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## General

# Header

```
// use better compiler options
#pragma GCC optimize("Ofast","unroll-loops")
#pragma GCC target("avx2,fma")
// include everything
#include <bits/stdc++.h>
#include <bits/extc++.h>
#include <svs/resource.h>
// namespaces
using namespace std;
using namespace gnu cxx; // rope
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio ios_base::sync_with_stdio(0);
\hookrightarrow cin.tie(0);
#define nostacklim rlimit RZ;getrlimit(3,&RZ);
→ RZ.rlim cur=-1:setrlimit(3.&RZ):
#define DEBUG(v) cout<<"DEBUG: "<<#v<<" = "<<v | }</pre>
\hookrightarrow <<' \n';
#define 11 long long
#define ull unsigned ll
#define i128 __int128
#define u128 unsigned i128
#define ld long double
// global variables
mt19937 rng((uint32_t)chrono::steady_clock::
→ now().time since epoch().count());
```

## Fast IO

```
void readn(unsigned int& n) {
char c: n = 0:
while ((c = getchar unlocked()) != ' ' && c
\hookrightarrow != '\n'
 n = n * 10 + c - '0':
void readn(int& n) {
char c; n = 0; int s = 1;
if ((c = getchar_unlocked()) == '-') s = -1;
else n = c - '0';
```

```
while ((c = getchar_unlocked()) != ' ' && c
\hookrightarrow != '\n')
 n = n * 10 + c - 0;
n *= s;
void readn(long double& n) {
char c: n = 0:
long double m = 0, o = 1; bool d = false; int
\hookrightarrow s = 1:
if ((c = getchar_unlocked()) == '-') s = -1;
else if (c == '.') d = true;
 else n = c - 0:
while ((c = getchar_unlocked()) != ' ' && c
 \hookrightarrow != '\n')
 if (c == '.') d = true:
 else if (d) { m = m * 10 + c - '0'; o *=
 \hookrightarrow 0.1: }
 else n = n * 10 + c - '0':
n = s * (n + m * o):
void readn(double& n) {
long double m: readn(m): n = m:
void readn(float& n) {
long double m; readn(m); n = m;
void readn(string& s) {
char c: s = "":
while((c = getchar_unlocked()) != ' ' && c !=
s += c:
bool readline(string& s) {
char c; s = "";
while(c = getchar unlocked()) {
 if (c == '\n') return true;
 if (c == EOF) return false;
 s += c:
return false;
void printn(unsigned int n) {
if (n / 10) printn(n / 10);
putchar unlocked(n % 10 + '0');
void printn(int n) {
if (n < 0) { putchar_unlocked('-'); n *= -1;</pre>
printn((unsigned int)n);
```

# 2 Algorithms

```
Min/Max Subarray
// max subarray - compare = a < b, reset = a <
// min subarray - compare = a > b, reset = a >
// returns {sum, {start, end}}
pair<int, pair<int, int>> ContiguousSubarray(

    bool(*reset)(int), int defbest = 0) {

 int best = defbest, cur = 0, start = 0, end = #define TERNCOMP(a,b) (a)<(b)
 \hookrightarrow 0, s = 0;
```

if ((\*compare)(best, cur)) { best = cur;

if ((\*reset)(cur)) { cur = 0; s = i + 1; }

for (int i = 0; i < size; i++) {</pre>

 $\hookrightarrow$  start = s; end = i; }

return {best, {start, end}};

# Quickselect

cur += a[i]:

```
#define QSNE -999999
int partition(int arr[], int 1, int r)
int x = arr[r], i = 1;
for (int j = 1; j <= r - 1; j++)
 if (arr[j] <= x)
 swap(arr[i++], arr[j]);
 swap(arr[i]. arr[r]):
return i;
// find k'th smallest element in unsorted
int quickselect(int arr[], int 1, int r, int k
\hookrightarrow )
if (!(k > 0 \&\& k \le r - 1 + 1)) return QSNE;
 swap(arr[l + rng() % (r-l+1)], arr[r]);
 int pos = partition(arr, 1, r);
if (pos-l == k-1) return arr[pos];
if (pos-l > k-1) return quickselect(arr, l,
 \hookrightarrow pos-1, k);
 return quickselect(arr, pos+1, r, k-pos+l-1);
// TODO: compare against std::nth_element()
```

