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1 General

```
run.sh
g++ -g -O2 -std=gnu++17 -static prog.cpp
./a.exe

test.sh
# compile and test all *.in and *.ans
g++ -g -O2 -std=gnu++17 -static prog.cpp
for i in *.in; do
    f=${i%.in}
    ./a.exe < $i > "$f.out"
    diff -b -q "$f.ans" "$f.out"
done

Header
// use better compiler options
#pragma GCC optimize("Ofast", "unroll-loops")
#pragma GCC target("avx2,fma")
// include everything
#include <bits/stdc++.h>
#include <bits/unistd.h>
#include <sys/resource.h>
// namespaces
using namespace std;
using namespace __gnu_cxx; // rope
using namespace __gnu_pbds; // tree/trie
// common defines
#define fastio
    ↪ ios_base::sync_with_stdio(0); cin.tie(0);
#define nostacklim rlimit RZ; getrlimit(3, &RZ)
    ↪ ); RZ.rlim_cur = -1; setrlimit(3, &RZ);
#define DEBUG(v) cerr<<__LINE__<<": "<<#v<<" =
    ↪ "<<v<<'\n';
#define TIMER
    ↪ cerr<<1.0*clock()/CLOCKS_PER_SEC<<"s\n";
#define ll long long
#define ull unsigned ll
#define i128 __int128
#define ui128 unsigned i128
#define ld long double
// global variables
mt19937 rng((uint32_t) chrono::steady)
    ↪ _clock::now().time_since_epoch().count());
```

Fast IO

```
#ifdef _WIN32
#define getch_unlocked() _getchar_nolock()
#define putchar_unlocked(x) _putchar_nolock(x)
#endif
void read(unsigned int& n) {
    char c; n = 0;
    while ((c = getch_unlocked()) != ' ' && c != '\n')
        n = n * 10 + c - '0';
}
void read(int& n) {
    char c; n = 0; int s = 1;
    if ((c = getch_unlocked()) == '-') s = -1;
    else n = c - '0';
    while ((c = getch_unlocked()) != ' ' && c != '\n') {
        n = n * 10 + c - '0';
        n *= s;
    }
}
void read(ld& n) {
    char c; n = 0;
    ld m = 0, o = 1; bool d = false; int s = 1;
    if ((c = getch_unlocked()) == '-') s = -1;
    else if (c == '.') d = true;
    else n = c - '0';
    while ((c = getch_unlocked()) != ' ' && c != '\n') {
        if (c == '.') d = true;
        else if (d) { m = m * 10 + c - '0'; o *= 0.1; }
    }
}
```

```
    else n = n * 10 + c - '0';
}
n = s * (n + m * o);
}
void read(double& n) {
    ld m; read(m); n = m;
}
void read(float& n) {
    ld m; read(m); n = m;
}
void read(string& s) {
    char c; s = "";
    while ((c = getch_unlocked()) != ' ' && c != '\n')
        s += c;
}
bool readline(string& s) {
    char c; s = "";
    while (c = getch_unlocked()) {
        if (c == '\n') return true;
        if (c == EOF) return false;
        s += c;
    }
    return false;
}
void print(unsigned int n) {
    if (n / 10) print(n / 10);
    putchar_unlocked(n % 10 + '0');
}
void print(int n) {
    if (n < 0) { putchar_unlocked('-'); n *= -1; }
    print((unsigned) n);
}
```

Common Structs

```
// n-dimension vectors
// Vec<2, int> v(n, m) = arr[n][m]
// Vec<2, int> v(n, m, -1) default init -1
template<int D, typename T>
struct Vec : public vector<Vec<D-1, T>> {
    template<typename... Args>
    Vec(int n=0, Args... args) : vector<Vec<D-1,
        ↪ T>>(n, Vec<D-1, T>(args...)) {}
};
template<typename T>
struct Vec<1, T> : public vector<T> {
    Vec(int n=0, T val=T()) : vector<T>(n, val)
    ↪ {}
};
```

2 Algorithms

Min/Max Subarray

```
// max - compare = a < b, reset = a < 0
// min - compare = a > b, reset = a > 0
// returns {sum, {start, end}}
pair<int, pair<int, int>>
    ContiguousSubarray(int* a, int size,
    ↪ bool(*compare)(int, int),
    ↪ bool(*reset)(int), int defbest = 0) {
    int best = defbest, cur = 0, start = 0, end =
    ↪ 0, s = 0;
    for (int i = 0; i < size; i++) {
        cur += a[i];
        if ((*compare)(best, cur)) { best = cur;
        ↪ start = s; end = i; }
        if ((*reset)(cur)) { cur = 0; s = i + 1; }
    }
    return {best, {start, end}};
}
```

Quickselect

```
#define QSNE -999999
int partition(int arr[], int l, int r)
{
    int x = arr[r], j = l;
    for (int i = l; i <= r - 1; j++)
        if (arr[j] <= x)
            swap(arr[i++], arr[j]);
    swap(arr[j], arr[r]);
    return j;
}
```

```
// find k'th smallest element in unsorted array
    ↪ only if all distinct
int qselect(int arr[], int l, int r, int k)
{
    if (!k > 0 && k <= r - l + 1) return QSNE;
    swap(arr[l + rng() % (r-l+1)], arr[r]);
    int pos = partition(arr, l, r);
    if (pos-1 == k-1) return arr[pos];
    if (pos-1 > k-1) return qselect(arr, l, pos-1, k);
    return qselect(arr, pos+1, r, k-pos+1-1);
}
// TODO: compare against std::nth_element()
```

Saddleback Search

```
// search for v in 2d array arr[x][y], sorted
    ↪ on both axis
pair<int, int> saddleback_search(int** arr, int
    ↪ x, int y, int v) {
    int i = x-1, j = 0;
    while (i >= 0 && j < y) {
        if (arr[i][j] == v) return {i, j};
        (arr[i][j] > v)? i--: j++;
    }
    return {-1, -1};
}
```

Ternary Search

```
// < max, > min, or any other unimodal func
#define TERNCOMP(a,b) (a)<(b)
int ternsearch(int a, int b, int (*f)(int)) {
    while (b-a > 4) {
        int m = (a+b)/2;
        if (TERNCOMP((*f)(m), (*f)(m+1))) a = m;
        else b = m+1;
    }
    for (int i = a+1; i <= b; i++)
        if (TERNCOMP((*f)(a), (*f)(i)))
            a = i;
    return a;
}
#define TERNPREC 0.000001
double ternsearch(double a, double b, double
    ↪ (*f)(double)) {
    while (b-a > TERNPREC * 4) {
        double m = (a+b)/2;
        if (TERNCOMP((*f)(m), (*f)(m + TERNPREC))) a
        ↪ = m;
        else b = m + TERNPREC;
    }
    for (double i = a + TERNPREC; i <= b; i +=
    ↪ TERNPREC)
        if (TERNCOMP((*f)(a), (*f)(i)))
            a = i;
    return a;
}
```

```
return a;
}
```

3 Structures

Fenwick Tree

```
// Fenwick tree, array of cumulative sums -
    ↪ O(log n) updates, O(log n) gets
struct Fenwick {
    int n; ll* tree;
```

```
void update(int i, int val) {
    ++i;
    while (i <= n) {
        tree[i] += val;
        i += i & (-i);
    }
}
Fenwick(int size) {
    n = size;
    tree = new ll[n+1];
    for (int i = 1; i <= n; i++)
        tree[i] = 0;
}
Fenwick(int* arr, int size) : Fenwick(size) {
    for (int i = 0; i < n; i++)
        update(i, arr[i]);
}
Fenwick() { delete[] tree; }
ll operator[](int i) {
    if (i < 0 || i > n) return 0;
    ll sum = 0;
    ++i;
    while (i > 0) {
        sum += tree[i];
        i -= i & (-i);
    }
    return sum;
}
ll getRange(int a, int b) { return
    ↪ operator[](b) - operator[](a-1); }
};
```

Hashtable

```
// similar to unordered_map, but faster
struct chash {
    const uint64_t C = (1ll)(2e18 * M_PI) + 71;
    ll operator()(ll x) const { return
    ↪ __builtin_bswap64(x*C); }
};
int main() {
    gp_hash_table<ll, int, chash>
    ↪ hashtable({}, {}, {}, {}, {1<16});
    for (int i = 0; i < 100; i++)
        hashtable[i] = 200+i;
    if (hashtable.find(10) != hashtable.end())
        cout << hashtable[10];
}
```

Ordered Set

```
template <typename T>
using oset = tree<T, null_type, less<T>, rb_tree
    ↪ tag, tree_order_statistics_node_update>;
template <typename T, typename D>
using omap = tree<T, D, less<T>, rb_tree
    ↪ tag, tree_order_statistics_node_update>;
int main()
{
    oset<int> o_set;
    o_set.insert(5); o_set.insert(1);
    ↪ o_set.insert(3);
    // get second smallest element
    cout << *(o_set.find_by_order(1));
    // number of elements less than k=4
    cout << ' ' << o_set.order_of_key(4) << '\n';
    // equivalent with ordered map
    omap<int, int> o_map;
    o_map[5]=1; o_map[1]=2; o_map[3]=3;
    cout << (*(o_map.find_by_order(1))).first;
    cout << ' ' << o_map.order_of_key(4) << '\n';
}
```

