```
else n = n * 10 + c - '0':
    General
                              6 Graphs
    Algorithms
                              7 2D Geometry
                                                             n = s * (n + m * o):
    Structures
                                  3D Geometry
                                                            void read(double& n) {
    Strings
                                                             ld m; read(m); n = m;
                                  Optimization
    Math
                              10 Additional
                                                            void read(float& n) {
 ld m: read(m): n = m:
    General
                                                            void read(string& s) {
run.sh
                                                             char c; s = "
g++ -g -02 -std=gnu++17 -static prog.cpp
                                                             while((c=getchar unlocked())!=' '&&c!='\n')
./a.exe
test.sh
                                                            bool readline(string& s) {
# compile and test all *.in and *.ans
                                                             char c; s = "";
while(c=getchar unlocked()) {
g++ -g -02 -std=gnu++17 -static prog.cpp for i in *.in; do
                                                              if (c == '\n') return true;
if (c == EOF) return false;
s += c;
.f=${i%.in}
 ./a.exe < $i > "$f.out"
diff -b -q "$f.ans" "$f.out"
                                                             return false;
Header
                                                            void print(unsigned int n) {
// use better compiler options
#pragma GCC optimize("Ofast", "unroll-loops")
                                                             if (n / 10) print(n / 10);
putchar_unlocked(n % 10 + '0');
#pragma GCC target("avx2.fma")
// include everything
                                                            void print(int n) {
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <sys/resource.h>
                                                             if (n < 0) { putchar_unlocked('-'); n*=-1; }
                                                             print((unsigned int)n);
// namespaces
using namespace std;
                                                            Common Structs
using namespace __gnu_cxx; // rope
                                                                n-dimension vectors
using namespace __gnu_pbds; // tree/trie
                                                                Vec<2, int>v(n, m) = arr[n][m]
// common defines
                                                             // Vec<2, int> v(n, m, -1) default init -1
                                                            template<int D, typename T>
#define fastio
                                                            struct Vec : public vector < Vec < D-1, T >> {
\rightarrow \quad ios\_base::sync\_with\_stdio(0);cin.tie(0);\\ \#define\_nostacklim\_rlimit
                                                               template<typename... Args>
                                                               Vec(int n=0, Args... args) : vector<Vec<D-1.
    RZ; getrlimit(3, &RZ); RZ.rlim_cur=-
                                                             \rightarrow T>>(n, Vec<D-1, T>(args...)) {}
    1; setrlimit(3, &RZ);
#define DEBUG(v) cerr<< LINE <<": "<<#v<<" =
                                                            template<typename T>
\Rightarrow "<<v<<'\n'; #define TIMER
                                                            struct Vec<1, T> : public vector<T> {
                                                              Vec(int n=0, T val=T()) : vector<T>(n, val)

    cerr<<1.0*clock()/CLOCKS PER SEC<<"s\n";
</pre>
                                                                {}
#define ll long long
#define ull unsigned ll
#define i128 __int128
#define u128 unsigned i128
                                                                 Algorithms
#define ld long double
                                                            Min/Max Subarray
// global variables
                                                               max - compare = a < b, reset = a < 0
mt19937 rng((uint32 t)chrono::steady
                                                             \frac{1}{min} - compare = a > b, reset = a > 0

    _clock::now().time_since_epoch().count());
                                                            // returns {sum, {start, end}}
pair<int, pair<int, int>>
Fast IO
                                                                 ContiguousSubarray(int* a, int size,
                                                                 bool(*compare)(int, int),
#define getchar_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
                                                             bool(*reset)(int), int defbest = 0) {
int best = defbest, cur = 0, start = 0, end =
                                                             0, s = 0;
for (int i = 0; i < size; i++) {
  cur += a[i];</pre>
void read(unsigned int& n) {
 char c; n = 0;
while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                              if ((*compare)(best, cur)) { best = cur;
  n = n * 10 + c - 0';
                                                             \rightarrow start = s; end = i; }
void read(int& n) {
   char c; n = 0; int s = 1;
   if ((c=getchar_unlocked())=='-') s = -1;
                                                              if ((*reset)(cur)) { cur = 0: s = i + 1: }
                                                             return {best, {start, end}}:
 else n = c - '0';
while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                            Quickselect
 n = n * 10 + c - 0;

n *= s;
                                                            #define QSNE -999999
                                                            int partition(int arr[], int 1, int r)
void read(ld& n) {
 char c; n = 0;
ld m = 0, o = 1; bool d = false; int s = 1;