## Saddleback Search

```
// search for v in 2d array arr[x][y], sorted
→ on both axis
pair<int, int> saddleback_search(int** arr,
\hookrightarrow int x, int y, int v) {
```

```
int i = x-1, j = 0;
while (i >= 0 && j < v) {
if (arr[i][j] == v) return {i, j};
 (arr[i][j] > v)? i--: j++;
return {-1, -1}:
```

## Ternary Search

```
→ int* a, int size, bool(*compare)(int, int), // < for max, > for min, or any other unimodal

    func

                                                 int ternary search(int a, int b, int (*f)(int)
                                                 → ) {
                                                  while (b-a > 4) {
                                                   int m = (a+b)/2:
                                                   if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
                                                   else b = m+1:
                                                  for (int i = a+1; i <= b; i++)</pre>
                                                   if (TERNCOMP((*f)(a), (*f)(i)))
                                                  return a;
                                                 #define TERNPREC 0.000001
                                                 double ternary_search(double a, double b,

    double (*f)(double)) {
                                                  while (b-a > TERNPREC * 4) {
                                                   double m = (a+b)/2;
                                                   if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
                                                   \hookrightarrow = m:
                                                   else b = m + TERNPREC:
                                                  for (double i = a + TERNPREC; i <= b; i +=</pre>

→ TERNPREC)

                                                      if (TERNCOMP((*f)(a), (*f)(i)))
                                                   a = i:
                                                  return a;
```

## Data Structures

## Fenwick Tree

```
// Fenwick tree, array of cumulative sums - 0(
\hookrightarrow log n) updates, O(log n) gets
struct Fenwick {
int n; ll* tree;
void update(int i, int val) {
 ++i:
 while (i \le n) {
  tree[i] += val:
  i += i & (-i);
 }
}
```

```
Fenwick(int size) {
 n = size:
 tree = new ll[n+1]:
 for (int i = 1; i <= n; i++)</pre>
  tree[i] = 0:
 Fenwick(int* arr, int size) : Fenwick(size) {
 for (int i = 0; i < n; i++)</pre>
  update(i, arr[i]);
 ~Fenwick() { delete[] tree: }
11 operator[](int i) {
 if (i < 0 || i > n) return 0;
 11 \text{ sum} = 0;
 ++i:
 while (i>0) {
  sum += tree[i];
  i -= i & (-i):
 return sum;
11 getRange(int a, int b) { return operator
}:
```

## Hashtable

```
// similar to unordered_map, but faster
struct chash {
const uint64_t C = (11)(2e18 * M_PI) + 71;
11 operator()(11 x) const { return
⇒ builtin bswap64(x*C); }
}:
int main() {
gp hash table<11,int,chash> hashtable
 for (int i = 0; i < 100; i++)</pre>
 hashtable[i] = 200+i;
if (hashtable.find(10) != hashtable.end())
 cout << hashtable[10];</pre>
```

# Ordered Set

```
typedef tree<int,null_type,less<int>,
\hookrightarrow rb tree tag,

→ tree_order_statistics_node_update>

→ ordered set;
int main()
   ordered set o set:
   o set.insert(5); o set.insert(1); o set.
   \hookrightarrow insert(3);
   // get second smallest element
   cout << *(o set.find by order(1)) << '\n';</pre>
```

```
// number of elements less than k=4
cout << o_set.order_of_key(4) << '\n';</pre>
```

# Rope

```
// O(log n) insert, delete, concatenate
int main() {
// generate rope
rope<int> v:
for (int i = 0; i < 100; i++)</pre>
 v.push back(i);
// move range to front
rope<int> copy = v.substr(10, 10);
v.erase(10, 10):
v.insert(copy.mutable begin(), copy);
// print elements of rope
for (auto it : v)
 cout << it << " ":
```