Rope

```
// O(log n) insert, delete, concatenate
int main() {
    // generate rope
    rope<int> v;
    for (int i = 0; i < 100; i++)
        v.push_back(i);
    // move range to front
    rope<int> copy = v.substr(10, 10);
    v.erase(10, 10);
```

```

v.insert(copy.mutable_begin(), copy);
// print elements of rope
for (auto it : v)
    cout << it << " ";
}

Segment Tree
//max(a,b), min(a,b), a+b, a*b, gcd(a,b), a^b
struct SegmentTree {
    typedef int T;
    static constexpr T UNIT = INT_MIN;
    T f(T a, T b) {
        if (a == UNIT) return b;
        if (b == UNIT) return a;
        return max(a, b);
    }
    int n; vector<T> s;
    SegmentTree(int n, T def=UNIT) : s(2*n, def),
        n(n) {}
    SegmentTree(vector<T> arr) :
        SegmentTree(arr.size()) {
        for (int i=0; i<arr.size(); i++)
            update(i, arr[i]);
    }
    void update(int pos, T val) {
        for (s[pos += n] = val; pos /= 2;)
            s[pos] = f(s[pos * 2], s[pos*2+1]);
    }
    T query(int b, int e) { // query [b, e)
        T ra = UNIT, rb = UNIT;
        for (b+=n, e+=n; b<e; b/=2, e/=2) {
            if (b % 2) ra = f(ra, s[b++]);
            if (e % 2) rb = f(s[--e], rb);
        }
        return f(ra, rb);
    }
    T get(int p) { return query(p, p+1); }
};

Trie
typedef trie<string, null_type,
    trie_string_access_traits<,
    pat_trie_tag, trie_prefix_search_node_update>
    trie_type;
int main() {
    // generate trie
    trie_type trie;
    for (int i = 0; i < 20; i++)
        trie.insert(to_string(i)); // true if new,
    // false if old
    // print things with prefix "1"
    auto range = trie.prefix_range("1");
    for (auto it = range.first; it !=
        range.second; it++)
        cout << *it << " ";
}

Wavelet Tree
using iter = vector<int>::iterator;
struct WaveletTree {
    Vec<2, int> C; int s;
    WaveletTree(vector<int>& a, int sigma) :
        s(sigma), C(sigma*2, 0) {
        build(a.begin(), a.end(), 0, s-1, 1);
    }
    void build(iter b, iter e, int L, int U, int
        u) {
        if (L == U) return;
        int M = (L+U)/2;
        C[u].reserve(e-b+1); C[u].push_back(0);
        for (auto it = b; it != e; ++it)
            C[u].push_back(C[u].back() + (*it<=M));
        auto p = stable_partition(b, e, [=](int
            i){return i<=M;});
        build(b, p, L, M, u*2);
        build(p, e, M+1, U, u*2+1);
    }
    // number of occurrences of x in [0, i)
    int rank(int x, int i) {
        int L = 0, U = s-1, u = 1, M, r;

```

```

        while (L != U) {
            M = (L+U)/2;
            r = C[u][i]; u*=2;
            if (x <= M) i = r, U = M;
            else i -= r, L = M+1, ++u;
        }
        return i;
    }
    // number of occurrences of x in [l, r)
    int count(int x, int l, int r) {
        return rank(x, r) - rank(x, l);
    }
    // kth smallest in [l, r)
    int kth(int k, int l, int r) const {
        int L = 0, U = s-1, u = 1, M, ri, rj;
        while (L != U) {
            M = (L+U)/2;
            ri = C[u][l]; rj = C[u][r]; u*=2;
            if (k <= rj-ri) l = ri, r = rj, U = M;
            else k -= rj-ri, l -= ri, r -= rj,
                L = M+1, ++u;
        }
        return U;
    }
    // # elements between [x, y] in [l, r)
    mutable int L, U;
    int range(int x, int y, int l, int r) const {
        if (y < x or r <= l) return 0;
        L = x; U = y;
        return range(l, r, 0, s-1, 1);
    }
    int range(int l, int r, int x, int y, int u)
        const {
        if (y < L or U < x) return 0;
        if (L <= x and y <= U) return r-l;
        int M = (x+y)/2, ri = C[u][l], rj = C[u][r];
        return range(ri, rj, x, M, u*2) + range(l-ri,
            r-rj, M+1, y, u*2+1);
    }
    // # elements <= x in [l, r)
    int lte(int x, int l, int r) {
        return range(INT_MIN, x, l, r);
    }
};

4 Strings
Aho Corasick
// range of alphabet for automata to consider
// MAXC = 26, OFFC = 'a' if only lowercase
const int MAXC = 256;
const int OFFC = 0;
struct aho_corasick {
    struct state
    {
        set<pair<int, int>> out;
        int fail; vector<int> go;
        state() : fail(-1), go(MAXC, -1) {}
    };
    vector<state> s;
    int id = 0;
    aho_corasick(string* arr, int size) : s(1) {
        for (int i = 0; i < size; i++) {
            int cur = 0;
            for (int c : arr[i]) {
                if (s[cur].go[c-OFFC] == -1) {
                    s[cur].go[c-OFFC] = s.size();
                    s.push_back(state());
                }
                cur = s[cur].go[c-OFFC];
            }
            s[cur].out.insert({arr[i].size(), id++});
        }
        for (int c = 0; c < MAXC; c++)
            if (s[0].go[c] == -1)
                s[0].go[c] = 0;
        queue<int> sq;
        for (int c = 0; c < MAXC; c++) {
            if (s[0].go[c] != 0) {
                s[s[0].go[c]].fail = 0;
                sq.push(s[0].go[c]);
            }

```

4 Strings

Aho Corasick

```

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// MAXC = 26, OFFC = 'a' if only lowercase
const int MAXC = 256;
const int OFFC = 0;
struct aho_corasick {
    struct state
    {
        set<pair<int, int>> out;
        int fail; vector<int> go;
        state() : fail(-1), go(MAXC, -1) {}
    };
    vector<state> s;
    int id = 0;
    aho_corasick(string* arr, int size) : s(1) {
        for (int i = 0; i < size; i++) {
            int cur = 0;
            for (int c : arr[i]) {
                if (s[cur].go[c-OFFC] == -1) {
                    s[cur].go[c-OFFC] = s.size();
                    s.push_back(state());
                }
                cur = s[cur].go[c-OFFC];
            }
            s[cur].out.insert({arr[i].size(), id++});
        }
        for (int c = 0; c < MAXC; c++)
            if (s[0].go[c] == -1)
                s[0].go[c] = 0;
        queue<int> sq;
        for (int c = 0; c < MAXC; c++) {
            if (s[0].go[c] != 0) {
                s[s[0].go[c]].fail = 0;
                sq.push(s[0].go[c]);
            }

```

```

        }
        while (sq.size()) {
            int e = sq.front(); sq.pop();
            for (int c = 0; c < MAXC; c++) {
                if (s[e].go[c] != -1) {
                    int failure = s[e].fail;
                    while (s[failure].go[c] == -1)
                        failure = s[failure].fail;
                    failure = s[failure].go[c];
                    s[s[e].go[c]].fail = failure;
                    for (auto length : s[failure].out)
                        s[s[e].go[c]].out.insert(length);
                    sq.push(s[e].go[c]);
                }
            }
        }
    }
    // list of {start pos, pattern id}
    vector<pair<int, int>> search(string text)
    {
        vector<pair<int, int>> toret;
        int cur = 0;
        for (int i = 0; i < text.size(); i++) {
            while (s[cur].go[text[i]-OFFC] == -1)
                cur = s[cur].fail;
            cur = s[cur].go[text[i]-OFFC];
            if (s[cur].out.size())
                for (auto end : s[cur].out)
                    toret.push_back({i - end.first + 1,
                        end.second});
        }
        return toret;
    }
};

Boyer Moore
struct definit { int i = -1; };
vector<int> boyer_moore(string txt, string pat)
{
    vector<int> toret; unordered_map<char, definit>
    badchar;
    int m = pat.size(), n = txt.size();
    for (int i = 0; i < m; i++) badchar[pat[i]].i
        = i;
    int s = 0;
    while (s <= n - m) {
        int j = m - 1;
        while (j >= 0 && pat[j] == txt[s + j]) j--;
        if (j < 0) {
            toret.push_back(s);
            s += (s + m < n) ? m - badchar[txt[s +
                m]].i : 1;
        }
        else
            s += max(1, j - badchar[txt[s + j]].i);
    }
    return toret;
}

English Conversion
const string ones[] = {"", "one", "two",
    "three", "four", "five", "six", "seven",
    "eight", "nine"};
const string teens[] = {"ten", "eleven",
    "twelve", "thirteen", "fourteen",
    "fifteen", "sixteen", "seventeen",
    "eighteen", "nineteen"};
const string tens[] = {"twenty", "thirty",
    "forty", "fifty", "sixty", "seventy",
    "eighty", "ninety"};
const string mags[] = {"thousand", "million",
    "billion", "trillion", "quadrillion",
    "quintillion", "sextillion",
    "septillion"};
string convert(int num, int carry) {
    if (num < 0) return "negative " +
        convert(-num, 0);
    if (num < 10) return ones[num];
    if (num < 20) return teens[num % 10];

```

Boyer Moore

```

struct definit { int i = -1; };
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{
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    badchar;
    int m = pat.size(), n = txt.size();
    for (int i = 0; i < m; i++) badchar[pat[i]].i
        = i;
    int s = 0;
    while (s <= n - m) {
        int j = m - 1;
        while (j >= 0 && pat[j] == txt[s + j]) j--;
        if (j < 0) {
            toret.push_back(s);
            s += (s + m < n) ? m - badchar[txt[s +
                m]].i : 1;
        }
        else
            s += max(1, j - badchar[txt[s + j]].i);
    }
    return toret;
}

English Conversion
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```

English Conversion

