT) return a;
 return max(a,b);
 }
 int n; vector<T> s;
 SegmentTree(int n, T def=UNIT) : s(2*n, def),
 n(n) {}
 SegmentTree(vector<T> arr) :
 SegmentTree(arr.size()) {
 for (int i=0;i<arr.size();i++)
 update(i,arr[i]);
 }
 void update(int pos, T val) {
 for (s[pos += n] = val; pos /= 2;)
 s[pos] = f(s[pos * 2], s[pos*2+1]);
```

```cpp
}
T query(int b, int e) { // query [b, e)
  T ra = UNIT, rb = UNIT;
  for (b+=n, e+=n; b<e; b/=2, e/=2) {
    if (b % 2) ra = f(ra, s[b++]);
    if (e % 2) rb = f(s[--e], rb);
  }
  return f(ra, rb);
}
T get(int p) { return query(p, p+1); }
};
```

Trie

```cpp
typedef trie<string, null_type,
↪  trie_string_access_traits<>,
  pat_trie_tag, trie_prefix_search_node_update>
↪  trie_type;
int main() {
  // generate trie
  trie_type trie;
  for (int i = 0; i < 20; i++)
    trie.insert(to_string(i)); // true if new,
↪   false if old
  // print things with prefix "1"
  auto range = trie.prefix_range("1");
  for (auto it = range.first; it !=
↪   range.second; it++)
    cout << *it << " ";
}
```

4 Strings

Aho Corasick

```cpp
// range of alphabet for automata to consider
// MAXC = 26, OFFC = 'a' if only lowercase
const int MAXC = 256;
const int OFFC = 0;
struct aho_corasick {
  struct state
  {
    set<pair<int, int>> out;
    int fail; vector<int> go;
    state() : fail(-1), go(MAXC, -1) {}
  };
  vector<state> s;
  int id = 0;
  aho_corasick(string* arr, int size) : s(1) {
    for (int i = 0; i < size; i++) {
      int cur = 0;
      for (int c : arr[i]) {
        if (s[cur].go[c-OFFC] == -1) {
          s[cur].go[c-OFFC] = s.size();
          s.push_back(state());
        }
        cur = s[cur].go[c-OFFC];
      }
      s[cur].out.insert({arr[i].size(), id++});
    }
    for (int c = 0; c < MAXC; c++)
      if (s[0].go[c] == -1)
        s[0].go[c] = 0;
    queue<int> sq;
    for (int c = 0; c < MAXC; c++) {
      if (s[0].go[c] != 0) {
        s[s[0].go[c]].fail = 0;
        sq.push(s[0].go[c]);
      }
    }
    while (sq.size()) {
      int e = sq.front(); sq.pop();
      for (int c = 0; c < MAXC; c++) {
        if (s[e].go[c] != -1) {
          int failure = s[e].fail;
          while (s[failure].go[c] == -1)
            failure = s[failure].fail;
          failure = s[failure].go[c];
          s[s[e].go[c]].fail = failure;
          for (auto length : s[failure].out)
            s[s[e].go[c]].out.insert(length);
          sq.push(s[e].go[c]);
        }
      }
```

```cpp
    }
  }
  // list of {start pos, pattern id}
  vector<pair<int, int>> search(string text)
  {
    vector<pair<int, int>> toret;
    int cur = 0;
    for (int i = 0; i < text.size(); i++) {
      while (s[cur].go[text[i]-OFFC] == -1)
        cur = s[cur].fail;
      cur = s[cur].go[text[i]-OFFC];
      if (s[cur].out.size())
        for (auto end : s[cur].out)
          toret.push_back({i - end.first + 1,
↪           end.second});
    }
    return toret;
  }
};
```

Boyer Moore

```cpp
struct defint { int i = -1; };
vector<int> boyermoore(string txt, string pat)
↪  {
  vector<int> toret; unordered_map<char, defint>
↪  badchar;
  int m = pat.size(), n = txt.size();
  for (int i = 0; i < m; i++) badchar[pat[i]].i
↪   = i;
  int s = 0;
  while (s <= n - m) {
    int j = m - 1;
    while (j >= 0 && pat[j] == txt[s + j]) j--;
    if (j < 0) {
      toret.push_back(s);
      s += (s + m < n) ? m - badchar[txt[s +
↪       m]].i : 1;
    } else
      s += max(1, j - badchar[txt[s + j]].i);
  }
  return toret;
}
```

English Conversion