if ((c=getchar_unlocked())=='-') s = -1;
                                                             int x = arr[r], i = 1;
for (int j = 1; j <= r - 1; j++)
    if (arr[j] <= x)</pre>
 else if (c == .'.') d = true;
else n = c - '0';
                                                               swap(arr[i++], arr[j]);
 while ((c=getchar_unlocked())!=' '&&c!='\n')
                                                             swap(arr[i], arr[r]);
 if (c == '.') d = true;
else if (d) { m=m*10+c-'0'; o*=0.1; }
                                                             return i:
```

```
|// find k'th smallest element in unsorted array,
→ only if all distinct
int gselect(int arr[], int 1, int r, int k)
 if (!(k > 0 && k <= r - l + 1)) return QSNE;
swap(arr[1 + rng() % (r-l+1)], arr[r]);
 int pos = partition(arr, 1, r);
if (pos-l==k-1) return arr[pos];
  if (pos-1>k-1) return qselect(arr,1,pos-1,k);
 return qselect(arr, pos+1, r, k-pos+1-1);
|}
|// TODO: compare against std::nth_element()
Saddleback Search
// search for v in 2d array arr[x][y], sorted
→ on both axis
pair<int, int> saddleback_search(int** arr, int
 \stackrel{\cdot}{\hookrightarrow} x, int y, int v) {
 int i = x-1, j = 0;
while (i >= 0 && j < y) {
  if (arr[i][j] == v) return {i, j};
  (arr[i][i] > v)? i--: i++:
 return {-1, -1}:
 Ternary Search
 // < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {
 while (b-a > 4) {
  int m = (a+b)/2
  if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
  else b = m+1:
  for (int i = a+1; i <= b; i++)
  if (TERNCOMP((*f)(a), (*f)(i)))
 ...a = i;
return a:
#define TERNPREC 0.000001
double ternsearch (double a, double b, double
 \rightarrow (*f)(double)) {
while (b-a > TERNPREC * 4) {
  \frac{\text{double m} = (a+b)/2;}{\text{if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a }} = \frac{\text{int main()}}{\text{int main()}} = \frac{\text{int main()}}{\text{centrate}}
  = m;
else b = m + TERNPREC;
  for (double i = a + TERNPREC; i <= b; i +=
    TERNPREC)
      if (TERNCOMP((*f)(a), (*f)(i)))
    a = i:
 return á;
     Structures
Fenwick Tree
// Fenwick tree, array of cumulative sums -
  \rightarrow O(log n) updates, O(log n) gets
struct Fenwick {
  int n; ll* tree;
  void update(int i, int val) {
  .++i;
  while (i <= n) {
  tree[i] += val;
   i += i & (-i);
  Fenwick(int size) {
  | n = size;
| tree = new | l[n+1];
| for (int i = 1; i <= n; i++)
| tree[i] = 0;
  Fenwick(int* arr, int size) : Fenwick(size) {
  for (int i = 0; i < n; i++)
update(i, arr[i]);
  ~Fenwick() { delete[] tree; }
 11 operator[](int i) {
```

```
.if (i < 0 || i > n) return 0;
.ll sum = 0;
  ++i;
  while (i>0)
  sum += tree[i];
   i = i & (-i);
  return sum:
 ll getRange(int a, int b) { return
operator[](b) - operator[](a-1); };
Hashtable
 // similar to unordered map, but faster
struct chash {
    const uint64_t C = (11)(2e18 * M_PI) + 71;
 ll operator()(ll x) const { return
    builtin bswap64(x*C); }
int main() {
  gp_hash_table<11,int,chash>
 \rightarrow hashtable({},{},{},{},{1<<16});
 for (int i = 0; i < 100; i++)
hashtable[i] = 200+i;
 if (hashtable.find(10) != hashtable.end())
.cout << hashtable[10];</pre>
Ordered Set
typedef tree<int,null_type,less<int>,rb_tree
     tag, tree order statistics node update>
    ordered_set;
 int main()
 ordered_set o_set;
 o set.insert(\overline{5}): o set.insert(1):
 \rightarrow o set.insert(3):
 // get second smallest element
 cout << *(o_set.find_by_order(1)) << '\n';</pre>
 // number of elements less than k=4
 cout << o set.order of key(4) << '\n';
Rope
 // O(\log n) insert, delete, concatenate
 // generate rope
 rope<int> v;
 for (int i = 0; i < 100; i++)
v.push_back(i);</pre>
 // move range to front
 rope<int> copy = v.substr(10, 10);
 v.erase(10, 10):
 v.insert(copy.mutable_begin(), copy);
 // print elements of rope
 for (auto it : v) cout << it << " ";
Segment Tree
 //max(a,b), min(a,b), a+b, a*b, qcd(a,b), a^b
struct SegmentTree {
 typedef int T;
 static constexpr T UNIT = INT_MIN;
 .T f(T a, T b) {
 if (a == UNIT) return b;
if (b == UNIT) return a;
  return max(a,b);
 int n; vector<T> s;
SegmentTree(int n, T def=UNIT) : s(2*n, def),
 → n(n) {}
.SegmentTree(vector<T> arr) :
 → SegmentTree(arr.size()) {
  for (int i=0:i<arr.size():i++)
    update(i,arr[i]);
 void update(int pos, T val) {
  for (s[pos += n] = val; pos /= 2;)
  s[pos] = f(s[pos * 2], s[pos*2+1]);
```

```
T query(int b, int e) { // query [b, e)
  T'ra = UNIT, rb = UNIT;
 for (b+=n, e+=n; b<=; b/=2, e/=2) {
    if (b % 2) ra = f(ra, s[b++]);
    if (e % 2) rb = f(s[--e], rb);
  return f(ra, rb);
T get(int p) { return query(p, p+1); }
};
Trie
typedef trie<string, null_type,

→ trie_string_access_traits<>,

 .pat_trie_tag, trie_prefix_search_node_update>

→ trie_type;

int main() {
 // generate trie
 trie_type trie;
 for (int i = 0; i < 20; i++)
 trie.insert(to_string(i)); // true if new,
\hookrightarrow false if old
 // print things with prefix "1"
 auto range = trie.prefix_range("1");
 for (auto it = range.first; it !=

→ range.second; it++)

  .cout << *it <<
    Strings
Aho Corasick
// range of alphabet for automata to consider
// MAXC = 26, OFFC = 'a' if only lowercase
const int MAXC = 256;
const int OFFC = 0:
struct aho_corasick {
  set<pair<int, int>> out;
 int fail; vector<int> go;
```

```
state() : fail(-1), go(MÁXC, -1) {}
 };
 vector<state> s;
 int id = 0;
 aho_corasick(string* arr, int size) : s(1) {
 for (int i = 0; i < size; i++) {
   int cur = 0;
 ...for (int c : arr[i]) {
...if (s[cur].go[c-OFFC] == -1) {
   s[cur].go[c-OFFC] = s.size();
    .s.push_back(state());
    cur = s[cur].go[c-OFFC];
   s[cur].out.insert({arr[i].size(), id++});
 for (int c = 0; c < MAXC; c++)
...if (s[0].go[c] == -1)
   s[0].go[c] = 0;
 queue<int> sq;
for (int c = 0; c < MAXC; c++) {
   if (s[0].go[c] != 0) {</pre>
  ...s[s[0].go[c]].fail = 0;
    sq.push(s[0].go[c]);
  while (sq.size()) {
  int e = sq.front(); sq.pop();
  for (int c = 0; c < MAXC; c++) {
   if (s[e].go[c] != -1) {
  int failure = s[e].fail;
      while (s[failure].go[c] == -1)
      failure = s[failure].fail;
failure = s[failure].go[c];
      s[s[e].go[c]].fail = failure;