```

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    "fifteen", "sixteen", "seventeen",
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    "forty", "fifty", "sixty", "seventy",
    "eighty", "ninety"};
const string mags[] = {"thousand", "million",
    "billion", "trillion", "quadrillion",
    "quintillion", "sextillion",
    "septillion"};
string convert(int num, int carry) {
    if (num < 0) return "negative " +
        convert(-num, 0);
    if (num < 10) return ones[num];
    if (num < 20) return teens[num % 10];

```

```

    if (num < 100) return tens[(num / 10) - 2] +
        (num%10==0?"":" ") + ones[num % 10];
    if (num < 1000) return ones[num / 100] +
        (num/100==0?"":" ") + "hundred" +
        (num%100==0?"":" ") + convert(num % 100,
            0);
    return convert(num / 1000, carry + 1) + " " +
        mags[carry] + " " + convert(num % 1000,
            0);
}
string convert(int num) {
    return (num == 0) ? "zero" : convert(num, 0);
}

Knuth Morris Pratt
vector<int> kmp(string txt, string pat) {
    vector<int> toret;
    int m = txt.length(), n = pat.length();
    int next[n + 1];
    for (int i = 0; i < n + 1; i++)
        next[i] = 0;
    for (int i = 1; i < n; i++) {
        int j = next[i + 1];
        while (j > 0 && pat[j] != pat[i])
            j = next[j];
        next[i + 1] = j + 1;
    }
    for (int i = 0, j = 0; i < m; i++) {
        if (txt[i] == pat[j]) {
            if (++j == n)
                toret.push_back(i - j + 1);
        }
        else if (j > 0) {
            j = next[j];
        }
        else
            j--;
    }
    return toret;
}

Longest Common Prefix (array)
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
    false) {
    if (!sorted) sort(arr, arr + n);
    string r = ""; int v = 0;
    while (v < arr[0].length() && arr[0][v] ==
        arr[n-1][v])
        r += arr[0][v++];
    return r;
}

Longest Common Subsequence
string lcs(string a, string b) {
    int m = a.length(), n = b.length();
    int L[m+1][n+1];
    for (int i = 0; i <= m; i++) {
        for (int j = 0; j <= n; j++) {
            if (i == 0 || j == 0) L[i][j] = 0;
            else if (a[i-1] == b[j-1]) L[i][j] =
                L[i-1][j-1] + 1;
            else L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    }
    // return L[m][n]; // length of lcs
    string out = "";
    int i = m - 1, j = n - 1;
    while (i >= 0 && j >= 0) {
        if (a[i] == b[j]) {
            out = a[i--] + out;
            j--;
        }
        else if (L[i][j+1] > L[i+1][j]) i--;
        else j--;
    }
    return out;
}

```

Knuth Morris Pratt

```

vector<int> kmp(string txt, string pat) {
    vector<int> toret;
    int m = txt.length(), n = pat.length();
    int next[n + 1];
    for (int i = 0; i < n + 1; i++)
        next[i] = 0;
    for (int i = 1; i < n; i++) {
        int j = next[i + 1];
        while (j > 0 && pat[j] != pat[i])
            j = next[j];
        next[i + 1] = j + 1;
    }
    for (int i = 0, j = 0; i < m; i++) {
        if (txt[i] == pat[j]) {
            if (++j == n)
                toret.push_back(i - j + 1);
        }
        else if (j > 0) {
            j = next[j];
        }
        else
            j--;
    }
    return toret;
}

Longest Common Prefix (array)
// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
    false) {
    if (!sorted) sort(arr, arr + n);
    string r = ""; int v = 0;
    while (v < arr[0].length() && arr[0][v] ==
        arr[n-1][v])
        r += arr[0][v++];
    return r;
}

Longest Common Subsequence
string lcs(string a, string b) {
    int m = a.length(), n = b.length();
    int L[m+1][n+1];
    for (int i = 0; i <= m; i++) {
        for (int j = 0; j <= n; j++) {
            if (i == 0 || j == 0) L[i][j] = 0;
            else if (a[i-1] == b[j-1]) L[i][j] =
                L[i-1][j-1] + 1;
            else L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    }
    // return L[m][n]; // length of lcs
    string out = "";
    int i = m - 1, j = n - 1;
    while (i >= 0 && j >= 0) {
        if (a[i] == b[j]) {
            out = a[i--] + out;
            j--;
        }
        else if (L[i][j+1] > L[i+1][j]) i--;
        else j--;
    }
    return out;
}

```

Longest Common Prefix (array)

```

// longest common prefix of strings in array
string lcp(string* arr, int n, bool sorted =
    false) {
    if (!sorted) sort(arr, arr + n);
    string r = ""; int v = 0;
    while (v < arr[0].length() && arr[0][v] ==
        arr[n-1][v])
        r += arr[0][v++];
    return r;
}

Longest Common Subsequence
string lcs(string a, string b) {
    int m = a.length(), n = b.length();
    int L[m+1][n+1];
    for (int i = 0; i <= m; i++) {
        for (int j = 0; j <= n; j++) {
            if (i == 0 || j == 0) L[i][j] = 0;
            else if (a[i-1] == b[j-1]) L[i][j] =
                L[i-1][j-1] + 1;
            else L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    }
    // return L[m][n]; // length of lcs
    string out = "";
    int i = m - 1, j = n - 1;
    while (i >= 0 && j >= 0) {
        if (a[i] == b[j]) {
            out = a[i--] + out;
            j--;
        }
        else if (L[i][j+1] > L[i+1][j]) i--;
        else j--;
    }
    return out;
}

```

Longest Common Subsequence

```

string lcs(string a, string b) {
    int m = a.length(), n = b.length();
    int L[m+1][n+1];
    for (int i = 0; i <= m; i++) {
        for (int j = 0; j <= n; j++) {
            if (i == 0 || j == 0) L[i][j] = 0;
            else if (a[i-1] == b[j-1]) L[i][j] =
                L[i-1][j-1] + 1;
            else L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    }
    // return L[m][n]; // length of lcs
    string out = "";
    int i = m - 1, j = n - 1;
    while (i >= 0 && j >= 0) {
        if (a[i] == b[j]) {
            out = a[i--] + out;
            j--;
        }
        else if (L[i][j+1] > L[i+1][j]) i--;
        else j--;
    }
    return out;
}

```

Longest Common Substring

```
// l is array of palindrome length at that
↪ index
int manacher(string s, int* l) {
    int n = s.length() * 2;
    for (int i = 0, j = 0, k; i < n; i += k, j =
    ↪ max(j-k, 0)) {
        while (i >= j && i + j + 1 < n && s[(i-j)/2])
        ↪ == s[(i+j+1)/2]) j++;
        l[i] = 1;
        for (k = 1; i >= k && j >= k && l[i-k] !=
        ↪ j-k; k++)
            l[i+k] = min(l[i-k], j-k);
        return *max_element(l, l + n);
    }
}
```

Cyclic Rotation (Lyndon)

```
// simple strings = smaller than its nontrivial
↪ suffixes
// lyndon factorization = simple strings
↪ factorized
// "abaaba" -> "ab", "aab", "a"
vector<string> duval(string s) {
    int n = s.length();
    vector<string> lyndon;
    for (int i = 0; i < n; i++) {
        int j = i+1, k = i;
        for (; j < n && s[k] <= s[j]; j++)
            if (s[k] < s[j]) k = i;
        else k++;
        for (; i <= k; i += j - k)
            lyndon.push_back(s.substr(i, j-k));
    }
    return lyndon;
}
// lexicographically smallest rotation
int minRotation(string s) {
    int n = s.length(); s += s;
    auto d = duval(s); int i = 0, a = 0;
    while (a + d[i].length() < n) a +=
    ↪ d[i++].length();
    while (i && d[i] == d[i-1]) a -=
    ↪ d[i--].length();
    return a;
}
```

Subsequence Count

```
// "banana", "ban" >> 3 (ban, ba..n, b..an)
ull subsequences(string body, string subs) {
    int m = subs.length(), n = body.length();
    if (m > n) return 0;
    ull** arr = new ull*[m+1];
    for (int i = 0; i <= m; i++) arr[i] = new
    ↪ ull[n+1];
    for (int i = 1; i <= m; i++) arr[i][0] = 0;
    for (int i = 0; i <= m; i++) arr[0][i] = 1;
    for (int i = 1; i <= m; i++)
        for (int j = 1; j <= n; j++)
            arr[i][j] = arr[i][j-1] + ((body[j-1] ==
            ↪ subs[i-1]) ? arr[i-1][j-1] : 0);
    return arr[m][n];
}
```

Suffix Array + LCP

```
struct SuffixArray {
    vector<int> sa, lcp;
    SuffixArray(string& s, int lim=256) {
        int n = s.length() + 1, k = 0, a, b;
        vector<int> x(begin(s), end(s)+1), y(n),
        ↪ ws(max(n, lim)), rank(n);
        sa = lcp = y;
        iota(begin(sa), end(sa), 0);
        for (int j = 0, p = 0; p < n; j = max(1, j *
        ↪ 2), lim = p) {
            p = j; iota(begin(y), end(y), n - j);
            for (int i = 0; i < (n); i++)
```