```cpp
const string ones[] = {"", "one", "two",
  "three", "four", "five", "six", "seven",
⇒  "eight", "nine"};
const string teens[] ={"ten", "eleven",
  "twelve", "thirteen", "fourteen",
⇒  "fifteen", "sixteen", "seventeen",
⇒  "eighteen", "nineteen"};
const string tens[] = {"twenty", "thirty",
  "forty", "fifty", "sixty", "seventy",
⇒  "eighty", "ninety"};
const string mags[] = {"thousand", "million",
  "billion", "trillion", "quadrillion",
⇒  "quintillion", "sextillion",
⇒  "septillion"};
string convert(int num, int carry) {
  if (num < 0) return "negative " +
↪   convert(-num, 0);
  if (num < 10) return ones[num];
  if (num < 20) return teens[num % 10];
  if (num < 100) return tens[(num / 10) - 2] +
↪   (num%10==0?"":" ") + ones[num % 10];
  if (num < 1000) return ones[num / 100] +
↪   (num/100==0?"":" ") + "hundred" +
↪   (num%100==0?"":" ") + convert(num % 100,
↪   0);
  return convert(num / 1000, carry + 1) + " " +
↪   mags[carry] + " " + convert(num % 1000,
↪   0);
}
string convert(int num) {
  return (num == 0) ? "zero" : convert(num, 0);
}
```

Knuth Morris Pratt

```cpp
vector<int> kmp(string txt, string pat) {
  vector<int> toret;
  int m = txt.length(), n = pat.length();
  int next[n + 1];
  for (int i = 0; i < n + 1; i++)
    next[i] = 0;
  for (int i = 1; i < n; i++) {
    int j = next[i + 1];
    while (j > 0 && pat[j] != pat[i])
      j = next[j];
    if (j > 0 || pat[j] == pat[i])
      next[i + 1] = j + 1;
  }
  for (int i = 0, j = 0; i < m; i++) {
    if (txt[i] == pat[j]) {
      if (++j == n)
        toret.push_back(i - j + 1);
    } else if (j > 0) {
      j = next[j];
      i--;
    }
  }
  return toret;
}
```

Longest Common Prefix (array)

```cpp
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
↪  false) {
  if (n == 0) return "";
  if (!sorted) sort(arr, arr + n);
  string r = ""; int v = 0;
  while (v < arr[0].length() && arr[0][v] ==
↪   arr[n-1][v])
    r += arr[0][v++];
  return r;
}
```

Longest Common Subsequence

```cpp
string lcs(string a, string b) {
  int m = a.length(), n = b.length();
  int L[m+1][n+1];
  for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
      if (i == 0 || j == 0) L[i][j] = 0;
      else if (a[i-1] == b[j-1]) L[i][j] =
↪       L[i-1][j-1]+1;
      else L[i][j] = max(L[i-1][j], L[i][j-1]);
    }
  }
  // return L[m][n]; // length of lcs
  string out = "";
  int i = m - 1, j = n - 1;
  while (i >= 0 && j >= 0) {
    if (a[i] == b[j]) {
      out = a[i--] + out;
      j--;
    }
    else if (L[i][j+1] > L[i+1][j]) i--;
    else j--;
  }
  return out;
}
```

Longest Common Substring

```cpp
// l is array of palindrome length at that
↪  index
int manacher(string s, int* l) {
  int n = s.length() * 2;
  for (int i = 0, j = 0, k; i < n; i += k, j =
↪   max(j-k, 0)) {
    while (i >= j && i + j + 1 < n && s[(i-j)/2]
↪     == s[(i+j+1)/2]) j++;
    l[i] = j;
    for (k = 1; i >= k && j >= k && l[i-k] !=
↪     j-k; k++)
      l[i+k] = min(l[i-k], j-k);
  }
  return *max_element(l, l + n);
}
```

Subsequence Count

```cpp
// "banana", "ban" >> 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
  int m = subs.length(), n = body.length();
  if (m > n) return 0;
  ull** arr = new ull*[m+1];
  for (int i = 0; i <= m; i++) arr[i] = new
↪   ull[n+1];
  for (int i = 1; i <= m; i++) arr[i][0] = 0;
  for (int i = 0; i <= n; i++) arr[0][i] = 1;
  for (int i = 1; i <= m; i++) {
    for (int j = 1; j <= n; j++)
      arr[i][j] = arr[i][j-1] + ((body[j-1] ==
↪       subs[i-1])? arr[i-1][j-1] : 0);
  }
  return arr[m][n];
}
```

Suffix Array + LCP

```cpp
struct SuffixArray {
  vector<int> sa, lcp;
  SuffixArray(string& s, int lim=256) {
    int n = s.length() + 1, k = 0, a, b;
    vector<int> x(begin(s), end(s)+1), y(n),
↪     ws(max(n, lim)), rank(n);
    sa = lcp = y;
    iota(begin(sa), end(sa), 0);
    for (int j = 0, p = 0; p < n; j = max(1, j *
↪     2), lim = p) {
      p = j; iota(begin(y), end(y), n - j);
      for (int i = 0; i < (n); i++)
        if (sa[i] >= j)
          y[p++] = sa[i] - j;
      fill(begin(ws), end(ws), 0);
      for (int i = 0; i < (n); i++) ws[x[i]]++;
      for (int i = 1; i < (lim); i++) ws[i] +=
↪       ws[i - 1];
      for (int i = n; i--;) sa[--ws[x[y[i]]]] =
↪       y[i];
      swap(x, y); p = 1; x[sa[0]] = 0;
      for (int i = 1; i < (n); i++) {
        a = sa[i - 1]; b = sa[i];
        x[b] = (y[a] == y[b] && y[a + j] == y[b +
↪         j]) ? p - 1 : p++;
      }
    }
    for (int i = 1; i < (n); i++) rank[sa[i]] =
↪     i;
    for (int i = 0, j; i < n - 1; lcp[rank[i++]]
↪     = k)
      for (k && k--, j = sa[rank[i] - 1];
        s[i + k] == s[j + k]; k++);
  }
};
```

String Utilities