  ....for (auto length : s[failure].out)
.....s[s[e].go[c]].out.insert(length);
....sq.push(s[e].go[c]);
```

```
// list of {start pos. pattern id}
 vector<pair<int. int>> search(string text)
  vector<pair<int, int>> toret:
  int cur = 0;
  for (int i = 0; i < text.size(); i++) {
  while (s[cur].go[text[i]-OFFC] == -1)</pre>
    cur = s[cur].fail;
   cur = s[cur].go[text[i]-OFFC];
   if (s[cur].out.size())
   for (auto end : s[cur].out)
  toret.push_back({i - end.first + 1,
    end.second});
 return toret;
Bover Moore
struct defint { int i = -1; };
vector<int> boyermoore(string txt, string pat)
vector<int> toret; unordered_map<char, defint> Longest Common Prefix (array)
   badchar;
int m = pat.size(), n = txt.size();
for (int i = 0; i < m; i++) badchar[pat[i]].i

\frac{1}{\text{int}} = i;

while (s <= n - m) {
  int j = m - 1;
  while (j \ge 0) \&\& pat[j] == txt[s + j]) j--;
 if (j < 0) {
  toret.push back(s);
   s += (s + m < n) ? m - badchar[txt[s +
   m]].i : 1;
 .} else
  s += max(1, j - badchar[txt[s + j]].i);
return toret:
English Conversion
const string ones[] = {"", "one", "two",
   "three", "four", "five", "six", "seven", "eight", "nine"];
const string teens[] ={"ten", "eleven",
   "twelve", "thirteen", "fourteen",
"fifteen", "sixteen", "seventeen",
"eighteen", "nineteen"};
const string tens[] = {"twenty", "thirty",
    "forty", "fifty", "sixty", "seventy",
   "eighty", "ninety"};
const string mags[] = {"thousand", "million",
    "billion", "trillion", "quadrillion",
    "quintillion", "sextillion",
   "septillion"};
string convert(int num, int carry) {
if (num < 0) return "negative"
    convert(-num, 0);
    (num < 10) réturn ones[num];
if (num < 20) return teens[num % 10];
if (num < 100) return tens[(num / 10) - 2] +
    (num%10==0?"":" ") + ones[num % 10];
    (num < 1000) return ones[num / 100]
    (num/100==0?"":" ") + "hundred" +
    (num%100==0?"":" ") + convert(num % 100,
   0);
return convert(num / 1000, carry + 1) + " " +
    mags[carry] + " " + convert(num % 1000,
   0):
string convert(int num) {
return (num == 0) ? "zero" : convert(num, 0):
Knuth Morris Pratt
```

```
|vector<int> kmp(string txt, string pat) {
    vector<int> toret;
 int m = txt.length(), n = pat.length();
 int next[n + 1];
for (int i = 0; i < n + 1; i++)
   next[i] = 0;</pre>
 for (int i = 1; i < n; i++) {
  int j = next[i + 1];</pre>
  while (j > 0 && pat[j] != pat[i])
   .j = next[j];
  if (j > 0 || pat[j] == pat[i])
next[i + 1] = j + 1;
 for (int i = 0, j = 0; i < m; i++) {
  if (txt[i] == pat[j]) {
   .if (++j == n)
    .toret.push_back(i - j + 1);
  } else if (j > 0) {
   .j = next[i];
 return toret:
 // longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =

  false) {
  if (n == 0) return "";

 if (!sorted) sort(arr, arr + n);
string r = ""; int v = 0;
 while (v < arr[0].length() && arr[0][v] ==
 → arr[n-1][v])
  r += arr[0][v++];
 return r:
Longest Common Subsequence
string lcs(string a, string b) {
 int m = a.length(), n = b.length();
 int L[m+1][n+1];
 for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
        if (i == 0 || j == 0) L[i][j] = 0;
        else if (a[i-1] == b[j-1]) L[i][j] =
    L[i-1][j-1]+1;
   else L[i][j] = \max(L[i-1][j], L[i][j-1]);
 // return L[m][n]; // length of lcs
 string out = "";
int i = m - 1, j = n - 1;
 while (i >= 0 && j >= 0) {
  .if (a[i] == b[j]) {
   out = a[i--] + out:
  else if (L[i][j+1] > L[i+1][j]) i--;
  else j--;
 return out:
Longest Common Substring
// l is array of palindrome length at that
\hookrightarrow index
int manacher(string s, int* 1) {
 int n = s.length() * 2;
 for (int i = 0, j = 0, k; i < n; i += k, j =
 \rightarrow max(j-k, 0)) {
 while (i \ge j \&\& i + j + 1 < n \&\& s[(i-j)/2]
 \Rightarrow == s[(i+j+1)/2]) j++;
 [i] = j;
  for (k = 1; i >= k \&\& i >= k \&\& 1[i-k] !=
 \rightarrow i-k: k++)
 l[i+k] = min(l[i-k], j-k);
 return *max_element(1, 1 + n);
```

```
Subsequence Count
// "banana". "ban" >> 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
int m = subs.length(), n = body.length();
 if (m > n) return 0:
ull** arr = new ull*[m+1];
for (int i = 0; i <= m; i++) arr[i] = new
\hookrightarrow ull[n+1];
\rightarrow subs[i-1])? arr[i-1][j-1] : 0);
return arr[m][n]:
Suffix Array + LCP
struct SuffixArray {
vector<int> sa. lcp:
SuffixArray(string&s, int lim=256) {
 int n = s.length() + 1, k = 0, a, b;
 vector<int> x(begin(s), end(s)+1), y(n),
 ws(max(n, lim)), rank(n);
  sa = `lcp =
  iota(begin(sa), end(sa), 0);
  for (int j = 0, p = 0; p < n; j = max(1, j *
 \rightarrow 2), lim = p) {
  p = j; iota(begin(y), end(y), n - j);
  for (int i = 0; i < (n); i++)
if (sa[i] >= j)
    y[p++] = sa[i] -
   fill(begin(ws), end(ws), 0);
   for (int i = 0; i < (n); i++) ws[x[i]]++;
   for (int i = 1; i < (lim); i++) ws[i] +=
   ws[i - 1];
   for (int i = n; i--;) sa[-ws[x[v[i]]]] =
   v[i];
   swap(x, y); p = 1; x[sa[0]] = 0;
   for (int i = 1; i < (n); i++) {
  a = sa[i - 1]; b = sa[i];
   x[b] = (y[a] = y[b] & x y[a + j] = y[b + j]
   i]) ? p - 1 : p++;
 for (int i = 1; i < (n); i++) rank[sa[i]] =
 for (int i = 0, j; i < n - 1; lcp[rank[i++]]
\rightarrow = k)
  for (k \&\& k--, j = sa[rank[i] - 1];
    s[i + k] == s[j + k]; k++);
String Utilities
void lowercase(string& s) {
transform(s.begin(), s.end(), s.begin(),
void uppercase(string& s) {
transform(s.begin(), s.end(), s.begin(),
\rightarrow ::toupper);
void trim(string &s) {
s.erase(s.begin(),find_if_not(s.begin(),s_
    .end(), [](int c){return
   isspace(c);}));
s.erase(find_if_not(s.rbegin(),s.rend(),[](int

    c){return isspace(c);}).base(),s.end());

vector<string> split(string& s, char token) {
    vector<string> v: stringstream ss(s):
    for (string e;getline(ss,e,token);)
        v.push_back(e);
    return v;
```

```
5 Math
```

```
Catalan Numbers
ull* catalan = new ull[1000000]:
void genCatalan(int n, int mod) {
 catalan[0] = catalan[1] = 1;
catalan[0] - catalan[1] - 1;
for (int i = 2; i <= n; i++) {
   catalan[i] = 0;
   for (int j = i - 1; j >= 0; j--) {
      catalan[i] += (catalan[j] * catalan[i-j-1])
   if (catalan[i] >= mod)
   catalan[i] -= mod;
// TODO: consider binomial coefficient method
```