## Trie

```
typedef trie<string, null_type,</pre>

→ trie string access traits<>.

 pat_trie_tag, trie_prefix_search_node_update
 → > trie_type;
int main() {
// generate trie
trie type trie;
for (int i = 0: i < 20: i++)
 trie.insert(to_string(i)); // true if new,

→ false if old

// print things with prefix "1"
auto range = trie.prefix_range("1");
for (auto it = range.first; it != range.
\hookrightarrow second: it++)
 cout << *it << " ":
```

# 4 String

## Aho Corasick

```
// range of alphabet for automata to consider
// MAXC = 26, OFFC = 'a' if only lowercase
→ letters
const int MAXC = 256:
const int OFFC = 0;
struct aho corasick {
 struct state
 set<pair<int, int>> out;
```

```
int fail; vector<int> go;
state() : fail(-1), go(MAXC, -1) {}
vector<state> s:
int id = 0:
aho_corasick(string* arr, int size) : s(1) { };
for (int i = 0; i < size; i++) {</pre>
 int cur = 0:
 for (int c : arr[i]) {
  if (s[cur].go[c-OFFC] == -1) {
   s[curl.go[c-OFFC] = s.size():
   s.push_back(state());
  }
  cur = s[cur].go[c-OFFC]:
 s[cur].out.insert({arr[i].size(), id++});
for (int c = 0; c < MAXC; c++)
 if (s[0].go[c] == -1)
  s[0].go[c] = 0;
queue<int> sa:
for (int c = 0; c < MAXC; c++) {</pre>
 if (s[0].go[c] != 0) {
  s[s[0].go[c]].fail = 0;
  sq.push(s[0].go[c]);
}
while (sq.size()) {
 int e = sq.front(); sq.pop();
 for (int c = 0; c < MAXC; c++) {</pre>
  if (s[e].go[c] != -1) {
   int failure = s[e].fail:
   while (s[failure].go[c] == -1)
     failure = s[failure].fail:
   failure = s[failure].go[c];
   s[s[e].go[c]].fail = failure;
   for (auto length : s[failure].out)
    s[s[e].go[c]].out.insert(length);
   sq.push(s[e].go[c]);
  }
 }
}
// list of {start pos, pattern id}
vector<pair<int, int>> search(string text)
vector<pair<int, int>> toret;
int cur = 0;
for (int i = 0; i < text.size(); i++) {</pre>
 while (s[cur].go[text[i]-OFFC] == -1)
  cur = s[cur].fail;
 cur = s[cur].go[text[i]-OFFC];
```

```
if (s[cur].out.size())
 for (auto end : s[cur].out)
  toret.push_back({i - end.first + 1, end.

    second});
}
return toret:
```

# **Boyer Moore**

```
struct defint { int i = -1; };
vector<int> boyermoore(string txt, string pat)
\hookrightarrow {
vector<int> toret; unordered map<char, defint
→ > badchar:
int m = pat.size(), n = txt.size();
for (int i = 0; i < m; i++) badchar[pat[i]].i</pre>
\hookrightarrow = i:
int s = 0;
while (s \le n - m) {
 int i = m - 1:
 while (i \ge 0 \&\& pat[i] == txt[s + i]) i--;
 if (j < 0) {
  toret.push back(s):
  s += (s + m < n) ? m - badchar[txt[s + m]].

    i : 1:

 } else
  s += max(1, j - badchar[txt[s + j]].i);
return toret;
```

## **English Conversion**

```
const string ones[] = {"", "one", "two", "

→ three", "four", "five", "six", "seven", "
\hookrightarrow eight", "nine"};
const string teens[] ={"ten", "eleven", "

→ twelve", "thirteen", "fourteen", "fifteen",

→ "sixteen". "seventeen". "eighteen". "
const string tens[] = {"twenty", "thirty", "
→ forty", "fifty", "sixty", "seventy", "
const string mags[] = {"thousand", "million".
→ "billion", "trillion", "quadrillion", "
string convert(int num, int carry) {
if (num < 0) return "negative " + convert(-</pre>
\hookrightarrow num. 0):
if (num < 10) return ones[num]:
if (num < 20) return teens[num % 10]:
if (num < 100) return tens[(num / 10) - 2] +

    (num%10==0?"":" ") + ones[num % 10]:
if (num < 1000) return ones[num / 100] + (num</pre>
\hookrightarrow /100==0?"":" ") + "hundred" + (num%100==0?
return convert(num / 1000, carrv + 1) + " " +
```

```
  mags[carry] + " " + convert(num % 1000,
  0);
}
string convert(int num) {
  return (num == 0) ? "zero" : convert(num, 0);
}
```