```cpp
void lowercase(string& s) {
  transform(s.begin(), s.end(), s.begin(),
↪   ::tolower);
}
void uppercase(string& s) {
  transform(s.begin(), s.end(), s.begin(),
↪   ::toupper);
}
void trim(string &s) {
  s.erase(s.begin(),find_if_not(s.begin(),s⌋
↪   .end(),[](int c){return
⇒   isspace(c);}));
  s.erase(find_if_not(s.rbegin(),s.rend(),[](int
↪   c){return isspace(c);}).base(),s.end());
}
vector<string> split(string& s, char token) {
  vector<string> v; stringstream ss(s);
  for (string e;getline(ss,e,token);)
    v.push_back(e);
  return v;
}
```

5 Math

Catalan Numbers

```cpp
ull* catalan = new ull[1000000];
void genCatalan(int n, int mod) {
  catalan[0] = catalan[1] = 1;
  for (int i = 2; i <= n; i++) {
    catalan[i] = 0;
    for (int j = i - 1; j >= 0; j--) {
      catalan[i] += (catalan[j] * catalan[i-j-1])
↪         % mod;
      if (catalan[i] >= mod)
        catalan[i] -= mod;
    }
  }
}
// TODO: consider binomial coefficient method
```

Combinatorics (nCr, nPr)

```cpp
// can optimize by precomputing factorials, and
↪   fact[n]/fact[n-r]
ull nPr(ull n, ull r) {
  ull v = 1;
  for (ull i = n-r+1; i <= n; i++)
    v *= i;
  return v;
}
ull nPr(ull n, ull r, ull m) {
  ull v = 1;
  for (ull i = n-r+1; i <= n; i++)
    v = (v * i) % m;
  return v;
}
ull nCr(ull n, ull r) {
  long double v = 1;
  for (ull i = 1; i <= r; i++)
    v = v * (n-r+i) /i;
  return (ull)(v + 0.001);
}
// requires modulo math
// can optimize by precomputing mfac and
↪   minv-mfac
ull nCr(ull n, ull r, ull m) {
  return mfac(n, m) * minv(mfac(k, m), m) % m *
↪   minv(mfac(n-k, m), m) % m;
}
```

Chinese Remainder Theorem

```cpp
bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
↪ {
  ll x, y, d; mo = m[0]; re = r[0];
  for (int i = 1; i < n; i++) {
    d = egcd(mo, m[i], x, y);
    if ((r[i] - re) % d != 0) return false;
    x = (r[i] - re) / d * x % (m[i] / d);
    re += x * mo;
    mo = mo / d * m[i];
    re %= mo;
  }
  re = (re + mo) % mo;
  return true;
}
```

Count Digit Occurences

```cpp
/*count(n,d) counts the number of occurences of
↪   a digit d in the range [0,n]*/
ll digit_count(ll n, ll d) {
  ll result = 0;
  while (n != 0) {
    result += ((n%10) == d ? 1 : 0);
    n /= 10;
  }
  return result;
}
ll count(ll n, ll d) {
  if (n < 10) return (d > 0 && n >= d);
  if ((n % 10) != 9) return digit_count(n, d) +
↪   count(n-1, d);
  return 10*count(n/10, d) + (n/10) + (d > 0);
}
```

Discrete Logarithm

```cpp
unordered_map<int, int> dlogc;
int discretelog(int a, int b, int m) {
  dlogc.clear();
  ll n = sqrt(m)+1, an = 1;
  for (int i = 0; i < n; i++)
    an = (an * a) % m;
  ll c = an;
  for (int i = 1; i <= n; i++) {
    if (!dlogc.count(c)) dlogc[c] = i;
    c = (c * an) % m;
  }
  c = b;
  for (int i = 0; i <= n; i++) {
    if (dlogc.count(c)) return (dlogc[c] * n - i
↪   + m - 1) % (m-1);
    c = (c * a) % m;
  }
  return -1;
}
```

Euler Phi / Totient

```cpp
int phi(int n) {
  int r = n;
  for (int i = 2; i * i <= n; i++) {
    if (n % i == 0) r -= r / i;
    while (n % i == 0) n /= i;
  }
  if (n > 1) r -= r / n;
  return r;
}
#define n 100000
ll phi[n+1];
void computeTotient() {
  for (int i=1; i<=n; i++) phi[i] = i;
  for (int p=2; p<=n; p++) {
    if (phi[p] == p) {
      phi[p] = p-1;
      for (int i = 2*p; i<=n; i += p) phi[i] =
↪   (phi[i]/p) * (p-1);
    }
  }
}
```

Factorials

```cpp
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
↪   M_E)) + (log10(2 * M_PI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
↪   M_PI * n) * pow(n / M_E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
```

Prime Factorization