```
                if (sa[i] >= j)
                    y[p++] = sa[i] - j;
                fill(begin(ws), end(ws), 0);
                for (int i = 0; i < (n); i++) ws[x[i]]++;
                for (int i = 1; i < (lim); i++) ws[i] +=
                ↪ ws[i-1];
                for (int i = n; i--;) sa[--ws[x[y[i]]]] =
                ↪ y[i];
                swap(x, y); p = 1; x[sa[0]] = 0;
                for (int i = 1; i < (n); i++) {
                    a = sa[i-1]; b = sa[i];
                    x[b] = (y[a] == y[b] && y[a + j] == y[b +
                    ↪ j]) ? p - 1 : p++;
                }
                for (int i = 1; i < (n); i++) rank[sa[i]] =
                ↪ i;
                for (int i = 0, j; i < n - 1; lcp[rank[i++]]
                ↪ = k)
                    for (k && k--, j = sa[rank[i] - 1];
                        s[i + k] == s[j + k]; k++);
            }
        }
    };
}
```

Suffix Tree (Ukkonen's)

```
struct SuffixTree {
    // n = 2*len+10 or so
    enum { N = 50010, ALPHA = 26 };
    int toi(char c) { return c - 'a'; }
    int
    ↪ t[N][ALPHA], l[N], r[N], p[N], s[N], v=0, q=0, m=2;
    string a;
    void ukkadd(int i, int c) { suff:
        if (r[v] <= q) {
            if (t[v][c] == -1) { t[v][c] = m; l[m] = i;
                p[m++] = v; v = s[v]; q = r[v]; goto suff; }
            v = t[v][c]; q = l[v];
        }
        if (q == -1 || c == toi(a[q])) q++; else {
            l[m+1] = i; p[m+1] = m; l[m] = l[v]; r[m] = q;
            p[m] = p[v]; t[m][c] = m+1; t[m][toi(a[q])] = v;
            l[v] = q; p[v] = m; t[p[m]] [toi(a[l[m]])] = m;
            v = s[p[m]]; q = l[m];
            while (q < r[m]) { v = t[v][toi(a[q])];
                ↪ q++ = r[v] - l[v]; }
            if (q == r[m]) s[m] = v; else s[m] = m+2;
            q = r[v] - (q - r[m]); m += 2; goto suff;
        }
    }
    SuffixTree(string a) : a(a) {
        fill(r, r+N, (int)(a.size()));
        memset(s, 0, sizeof s);
        memset(t, -1, sizeof t);
        fill(t[1], t[1]+ALPHA, 0);
        s[0] = 1; l[0] = 1; l[1] = -1; r[0] = r[1] = p[0] = p[1] = 0;
        for (int i = 0; i < a.size(); i++)
            ↪ ukkadd(i, toi(a[i]));
        // Longest Common Substring between 2 strings
        // returns {length, offset from first string}
        pair<int, int> best;
        int lcs(int node, int i1, int i2, int olen) {
            if (l[node] <= i1 && i1 < r[node]) return 1;
            if (l[node] <= i2 && i2 < r[node]) return 2;
            int mask = 0;
            ↪ len = node ? olen + (r[node] - l[node]) : 0;
            for (int c = 0; c < ALPHA; c++) if
                ↪ (t[node][c] != -1)
                    mask |= lcs(t[node][c], i1, i2, len);
            if (mask == 3)
                ↪ best = max(best, {len, r[node] - len});
            return mask;
        }
        static pair<int, int> LCS(string s, string t)
        ↪ {
            SuffixTree
            ↪ st(s+(char)('z'+1)+t+(char)('z'+2));
            st.lcs(0, s.size(), s.size()+t.size()+1, 0);
            return st.best;
        }
    };
}
```

```
}
};
```

String Utilities

```
void lowercase(string& s) {
    transform(s.begin(), s.end(), s.begin(),
    ↪ ::tolower);
}
void uppercase(string& s) {
    transform(s.begin(), s.end(), s.begin(),
    ↪ ::toupper);
}
void trim(string& s) {
    s.erase(s.begin(), find_if_not(s.begin(), s
    ↪
        .end(), [](int c){return
        ↪ isspace(c);}));
    s.erase(find_if_not(s.rbegin(), s.rend(), [](int
    ↪
        c){return isspace(c);}).base(), s.end());
}
vector<string> split(string& s, char token) {
    vector<string> v; stringstream ss(s);
    for (string e; getline(ss, e, token);)
        v.push_back(e);
    return v;
}
```

5 Greedy

Interval Cover

```
// L,R = interval [L,R], in = {{l,r}, index}
// does not handle case where L == R
vector<int> intervalCover(double L, double R,
    ↪ vector<pair<pair<double, double>, int>> in) {
    int i = 0; pair<double, int> pos = {L, -1};
    ↪ vector<int> a;
    sort(begin(in), end(in));
    while (pos.first < R) {
        double cur = pos.first;
        while (i < (int)in.size() &&
        ↪ in[i].first <= cur)
            pos = in[i].first.second, in[i].second;
        ↪ i++;
        if (pos.first == cur) return {};
        a.push_back(pos.second);
    }
    return a;
}
```

6 Math

Catalan Numbers

```
ull* catalan = new ull[1000000];
void genCatalan(int n, int mod) {
    catalan[0] = catalan[1] = 1;
    for (int i = 2; i <= n; i++) {
        catalan[i] = 0;
        for (int j = i - 1; j >= 0; j--) {
            catalan[i] += (catalan[j] * catalan[i-j-1])
            ↪ % mod;
        }
        catalan[i] -= mod;
    }
}
// TODO: consider binomial coefficient method
```

Combinatorics (nCr, nPr)

```
// can optimize by precomputing factorials, and
↪ fact[n]/fact[n-r]
ull nPr(ull n, ull r) {
    ull v = 1;
    for (ull i = n-r+1; i <= n; i++)
        v *= i;
    return v;
}
ull nPr(ull n, ull r, ull m) {
    ull v = 1;
    for (ull i = n-r+1; i <= n; i++)
        v = (v * i) % m;
```

```
return v;
}
ull nCr(ull n, ull r) {
    long double v = 1;
    for (ull i = 1; i <= r; i++)
        v = v * (n-r+i) / i;
    return (ull)(v + 0.001);
}
// requires modulo math
// can optimize by precomputing mfac and
↪ minv-mfac
ull nCr(ull n, ull r, ull m) {
    return mfac(n, m) * minv(mfac(k, m), m) % m *
    ↪ minv(mfac(n-k, m), m) % m;
}
```

Multinomials

```
ll multinomial(vector<int>& v) {
    ll c = 1, m = v.empty() ? 1 : v[0];
    for (int i = 1; i < v.size(); i++)
        for (int j = 0; j < v[i]; j++)
            c = c * ++m / (j+1);
    return c;
}
```

Chinese Remainder Theorem

```
bool ecrt(ll* r, ll* m, int n, ll& re, ll& mo)
    ↪ {
    ll x, y, d; mo = m[0]; re = r[0];
    for (int i = 1; i < n; i++) {
        d = egcd(mo, m[i], x, y);
        if ((r[i] - re) % d != 0) return false;
        x = (x * mo - re) / d * x % (m[i] / d);
        re += x * mo;
        mo = mo / d * m[i];
        re %= mo;
    }
    re = (re + mo) % mo;
    return true;
}
```

Count Digit Occurrences

```
/*count(n,d) counts the number of occurrences of
↪ a digit d in the range [0,n]*/
ll digit_count(ll n, ll d) {
    ll result = 0;
    while (n != 0) {
        result += ((n%10) == d ? 1 : 0);
        n /= 10;
    }
    return result;
}
ll count(ll n, ll d) {
    if (n < 10) return (d > 0 && n == d);
    if ((n % 10) != 9) return digit_count(n, d) +
    ↪ count(n-1, d);
    return 10*count(n/10, d) + (n/10) + (d > 0);
}
```

Discrete Logarithm

```
unordered_map<int, int> dlogc;
int discretelog(int a, int b, int m) {
    dlogc.clear();
    ll n = sqrt(m)+1, an = 1;
    for (int i = 0; i < n; i++)
        an = (an * a) % m;
    ll c = an;
    for (int i = 1; i <= n; i++) {
        if (!dlogc.count(c)) dlogc[c] = i;
        c = (c * an) % m;
    }
    c = b;
    for (int i = 0; i <= n; i++) {
        if (dlogc.count(c)) return (dlogc[c] * n - i
        ↪ + m - 1) % (m-1);
        c = (c * a) % m;
    }
    return -1;
}
```


Euler Phi / Totient

```
int phi(int n) {
    int r = n;
    for (int i = 2; i * i <= n; i++) {
        if (n % i == 0) r -= r / i;
        while (n % i == 0) n /= i;
    }
    if (n > 1) r -= r / n;
    return r;
}

#define n 100000
ll phi[n+1];
void computeTotient() {
    for (int i=1; i<=n; i++) phi[i] = i;
    for (int p=2; p<=n; p++) {
        if (phi[p] == p) {
            phi[p] = p-1;
            for (int i = 2*p; i<=n; i += p) phi[i] =
                (phi[i]/p) * (p-1);
        }
    }
}
```

Factorials

```
// digits in factorial
#define kamenetsky(n) (floor((n * log10(n /
    ↪ M_E)) + (log10(2 * M_PI * n) / 2.0)) + 1)
// approximation of factorial
#define stirling(n) ((n == 1) ? 1 : sqrt(2 *
    ↪ M_PI * n) * pow(n / M_E, n))
// natural log of factorial
#define lfactorial(n) (lgamma(n+1))
```

Prime Factorization