## **Knuth Morris Pratt**

```
vector<int> kmp(string txt, string pat) {
   vector<int> toret:
int m = txt.length(), n = pat.length();
int next[n + 1]:
 for (int i = 0; i < n + 1; i++)
 next[i] = 0:
 for (int i = 1; i < n; i++) {</pre>
 int j = next[i + 1];
 while (j > 0 && pat[j] != pat[i])
 j = next[i];
 if (j > 0 || pat[j] == pat[i])
  next[i + 1] = i + 1;
for (int i = 0, j = 0; i < m; i++) {
 if (txt[i] == pat[j]) {
  if (++j == n)
   toret.push_back(i - j + 1);
 } else if (i > 0) {
  i = next[i];
  i--:
return toret:
```

# Longest Common Prefix

# Longest Common Subsequence

```
string lcs(string a, string b) {
  int m = a.length(), n = b.length();

int L[m+1][n+1];
  for (int i = 0; i <= m; i++) {
    for (int j = 0; j <= n; j++) {
      if (i == 0 || j == 0) L[i][j] = 0;
      else if (a[i-1] == b[j-1]) L[i][j] = L[i</pre>
```

## Longest Common Substring

# Subsequence Count

# Math

## Combinatorics (nCr, nPr)

and fact[n]/fact[n-r]

ull nPr(ull n. ull r) {

```
ull v = 1:
for (ull i = n-r+1; i <= n; i++)</pre>
 v *= i:
 return v;
ull nPr(ull n, ull r, ull m) {
ull v = 1:
for (ull i = n-r+1: i <= n: i++)
 v = (v * i) % m;
return v:
ull nCr(ull n. ull r) {
long double v = 1:
for (ull i = 1: i <= r: i++)</pre>
 v = v * (n-r+i) /i:
 return (ull)(v + 0.001);
// requires modulo math
// can optimize by precomputing mfac and minv-
```

// can optimize by precomputing factorials,

# Chinese Remainder Theorem

ull nCr(ull n. ull r. ull m) {

 $\hookrightarrow$  minv(mfac(n-k, m), m) % m;

return mfac(n, m) \* minv(mfac(k, m), m) % m \*

```
x = (r[i] - re) / d * x % (m[i] / d);
re += x * mo;
mo = mo / d * m[i];
re %= mo;
}
re = (re + mo) % mo;
return true;
}
```

# Count Digit Occurences

## Discrete Logarithm

# Euler Phi / Totient

```
int phi(int n) {
  int r = n;
  for (int i = 2; i * i <= n; i++) {</pre>
```

```
if (n % i == 0) r -= r / i;
 while (n \% i == 0) n /= i;
if (n > 1) r = r / n;
return r:
#define n 100000
11 phi[n+1];
void computeTotient() {
   for (int i=1: i<=n: i++) phi[i] = i:</pre>
   for (int p=2; p<=n; p++) {</pre>
       if (phi[p] == p) {
           phi[p] = p-1;
           for (int i = 2*p; i<=n; i += p) phi</pre>
           \hookrightarrow [i] = (phi[i]/p) * (p-1);
       }
   }
```

## **Factorials**

```
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
\hookrightarrow M E)) + (log10(2 * M PI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
\hookrightarrow M PI * n) * pow(n / M E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
```