```cpp
// do not call directly
ll pollard_rho(ll n, ll s) {
  ll x, y;
  x = y = rand() % (n - 1) + 1;
  int head = 1, tail = 2;
  while (true) {
    x = mult(x, x, n);
    x = (x + s) % n;
    if (x == y) return n;
    ll d = __gcd(max(x - y, y - x), n);
    if (1 < d && d < n) return d;
    if (++head == tail) y = x, tail <<= 1;
  }
}
// call for prime factors
void factorize(ll n, vector<ll> &divisor) {
  if (n == 1) return;
  if (isPrime(n)) divisor.push_back(n);
  else {
    ll d = n;
    while (d >= n) d = pollard_rho(n, rand() % (n
↪   - 1) + 1);
    factorize(n / d, divisor);
    factorize(d, divisor);
  }
}
```

Farey Fractions

```cpp
// generate 0 <= a/b <= 1 ordered, b <= n
// farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
  int h = 0, k = 1, x = 1, y = 0, r;
  vector<pair<int, int>> v;
  do {
    v.push_back({h, k});
    r = (n-y)/k;
    y += r*k; x += r*h;
    swap(x,h); swap(y,k);
    x = -x; y = -y;
  } while (k > 1);
  v.push_back({1, 1});
  return v;
}
```

Fast Fourier Transform

```cpp
#define cd complex<double>
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert) {
  int n = a.size();
  for (int i = 1, j = 0; i < n; i++) {
    int bit = n >> 1;
    for (; j & bit; bit >>= 1) j ^= bit;
    j ^= bit;
    if (i < j) swap(a[i], a[j]);
  }
  for (int len = 2; len <= n; len <<= 1) {
    double ang = 2 * PI / len * (invert ? -1 :
↪   1);
    cd wlen(cos(ang), sin(ang));
    for (int i = 0; i < n; i += len) {
      cd w(1);
      for (int j = 0; j < len / 2; j++) {
        cd u = a[i+j], v = a[i+j+len/2] * w;
        a[i+j] = u + v;
        a[i+j+len/2] = u - v;
        w *= wlen;
      }
    }
  }
  if (invert)
    for (auto& x : a)
      x /= n;
}

vector<int> fftmult(vector<int> const& a,
↪   vector<int> const& b) {
  vector<cd> fa(a.begin(), a.end()),
↪   fb(b.begin(), b.end());
  int n = 1 << (32 - __builtin_clz(a.size() +
↪   b.size() - 1));
  fa.resize(n); fb.resize(n);
  fft(fa, false); fft(fb, false);
  for (int i = 0; i < n; i++) fa[i] *= fb[i];
  fft(fa, true);
  vector<int> toret(n);
  for (int i = 0; i < n; i++) toret[i] =
↪   round(fa[i].real());
  return toret;
}
```

Greatest Common Denominator

```cpp
ll egcd(ll a, ll b, ll& x, ll& y) {
  if (b == 0) { x = 1; y = 0; return a; }
  ll gcd = egcd(b, a % b, x, y);
  x -= a / b * y;
  swap(x, y);
  return gcd;
}
```

Josephus Problem

```cpp
// 0-indexed, arbitrary k
int josephus(int n, int k) {
  if (n == 1) return 0;
  if (k == 1) return n-1;
  if (k > n) return (josephus(n-1,k)+k)%n;
  int res = josephus(n-n/k,k)-n%k;
  return res + ((res<0)?n:res/(k-1));
}
// fast case if k=2, traditional josephus
int josephus(int n) {
  return 2*(n-(1<<(32-__builtin_clz(n)-1)));
}
```

Least Common Multiple

```cpp
#define lcm(a,b) ((a*b)/__gcd(a,b))
```

Modulo Operations

```cpp
#define MOD 1000000007
#define madd(a,b,m) (a+b-((a+b-m>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a<b)?m:0))
ll mpow(ll b, ll e, ll m) {
  ll x = 1;
  while (e > 0) {
    if (e % 2) x = (x * b) % m;
    b = (b * b) % m;
    e /= 2;
  }
  return x % m;
}
ull mfac(ull n, ull m) {
  ull f = 1;
  for (int i = n; i > 1; i--)
    f = (f * i) % m;
  return f;
}
// if m is not guaranteed to be prime
ll minv(ll b, ll m) {
  ll x = 0, y = 0;
  if (egcd(b, m, x, y) != 1) return -1;
  return (x % m + m) % m;
}
ll mdiv_compmod(int a, int b, int m) {
  if (__gcd(b, m) != 1) return -1;
  return mult(a, minv(b, m), m);
}
// if m is prime (like 10^9+7)
ll mdiv_primemod (int a, int b, int m) {
  return mult(a, mpow(b, m-2, m), m);
}
```

Miller-Rabin Primality Test

```cpp
// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
  if (n < 2) return false;
  if (n == 2) return true;
  if (n % 2 == 0) return false;
  ull s = n - 1;
  while (s % 2 == 0) s /= 2;
  for (int i = 0; i < 10; i++) {
    ull temp = s;
    ull a = rand() % (n - 1) + 1;
    ull mod = mpow(a, temp, n);
    while (temp!=n-1&&mod!=1&&mod!=n-1) {
      mod = mult(mod, mod, n);
      temp *= 2;
    }
    if (mod!=n-1&&temp%2==0) return false;
  }
  return true;
}
```

Sieve of Eratosthenes