Combinatorics (nCr, nPr)

```
// can optimize by precomputing factorials, and
\rightarrow fact[n]/fact[n-r]
ull nPr(ull n, ull r) {
 . 11]] v = '
 for (ull i = n-r+1; i <= n; i++)
return v;
ull nPr(ull n, ull r, ull m) {
ull v = 1:
 for (ull i = n-r+1; i <= n; i++)
v = (v * i) \sqrt[n]{m};
return v;
ull nCr(ull n. ull r) {
long double v = 1;
for (ull i = 1; i <= r; i++)
.v = v * (n-r+i) /i;
.return (ull)(v + 0.001);
// requires modulo math
// can optimize by precomputing mfac and
ull nCr(ull n, ull r, ull m) {
return mfac(n, m) * minv(mfac(k, m), m) % m *
\rightarrow minv(mfac(n-k, m), m) % m;
```

Chinese Remainder Theorem

```
bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
mo = mo / d * m[i];
 re %= mo;
re = (re + mo) \% mo;
return true;
```

Count Digit Occurences

```
/*count(n,d) counts the number of occurences of
 \rightarrow a digit d in the range [0,n]*/
11 digit_count(ll n, ll d) {
 11 \text{ result} = 0;
 while (n != 0) {
    result += ((n%10) == d ? 1 : 0);
  n /= 10;
 return result:
11 count(11 n, 11 d) {
    if (n < 10) return (d > 0 && n >= d);
    if ((n % 10) != 9) return digit_count(n, d) +
\hookrightarrow count(n-1, d);
return 10*count(n/10, d) + (n/10) + (d > 0);
```

```
Discrete Logarithm
unordered map<int, int> dlogc;
int discretelog(int a, int b, int m) {
dlogc.clear();
ll n = sqrt(m)+1, an = 1;
for (int i = 0; i < n; i++)
an = (an * a) % m;
 11 c = an:
for (int i = 1; i \le n; i++)
 if (!dlogc.count(c)) dlogc[c] = i;
 c = (c * an) \% m;
c = b;
for (int i = 0; i <= n; i++) {
 if (dlogc.count(c)) return (dlogc[c] * n - i
return -1;
Euler Phi / Totient
int phi(int n) {
 int r = n;
```

```
for (int i = 2; i * i <= n; i++) {
    if (n % i == 0) r -= r / i;
    while (n % i == 0) n /= i;
 if (n > 1) r = r / n;
 return r;
#define n 100000
ll phi[n+1];
void computeTotient() {
 for (int i=1; i<=n; i++) phi[i] = i;
 for (int p=2; p<=n; p++) {
  .if (phi[p] == p) {
   phi[p] = p-1;
for (int i = 2*p; i<=n; i += p) phi[i] =</pre>
     (phi[i]/p) * (p-1);
```

Factorials

```
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
 \rightarrow ME)) + (log10(2 * MPI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
 \hookrightarrow M PI * n) * pow(n / M_E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
```

Prime Factorization

```
// do not call directly
ll pollard rho(ll n. ll s) {
 ll x, y;
x = y = rand() % (n - 1) + 1;
int head = 1, tail = 2;
while (true) {
 while (tide) {
   x = mult(x, x, n);
   x = (x + s) % n;
   if (x == y) return n;
 ll d = _gcd(max(x - y, y - x), n);
if (1 < d && d < n) return d;
  if (++head == tail) y = x, tail <<= 1;
// call for prime factors
void factorize(ll n. vector<ll> &divisor) {
 if (n == 1) return;
 if (isPrime(n)) divisor.push back(n):
```

- 1) + 1);
factorize(n / d, divisor);

factorize(d, divisor);

Josephus Problem

x = a / b * y;

swap(x, y);

return gcd;

```
// 0-indexed, arbitrary k
while (d >= n) d = pollard_rho(n, rand() % (n int josephus(int n, int k) {
                                                   if (n == 1) return 0;
if (k == 1) return n-1;
                                                   if (k > n) return (josephus(n-1,k)+k)%n;
                                                   int res = josephus(n-n/k,k)-n\%k;
                                                   return res + ((res<0)?n:res/(k-1));
```