## Prime Factorization

```
// do not call directly
ll pollard rho(ll n, ll s) {
11 x, y;
x = y = rand() \% (n - 1) + 1;
int head = 1, tail = 2;
 while (true) {
 x = mult(x, x, n);
 x = (x + s) \% n;
 if (x == v) return n:
 11 d = _{-gcd(max(x - y, y - x), n)};
 if (1 < d && d < n) return d:
 if (++head == tail) y = x, tail <<= 1;</pre>
}
// call for prime factors
void factorize(ll n. vector<ll> &divisor) {
if (n == 1) return:
if (isPrime(n)) divisor.push_back(n);
 else {
 11 d = n;
 while (d >= n) d = pollard_rho(n, rand() % (
 \hookrightarrow n - 1) + 1):
 factorize(n / d. divisor):
```

```
factorize(d, divisor);
Farev Fractions
```

```
// generate 0 <= a/b <= 1 ordered, b <= n
// farev(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
 int h = 0, k = 1, x = 1, y = 0, r;
 vector<pair<int, int>> v;
 do {
 v.push_back({h, k});
 r = (n-v)/k:
 v += r*k: x += r*h:
 swap(x,h); swap(y,k);
 x = -x; y = -y;
 } while (k > 1);
 v.push back({1, 1});
 return v:
```

#### Fast Fourier Transform

```
#define cd complex<double>
const double PI = acos(-1):
void fft(vector<cd>& a, bool invert) {
int n = a.size():
for (int i = 1, i = 0; i < n; i++) {
 int bit = n >> 1;
 for (: i & bit: bit >>= 1) i ^= bit:
 i ^= bit:
 if (i < j) swap(a[i], a[j]);</pre>
for (int len = 2: len <= n: len <<= 1) {
 double ang = 2 * PI / len * (invert ? -1 :
 \hookrightarrow 1):
 cd wlen(cos(ang), sin(ang));
 for (int i = 0; i < n; i += len) {</pre>
  cd w(1):
  for (int j = 0; j < len / 2; j++) {
   cd u = a[i+j], v = a[i+j+len/2] * w;
   a[i+i] = u + v:
   a[i+j+len/2] = u - v;
   w *= wlen:
  }
 }
if (invert)
 for (auto& x : a)
  x /= n;
```

```
vector<int> fftmult(vector<int> const& a.

    vector<int> const& b) {
vector<cd> fa(a.begin(), a.end()), fb(b.begin |}
 \hookrightarrow (), b.end()):
 int n = 1 << (32 - _builtin_clz(a.size() + b | if (_gcd(b, m) != 1) return -1;
 \hookrightarrow .size() - 1)):
 fa.resize(n); fb.resize(n);
 fft(fa, false); fft(fb, false);
 for (int i = 0: i < n: i++) fa[i] *= fb[i]:
fft(fa, true);
 vector<int> toret(n):
 for (int i = 0; i < n; i++) toret[i] = round( Miller-Rabin Primality Test
 \hookrightarrow fa[i].real()):
return toret;
```

## Greatest Common Denominator

```
ll egcd(ll a. 11 b. 11& x. 11& v) {
if (b == 0) { x = 1; y = 0; return a; }
ll gcd = egcd(b, a \% b, x, y);
x -= a / b * v:
swap(x, y);
return gcd:
```

## Least Common Multiple

```
#define lcm(a,b) ((a*b)/ gcd(a,b))
```

## Modulo Operations

```
#define MOD 1000000007
#define madd(a,b,m) (a+b-((a+b-m>=0)?m:0))
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a<b)?m:0))
ll mpow(ll b. ll e. ll m) {
11 x = 1:
while (e > 0) {
 if (e \% 2) x = (x * b) \% m;
 b = (b * b) \% m:
 e /= 2:
return x % m;
ull mfac(ull n, ull m) {
n11 f = 1:
for (int i = n; i > 1; i--)
 f = (f * i) % m:
return f:
// if m is not guaranteed to be prime
ll minv(ll b, ll m) {
```

```
11 x = 0, y = 0;
 if (egcd(b, m, x, y) != 1) return -1;
 return (x % m + m) % m:
11 mdiv compmod(int a, int b, int m) {
 return mult(a, minv(b, m), m);
// if m is prime (like 10^9+7)
11 mdiv primemod (int a, int b, int m) {
return mult(a, mpow(b, m-2, m), m);
```

```
// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
if (n < 2) return false:
if (n == 2) return true;
if (n % 2 == 0) return false;
ull s = n - 1:
while (s \% 2 == 0) s /= 2:
for (int i = 0: i < 10: i++) {
 ull temp = s:
 ull a = rand() \% (n - 1) + 1;
 ull mod = mpow(a, temp, n);
 while (temp != n - 1 && mod != 1 && mod != n

→ - 1) {

  mod = mult(mod, mod, n):
  temp *= 2:
 if (mod != n - 1 && temp % 2 == 0) return
 \hookrightarrow false;
}
return true:
```