```cpp
bitset<100000001> sieve;
// generate sieve - O(n log n)
void genSieve(int n) {
  sieve[0] = sieve[1] = 1;
  for (ull i = 3; i * i < n; i += 2)
    if (!sieve[i])
      for (ull j = i * 3; j <= n; j += i * 2)
        sieve[j] = 1;
}
// query sieve after it's generated - O(1)
bool querySieve(int n) {
  return n == 2 || (n % 2 != 0 && !sieve[n]);
}
```

Simpson's / Approximate Integrals

```cpp
// integrate f from a to b, k iterations
// error <= (b-a)/18.0 * M * ((b-a)/2k)^4
// where M = max(abs(f````(x))) for x in [a,b]
// "f" is a function "double func(double x)"
double Simpsons(double a, double b, int k,
→   double (*f)(double)) {
  double dx = (b-a)/(2.0*k), t = 0;
  for (int i = 0; i < k; i++)
    t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
→     (*f)(a+(2*i+1)*dx);
  return (t + (*f)(b)) * (b-a) / 6.0 / k;
}
```

Common Equations Solvers

```cpp
// ax^2 + bx + c = 0, find x
vector<double> solveEq(double a, double b,
→   double c) {
  vector<double> r;
  double z = b * b - 4 * a * c;
  if (z == 0)
    r.push_back(-b/(2*a));
  else if (z > 0) {
    r.push_back((sqrt(z)-b)/(2*a));
    r.push_back((sqrt(z)+b)/(2*a));
  }
  return r;
}
// ax^3 + bx^2 + cx + d = 0, find x
vector<double> solveEq(double a, double b,
→   double c, double d) {
  vector<double> res;
  long double a1 = b/a, a2 = c/a, a3 = d/a;
  long double q = (a1*a1 - 3*a2)/9.0, sq =
→   -2*sqrt(q);
  long double r = (2*a1*a1*a1 - 9*a1*a2 +
→   27*a3)/54.0;
  long double z = r*r-q*q*q, theta;
  if (z <= 0) {
    theta = acos(r/sqrt(q*q*q));
    res.push_back(sq*cos(theta/3.0) - a1/3.0);
    res.push_back(sq*cos((theta+2.0*PI)/3.0) -
→     a1/3.0);
    res.push_back(sq*cos((theta+4.0*PI)/3.0) -
→     a1/3.0);
  }
  else {
    res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
    res[0] = (res[0] + q / res[0]) * ((r<0)?1:-1)
→     - a1 / 3.0;
  }
  return res;
}
// linear diophantine equation ax + by = c,
→   find x and y
// infinite solutions of form x+k*b/g, y-k*a/g
bool solveEq(ll a, ll b, ll c, ll &x, ll &y, ll
→   &g) {
  g = egcd(abs(a), abs(b), x, y);
  if (c % g) return false;
  x *= c / g * ((a < 0) ? -1 : 1);
  y *= c / g * ((b < 0) ? -1 : 1);
  return true;
}
// m = # equations, n = # variables, a[m][n+1]
→   = coefficient matrix
// a[i][0]x + a[i][1]y + ... + a[i][n]z =
→   a[i][n+1]
const double eps = 1e-7;
bool zero(double a) { return (a < eps) && (a >
→   -eps); }
vector<double> solveEq(double **a, int m, int
→   n) {
  int cur = 0;
  for (int i = 0; i < n; i++) {
    for (int j = cur; j < m; j++) {
      if (!zero(a[j][i])) {
        if (j != cur) swap(a[j], a[cur]);
```

```cpp
        for (int sat = 0; sat < m; sat++) {
          if (sat == cur) continue;
          double num = a[sat][i] / a[cur][i];
          for (int sot = 0; sot <= n; sot++)
            a[sat][sot] -= a[cur][sot] * num;
        }
        cur++;
        break;
      }
    }
  }
  for (int j = cur; j < m; j++)
    if (!zero(a[j][n])) return vector<double>();
  vector<double> ans(n,0);
  for (int i = 0, sat = 0; i < n; i++)
    if (sat < m && !zero(a[sat][i]))
      ans[i] = a[sat][n] / a[sat++][i];
  return ans;
```

Graycode Conversions

```cpp
ull graycode2ull(ull n) {
  ull i = 0;
  for (; n; n = n >> 1) i ^= n;
  return i;
}
ull ull2graycode(ull n) {
  return n ^ (n >> 1);
}
```

6 Graphs

```cpp
struct edge {
  int u,v,w;
  edge (int u,int v,int w) : u(u),v(v),w(w) {}
  edge () : u(0), v(0), w(0) {}
};
bool operator < (const edge &e1, const edge
→   &e2) { return e1.w < e2.w; }
bool operator > (const edge &e1, const edge
→   &e2) { return e1.w > e2.w; }
struct subset { int p, rank; };
```

Eulerian Path