```
// do not call directly
ll pollard_rho(ll n, ll s) {
    ll x, y;
    x = y = rand() % (n - 1) + 1;
    int head = 1, tail = 2;
    while (true) {
        x = mult(x, x, n);
        x = (x + s) % n;
        if (x == y) return n;
        ll d = __gcd(max(x - y, y - x), n);
        if (1 < d && d < n) return d;
        if (++head == tail) y = x, tail <= 1;
    }
}

// call for prime factors
void factorize(ll n, vector<ll> &divisor) {
    if (n == 1) return;
    if (isPrime(n)) divisor.push_back(n);
    else {
        ll d = n;
        while (d >= n) d = pollard_rho(n, rand() % (n
            ↪ - 1) + 1);
        factorize(n / d, divisor);
        factorize(d, divisor);
    }
}
```

Farey Fractions

```
// generate 0 <= a/b <= 1 ordered, b <= n
// farey(4) = 0/1 1/4 1/3 1/2 2/3 3/4 1/1
// length is sum of phi(i) for i = 1 to n
vector<pair<int, int>> farey(int n) {
    int h = 0, k = 1, x = 1, y = 0, r;
    vector<pair<int, int>> v;
    do {
        v.push_back({h, k});
        r = (n-y)/k;
        y += r*k; x += r*h;
        swap(x,h); swap(y,k);
        x = -x; y = -y;
    } while (k > 1);
    v.push_back({1, 1});
    return v;
}
```

Fast Fourier Transform

```
#define cd complex<double>
const double PI = acos(-1);
void fft(vector<cd>& a, bool invert) {
    int n = a.size();
    for (int i = 1, j = 0; i < n; i++) {
        int bit = n >> 1;
        for (; j & bit; bit >>= 1) j ^= bit;
        j ^= bit;
        if (i < j) swap(a[i], a[j]);
    }
    for (int len = 2; len <= n; len <= 1) {
        double ang = 2 * PI / len * (invert ? -1 :
            ↪ 1);
        cd wlen(cos(ang), sin(ang));
        for (int i = 0; i < n; i += len) {
            cd w(1);
            for (int j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w *= wlen;
            }
        }
        if (invert)
            for (auto& x : a)
                x /= n;
    }
}

vector<int> fftmult(vector<int> const& a,
    ↪ vector<int> const& b) {
    vector<cd> fa(a.begin(), a.end()),
    ↪ fb(b.begin(), b.end());
    int n = 1 << (32 - __builtin_clz(a.size() +
        ↪ b.size()) - 1));
    fa.resize(n); fb.resize(n);
    fft(fa, false); fft(fb, false);
    for (int i = 0; i < n; i++) fa[i] *= fb[i];
    fft(fa, true);
    vector<int> toret(n);
    for (int i = 0; i < n; i++) toret[i] =
        ↪ round(fa[i].real());
    return toret;
}
```

Greatest Common Denominator

```
ll egcd(ll a, ll b, ll& x, ll& y) {
    if (b == 0) { x = 1; y = 0; return a; }
    ll gcd = egcd(b, a % b, x, y);
    x -= a / b * y;
    swap(x, y);
    return gcd;
}

// fast case if k=2, traditional josephus
int josephus(int n) {
    return 2*(n-(1<<(32-__builtin_clz(n)-1)));
}
```

Least Common Multiple

```
#define lcm(a,b) ((a*b)/__gcd(a,b))
```

Modulo Operations

```
#define MOD 1000000007
#define madd(a,b,m) (a+b-((a+b-m)>=0)?m:0)
#define mult(a,b,m) ((ull)a*b%m)
#define msub(a,b,m) (a-b+((a<b)?m:0))
ll mpow(ll b, ll e, ll m) {
    ll x = 1;
    while (e > 0) {
        if (e % 2) x = (x * b) % m;
```

```
        b = (b * b) % m;
        e /= 2;
    }
    return x % m;
}

ull mfac(ull n, ull m) {
    ull f = 1;
    for (int i = n; i > 1; i--)
        f = (f * i) % m;
    return f;
}

// if m is not guaranteed to be prime
ll minv(ll b, ll m) {
    ll x = 0, y = 0;
    if (egcd(b, m, x, y) != 1) return -1;
    return (x % m + m) % m;
}

ll mdiv_compmo(int a, int b, int m) {
    if (__gcd(b, m) != 1) return -1;
    return mult(a, minv(b, m), m);
}

// if m is prime (like 10^9+7)
ll mdiv_primemo(int a, int b, int m) {
    return mult(a, mpow(b, m-2, m), m);
}
```

Modulo Tetration

```
ll tetraloop(ll a, ll b, ll m) {
    if (b == 0 || a == 1) return 1;
    ll w = tetraloop(a, b-1, phi(m)), r = 1;
    for (; w; w/=2) {
        if (w&1) {
            r *= a; if (r >= m) r -= (r-m-1)*m;
            a *= a; if (a >= m) a -= (a-m-1)*m;
        }
        return r;
    }
}

int tetration(int a, int b, int m) {
    if (a == 0 || m == 1) return ((b+1)&1)%m;
    return tetraloop(a, b, m) % m;
}
```

Matrix

```
template<typename T>
struct Mat : public Vec<2, T> {
    int w, h;
    Mat(int x, int y) : Vec<2, T>(x, y), w(x),
        ↪ h(y) {}
    static Mat<T> identity(int n) { Mat<T> m(n,n);
        ↪ for (int i=0; i<n; i++) m[i][i] = 1; return
        ↪ m; }
    Mat<T>& operator+=(const Mat<T>& m) {
        ↪ for (int i = 0; i < w; i++)
        ↪ for (int j = 0; j < h; j++)
        ↪ (*this)[i][j] += m[i][j];
        ↪ return *this;
    }
    Mat<T>& operator-=(const Mat<T>& m) {
        ↪ for (int i = 0; i < w; i++)
        ↪ for (int j = 0; j < h; j++)
        ↪ (*this)[i][j] -= m[i][j];
        ↪ return *this;
    }
    Mat<T> operator*(const Mat<T>& m) {
        ↪ Mat<T> z(w,m.h);
        ↪ for (int i = 0; i < w; i++)
        ↪ for (int j = 0; j < h; j++)
        ↪ for (int k = 0; k < m.h; k++)
        ↪ z[i][k] += (*this)[i][j] * m[j][k];
        ↪ return z;
    }
    Mat<T> operator+(const Mat<T>& m) { Mat<T>
        ↪ a=*this; return a+m; }
    Mat<T> operator-(const Mat<T>& m) { Mat<T>
        ↪ a=*this; return a-m; }
    Mat<T>& operator*=(const Mat<T>& m) { return
        ↪ *this = (*this)*m; }
    Mat<T> power(int n) {
        ↪ Mat<T> a = Mat<T>::identity(w), m=*this;
        ↪ for (; n; n/=2, m*=m) if (n&1) a *= m;
        ↪ return a;
    }
}
```

```
}
};

Matrix Exponentiation
// F(n) = c[0]*F(n-1) + c[1]*F(n-2) + ...
// b is the base cases of same length c
ll matrix_exponentiation(ll n, vector<ll> c,
    ↪ vector<ll> b) {
    if (nth < b.size()) return b[nth-1];
    Mat<ll> a(c.size(), c.size()); ll s = 0;
    for (int i = 0; i < c.size(); i++) a[i][0] =
        ↪ c[i];
    for (int i = 0; i < c.size() - 1; i++)
        ↪ a[i][i+1] = 1;
    a = a.power(nth - c.size());
    for (int i = 0; i < c.size(); i++)
        ↪ s += a[i][0] * b[i];
    return s;
}
```

Matrix Subarray Sums

```
template<class T> struct MatrixSum {
    Vec<2, T> p;
    MatrixSum(Vec<2, T>& v) {
        p = Vec<2, T>(v.size()+1, v[0].size()+1);
        for (int i = 0; i < v.size(); i++)
            ↪ for (int j = 0; j < v[0].size(); j++)
            ↪ p[i+1][j+1] = v[i][j] + p[i][j+1] +
            ↪ p[i+1][j] - p[i][j];
        T sum(int u, int l, int d, int r) {
            ↪ return p[d][r] - p[d][l] - p[u][r] + p[u][l];
        }
    };
};
```

Nimber Arithmetic

```
#define nimAdd(a,b) ((a)^(b))
ull nimMul(ull a, ull b, int i=6) {
    static const ull M[] = {INT_MIN>>32,
        ↪ M[0]^(M[0]<<16), M[1]^(M[1]<<8),
        ↪ M[2]^(M[2]<<4), M[3]^(M[3]<<2),
        ↪ M[4]^(M[4]<<1)};
    if (i-- == 0) return a&b;
    int k=1<<i;
    ull s=nimMul(a,b,i), m=M[5-i],
        ↪ t=nimMul(((a^(a>>k))&m)|(s&m),
        ↪ ((b^(b>>k))&m)|(m&(m>>1))<<k, i);
    return ((s^t)&m)<<k|((s^(t>>k))&m);
}
```

Permutation