Greatest Common Denominator

ll egcd(ll a, ll b, ll& x, ll& y) {
 if (b == 0) { x = 1; y = 0; return a; }
 ll gcd = egcd(b, a % b, x, y);

```
Farey Fractions
// generate 0 <= a/b <= 1 ordered, b <= n
   farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
 int h = 0, k = 1, x = 1, y = 0, r;
 vector<pair<int, int>> v;
 v.push back({h, k});
  r = (n-y)/k;
 v += r*k: x += r*h:
 swap(x,h); swap(y,k);
x = -x; y = -y;
} while (k > 1);
 v.push_back(\{1, 1\});
 return v;
Fast Fourier Transform
const double PI = acos(-1):
void fft(vector<cd>& a, bool invert) {
 int n = a.size();
 for (int i = 1, j = 0; i < n; i++) {
  int bit = n >> 
  .int bit = n >> 1;
.for (; j & bit; bit >>= 1) j ^= bit;
  j ^= bit;
                                                      for (int i = n; i > 1; i--)

f = (f * i) % m;

return f;
  if (i < j) swap(a[i], a[j]);
 for (int len = 2; len <= n; len <<= 1) {
    double ang = 2 * PI / len * (invert ? -1 :
                                                      // if m is not quaranteed to be prime
                                                     ll minv(ll b, ll m) {
                                                      11 x = 0, y' = 0;
  cd wlen(cos(ang), sin(ang));
                                                      if (egcd(b, m, x, y) != 1) return -1;
  for (int i = 0; i < n; i += len) {
                                                      return (x % m + m) % m;
   .cd w(1):
   for (int j = 0; j < len / 2; j++) {
                                                      11 mdiv_compmod(int a, int b, int m) {
    cd u = a[i+j], v = a[i+j+len/2] * w;
                                                      if (__gcd(b, m) != 1) return -1;
    a[i+j] = u + v;
a[i+j+len/2] = u - v;
                                                      return mult(a, minv(b, m), m);
    .w *= wlen:
                                                      // if m is prime (like 10^9+7)
                                                     11 mdiv primemod (int a, int b, int m) {
                                                      return mult(a, mpow(b, m-2, m), m);
 if (invert)
  for (auto& x : a)
                                                      Miller-Rabin Primality Test
vector<int> fftmult(vector<int> const& a,
                                                      // Miller-Rabin primality test - O(10 log^3 n)
                                                      bool isPrime(ull n) {
 → vector<int> const& b) {
 vector<cd> fa(a.begin(), a.end()),

→ fb(b.begin(), b.end());
int n = 1 << (32 - _builtin_clz(a.size() +

→ b.size() - 1));
fa.resize(n); fb.resize(n);
 fft(fa. false): fft(fb. false)
 for (int i = 0; i < n; i++) fa[i] *= fb[i];
 fft(fa. true):
 vector<int> toret(n);
 for (int i = 0; i < n; i++) toret[i] =
cound(fa[i].real());
return toret;
                                                      .}
.return true:
```

oool isfrime(uli n) { if (n < 2) return false; if (n == 2) return true; if (n % 2 == 0) return false; ull s = n - 1; while (s % 2 == 0) s /= 2; for (int i = 0; i < 10; i++) { ull temp = s: ull a = rand() % (n - 1) + 1; ull mod = mpow(a, temp, n); while (temp!=n-1&&mod!=1&&mod!=n-1) { mod = mult(mod, mod, n); temp *= 2; if (mod!=n-1&&temp%2==0) return false;

Sieve of Eratosthenes

```
bitset<100000001> sieve;
// generate sieve - O(n \log n)
void genSieve(int n) {
void gensleve(int in )
sieve[0] = sieve[1] = 1;
for (ull i = 3; i * i < n; i += 2)
    if (!sieve[i])
        for (ull j = i * 3; j <= n; j += i * 2)</pre>
   ..sieve[i] = 1:
^{\prime}// query sieve after it's generated - O(1)
bool quervSieve(int n) {
return n == 2 || (n % 2 != 0 && !sieve[n]);
```

```
// fast case if k=2, traditional josephus
int josephus(int n) {
return 2*(n-(1<<(32-builtin clz(n)-1)));
Least Common Multiple
#define lcm(a,b) ((a*b)/qcd(a,b))
Modulo Operations
```