```cpp
#define edge_list vector<edge>
#define adj_sets vector<set<int>>
struct EulerPathGraph {
  adj_sets graph; // actually indexes incident
→   edges
  edge_list edges; int n; vector<int> indeg;
  EulerPathGraph(int n): n(n) {
    indeg = *(new vector<int>(n,0));
    graph = *(new adj_sets(n, set<int>()));
  }
  void add_edge(int u, int v) {
    graph[u].insert(edges.size());
    indeg[v]++;
    edges.push_back(edge(u,v,0));
  }
  bool eulerian_path(vector<int> &circuit) {
    if(edges.size()==0) return false;
    stack<int> st;
    int a[] = {-1, -1};
    for(int v=0;v<n;v++) {
      if(indeg[v]!=graph[v].size()) {
        bool b = indeg[v] > graph[v].size();
        if (abs(((int)indeg[v])-((int)graph[v]
→       .size())) > 1) return
→       false;
        if (a[b] != -1) return false;
        a[b] = v;
      }
    }
    int s = (a[0]!=-1 && a[1]!=-1 ? a[0] :
→     (a[0]==-1 && a[1]==-1 ? edges[0].u : -1));
    if(s==-1) return false;
    while(!st.empty() || !graph[s].empty()) {
      if (graph[s].empty()) {
        circuit.push_back(s); s = st.top();
⇒       st.pop(); }
      else {
```

```cpp
        int w = edges[*graph[s].begin()].v;
        graph[s].erase(graph[s].begin());
        st.push(s); s = w;
      }
    }
    circuit.push_back(s);
    return circuit.size()-1==edges.size();
  }
};
```

Minimum Spanning Tree

```cpp
// returns vector of edges in the mst
// graph[i] = vector of edges incident to
→   vertex i
// places total weight of the mst in &total
// if returned vector has size != n-1, there is
→   no MST
vector<edge> mst(vector<vector<edge>> graph,
→   ll &total) {
  total = 0;
  priority_queue<edge, vector<edge>,
→   greater<edge>> pq;
  vector<edge> MST;
  bitset<20001> marked; // change size as needed
  marked[0] = 1;
  for (edge ep : graph[0]) pq.push(ep);
  while(MST.size()!=graph.size()-1 &&
→   pq.size()!=0) {
    edge e = pq.top(); pq.pop();
    int u = e.u, v = e.v, w = e.w;
    if(marked[u] && marked[v]) continue;
    else if(marked[u]) swap(u, v);
    for(edge ep : graph[u]) pq.push(ep);
    marked[u] = 1;
    MST.push_back(e);
    total += e.w;
  }
  return MST;
}
```

Union Find

```cpp
int uf_find(subset* s, int i) {
  if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
  return s[i].p;
}
void uf_union(subset* s, int x, int y) {
  int xp = uf_find(s, x), yp = uf_find(s, y);
  if (s[xp].rank > s[yp].rank) s[yp].p = xp;
  else if (s[xp].rank < s[yp].rank) s[xp].p =
→   yp;
  else { s[yp].p = xp; s[xp].rank++; }
}
```

7 2D Geometry

```cpp
#define point complex<double>
#define EPS 0.0000001
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double dot(point a, point b) { return
→   real(conj(a)*b); }
double cross(point a, point b) { return
→   imag(conj(a)*b); }
struct line { point a, b; };
struct circle { point c; double r; };
struct segment { point a, b; };
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
struct convex_polygon {
  vector<point> points;
  convex_polygon(vector<point> points) :
→   points(points) {}
  convex_polygon(triangle a) {
    points.push_back(a.a); points.push_back(a.b);
→   points.push_back(a.c);
  };
  convex_polygon(rectangle a) {
    points.push_back(a.tl);
    points.push_back({real(a.tl),
⇒   imag(a.br)});
```

```cpp
    points.push_back(a.br);
    points.push_back({real(a.br),
⇒   imag(a.tl)});
  }
}
struct polygon {
  vector<point> points;
  polygon(vector<point> points) : points(points)
→   {}
  polygon(triangle a) {
    points.push_back(a.a); points.push_back(a.b);
    points.push_back(a.c);
  }
  polygon(rectangle a) {
    points.push_back(a.tl);
    points.push_back({real(a.tl),
⇒   imag(a.br)});
    points.push_back(a.br);
    points.push_back({real(a.br),
⇒   imag(a.tl)});
  }
  polygon(convex_polygon a) {
    for (point v : a.points)
      points.push_back(v);
  }
};
// triangle methods
double area_heron(double a, double b, double c)
→   {
  if (a < b) swap(a, b);
  if (a < c) swap(a, c);
  if (b < c) swap(b, c);
  if (a > b + c) return -1;
  return sqrt((a+b+c)*(c-a+b)*(c+a-b)*(a+b-c)
→   /16.0);
}
// segment methods
double lengthsq(segment a) { return
    sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
⇒   imag(a.b)); }
double length(segment a) { return
→   sqrt(lengthsq(a)); }
// circle methods
double circumference(circle a) { return 2 * a.r
→   * M_PI; }
double area(circle a) { return sq(a.r) * M_PI;
→   }
// rectangle methods
double width(rectangle a) { return
→   abs(real(a.br) - real(a.tl)); }
double height(rectangle a) { return
→   abs(imag(a.br) - imag(a.tl)); }
double diagonal(rectangle a) { return
→   sqrt(sq(width(a)) + sq(height(a))); }
double area(rectangle a) { return width(a) *
→   height(a); }
double perimeter(rectangle a) { return 2 *
→   (width(a) + height(a)); }
// check if `a` fit's inside `b`
// swap equalities to exclude tight fits
bool doesFitInside(rectangle a, rectangle b) {
  int x = width(a), w = width(b), y = height(a),
→   h = height(b);
  if (x > y) swap(x, y);
  if (w > h) swap(w, h);
  if (w < x) return false;
  if (y <= h) return true;
  double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
  return sq(a) <= sq(b) + sq(c);
}
// polygon methods
// negative area = CCW, positive = CW
double area(polygon a) {
```