```
// c = array size, n = nth perm, return index
vector<int> gen_permutation(int c, int n) {
    vector<int> idx(c), per(c), fac(c); int i;
    for (i = 0; i < c; i++) idx[i] = i;
    for (i = 1; i <= c; i++) fac[i-1] = n%i, n/=i;
    for (i = c-1; i >= 0; i--)
        ↪ per[c-i-1] = idx[fac[i]],
        ↪ idx.erase(idx.begin() + fac[i]);
    return per;
}

// get what nth permutation of vector
int get_permutation(vector<int>& v) {
    int use = 0, i = 1, r = 0;
    for (int e : v) {
        ↪ r = r * i++ + __builtin_popcount(use &
        ↪ -(1<<e));
        ↪ use |= 1 << e;
    }
    return r;
}
```

Permutation (string/multiset)

```
string freq2str(vector<int>& v) {
    string s;
    for (int i = 0; i < v.size(); i++)
        ↪ for (int j = 0; j < v[i]; j++)
        ↪ s += (char)(i + 'A');
    return s;
}

// nth perm of multiset, n is 0-indexed
string gen_permutation(string s, ll n) {
```

```

vector<int> freq(26, 0);
for (auto e : s) freq[e - 'A']++;
for (int i = 0; i < 26; i++) if (freq[i] > 0)
{
    freq[i]--; ll v = multinomial(freq);
    if (n < v) return (char)(i+'A') +
    gen_permutation(freq2str(freq), n);
    freq[i]++; n -= v;
}
return "";
}

```

Miller-Rabin Primality Test

```

// Miller-Rabin primality test - O(10 log^3 n)
bool isPrime(ull n) {
    if (n < 2) return false;
    if (n == 2) return true;
    if (n % 2 == 0) return false;
    ull s = n - 1;
    while (s % 2 == 0) s /= 2;
    for (int i = 0; i < 10; i++) {
        ull temp = s;
        ull a = rand() % (n - 1) + 1;
        ull mod = mpow(a, temp, n);
        while (temp != n-1 && mod != 1 && mod != n-1) {
            mod = mult(mod, mod, n);
            temp *= 2;
        }
        if (mod != n-1 && temp % 2 == 0) return false;
    }
    return true;
}

```

Sieve of Eratosthenes

```

bitset<1000000001> sieve;
// generate sieve - O(n log n)
void genSieve(int n) {
    sieve[0] = sieve[1] = 1;
    for (ull i = 3; i * i < n; i += 2)
        if (!sieve[i])
            for (ull j = i * 3; j <= n; j += i * 2)
                sieve[j] = 1;
}
// query sieve after it's generated - O(1)
bool querySieve(int n) {
    return n == 2 || (n % 2 != 0 && !sieve[n]);
}

```

Simpson's / Approximate Integrals

```

// integrate f from a to b, k iterations
// error <= (b-a)/18.0 * M * ((b-a)/2k)^4
// where M = max(abs(f''''(x))) for x in [a,b]
// "f" is a function "double func(double x)"
double Simpsons(double a, double b, int k,
    double (*f)(double)) {
    double dx = (b-a)/(2.0*k), t = 0;
    for (int i = 0; i < k; i++)
        t += ((i==0)?1:2)*(*f)(a+2*i*dx) + 4 *
        (*f)(a+(2*i+1)*dx);
    return (t + (*f)(b)) * (b-a) / 6.0 / k;
}

```

Common Equations Solvers

```

// ax^2 + bx + c = 0, find x
vector<double> solveEq(double a, double b,
    double c) {
    vector<double> r;
    double z = b * b - 4 * a * c;
    if (z == 0)
        r.push_back(-b/(2*a));
    else if (z > 0) {
        r.push_back((sqrt(z)-b)/(2*a));
        r.push_back((sqrt(z)+b)/(2*a));
    }
    return r;
}
// ax^3 + bx^2 + cx + d = 0, find x
vector<double> solveEq(double a, double b,
    double c, double d) {
    vector<double> res;
    long double a1 = b/a, a2 = c/a, a3 = d/a;

```

```

    long double q = (a1*a1 - 3*a2)/9.0, sq =
    -2*sqrt(q);
    long double r = (2*a1*a1*a1 - 9*a1*a2 +
    27*a3)/54.0;
    long double z = r*r-q*q*q, theta;
    if (z <= 0) {
        theta = acos(r/sqrt(q*q*q));
        res.push_back(sq*cos(theta/3.0) - a1/3.0);
        res.push_back(sq*cos((theta+2.0*PI)/3.0) -
        a1/3.0);
        res.push_back(sq*cos((theta+4.0*PI)/3.0) -
        a1/3.0);
    }
    else {
        res.push_back(pow(sqrt(z)+fabs(r), 1/3.0));
        res[0] = (res[0] + q / res[0]) *
        ((r<0)?1:-1) - a1 / 3.0;
    }
    return res;
}
// linear diophantine equation ax + by = c,
// find x and y
// infinite solutions of form x+k*b/g, y-k*a/g
bool solveEq(ll a, ll b, ll c, ll &x, ll &y, ll
    &g) {
    g = egcd(abs(a), abs(b), x, y);
    if (c % g) return false;
    x *= c / g * ((a < 0) ? -1 : 1);
    y *= c / g * ((b < 0) ? -1 : 1);
    return true;
}
// m = # equations, n = # variables, a[m][n+1]
// = coefficient matrix
// a[i][0]*x + a[i][1]*y + ... + a[i][n]*z =
// a[i][n+1]
// find a solution of some kind to linear
// equation
const double eps = 1e-7;
bool zero(double a) { return (a < eps) && (a >
    -eps); }
vector<double> solveEq(double **a, int m, int
    n) {
    int cur = 0;
    for (int i = 0; i < n; i++) {
        for (int j = cur; j < m; j++) {
            if (!zero(a[j][i])) {
                if (j != cur) swap(a[j], a[cur]);
                for (int sat = 0; sat < m; sat++) {
                    if (sat == cur) continue;
                    double num = a[sat][i] / a[cur][i];
                    for (int sot = 0; sot <= n; sot++)
                        a[sat][sot] -= a[cur][sot] * num;
                }
                cur++;
                break;
            }
        }
    }
    for (int j = cur; j < m; j++)
        if (!zero(a[j][n])) return vector<double>();
    vector<double> ans(n, 0);
    for (int i = 0, sat = 0; i < n; i++)
        if (sat < m && !zero(a[sat][i]))
            ans[i] = a[sat][n] / a[sat++][i];
    return ans;
}
// solve A[n][n] * x[n] = b[n] linear equation
// rank < n is multiple solutions, -1 is no
// solutions
// 'alls' is whether to find all solutions, or
// any
const double eps = 1e-12;
int solveEq(Vec<2, double>& A, Vec<1, double>&
    b, Vec<1, double>& x, bool alls=false) {
    int n = A.size(), m = x.size(), rank = 0, br,
    bc;
    vector<int> col(m); iota(begin(col), end(col),
    0);
    for (int i = 0; i < n; i++) {

```

```

        double v, bv = 0;
        for (int r = i; r < n; r++)
            for (int c = i; c < n; c++)
                if ((v = fabs(A[r][c])) > bv)
                    br = r, bc = c, bv = v;
        if (bv <= eps) {
            for (int j = i; j < n; j++)
                if (fabs(b[j]) > eps)
                    return -1;
            break;
        }
        swap(A[i], A[br]);
        swap(b[i], b[br]);
        swap(col[i], col[bc]);
        for (int j = 0; j < n; j++)
            swap(A[j][i], A[j][bc]);
        bv = 1.0 / A[i][i];
        for (int j = (alls)?0:i+1; j < n; j++) {
            if (j != i) {
                double fac = A[j][i] * bv;
                b[j] -= fac * b[i];
                for (int k = i+1; k < m; k++)
                    A[j][k] -= fac*A[i][k];
            }
        }
        rank++;
        if (alls) for (int i = 0; i < m; i++) x[i] =
        -DBL_MAX;
        for (int i = rank; i--;) {
            bool isGood = true;
            if (alls)
                for (int j = rank; isGood && j < m; j++)
                    if (fabs(A[i][j]) > eps)
                        isGood = false;
            b[i] /= A[i][i];
            if (isGood) x[col[i]] = b[i];
            if (!alls)
                for (int j = 0; j < i; j++)
                    b[j] -= A[j][i] * b[i];
        }
        return rank;
}

```

Graycode Conversions

```

ull graycode2ull(ull n) {
    ull i = 0;
    for (; n; n = n >> 1) i ^= n;
    return i;
}
ull ull2graycode(ull n) {
    return n ^ (n >> 1);
}

```

Unix/Epoch Time

```

// 0-indexed month/time, 1-indexed day
// minimum 1970, 0, 1, 0, 0, 0
ull toEpoch(int year, int month, int day, int
    hour, int minute, int second) {
    struct tm t; time_t epoch;
    t.tm_year = year - 1900; t.tm_mon = month;
    t.tm_mday = day; t.tm_hour = hour;
    t.tm_min = minute; t.tm_sec = second;
    t.tm_isdst = 0; // 1 = daylight savings
    epoch = mktime(&t);
    return (ull)epoch;
}
vector<int> toDate(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return {t.tm_year+1900,t.tm_mon,t.tm_mday,t
    .tm_hour,t.tm_min,t.tm_sec};
}
int getWeekday(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return t.tm_wday; // 0-6, 0 = sunday
}
int getDayOfYear(ull epoch) {
    time_t e=epoch; struct tm t=*localtime(&e);
    return t.tm_yday; // 0-365
}

```