#define MOD 1000000007 #define madd(a,b,m) (a+b-((a+b-m>=0)?m:0)) #define mult(a,b,m) ((ull)a*b%m)#define msub(a,b,m) (a-b+((a<b)?m:0))ll mpow(ll b, ll e, ll m) { .11 x = 1; while (e > 0) { if (e % 2) x = (x * b) % m; b = (b * b) % m; e /= 2; return x % m; ull mfac(ull n, ull m) { ull f = 1;

```
.for (int sat = 0; sat < m; sat++) {
. if (sat == cur) continue;</pre>
Simpson's / Approximate Integrals
// integrate f from a to b, k iterations

// error <= (b-a)/18.0 * M * ((b-a)/2k)^4

// where M = max(abs(f^{```}(x))) for x in [a,b]

// "f" is a function "double func(double x)"
                                                                 double num = a[sat][i] / a[cur][i];
                                                                 for (int sot = 0; sot <= n; sot++)
a[sat][sot] -= a[cur][sot] * num;
                                                                ćur++;
double Simpsons(double a, double b, int k,
                                                               break;

    double (*f)(double)) {
    double dx = (b-a)/(2.0*k), t = 0;
    for (int i = 0; i < k; i++)
    t + = ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
}
</pre>
                                                            for (int j = cur; j < m; j++)
\leftrightarrow (*f)(a+(2*i+1)*dx);
                                                             if (!zero(a[i][n])) return vector<double>():
return (t + (*f)(b)) * (b-a) / 6.0 / k;
                                                            vector<double> ans(n,0);
                                                            for (int i = 0, sat = 0; i < n; i++)
    if (sat < m && !zero(a[sat][i]))
    ans[i] = a[sat][n] / a[sat++][i];
    return ans;
Common Equations Solvers
// ax^2 + bx + c = 0, find x
vector < double > solve Eq (double a, double b,
                                                           Graycode Conversions

    double c) {
    vector < double > r;
}
                                                           ull graycode2ull(ull n) {
 double z = b * b - 4 * a * c;
if (z == 0)
                                                                ull i = 0;
for (; n; n = n >> 1) i ^= n;
return i;
 r.push_back(-b/(2*a));
 else if (z > 0) {
  r.push_back((sqrt(z)-b)/(2*a));
                                                           ull ull2graycode(ull n) {
  r.push_back((sqrt(z)+b)/(2*a));
                                                                return \tilde{n} (n >> 1);
 return r;
\frac{1}{2} // ax^3 + bx^2 + cx + d = 0, find x
                                                                Graphs
                                                           struct edge {
vector < double > solve Eq (double a, double b,
                                                            int u, v, w;

    double c, double d) {
    vector < double > res;
}

                                                            edge (int u,int v,int w) : u(u),v(v),w(w) {}
                                                            edge (): u(0), v(0), w(0) {}
 long double a1 = b/a, a2 = c/a, a3 = d/a;
 long double q = (a1*a1 - 3*a2)/9.0, sq =
                                                           bool operator < (const edge &e1, const edge
\rightarrow -2*sqrt(q);
                                                            \rightarrow &e2) { return e1.w < e2.w: }
 long double r = (2*a1*a1*a1 - 9*a1*a2 +
                                                           bool operator > (const edge &e1, const edge
\rightarrow 27*a3)/54.0;
long double z = r*r-q*q*q, theta;
                                                           \rightarrow &e2) { return e1.w > e2.w; }
                                                           struct subset { int p, rank; };
 if (z \le 0) {
  theta = acos(r/sqrt(q*q*q));
                                                           Eulerian Path
  res.push_back(sq*cos(theta/3.0) - a1/3.0);
                                                           #define edge_list vector<edge>
#define adj sets vector<set<int>>
 res.push_back(sq*cos((theta+2.0*PI)/3.0) -
\rightarrow a1/3.0);
                                                           struct EulerPathGraph {
 res.push back(sq*cos((theta+4.0*PI)/3.0) -
                                                            adj_sets graph; // actually indexes incident
\rightarrow a1/3.0);
                                                            edge_list edges; int n; vector<int> indeg;
 else {
                                                            EulerPathGraph(int n): n(n) {
 res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
                                                             indeg = *(new vector<int>(n,0));
 res[0] = (res[0] + q / res[0]) * ((r<0)?1:-1)
                                                             graph = *(new adj_sets(n, set<int>()));
\rightarrow - a1 / 3.0:
 return res;
                                                            void add_edge(int u, int v) {
                                                              graph[u].insert(edges.size());
// linear diophantine equation ax + by = c,
                                                             indeg[v]++;
\hookrightarrow find x and y
                                                              edges.push_back(edge(u,v,0));
// infinite solutions of form x+k*b/g, y-k*a/g bool solveEq(ll a, ll b, ll c, ll &x, ll &y, ll
                                                            bool eulerian_path(vector<int> &circuit) {
                                                             if(edges.size()==0) return false;
g = egcd(abs(a), abs(b), x, y);
                                                              stack<int> st;
                                                             int a[] = {-1};
for(int v=0;v<n;v++) {
   if(indeg[v]!=graph[v].size()) {</pre>
 if (c % g) return false;
 x *= c / g * ((a < 0) ? -1 : 1);
 y *= c / g * ((b < 0) ? -1 : 1);
                                                               bool b = indeg[v] > graph[v].size();
 return true;
                                                               if (abs(((int)indeg[v])-((int)graph[v]
// m = # equations, n = # variables, a[m][n+1]
                                                                .size())) > 1) return
\rightarrow = coefficient matrix
                                                               false
// a[i][0]x + a[i][1]y + ... + a[i][n]z =
                                                               if (a[b] != -1) return false;
                                                             a[b] = v;
\hookrightarrow a[i][n+1]
const double eps = 1e-7;
bool zero(double a) { return (a < eps) && (a >
                                                             int s = (a[0]!=-1 \&\& a[1]!=-1 ? a[0] :
\rightarrow -eps); }
                                                               (a[0]=-1 \&\& a[1]=-1 ? edges[0].u : -1));
vector < double > solve Eq (double **a, int m, int
                                                             if(s==-1) return false:
\hookrightarrow n) {
                                                              while(!st.empty() || !graph[s].empty()) {
int cur = 0;
for (int i = 0; i < n; i++) {
                                                              if (graph[s].empty()) {
for (int j = cur; j < m; j++) {
                                                                circuit.push_back(s); s = st.top();
...if (!zero(a[j][i])) {
                                                               st.pop(); }
... if (j != cur) swap(a[j], a[cur]);
                                                              else {
```

```
int w = edges[*graph[s].begin()].v;
    graph[s].erase(graph[s].begin());
    st.push(s); s = w:
  circuit.push_back(s);
  return circuit.size()-1==edges.size();
Minimum Spanning Tree
// returns vector of edges in the mst
// graph[i] = vector of edges incident to
    vertex i
   places total weight of the mst in Stotal
// if returned vector has size != n-1, there is
vector<edge> mst(vector<vector<edge>> graph.
 total = 0;
 priority_queue<edge, vector<edge>,

→ greater<edge>> pq;

 vector<edge> MST;
 bitset<20001> marked; // change size as needed
 marked[0] = 1;
 for (edge ep : graph[0]) pq.push(ep);
while(MST.size()!=graph.size()-1 &&
   pq.size()!=0) {
  edge e = pq.top(); pq.pop();
  int u = e.u, v = e.v, w = e.w;
if(marked[u] && marked[v]) continue;
  else if(marked[u]) swap(u, v);
  for(edge ep : graph[u]) pq.push(ep);
marked[u] = 1;
  MST.push_back(e);
  total += e.w;
 return MST:
Union Find
int uf_find(subset* s, int i) {
  if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
 return s[i].p;
void uf union(subset* s. int x. int v) {
 int xp = uf_find(s, x), yp = uf_find(s, y);
if (s[xp].rank > s[yp].rank) s[yp].p = xp;
else if (s[xp].rank < s[yp].rank) s[xp].p =</pre>
 else { s[yp].p = xp; s[xp].rank++; }
     2D Geometry
#define point complex<double>
#define EPS 0.0000001
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double dot(point a, point b) { return

    real(conj(a)*b);
}
double cross(point a, point b) { return
\rightarrow imag(conj(a)*b); }
struct line { point a, b; };
struct circle { point c; double r; };
struct segment { point a, point b; };
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
struct convex_polygon {
 vector<point points:
 convex polygon(vector<point> points) :
 → points(points) {}
 convex_polygon(triangle a) {
  points.push_back(a.a); points.push_back(a.b);
   points.push_back(a.c);
 convex_polygon(rectangle a) {
  points.push_back(a.tl);
    points.push_back({real(a.tl),