```cpp
    double area = 0.0; int n = a.points.size();
    for (int i = 0, j = 1; i < n; i++, j = (j +
↪    1) % n)
        area +=
        (real(a.points[j]-a.points[i]))*(imag(a
↪    .points[j]+a.points[i]));
    return area / 2.0;
}
// get both unsigned area and centroid
pair<double, point> area_centroid(polygon a) {
    int n = a.points.size();
    double area = 0;
    point c(0, 0);
    for (int i = n - 1, j = 0; j < n; i = j++) {
        double v = cross(a.points[i], a.points[j]) /
↪    2;
        area += v;
        c += (a.points[i] + a.points[j]) * (v / 3);
    }
    c /= area;
    return {area, c};
}
```

Intersection

```cpp
// -1 coincide, 0 parallel, 1 intersection
int intersection(line a, line b, point& p) {
    if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
        p = cross(b.a - a.a, b.b - a.b) / cross(a.b -
↪    a.a, b.b - b.a) * (b - a) + a;
        return 1;
    }
    if (abs(cross(a.b - a.a, a.b - b.a)) > EPS)
↪    return 0;
    return -1;
}
// area of intersection
double intersection(circle a, circle b) {
    double d = abs(a.c - b.c);
    if (d <= b.r - a.r) return area(a);
    if (d <= a.r - b.r) return area(b);
    if (d >= a.r + b.r) return 0;
    double alpha = acos((sq(a.r) + sq(d) -
↪    sq(b.r)) / (2 * a.r * d));
    double beta = acos((sq(b.r) + sq(d) - sq(a.r))
↪    / (2 * b.r * d));
    return sq(a.r) * (alpha - 0.5 * sin(2 *
↪    alpha)) + sq(b.r) * (beta - 0.5 * sin(2 *
↪    beta));
}
// -1 outside, 0 inside, 1 tangent, 2
↪    intersection
int intersection(circle a, circle b,
↪    vector<point>& inter) {
    double d2 = norm(b.c - a.c), rS = a.r + b.r,
↪    rD = a.r - b.r;
    if (d2 > sq(rS)) return -1;
    if (d2 < sq(rD)) return 0;
    double ca = 0.5 * (1 + rS * rD / d2);
    point z = point(ca, sqrt(sq(a.r) / d2 -
↪    sq(ca)));
    inter.push_back(a.c + (b.c - a.c) * z);
    if (abs(imag(z)) > EPS) inter.push_back(a.c +
↪    (b.c - a.c) * conj(z));
    return inter.size();
}
// points of intersection
vector<point> intersection(line a, circle c) {
    vector<point> inter;
    c.c -= a.a;
    a.b -= a.a;
    point m = a.b * real(c.c / a.b);
    double d2 = norm(m - c.c);
    if (d2 > sq(c.r)) return 0;
    double l = sqrt((sq(c.r) - d2) / norm(a.b));
    inter.push_back(a.a + m + l * a.b);
    if (abs(l) > EPS) inter.push_back(a.a + m - l
↪    * a.b);
    return inter;
}
// area of intersection
```

```cpp
double intersection(rectangle a, rectangle b) {
    double x1 = max(real(a.tl), real(b.tl)), y1 =
↪    max(imag(a.tl), imag(b.tl));
    double x2 = min(real(a.br), real(b.br)), y2 =
↪    min(imag(a.br), imag(b.br));
    return (x2 <= x1 || y2 <= y1) ? 0 :
↪    (x2-x1)*(y2-y1);
}
```

Convex Hull

```cpp
bool cmp(point a, point b) {
    if (abs(real(a) - real(b)) > EPS) return
↪    real(a) < real(b);
    if (abs(imag(a) - imag(b)) > EPS) return
↪    imag(a) < imag(b);
    return false;
}
convex_polygon convexhull(polygon a) {
    sort(a.points.begin(), a.points.end(), cmp);
    vector<point> lower, upper;
    for (int i = 0; i < a.points.size(); i++) {
        while (lower.size() >= 2 &&
            cross(lower.back() - lower[lower.size() -
↪    2], a.points[i] - lower.back()) < EPS)
            lower.pop_back();
        while (upper.size() >= 2 &&
            cross(upper.back() - upper[upper.size() -
↪    2], a.points[i] - upper.back()) > -EPS)
            upper.pop_back();
        lower.push_back(a.points[i]);
        upper.push_back(a.points[i]);
    }
    lower.insert(lower.end(), upper.rbegin() + 1,
↪    upper.rend());
    return convex_polygon(lower);
}
```

8   3D Geometry