```

const int months[] =
    {31,28,31,30,31,30,31,31,30,31,30,31};
bool validate(int year, int month, int day) {
    bool leap = !(year%(year%25?4:16));
    if (month >= 12) return false;
    return day <= months[month] + (leap &&
    month == 1);
}

```

Theorems and Formulae

Montmort Numbers count the number of derangements (permutations where no element appears in its original position) of a set of size n . $!0 = 1$, $!1 = 0$, $!n = (n+1)!(n-1)+!(n-2)$), $!n = n! \sum_{i=0}^n \frac{(-1)^i}{i!}$, $!n = \lfloor \frac{n!}{e} \rfloor$

In a partially ordered set, a chain is a subset of elements that are all comparable to each other. An antichain is a subset where no two are comparable.

Dilworth's theorem states the size of a maximal antichain equals the size of a minimal chain cover of a partially ordered set S . The width of S is the maximum size of an antichain in S , which is equal to the minimum number of chains needed to cover S , or the minimum number of chains such that all elements are in at least one chain.

Rosser's Theorem states the n th prime number is greater than $n * \ln(n)$ for $n > 1$.

Nicomachi's Theorem states $1^3 + 2^3 + \dots + n^3 = (1 + 2 + \dots + n)^2$ and is equivalent to $(n \frac{n+1}{2})^2$.

Lagrange's Four Square Theorem states every natural number is the sum of the squares of four non-negative integers. This is a special case of the **Fermat Polygonal Number Theorem** where every positive integer is a sum of at most n s -gonal numbers. The n th

s -gonal number $P(s, n) = (s-2) \frac{n(n-1)}{2} + n$

7 Graphs

```

struct edge {
    int u,v,w;
    edge (int u,int v,int w) : u(u),v(v),w(w) {}
    edge () : u(0), v(0), w(0) {}
};
bool operator < (const edge &e1, const edge
    &e2) { return e1.w < e2.w; }
bool operator > (const edge &e1, const edge
    &e2) { return e1.w > e2.w; }
struct subset { int p, rank; };

```

Eulerian Path

```

#define edge_list vector<edge>
#define adj_sets vector<set<int>>
struct EulerPathGraph {
    adj_sets graph; // actually indexes incident
    edges
    edge_list edges; int n; vector<int> indeg;
    EulerPathGraph(int n): n(n) {
        indeg = *(new vector<int>(n,0));
        graph = *(new adj_sets(n, set<int>()));
    }
    void add_edge(int u, int v) {

```

```

graph[u].insert(edges.size());
indeg[v]++;
edges.push_back(edge(u,v,0));
}
bool eulerian_path(vector<int> &circuit) {
    if(edges.size()==0) return false;
    stack<int> st;
    int a[] = {-1, -1};
    for(int v=0;v<n;v++) {
        if(indeg[v]!=graph[v].size()) {
            bool b = indeg[v] > graph[v].size();
            if (abs(((int)indeg[v])-(int)graph[v].size())) > 1) return false;
            if (a[b] != -1) return false;
            a[b] = v;
        }
    }
    int s = (a[0]!==-1 && a[1]!==-1 ? a[0] : (a[0]!==-1 && a[1]!==-1 ? edges[0].u : -1));
    if(s!=-1) return false;
    while(!st.empty() || graph[s].empty()) {
        if (graph[s].empty()) {
            circuit.push_back(s); s = st.top();
            st.pop(); }
        else {
            int w = edges[*graph[s].begin()].v;
            graph[s].erase(graph[s].begin());
            st.push(s); s = w;
        }
    }
    circuit.push_back(s);
    return circuit.size()-1==edges.size();
};

```

Floyd Warshall

```

const ll inf = 1LL << 62;
#define FOR(i,n) for (int i = 0; i < n; i++)
void floydWarshall(Vec<2, ll>& m) {
    int n = m.size();
    FOR(i,n) m[i][i] = min(m[i][i], 0LL);
    FOR(k,n) FOR(i,n) FOR(j,n) if (m[i][k] != inf
    && m[k][j] != inf) {
        auto newDist = max(m[i][k] + m[k][j], -inf);
        m[i][j] = min(m[i][j], newDist);
    }
    FOR(k,n) if (m[k][k] < 0) FOR(i,n) FOR(j,n)
    if (m[i][k] != inf && m[k][j] != inf)
    m[i][j] = -inf;
}

```

Minimum Spanning Tree

```

// returns vector of edges in the mst
// graph[i] = vector of edges incident to
// vertex i
// places total weight of the mst in &total
// if returned vector has size != n-1, there is
// no MST
vector<edge> mst(vector<vector<edge>> graph,
    int &total) {
    total = 0;
    priority_queue<edge, vector<edge>,
    greater<edge>> pq;
    vector<edge> MST;
    bitset<20001> marked; // change size as needed
    marked[0] = 1;
    for (edge ep : graph[0]) pq.push(ep);
    while(MST.size()!=graph.size()-1 &&
    pq.size()!=0) {
        edge e = pq.top(); pq.pop();
        int u = e.u, v = e.v, w = e.w;
        if(marked[u] && marked[v]) continue;
        else if(marked[u]) swap(u, v);
        for(edge ep : graph[u]) pq.push(ep);
        marked[u] = 1;
        MST.push_back(e);
        total += e.w;
    }
}

```

```

}
return MST;
}
Union Find
int uf_find(subset* s, int i) {
    if (s[i].p != i) s[i].p = uf_find(s, s[i].p);
    return s[i].p;
}
void uf_union(subset* s, int x, int y) {
    int xp = uf_find(s, x), yp = uf_find(s, y);
    if (s[xp].rank > s[yp].rank) s[yp].p = xp;
    else if (s[xp].rank < s[yp].rank) s[xp].p = yp;
    else { s[yp].p = xp; s[xp].rank++; }
}

```

2D Grid Shortcut

```

#define inbound(x,n) (0<=x&&x<n)
#define fordir(x,y,n,m) for(auto [dx,dy]:dir)if(
    (inbound(x+dx,n)&&inbound(y+dy,m))
const pair<int,int> dir[] =
    {{1,0},{0,1},{-1,0},{0,-1}};

```

8 2D Geometry

```

#define point complex<double>
#define EPS 0.0000001
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double dot(point a, point b) { return
    real(conj(a)*b); }
double cross(point a, point b) { return
    imag(conj(a)*b); }
struct line { point a, b; };
struct circle { point c; double r; };
struct segment { point a, b; };
struct triangle { point a, b, c; };
struct rectangle { point tl, br; };
struct convex_polygon {
    vector<point> points;
    convex_polygon(vector<point> points) :
    points(points) {}
    convex_polygon(triangle a) {
        points.push_back(a.a); points.push_back(a.b);
        points.push_back(a.c);
    };
    convex_polygon(rectangle a) {
        points.push_back(a.tl);
        points.push_back({real(a.tl),
        imag(a.br)}});
        points.push_back(a.br);
        points.push_back({real(a.br),
        imag(a.tl)}});
    };
};
struct polygon {
    vector<point> points;
    polygon(vector<point> points) :
    points(points) {}
    polygon(triangle a) {
        points.push_back(a.a); points.push_back(a.b);
        points.push_back(a.c);
    };
    polygon(rectangle a) {
        points.push_back(a.tl);
        points.push_back({real(a.tl),
        imag(a.br)}});
        points.push_back(a.br);
        points.push_back({real(a.br),
        imag(a.tl)}});
    };
};
polygon(convex_polygon a) {
    for (point v : a.points)
    points.push_back(v);
}

```

```

};
// triangle methods
double area_heron(double a, double b, double
    c) {
    if (a < b) swap(a, b);
    if (a < c) swap(a, c);
    if (b < c) swap(b, c);
    if (a > b + c) return -1;
    return sqrt((a+b+c)*(c-a+b)*(c+a-b)
    /16.0);
// segment methods
double lengthsq(segment a) { return
    sq(real(a.a) - real(a.b)) + sq(imag(a.a) -
    imag(a.b)); }
double length(segment a) { return
    sqrt(lengthsq(a)); }
// circle methods
double circumference(circle a) { return 2 * a.r
    * M_PI; }
double area(circle a) { return sq(a.r) * M_PI;
    };
// rectangle methods
double width(rectangle a) { return
    abs(real(a.br) - real(a.tl)); }
double height(rectangle a) { return
    abs(imag(a.br) - real(a.tl)); }
double diagonal(rectangle a) { return
    sqrt(sq(width(a)) + sq(height(a))); }
double area(rectangle a) { return width(a) *
    height(a); }
double perimeter(rectangle a) { return 2 *
    (width(a) + height(a)); }
// check if 'a' fit's inside 'b'
// swap equalities to exclude tight fits
bool doesFitInside(rectangle a, rectangle b) {
    int x = width(a), w = width(b), y = height(a),
    h = height(b);
    if (x > y) swap(x, y);
    if (w > h) swap(w, h);
    if (w < x) return false;
    if (y <= h) return true;
    double a=sq(y)-sq(x), b=x*h-y*w, c=x*w-y*h;
    return sq(a) <= sq(b) + sq(c);
}
// polygon methods
// negative area = CCW, positive = CW
double area(polygon a) {
    double area = 0.0; int n = a.points.size();
    for (int i = 0, j = 1; i < n; i++, j = (j +
    1) % n)
        area += (real(a.points[j]-a.points[i]))*
        (imag(a.points[j]+a.points[i]));
    return area / 2.0;
}

```