    imag(a.br)});
```

```
points.push_back(a.br);
    points.push_back({real(a.br),
    imag(a.tl)}):
struct polygon {
vector <point > points;
 polygon(vector<point> points) : points(points)
polygon(triangle a) {
 points.push_back(a.a); points.push_back(a.b);
   points.push back(a.c):
 polygon(rectangle a) {
 points.push_back(a.tl);
   points.push back({real(a.tl),
   imag(a.br)});
 points.push_back(a.br);
   points.push back({real(a.br),
    imag(a.tl)});
polygon(convex_polygon a) {
  for (point v : a.points)
   points.push_back(v);
   triangle methods
double area_heron(double a, double b, double c)
if (a < b) swap(a, b);
if (a < c) swap(a, c);
if (b < c) swap(b, c);
if (a > b + c) return -1;
return sqrt((a+b+c)*(c-a+b)*(c+a-b)*(a+b-c)
   /16.0):
// seament methods
double lengthsq(segment a) { return
    sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
\stackrel{\longrightarrow}{\Rightarrow} imag(a.b)); }
double length(segment a) { return

    sgrt(lengthsq(a)); }

// circle methods
double circumference(circle a) { return 2 * a.r
→ * M_PI; }
double area(circle a) { return sq(a.r) * M PI;
\stackrel{\hookrightarrow}{//} rectangle methods
double width(rectangle a) { return

    abs(real(a.br) - real(a.tl)); }

double height (rectangle a) { return

    abs(imag(a.br) - real(a.tl)); }

double diagonal (rectangle a) { return
   sqrt(sq(width(a)) + sq(height(a))); }
double area (rectangle a) { return width(a) *
   height(a); }
double perimeter(rectangle a) { return 2 *
   (width(a) + height(a)); }
   check if `a` fit's inside `b
// swap equalities to exclude tight fits
bool doesFitInside(rectangle a, rectangle b) {
int x = width(a), w = width(b), y = height(a).
\hookrightarrow h = height(b);
if (x > y) swap(x, y);
 if (w > h) swap(w, h);
 if (w < x) return false;
 if (y <= h) return true;
 double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
return sq(a) \le sq(b) + sq(c);
// polygon methods
// negative area = CCW, positive = CW
double area(polygon a) {
```

```
double area = 0.0; int n = a.points.size();
                                                       double intersection (rectangle a, rectangle b) {| int b = a & -a, c = a + b;
                                                                                                              return c | ((a^ c) >> 2) / b:
  for (int i = 0, j = 1; i < n; i++, j = (j +
                                                        double x1 = max(real(a.tl), real(b.tl)), y1 =
    1) % n)
                                                           max(imag(a.tl), imag(b.tl)):
                                                                                                                // example usage
                                                        double x2 = min(real(a.br), real(b.br)), y2 =
                                                                                                              int main() {
   char l1[] = {'1', '2', '3', '4', '
   char l2[] = {'a', 'b', 'c', 'd'};
   int d1 = 5, d2 = 4;
   // prints 12345abcd, 1234a5bcd, ...
    (real(a.points[j]-a.points[i]))*(imag(a)
                                                           min(imag(a.br), imag(b.br));
    .points[j]+a.points[i]));
                                                        return (x2 \le x1 \mid | y2 \le y1) ? 0 :
  return area / 2.0;
                                                           (x2-x1)*(y2-y1);
// get both unsigned area and centroid
                                                                                                                int min = (1<<d1)-1, max = min << d2;</pre>
pair double, point area_centroid(polygon a) { Convex Hull
                                                                                                               for (int i = min; i < = max; i = snoob(i)) {
   int p1 = 0, p2 = 0, v = i;
   while (p1 < d1 || p2 < d2) {
      cout << ((v & 1) ? 11[p1++] : 12[p2++]);
 int n = a.points.size();
                                                       bool cmp(point a, point b) {
 double area = 0;
point c(0, 0);
                                                        if (abs(real(a) - real(b)) > EPS) return
                                                           real(a) < real(b);
                                                        if (abs(imag(a) - imag(b)) > EPS) return
 for (int i = n - 1, j = 0; j < n; i = j++) {
                                                                                                                 .v /= 2;
 double v = cross(a.points[i], a.points[j]) /
                                                           imag(a) < imag(b);</pre>
                                                                                                                cout << '\n':

→ 2;

                                                        return false:
  area += v:
  c += (a.points[i] + a.points[j]) * (v / 3);
                                                       convex_polygon convexhull(polygon a) {
                                                                                                               Powers
                                                        sort(a.points.begin(), a.points.end(), cmp);
 c /= area:
                                                                                                               bool isPowerOf2(ll a) {
                                                        vector<point> lower, upper;
 return {area, c};
                                                                                                               return a > 0 && !(a & a-1):
                                                        for (int i = 0; i < a.points.size(); i++) {</pre>
                                                         while (lower.size() >= 2 &&
                                                                                                              bool isPowerOf3(11 a) {
return a>0&&!(12157665459056928801u11%a);
Intersection
                                                            cross(lower.back() - lower[lower.size()
// -1 coincide, 0 parallel, 1 intersection
                                                            2], a.points[i] - lower.back()) < EPS)
int intersection(line a, line b, point& p) {
  if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
                                                          lower.pop_back();
                                                                                                              bool isPower(ll a, ll b) {
  double x = log(a) / log(b);
                                                         while (upper.size() >= 2 &&
 p = cross(b.a - a.a, b.b - a.b) / cross(a.b)
                                                                                                               return abs(x-round(x)) < 0.00000000001:
                                                            cross(upper.back() - upper[upper.size() -
\rightarrow a.a, b.b - b.a) * (b - a) + a:
                                                           2], a.points[i] - upper.back()) > -EPS)
  return 1:
                                                                                                              10 Additional
                                                          upper.pop_back();
                                                         lower.push_back(a.points[i]);
 if (abs(cross(a.b - a.a. a.b - b.a)) > EPS)
                                                                                                              Judge Speed

→ return 0:

                                                         upper.push back(a.points[i]);
                                                                                                                 kattis: 0.50s
 return -1;
                                                                                                                 codeforces: 0.421s
                                                        lower.insert(lower.end(), upper.rbegin() + 1,
                                                                                                              // atcoder: 0.455s
// area of intersection
                                                           upper.rend());
                                                                                                              #include <bits/stdc++.h>
double intersection(circle a, circle b) {
                                                        return convex_polygon(lower);
                                                                                                              using namespace std;
 double d = abs(a.c - b.c):
                                                                                                              int v = 1e9/2, p = 1;
if (d = b.r - a.r) return area(a);
if (d <= a.r - b.r) return area(b);
if (d >= a.r + b.r) return 0;
                                                                                                              int main() {
                                                            3D Geometry
                                                                                                                   for (int i = 1; i <= v; i++) p *= i;
                                                                                                                   cout << p:
                                                       struct point3d {
 double alpha = acos((sq(a.r)' + sq(d) -
                                                        double x, y, z;
\rightarrow sq(b.r)) / (2 * a.r * d));