## Sieve of Eratosthenes

```
bitset<100000001> sieve:
// generate sieve - O(n log n)
void genSieve(int n) {
sieve[0] = sieve[1] = 1;
for (ull i = 3; i * i < n; i += 2)</pre>
 if (!sieve[i])
 for (ull j = i * 3; j <= n; j += i * 2)
   sieve[j] = 1;
// query sieve after it's generated - 0(1)
bool querySieve(int n) {
return n == 2 || (n % 2 != 0 && !sieve[n]);
```

## Simpson's / Approximate Integrals

```
// integrate f from a to b, k iterations
// \text{ error} \le (b-a)/18.0 * M * ((b-a)/2k)^4
// where M = \max(abs(f''(x))) for x in [a,b]
// "f" is a function "double func(double x)"
double Simpsons(double a, double b, int k,

    double (*f)(double)) {
double dx = (b-a)/(2.0*k), t = 0;
 for (int i = 0; i < k; i++)</pre>
 t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 * (*f)(|const|double|eps = 1e-7;
 \hookrightarrow a+(2*i+1)*dx):
return (t + (*f)(b)) * (b-a) / 6.0 / k:
```

## Common Equations Solvers

```
// ax^2 + bx + c = 0, find x
vector<double> solveEq(double a, double b.
\hookrightarrow double c) {
vector<double> r;
 double z = b * b - 4 * a * c:
if (z == 0)
 r.push_back(-b/(2*a));
 else if (z > 0) {
 r.push_back((sqrt(z)-b)/(2*a));
 r.push back((sqrt(z)+b)/(2*a)):
return r;
// ax^3 + bx^2 + cx + d = 0, find x
vector<double> solveEq(double a, double b,
\hookrightarrow double c, double d) {
vector<double> res:
long double a1 = b/a, a2 = c/a, a3 = d/a;
long double q = (a1*a1 - 3*a2)/9.0, sq = -2*
 \hookrightarrow sart(a):
long double r = (2*a1*a1*a1 - 9*a1*a2 + 27*a3)
 \hookrightarrow )/54.0:
long double z = r*r-q*q*q, theta:
 if (z \le 0) {
 theta = acos(r/sqrt(q*q*q));
 res.push_back(sq*cos(theta/3.0) - a1/3.0);
 res.push back(sq*cos((theta+2.0*PI)/3.0) -
  \hookrightarrow a1/3.0):
 res.push back(sq*cos((theta+4.0*PI)/3.0) -
  \hookrightarrow a1/3.0):
 else {
 res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
 res[0] = (res[0] + q / res[0]) * ((r<0)
```

```
\hookrightarrow ?1:-1) - a1 / 3.0;
 return res:
// m = # equations, n = # variables, a[m][n+1]
// a[i][0]x + a[i][1]y + ... + a[i][n]z = a[i]
→ ][n+1]
bool zero(double a) { return (a < eps) && (a >
vector<double> solveEq(double **a, int m, int
 int cur = 0;
 for (int i = 0: i < n: i++) {</pre>
  for (int j = cur; j < m; j++) {</pre>
  if (!zero(a[j][i])) {
    if (j != cur) swap(a[j], a[cur]);
    for (int sat = 0; sat < m; sat++) {</pre>
    if (sat == cur) continue;
    double num = a[sat][i] / a[cur][i];
    for (int sot = 0; sot <= n; sot++)</pre>
     a[sat][sot] -= a[cur][sot] * num:
    cur++:
   break:
  }
  }
 for (int j = cur; j < m; j++)
  if (!zero(a[j][n])) return vector<double>();
 vector<double> ans(n.0):
 for (int i = 0, sat = 0; i < n; i++)</pre>
  if (sat < m && !zero(a[sat][i]))</pre>
  ans[i] = a[sat][n] / a[sat++][i];
 return ans:
     Graph