```

// get both unsigned area and centroid
pair<double, point> area_centroid(polygon a) {
    int n = a.points.size();
    double area = 0;
    point c(0, 0);
    for (int i = n - 1, j = 0; j < n; i = j++) {
        double v = cross(a.points[i], a.points[j]) /
        2;
        area += v;
        c += (a.points[i] + a.points[j]) * (v / 3);
    }
    c /= area;
    return {area, c};
}

```

Intersection

```

// -1 coincide, 0 parallel, 1 intersection
int intersection(line a, line b, point& p) {
    if (abs(cross(a.b - a.a, b.b - b.a)) > EPS) {
        p = cross(b.a - a.a, b.b - a.b) / cross(a.b
        - a.a, b.b - b.a) * (b - a) + a;
        return 1;
    }
}

```

```

}
if (abs(cross(a.b - a.a, a.b - b.a)) > EPS)
    return 0;
return -1;
// area of intersection
double intersection(circle a, circle b) {
    double d = abs(a.c - b.c);
    if (d <= b.r - a.r) return area(a);
    if (d <= a.r - b.r) return area(b);
    if (d >= a.r + b.r) return 0;
    double alpha = acos((sq(a.r) + sq(d) -
    sq(b.r)) / (2 * a.r * d));
    double beta = acos((sq(b.r) + sq(d) - sq(a.r))
    / (2 * b.r * d));
    return sq(a.r) * (alpha - 0.5 * sin(2 *
    alpha)) + sq(b.r) * (beta - 0.5 * sin(2 *
    beta));
}
// -1 outside, 0 inside, 1 tangent, 2
// intersection
int intersection(circle a, circle b,
    vector<point>& inter) {
    double d2 = norm(b.c - a.c), rS = a.r + b.r,
    rD = a.r - b.r;
    if (d2 > sq(rS)) return -1;
    if (d2 < sq(rD)) return 0;
    double ca = 0.5 * (1 + rS * rD / d2);
    point z = point(ca, sqrt(sq(a.r) / d2 -
    sq(ca)));
    inter.push_back(a.c + (b.c - a.c) * z);
    if (abs(imag(z)) > EPS) inter.push_back(a.c +
    (b.c - a.c) * conj(z));
    return inter.size();
}
// points of intersection
vector<point> intersection(line a, circle c) {
    vector<point> inter;
    c.c = a.a;
    a.b = a.a;
    point m = a.b * real(c.c / a.b);
    double d2 = norm(m - c.c);
    if (d2 > sq(c.r)) return 0;
    double l = sqrt((sq(c.r) - d2) / norm(a.b));
    inter.push_back(a.a + m + l * a.b);
    if (abs(l) > EPS) inter.push_back(a.a + m - l
    * a.b);
    return inter;
}
// area of intersection
double intersection(rectangle a, rectangle b) {
    double x1 = max(real(a.tl), real(b.tl)), y1 =
    max(imag(a.tl), imag(b.tl));
    double x2 = min(real(a.br), real(b.br)), y2 =
    min(imag(a.br), imag(b.br));
    return (x2 <= x1 || y2 <= y1) ? 0 :
    (x2-x1)*(y2-y1);
}

```

Convex Hull

```

bool cmp(point a, point b) {
    if (abs(real(a) - real(b)) > EPS) return
    real(a) < real(b);
    if (abs(imag(a) - imag(b)) > EPS) return
    imag(a) < imag(b);
    return false;
}
convex_polygon convexhull(polygon a) {
    sort(a.points.begin(), a.points.end(), cmp);
    vector<point> lower, upper;
    for (int i = 0; i < a.points.size(); i++) {
        while (lower.size() >= 2 &&
        cross(lower.back() - lower[lower.size() -
        2], a.points[i] - lower.back()) < EPS)
            lower.pop_back();
        while (upper.size() >= 2 &&
        cross(upper.back() - upper[upper.size() -
        2], a.points[i] - upper.back()) > -EPS)
            upper.pop_back();
    }
}

```



```

    upper.pop_back();
    lower.push_back(a.points[i]);
    upper.push_back(a.points[i]);
}
lower.insert(lower.end(), upper.rbegin() + 1,
    upper.rend());
return convex_polygon(lower);
}

```

9 3D Geometry

```

struct point3d {
    double x, y, z;
    point3d operator+(point3d a) const { return
    ↪ {x+a.x, y+a.y, z+a.z}; }
    point3d operator*(double a) const { return
    ↪ {x*a, y*a, z*a}; }
    point3d operator-() const { return {-x, -y,
    ↪ -z}; }
    point3d operator-(point3d a) const { return
    ↪ *this + -a; }
    point3d operator/(double a) const { return
    ↪ *this * (1/a); }
    double norm() { return x*x + y*y + z*z; }
    double abs() { return sqrt(norm()); }
    point3d normalize() { return *this /
    ↪ this->abs(); }
};
double dot(point3d a, point3d b) { return
    ↪ a.x*b.x + a.y*b.y + a.z*b.z; }
point3d cross(point3d a, point3d b) { return
    ↪ {a.y*b.z - a.z*b.y, a.z*b.x - a.x*b.z,
    ↪ a.x*b.y - a.y*b.x}; }
struct line3d { point3d a, b; };
struct plane { double a, b, c, d; } // a*x +
    ↪ b*y + c*z + d = 0
struct sphere { point3d c; double r; };
#define sq(a) ((a)*(a))
#define cb(a) ((a)*(a)*(a))
double surface(circle a) { return 4 * sq(a.r) *
    ↪ M_PI; }
double volume(circle a) { return 4.0/3.0 *
    ↪ cb(a.r) * M_PI; }

```

10 Optimization

Snoob

```

// SameNumberOfOneBits, next permutation
int snoob(int a) {
    int b = a & -a, c = a + b;
    return c | ((a ^ c) >> 2) / b;
}
// example usage
int main() {
    char l1[] = {'1', '2', '3', '4', '5'};
    char l2[] = {'a', 'b', 'c', 'd'};
    int d1 = 5, d2 = 4;
    // prints 12345abcd, 1234a5bcd, ...
    int min = (1<<d1)-1, max = min << d2;
    for (int i = min; i <= max; i = snoob(i)) {
        int p1 = 0, p2 = 0, v = i;
        while (p1 < d1 || p2 < d2) {
            cout << ((v & 1) ? l1[p1++] : l2[p2++]);
            v /= 2;
        }
        cout << '\n';
    }
}

```

Powers

```

bool isPowerOf2(ll a) {
    return a > 0 && !(a & a-1);
}
bool isPowerOf3(ll a) {
    return a>0&&!(12157665459056928801ull%a);
}
bool isPower(ll a, ll b) {
    double x = log(a) / log(b);
    return abs(x-round(x)) < 0.00000000001;
}

```

11 Additional

Judge Speed

```

// kattis: 0.50s
// codeforces: 0.421s
// atcoder: 0.455s
#include <bits/stdc++.h>
using namespace std;
int v = 1e9/2, p = 1;
int main() {
    for (int i = 1; i <= v; i++) p *= i;
    cout << p;
}

```

Judge Pre-Contest Checks

- __int128 and __float128 support?

- does extra or missing whitespace cause WA?

- documentation up to date?

- printer usage available and functional?

```

// each case tests a different fail condition
// try them before contests to see error codes
struct g { int arr[1000000]; g(){};
vector<g> a;
// 0=WA 1=TLE 2=MLE 3=OLE 4=SIGABRT 5=SIGFPE
    ↪ 6=SIGSEGV 7=recursive MLE
int judge(int n) {
    if (n == 0) exit(0);
    if (n == 1) while(1);
    if (n == 2) while(1) a.push_back(g());
    if (n == 3) while(1) putchar_unlocked('a');
    if (n == 4) assert(0);
    if (n == 5) 0 / 0;
    if (n == 6) *(int*)(0) = 0;
    return n + judge(n + 1);
}

```

GCC Builtin Docs

```

// 128-bit integer
__int128 a;
unsigned __int128 b;
// 128-bit float
// minor improvements over long double
float128 c;
// log2 floor
__lg(n);
// number of 1 bits
// can add ll like popcountll for long longs
__builtin_popcount(n);
// number of trailing zeroes
__builtin_ctz(n);
// number of leading zeroes
__builtin_clz(n);
// 1-indexed least significant 1 bit
__builtin_ffs(n);
// parity of number
__builtin_parity(n);

```

Limits

| | | | |
|------|------------------------|-----------------------|------------------|
| int | ±2147483647 | ±2 ³¹ − 1 | 10 ⁹ |
| uint | 4294967295 | 2 ³² − 1 | 10 ⁹ |
| ll | ±9223372036854775807 | ±2 ⁶³ − 1 | 10 ¹⁸ |
| ull | 18446744073709551615 | 2 ⁶⁴ − 1 | 10 ¹⁹ |
| i128 | ±170141183460469231... | ±2 ¹²⁷ − 1 | 10 ³⁸ |
| u128 | 340282366920938463... | 2 ¹²⁸ − 1 | 10 ³⁸ |

Complexity classes input size (per second):

| | |
|---------------------|----------------|
| $O(n^n)$ or $O(n!)$ | $n \leq 10$ |
| $O(2^n)$ | $n \leq 30$ |
| $O(n^3)$ | $n \leq 1000$ |
| $O(n^2)$ | $n \leq 30000$ |
| $O(n\sqrt{n})$ | $n \leq 10^6$ |
| $O(n \log n)$ | $n \leq 10^7$ |
| $O(n)$ | $n < 10^9$ |