```cpp
struct point3d {
    double x, y, z;
    point3d operator+(point3d a) const { return
↪    {x+a.x, y+a.y, z+a.z}; }
    point3d operator*(double a) const { return
↪    {x*a, y*a, z*a}; }
    point3d operator-() const { return {-x, -y,
↪    -z}; }
    point3d operator-(point3d a) const { return
↪    *this + -a; }
    point3d operator/(double a) const { return
↪    *this * (1/a); }
    double norm() { return x*x + y*y + z*z; }
    double abs() { return sqrt(norm()); }
    point3d normalize() { return *this /
↪    this->abs(); }
};
double dot(point3d a, point3d b) { return
↪    a.x*b.x + a.y*b.y + a.z*b.z; }
point3d cross(point3d a, point3d b) { return
    {a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,
↪    a.x*b.y - a.y*b.x}; }
struct line3d { point3d a, b; };
struct plane { double a, b, c, d; } // a*x +
↪    b*y + c*z + d = 0
struct sphere { point3d c; double r; };
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double surface(circle a) { return 4 * sq(a.r) *
↪    M_PI; }
double volume(circle a) { return 4.0/3.0 *
↪    cb(a.r) * M_PI; }
```

9   Optimization

Snoob

```cpp
// SameNumberOfOneBits, next permutation
int snoob(int a) {
```

```cpp
    int b = a & -a, c = a + b;
    return c | ((a ^ c) >> 2) / b;
}
// example usage
int main() {
    char l1[] = {'1', '2', '3', '4', '5'};
    char l2[] = {'a', 'b', 'c', 'd'};
    int d1 = 5, d2 = 4;
    // prints 12345abcd, 1234a5bcd, ...
    int min = (1<<d1)-1, max = min << d2;
    for (int i = min; i <= max; i = snoob(i)) {
        int p1 = 0, p2 = 0, v = i;
        while (p1 < d1 || p2 < d2) {
            cout << ((v & 1) ? l1[p1++] : l2[p2++]);
            v /= 2;
        }
        cout << '\n';
    }
}
```

Powers

```cpp
bool isPowerOf2(ll a) {
    return a > 0 && !(a & a-1);
}
bool isPowerOf3(ll a) {
    return a>0&&!(12157665459056928801ull%a);
}
bool isPower(ll a, ll b) {
    double x = log(a) / log(b);
    return abs(x-round(x)) < 0.00000000001;
}
```

10   Additional

Judge Speed

```cpp
// kattis: 0.50s
// codeforces: 0.421s
// atcoder: 0.455s
#include <bits/stdc++.h>
using namespace std;
int v = 1e9/2, p = 1;
int main() {
    for (int i = 1; i <= v; i++) p *= i;
    cout << p;
}
```

Judge Error Codes

```cpp
// each case tests a different fail condition
// try them before contests to see error codes
struct g { int arr[1000000]; g(){}};
vector<g> a;
// 0=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
↪    6=SIGSEGV 7=recursive MLE
int judge(int n) {
    if (n == 0) exit(0);
    if (n == 1) while(1);
    if (n == 2) while(1) a.push_back(g());
    if (n == 3) while(1) putchar_unlocked('a');
    if (n == 4) assert(0);
    if (n == 5) 0 / 0;
    if (n == 6) *(int*)(0) = 0;
    return n + judge(n + 1);
}
```

GCC Builtin Docs

```cpp
// log2 floor
__lg(n)
// number of 1 bits
// can add ll like popcountll for long longs
__builtin_popcount(n)
// number of trailing zeroes
__builtin_ctz(n)
// number of leading zeroes
__builtin_clz(n)
// 1-indexed least significant 1 bit
__builtin_ffs(n)
// parity of number
__builtin_parity(n)
```

Limits

int	± 2147483647	$\pm 2^{31} - 1$	10^9
uint	4294967295	$2^{32} - 1$	10^9
ll	± 9223372036854775807	$\pm 2^{63} - 1$	10^{18}
ull	18446744073709551615	$2^{64} - 1$	10^{19}
i128	$\pm 170141183460469231...$	$\pm 2^{127} - 1$	10^{38}
u128	$340282366920938463...$	$2^{128} - 1$	10^{38}

Complexity classes input size (per second):

$O(n^n)$ or $O(n!)$	$n \le 10$
$O(2^n)$	$n \le 30$
$O(n^3)$	$n \le 1000$
$O(n^2)$	$n \le 30000$
$O(n\sqrt{n})$	$n \le 10^6$
$O(n \log n)$	$n \le 10^7$
$O(n)$	$n < 10^9$