                                                        point3d operator+(point3d a) const { return
                                                                                                              Judge Error Codes
 double beta = acos((sq(b.r) + sq(d) - sq(a.r))
                                                           \{x+a.x, y+a.y, z+a.z\}; \}
                                                                                                               // each case tests a different fail condition
\rightarrow / (2 * b.r. * d))
                                                        point3d operator*(double a) const { return
                                                                                                               // try them before contests to see error codes
return sq(a.r) * (alpha - 0.5 * sin(2 *
                                                                                                              struct g { int arr[1000000]; g(){}}:
                                                           \{x*a, v*a, z*a\}: \}
    alpha)) + sq(b.r) * (beta - 0.5 * sin(2 *
                                                        point3d operator-() const { return {-x, -y,
                                                                                                              vector<g> a;
                                                                                                               // O=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
    beta));
                                                        \rightarrow -z}; }
                                                                                                                   6=SIGSEGV 7=recursive MLE
                                                        point3d operator-(point3d a) const { return
// -1 outside, 0 inside, 1 tangent, 2
                                                                                                                   judge(int n) {
                                                        \rightarrow *this + -a; }
                                                                                                               if (n == 0) exit(0);

if (n == 1) while(1);

if (n == 2) while(1) a.push_back(g());

if (n == 3) while(1) putchar_unlocked('a');
int intersection(circle a. circle b.
                                                        point3d operator/(double a) const { return
→ vector<point>& inter) {
                                                         \rightarrow *this * (1/a); }
                                                        double norm() { return x*x + y*y + z*z; }
 double d2 = norm(b.c - a.c), rS = a.r + b.r,
                                                        double abs() { return sqrt(norm()); }
                                                                                                               if (n == 4) assert(0);
if (n == 5) 0 / 0;
if (n == 6) *(int*)(0) = 0;
\hookrightarrow rD = a.r - b.r;
                                                        point3d normalize() { return *this /
 if (d2 > sq(rS)) return -1;
 if (d2 < sq(rD)) return 0;
                                                           this->abs(): }
 double ca = 0.5 * (1 + rS * rD / d2);
                                                                                                               return n + judge(n + 1);
 point z = point(ca, sqrt(sq(a.r) / d2 -
                                                       double dot(point3d a, point3d b) { return
\rightarrow sq(ca)));
                                                        \rightarrow a.x*b.x + a.y*b.y + a.z*b.z; }
                                                                                                              Limits
 inter.push back(a.c + (b.c - a.c) * z);
                                                       point3d cross(point3d a, point3d b) { return
                                                                                                                                  \pm 2147483647 \mid \pm 2^{31} - 1 \mid 10^9
                                                                                                              int
 if (abs(imag(z)) > EPS) inter.push_back(a.c +
                                                           \{a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,
                                                                                                                                                      \overline{2^{32}} - \overline{1|10^9}
                                                                                                                                    4294967295
                                                                                                              uint
\rightarrow (b.c - a.c) * conj(z));
                                                           a.x*b.y - a.y*b.x; }
                                                                                                                      \pm 9223372036854775807 | \pm \overline{2}^{63} - 1 | \overline{10}^{18}
 return inter.size();
                                                       struct line3d { point3d a, b; };
                                                                                                                                                      2^{64} - 1|10^{19}
                                                                                                              ull
                                                                                                                      18446744073709551615
                                                       struct plane { double a, b, c, d; } // a*x +
// points of intersection
                                                                                                                     |\pm 170141183460469231...|\pm 2^{\overline{1}27} - 1|10^{38}
                                                        \rightarrow b*y + c*z + d = 0
vector<point> intersection(line a. circle c) {
                                                       struct sphere { point3d c; double r; };
#define sq(a) ((a)*(a))
                                                                                                                                                    2^{128} - 1 | 10^{38}
vector<point> inter;
c.c -= a.a;
a.b -= a.a;
                                                                                                              |u128| 340282366920938463...|
                                                                                                              Complexity classes input size (per second):
                                                       #define cb(a) ((a)*(a)*(a))
 point m = a.b * real(c.c / a.b);
                                                       double surface(circle a) { return 4 * sq(a.r)
                                                                                                              |O(n^n)| or O(n!)
                                                                                                                                                             n < 10
 double d2 = norm(m - c.c);
                                                                                                              O(2^n)
                                                                                                                                                             n < 30
 if (d2 > sq(c.r)) return 0;
                                                       double volume(circle a) { return 4.0/3.0 *
 double l = sqrt((sq(c.r) - d2) / norm(a.b));
                                                                                                              |O(n^3)|
                                                                                                                                                          n < 1000
                                                        \rightarrow cb(a.r) * M PI; }
 inter.push_back(a.a + m + 1 * a.b);
                                                                                                              O(n^2)
                                                                                                                                                         n < 30000
                                                            Optimization
 if (abs(1) > EPS) inter.push_back(a.a + m - 1
                                                                                                              O(n\sqrt{n})
                                                                                                                                                            n < 10^{6}
\rightarrow * a.b);
return inter;
                                                                                                              O(n \log n)
                                                                                                                                                           n \le 10^7
                                                       // SameNumberOfOneBits, next permutation
}
// area of intersection
                                                       int snoob(int a) {
                                                                                                              |O(n)|
                                                                                                                                                            n < 10^9
```