Setup
struct edge {
    edge (int u, int v, int w) : u(u), v(v), w(
    \hookrightarrow w) \{\}
    edge (): u(0), v(0), w(0) {}
```

```
bool operator < (const edge &e1, const edge &
```

```
\hookrightarrow e2) { return e1.w < e2.w; }
bool operator > (const edge &e1, const edge &
\hookrightarrow e2) { return e1.w > e2.w: }
struct subset { int p, rank; };
Eulerian Path
#define edge list vector<edge>
#define adj sets vector<set<int>>
struct EulerPathGraph {
 adj sets graph; // actually indexes incident
 → edges
 edge_list edges; int n; vector<int> indeg;
 EulerPathGraph(int n): n(n) {
 indeg = *(new vector<int>(n.0));
 graph = *(new adj sets(n, set<int>()));
 void add edge(int u, int v) {
 graph[u].insert(edges.size());
 indeg[v]++:
 edges.push_back(edge(u,v,0));
 bool eulerian path(vector<int> &circuit) {
 if(edges.size()==0) return false;
 stack<int> st;
  int a[] = \{-1, -1\}:
  for(int v=0;v<n;v++) {</pre>
  if(indeg[v]!=graph[v].size()) {
   bool b = indeg[v] > graph[v].size();
   if (abs(((int)indeg[v])-((int)graph[v].size
   \hookrightarrow ())) > 1) return false:
   if (a[b] != -1) return false;
   a[b] = v;
  int s = (a[0]!=-1 \&\& a[1]!=-1 ? a[0] : (a
  \hookrightarrow [0]==-1 && a[1]==-1 ? edges[0].u : -1));
  if(s==-1) return false;
  while(!st.empty() || !graph[s].empty()) {
  if (graph[s].empty()) { circuit.push back(s
  \hookrightarrow ); s = st.top(); st.pop(); }
  else {
   int w = edges[*graph[s].begin()].v;
    graph[s].erase(graph[s].begin());
```

st.push(s): s = w:

}

```
circuit.push_back(s);
 return circuit.size()-1==edges.size();
};
```

# Minimum Spanning Tree

```
// returns vector of edges in the mst
// graph[i] = vector of edges incident to

→ vertex i

// places total weight of the mst in &total
// if returned vector has size != n-1, there
vector<edge> mst(vector<vector<edge>> graph.
→ 11 &total) {
   total = 0:
   priority_queue<edge, vector<edge>, greater<</pre>

→ edge>> pq;

   vector<edge> MST;
   bitset<20001> marked; // change size as
   \hookrightarrow needed
   marked[0] = 1:
   for (edge ep : graph[0]) pq.push(ep);
   while(MST.size()!=graph.size()-1 && pq.size
   \hookrightarrow ()!=0) {
        edge e = pq.top(); pq.pop();
       int u = e.u. v = e.v. w = e.w:
       if(marked[u] && marked[v]) continue;
       else if(marked[u]) swap(u, v);
       for(edge ep : graph[u]) pq.push(ep);
       marked[u] = 1;
       MST.push back(e):
       total += e.w:
   return MST:
```

## Union Find

```
int uf find(subset* s, int i) {
if (s[i], p != i) s[i], p = uf find(s, s[i], p):
return s[i].p;
void uf union(subset* s, int x, int y) {
int xp = uf find(s, x), vp = uf find(s, v);
if (s[xp].rank > s[yp].rank) s[yp].p = xp;
else if (s[xp].rank < s[yp].rank) s[xp].p =</pre>
else { s[vp].p = xp; s[xp].rank++; }
```